


Result:	 092910 000034	Neptun ID: <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/> <input style="width: 20px; height: 20px;" type="text"/>	Draft papers: <input style="width: 20px; height: 20px;" type="checkbox"/>
Name: _____			

The test consists of **4 questions**. The available time to solve the quiz is **20 minutes**. Please use a blue coloured pen; the use of any other tools is forbidden.

- |     |                          |                          |                          |                          |
|-----|--------------------------|--------------------------|--------------------------|--------------------------|
|     | <b>a</b>                 | <b>b</b>                 | <b>c</b>                 | <b>d</b>                 |
| 1.) | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| 2.) | (essay)                  |                          |                          |                          |
| 3.) | (essay)                  |                          |                          |                          |
| 4.) | (essay)                  |                          |                          |                          |

Please copy the multiple choice questions' solution in the attached table. For each correct answer marked, 2 points are awarded; for each incorrect answer marked, -1 point is awarded. There is no limit to the number of correct answers per question. A negative aggregate score will be interpreted as 0 points.

✦

1.) How can we formalize the following statement by using a zero-order language with  $Con = \{p, q, r\}$ ?

*The sky is blue if and only if where there are no clouds and it is daytime.*

$p \Leftrightarrow$  *The sky is blue.*     $q \Leftrightarrow$  *There are clouds on the sky.*     $r \Leftrightarrow$  *It is daytime.*

- (a)  $(\neg q \wedge r) \supset p$
- (b)  $p \supset (\neg q \wedge r)$
- (c)  $p \equiv \neg q \wedge r$
- (d)  $(\neg q \wedge r) \equiv p$

✦

2.) What is the conjunctive normal form of  $((p \supset q) \supset r) \supset w$ ?

3.) Construct the prenex form of

$$(\forall x P(x) \supset \exists x (Q(x, y) \supset \neg \forall x (Q(x, z) \vee P(z)))) .$$

4.) Prove the following with sequent calculus.

$$(p \supset q) \wedge (p \supset \neg q) \vdash \neg p$$

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