ISE 5103 Intelligent Data Analytics
Homework #3

Instructor: Charles Nicholson

Due: See course website for due date

Learning objective: Data understanding and preparation with an emphasis on transformations, missing value imputation, and feature engineering.

Submission notes:

1. Clearly identify each problem (e.g. Problem 1a, Problem 2b, etc.)

2. Do not zip your files for submission. Submit exactly two files. Name the files "LastName-HW1" with the appropriate file extension (that is, .R, .pdf, or .docx)

3. You will submit your complete R script. Note: include `library` commands to load *all* packages that are used in the completion of the assignment. Place these statements at the top of your script. The R code itself is part of your solution – make sure to *provide comments* on what your code is doing. Keep it clean and clear!

4. For the write-up, the goal is to limit your complete homework submission to under 10 pages (12 page max).

1 Glass Identification

The study of classification of types of glass is motivated by criminological investigations. At the scene of the crime, the glass left can be used as evidence... if it is correctly identified.

The data set we consider consists of 214 glass samples labeled as one of seven class categories. There are nine predictors, including the refractive index and percentages of eight elements: Na (Sodium), Mg (Magnesium), Al (Aluminum), Si (Silicon), K (Potassium), Ca (Calcium), Ba (Barium), and Fe (Iron).

The data is available here: `http://archive.ics.uci.edu/ml/datasets/Glass+Identification` and is also available in the `mlbench` package as the dataset `Glass`.

(a) Using visualizations, explore the predictor variables to understand their distributions as well as the relationships between predictors. Do there appear to be any outliers in the data? Are any predictors skewed?

(b) Identify three attributes that you think could benefit from a skew transformation (there might be more than three that could benefit, but three is enough for this problem). For these attributes,
   i. Use the `symbox` function from package `car` to consider possible power transformations
   ii. Use the `boxcox` method from the `EnvStats` package to determine an optimal value for Box-Cox value of λ.

(c) Use PCA to help evaluate the data. Does this provide any insight? If so, what?

(d) Perform a linear discriminant analysis (LDA) using the `lda` function from the `MASS` package. Compare and contrast the results of LDA with PCA.

2 Missing Data

The `freetrade` data frame in the `Amelia` package has economic and political data on nine developing countries in Asia from 1980 to 1999. These 9 variables include year, country, average tariff rates, Polity IV score, total population, gross domestic product per capita, gross international reserves, a dummy variable for if the country had signed an IMF agreement in that year, a measure of financial openness, and a measure of US hegemony. Unfortunately, this data has missing values.

You will perform the following linear regression to predict the value of `tariff`:
`lm(data=freetrade,tariff year+country+polity+pop+gdp.pc+intresmi+signed+fiveop+usheg)`

(a) Perform the regression using listwise deletion.

(b) Perform the regression after using mean imputation.

(c) Perform the regression after using multiple imputation – in particular, *multivariate imputation by chained equations*. Note: you will have to find an imputation method that will work with this data! Please use one imputation method for the full data.

(d) Can you improve your results in (c) by selecting single imputation approaches specific to each variable? Implement these choices and run the analysis model (the regression model).

(e) Compare the regression coefficients for each of the analysis models.

(f) Which missing value deletion or imputation strategy do you recommend for this data set? Why?

3 Truck - Bridge Sensor Data

This assignment is based on a real research project and real-world data; as such the introduction is a bit long.

The data set **"bridgeSensor.csv"** contains about 30 seconds of real sensor data from a bridge on I-35 (near Purcell, OK). The measurements are accelerometer data associated with the structure vibrations when large vehicles cross the bridge at highway speeds. There are several identical sensors on the bridge placed in different locations. The data in the file corresponds to *two* of those sensors. Each sensor collects about 100 measurements per second. The bridge also has a video camera which records passing vehicles – the still images corresponding to the data are in the document, **"bridge truck events.pdf"** (Note: The first two pages coincide with the data in "bridgeSensor.csv"). The goal of this research project was to be able use accelerometer data to automatically identify the type of vehicle crossing the bridge, e.g. based on truck weight, number of axles, aerodynamics, etc.

Now, obviously I am not asking you to solve this problem in a single homework assignment! However, I want you to examine the data and consider certain aspects relating to (1) problem understanding, (2) data understanding, and (3) data preparation. This is most likely a type of data that you have not worked with before. Therefore, I will provide you with information to help you get started. Some of the following information is adapted from `http://www.di.fc.ul.pt/~jpn/r/fourier/fourier.html` which is a good site for understanding the basic principles.

Dealing with signal data in wave form. Joseph Fourier showed that any periodic wave can be decomposed into a series of sine waves. This is the basis of the Fourier Series. A standard data transformation technique for wave data is based on the Fourier Transform. The Fourier Transforms converts a wave from the *time domain* into the *frequency domain*. That is, if the wave form can be represented as a sum of simple sine waves, what are the frequencies and amplitudes of the sine waves that together represent the signal.

The *fast fourier transorm* (FFT) is an efficient procedure for applying the transform and is available in R through the command `fft` from the `stats` package. A plot of frequency versus strength (amplitude) on an x-y graph of these sine wave components is called a frequency spectrum. Code is provided to help you convert the data from the time-domain to the frequency-domain and plot the results. The code is available in course website in the file `FFTexample.R`.

(a) Given that the goal of the research project was to classify vehicles based on the sensor data, develop a *well thought out* list of candidate features for a classification model. Provide a meaningful description for each.

(b) Use the available data to construct the features as possible from part (a). Make sure you submit the complete R script associated with the feature construction/extraction.

(c) Describe any difficulties that you encounter in engineering the features. What are possible solutions to overcome those difficulties?