1. Using Newton's method, find an approximation recursive formula for $\sqrt{2}$.

To help you, remember that $\sqrt{2}$ is the positive solution for x^2-2 , so you can use $f(x)=x^2-2$.

- $\bigcirc x_{k+1} = x_k \frac{2x_k}{x_k^2-2}$
- $O x_{k+1} = \frac{x_k^2-2}{2x_k}$
- $\bigcirc x_{k+1} = \frac{2x_k}{x_k^2-2}$
- $igotimes x_{k+1} = x_k rac{x_k^2-2}{2x_k}$
- 2. Regarding the previous question, suppose you don't know any approximation for $\sqrt{2}$ and only that it is a positive real number such that $x^2=2$. Which value from the list below will result in the fastest convergence?
- 1 point

1 point

- O 4
- O 3
- 2
- The initial value does not impact in the Newton's method convergence.
- 3. Let's continue investigating the method we are developing to compute the $\sqrt{2}$. Remember that we used the fact that $\sqrt{2}$ is one of the roots of x^2-2 . What would happen if we have chosen a negative value as initial point?
- 1 point

- The algorithm would not converge.
- \bigcirc The algorithm would converge to $\sqrt{2}$.
- lacksquare The algorithm would converge to the negative root of x^2-2 .
- \bigcirc The algorithm would converge to 0.
- 4. Did you know that it is possible to calculate the *reciprocal* of any number *without performing division?* (The reciprocal of a non-zero real number a is $\frac{1}{a}$).

- point

Setting a non-zero real number a , use the function $f(x)=a-rac{1}{x}=a$ – x^{-1} to find such formula.

This method was in fact used in older IBM computers to implement division in hardware!

So, the iteration formula to find the reciprocal of a, in this case, is:

- $\bigcirc \ x_{k+1} = 2x_k + ax_k^2$
- $\bigcirc \ x_{k+1} = 2x_k x_k^2$
- $\bigcirc \ x_{k+1} = x_k a x_k^2$

- 1 point
- 5. Suppose we want to find the minimum value (suppose we already know that the minimum exists and is unique) of $x\log(x)$ where $x\in(0,+\infty)$. Using Newton's method, what recursion formula we must use?

Hint: $f(x) = x \log(x)$, $f'(x) = \log(x) + 1$ and $f''(x) = \frac{1}{x}$

- $\bigcirc x_{k+1} = x_k rac{x_k \log(x_k)}{\log(x_k) + 1}$
- $\bigcirc \ x_{k+1} = x_k x_k^2 \log(x_k)$
- $\bigcirc \ x_{k+1} = x_k \log(x_k)$
- 6. Regarding the Second Derivative Test to decide whether a point with $f^{\circ}(x)=0$ is a local minimum or local maximum, check all that apply.

1 point

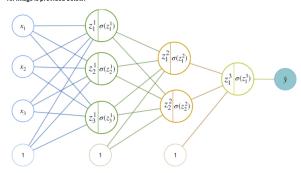
- ightharpoonup If $f^{\prime\prime}(x)>0$ then x is a local minimum.
- ightharpoons If f``(x) = 0 then the test is inconclusive.

1 point

- 7. Let $f(x,y)=x^2+y^3$, then the Hessian matrix,H(x,y) is:
 - $O \hspace{1cm} H(x,y) = \left[egin{array}{cc} 2x & 3y^2 \ 3y^2 & 2x \end{array}
 ight]$
 - $lackbox{igspace{0.95\textwidth} $H(x,y)=\left[egin{array}{cc} 2 & 0 \ 0 & 6y \end{array}
 ight]$}$
 - $egin{array}{ccc} H(x,y) = \left[egin{array}{ccc} 0 & 2 \ 6y & 0 \end{array}
 ight] \end{array}$
 - $egin{array}{ccc} H(x,y) = \left[egin{array}{ccc} 0 & 0 \ 0 & 0 \end{array}
 ight] \end{array}$
- 8. How many parameters has a Neural Network with:

- Input layer of size 3
- One hidden layer with 3 neurons
- One hidden layer with 2 neurons
- Output layer with size 1

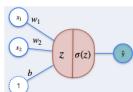
An image is provided below:



- O 11
- O 8
- 23
- O 3
- 9. Given the following Single Layer Perceptron with Sigmoid function as activation function, and log-loss as Loss Function (L), the value for $\frac{\partial L}{\partial w_i}$ is:

1 point

1 point



- $\bigcirc -(y-\hat{y})$
- $\bigcirc \hspace{0.1cm} -(y-\hat{y})x_1$
- $\bigcirc \ -(y-\hat{y})x_2$
- O 1
- 10. Suppose you have a function f(x,y) with $abla f(x_0,y_0)=(0,0)$ and such that

$$H(x_0,y_0)=\left[egin{array}{cc} 2 & 0 \ 0 & 10 \end{array}
ight]$$

Then the point (x_0,y_0) is a:

- O Local maximum.
- Local minimum.
- O Saddle point.
- We can't infer anything with the given information.