

1)

```
def mySqrt(x):
    if x == 0 or x == 1:
        return x

    left, right = 0, x
    while left <= right:
        mid = (left + right) // 2
        square = mid * mid

        if square == x:
            return mid
        elif square > x:
            right = mid - 1
        else:
            left = mid + 1

    return right
```

```
print(mySqrt(4)) # Output: 2
print(mySqrt(8)) # Output: 2
```

2)

```
def findPeakElement(nums):
    left = 0
    right = len(nums) - 1

    while left < right:
        mid = left + (right - left) // 2

        if nums[mid] < nums[mid + 1]:
            left = mid + 1
        else:
            right = mid

    return left
```

Test the function

```
nums = [1, 2, 3, 1]
```

```
print(findPeakElement(nums)) # Output: 2
```

```
nums = [1, 2, 1, 3, 5, 6, 4]
```

```
print(findPeakElement(nums)) # Output: 5
```

3)

```
def missingNumber(nums):
    missing = len(nums)
```

```

    for i, num in enumerate(nums):
        missing ^= i ^ num
    return missing

```

Test the function

```
nums = [3, 0, 1]
```

```
print(missingNumber(nums)) # Output: 2
```

```
nums = [0, 1]
```

```
print(missingNumber(nums)) # Output: 2
```

```
nums = [9, 6, 4, 2, 3, 5, 7, 0, 1]
```

```
print(missingNumber(nums)) # Output: 8
```

4)

```
def findDuplicate(nums):
```

```
    slow = nums[0]
```

```
    fast = nums[0]
```

```
    # Detect the cycle
```

```
    while True:
```

```
        slow = nums[slow]
```

```
        fast = nums[nums[fast]]
```

```
        if slow == fast:
```

```
            break
```

```
    # Find the start of the cycle
```

```
    slow = nums[0]
```

```
    while slow != fast:
```

```
        slow = nums[slow]
```

```
        fast = nums[fast]
```

```
    return slow
```

Test the function

```
nums = [1, 3, 4, 2, 2]
```

```
print(findDuplicate(nums)) # Output: 2
```

```
nums = [3, 1, 3, 4, 2]
```

```
print(findDuplicate(nums)) # Output: 3
```

5)

```
def intersection(nums1, nums2):
```

```
    set1 = set(nums1)
```

```
    set2 = set(nums2)
```

```
    return list(set1.intersection(set2))
```

Test the function

```
nums1 = [1, 2, 2, 1]
nums2 = [2, 2]
print(intersection(nums1, nums2)) # Output: [2]
```

```
nums1 = [4, 9, 5]
nums2 = [9, 4, 9, 8, 4]
print(intersection(nums1, nums2)) # Output: [9, 4]
```

6)

```
def findMin(nums):
    left = 0
    right = len(nums) - 1

    while left < right:
        mid = left + (right - left) // 2

        if nums[mid] > nums[right]:
            left = mid + 1
        else:
            right = mid

    return nums[left]
```

Test the function

```
nums = [3, 4, 5, 1, 2]
print(findMin(nums)) # Output: 1
```

```
nums = [4, 5, 6, 7, 0, 1, 2]
print(findMin(nums)) # Output: 0
```

```
nums = [11, 13, 15, 17]
print(findMin(nums)) # Output: 11
```

7)

```
def searchRange(nums, target):
    left = findLeftPosition(nums, target)
    right = findRightPosition(nums, target)
    return [left, right]
```

```
def findLeftPosition(nums, target):
    left = 0
    right = len(nums) - 1
    result = -1
```

```
    while left <= right:
        mid = left + (right - left) // 2
```

```
    if nums[mid] == target:
```

```

    result = mid
    right = mid - 1
    elif nums[mid] < target:
        left = mid + 1
    else:
        right = mid - 1

    return result

```

```

def findRightPosition(nums, target):
    left = 0
    right = len(nums) - 1
    result = -1

    while left <= right:
        mid = left + (right - left) // 2

        if nums[mid] == target:
            result = mid
            left = mid + 1
        elif nums[mid] < target:
            left = mid + 1
        else:
            right = mid - 1

    return result

```

```

# Test the function
nums = [5, 7, 7, 8, 8, 10]
target = 8
print(searchRange(nums, target)) # Output: [3, 4]

```

```

nums = [5, 7, 7, 8, 8, 10]
target = 6
print(searchRange(nums, target)) # Output: [-1, -1]

```

```

nums = []
target = 0
print(searchRange(nums, target)) # Output: [-1, -1]

```

8)

```

from collections import Counter

```

```

def intersect(nums1, nums2):
    counter1 = Counter(nums1)
    result = []

    for num in nums2:

```

```
if num in counter1 and counter1[num] > 0:  
    result.append(num)  
    counter1[num] -= 1
```

```
return result
```

```
# Test the function
```

```
nums1 = [1, 2, 2, 1]
```

```
nums2 = [2, 2]
```

```
print(intersect(nums1, nums2)) # Output: [2, 2]
```

```
nums1 = [4, 9, 5]
```

```
nums2 = [9, 4, 9, 8, 4]
```

```
print(intersect(nums1, nums2)) # Output: [4, 9]
```