

Periodic Functions

Periodic Function: repeats a pattern of y-values (outputs) at regular intervals
Cycle: may begin at any point in a graph
Period: is the horizontal length of one cycle.

Special Right Angles

45-45-90

$h = \sqrt{2}$ times /

30-60-90

$h = 2$ times s

$l = \sqrt{3}$ times s

s = short leg

l = long leg

Properties Of Sine Functions

$y = a \sin b \theta$

period = $2\pi/b$

$|a|$ = amplitude

b = number of cycles (0 to 2π)

Quadratic Functions

Standard Form

$f(x) = ax^2 + bx + c$

ax^2

Quadratic term

bx

Linear term

c

constant term

Exponential Growth & Exponential Decay

$b = 1 + r$

$b > 1$ = expon. growth

When $b < 1$, b is a decay factor

x-axis = asymptote

$0 < b < 1$

$b = 1 + (-r)$

Exponential Growth & Exponential Decay (cont)

$y = ab^x$

b = growth factor

r = increase in rate

e & Its Importance

$A = Pe^{rt}$

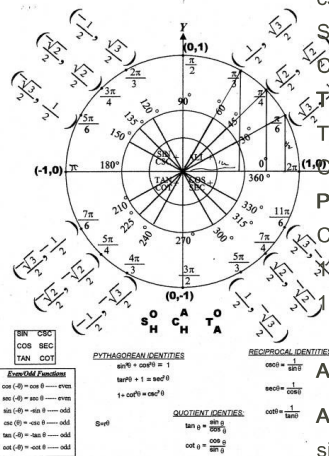
A = amount in account

P = principal (what you start with)

r = rate in interest (annually)

t = time (in years)

Unit Circle



radian 2π , tangent 0
radian $\pi/6$, tangent $\sqrt{3}/3$
radian $\pi/4$, tangent 1
radian $\pi/3$, tangent $\sqrt{3}$
radian $\pi/2$, tangent undefined
radian $2\pi/3$, tangent $-\sqrt{3}/3$
radian $3\pi/4$, tangent -1
radian $5\pi/6$, tangent $-\sqrt{3}/3$
radian π , tangent 0
radian $7\pi/6$, tangent $\sqrt{3}/3$
radian $5\pi/4$, tangent 1
radian $4\pi/3$, tangent $\sqrt{3}$
radian $3\pi/2$, tangent undefined
radian $5\pi/3$, tangent $-\sqrt{3}/3$
radian $7\pi/4$, tangent -1
radian $11\pi/6$, tangent $\sqrt{3}/3$

Sine, Cosine, Tangent

Sine = opp./adj.

Cosine = Adj./Hypo.

Tangent = Opp./Adj.

Mazimun & Minimum

$y = ax^2 + bx + c$

AOS: $x = -b/2a$

1. vertex

2. c

3. another point

Area = length times width

Trigonometric Identities

Reciprocal Identities

$\csc \theta = 1/\sin \theta$

$\sec \theta = 1/\cos \theta$

$\cot \theta = 1/\tan \theta$

Tangent & Cotangent Identities

$\tan \theta = \sin \theta / \cos \theta$

$\cot \theta = \cos \theta / \sin \theta$

Pythagorean Identities

$\cos^2 \theta + \sin^2 \theta = 1$

$1 + \tan^2 \theta = \sec^2 \theta$

$1 + \cot^2 \theta = \csc^2 \theta$

Angle Identities

Angle Difference Identities

$\sin(A - B) = \sin A \cos B - \cos A \sin B$

Angle Identities (cont)

$\cos(A - B) = \cos A \cos B + \sin A \sin B$

$\sin B$

$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$

$\tan B$

Angle Sum Identities

$\sin(A + B) = \sin A \cos B + \cos A \sin B$

$\sin B$

$\cos(A + B) = \cos A \cos B - \sin A \sin B$

$\sin B$

$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

$\tan B$

Identities

Double-Angle Identities

$\cos 2x = \cos^2 x - \sin^2 x$

$\cos 2x = 2\cos^2 x - 1$

$\cos 2x = 1 - 2\sin^2 x$

$\sin 2x = 2\sin x \cos x$

$\tan 2x = \frac{2\tan x}{1 - \tan^2 x}$

Half Angle Identities

$\sin A/2 = \pm \sqrt{1 - \cos A}/2$

$\cos A/2 = \pm \sqrt{1 + \cos A}/2$

$\tan A/2 = \pm \sqrt{1 - \cos A}/1 + \cos A$

$\cos A/1 + \cos A$

Logarithms

- to base b of a positive number

y is defined as...

If $y = ab^x$, then $\log_b y = x$

Log In Life

$pH = -\log[H^+]$

b is not equal to 1

b must be positive

log of 0 or negative number = undefined

$\log = \log \text{ base } 10$

Log Are Inverses Of Exponentials

1. Graph exponential function
2. Graph $y = x$
3. Reflect exponential function over $y = x$ (reverse coordinates)

Properties Of Log

$\log_b MN = \log_b M + \log_b N$ <---- product property
 $\log_b M/N = \log_b M - \log_b N$ <---- Quotient property
 $\log_b M^x = x \log_b M$ <---- Power property

WATCH OUT FOR ERRORS

$\log_b a / \log_b c$ does not equal $\log_b a/c$

$\log_b a$ times c does not equal $\log_b a$ times $\log_b c$

Expanding Log

$$\log_2 7b = \log_2 7 + \log_2 b$$

left to right = expand

right to left = simplify

Natural Log

Write $3\ln 6 - \ln 8$ as a single natural log

$$\ln 6^3/8 \rightarrow \ln 216/8 \rightarrow \ln 27$$

Solving Log Equations

Pt 1

$$\text{solve } \log(3x+1) = 5$$

$$3x+1 = 10^5$$

$$3x+1 = 100000$$

$$3x = 99,999$$

$$x = 33,333$$

Pt 2

Solving Log Equations (cont)

$$\text{Solve } 2\log x - \log 3 = 2$$

$$\log(x^2/3) = 2$$

$$x^2/3 = 10^2$$

$$x^2 = 2(100)$$

$$x = 10\sqrt{2} \text{ or } 17.32$$

Pairs Of Relations are Inverse Of Each Other

$$y = x - 7/2$$

$$y = 2x+7$$

$$y = 3x - 1$$

$$y = x + 1/3$$

$$y = -x + 4$$

$$y = -x + 4/-1$$

$$y = x + 4/5$$

$$y = 5x - 4$$



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