

Testing examples in saemix 3.0 - continuous models

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Objective

Check saemix for continuous data models

Setup

- set up work directories
- two versions toggled by testMode
 - if testMode is FALSE, load the functions in R
 - if testMode is TRUE, load the library in a dev_mode environment
- aim: check the examples used in the online documentation
 - all examples must run without error

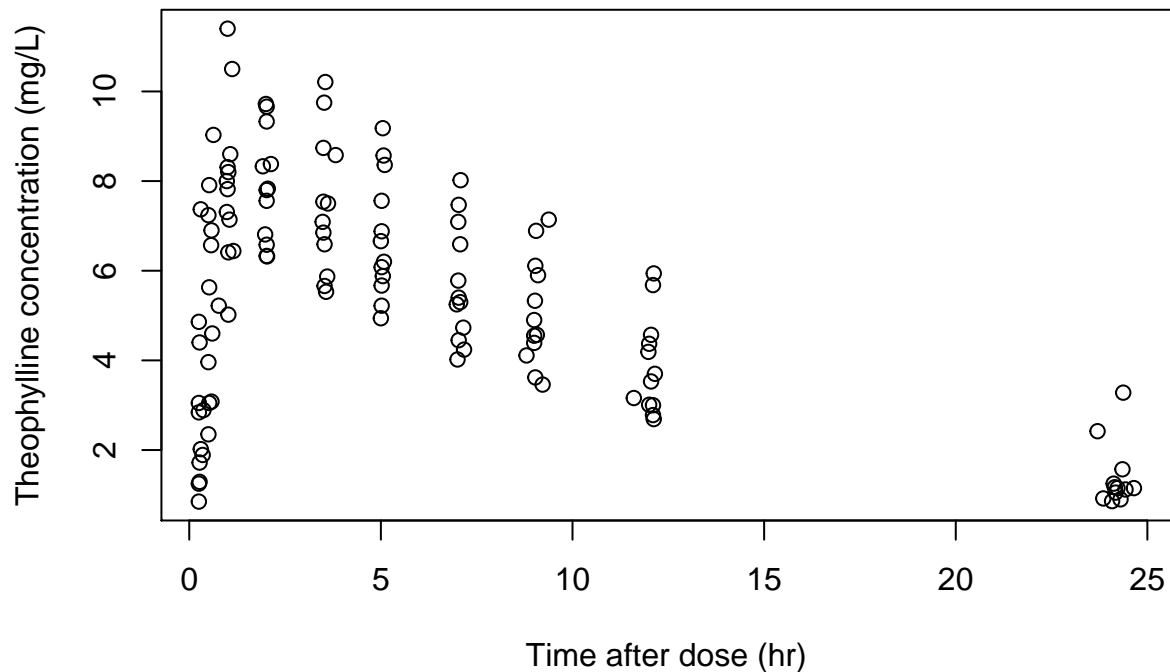
Testing library

Continuous response model

Theophylline

```
if(testMode)
  data(theo.saemix) else
  theo.saemix<-read.table(file.path(datDir, "theo.saemix.tab"), header=TRUE)

#Plotting the theophylline data
plot(Concentration~Time,data=theo.saemix,xlab="Time after dose (hr)",
ylab="Theophylline concentration (mg/L)")
```



```
saemix.data<-saemixData(name.data=theo.saemix,header=TRUE,sep=" ",na=NA,
  name.group=c("Id"),name.predictors=c("Dose","Time"),
  name.response=c("Concentration"),name.covariates=c("Weight","Sex"),
  units=list(x="hr",y="mg/L",covariates=c("kg","-")), name.X="Time")
```

```
## [1] "Weight" "Sex"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset theo.saemix
##   Structured data: Concentration ~ Dose + Time | Id
##   X variable for graphs: Time (hr)
##   covariates: Weight (kg), Sex (-)
##   reference class for covariate Sex : 0
```

```
model1cpt<-function(psi,id,xidep) {
  dose<-xidep[,1]
  tim<-xidep[,2]
  ka<-psi[id,1]
  V<-psi[id,2]
  CL<-psi[id,3]
  k<-CL/V
  ypred<-dose*ka/(V*(ka-k))*(exp(-k*tim)-exp(-ka*tim))
  return(ypred)
}
# Default model, no covariate
saemix.model<-saemixModel(model=model1cpt,
  description="One-compartment model with first-order absorption",
  psi0=matrix(c(1.,20,0.5,0.1,0,-0.01),ncol=3,byrow=TRUE,
  dimnames=list(NULL, c("ka","V","CL"))),transform.par=c(1,1,1))
```

```
##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: One-compartment model with first-order absorption
## Model type: structural
## function(psi,id,xidep) {
##     dose<-xidep[,1]
##     tim<-xidep[,2]
##     ka<-psi[id,1]
##     V<-psi[id,2]
##     CL<-psi[id,3]
##     k<-CL/V
##     ypred<-dose*ka/(V*(ka-k))*(exp(-k*tim)-exp(-ka*tim))
##     return(ypred)
## }
## Nb of parameters: 3
##     parameter names: ka V CL
##     distribution:
##     Parameter Distribution Estimated
## [1,] ka          log-normal Estimated
## [2,] V          log-normal Estimated
## [3,] CL          log-normal Estimated
## Variance-covariance matrix:
##     ka V CL
## ka  1 0  0
## V   0 1  0
## CL  0 0  1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
##           ka V CL
## Pop.CondInit 1.0 20 0.50
## Cov.CondInit 0.1  0 -0.01

# Note: remove the options save=FALSE and save.graphs=FALSE
# to save the results and graphs
saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

saemix.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset theo.saemix
## Structured data: Concentration ~ Dose + Time | Id
## X variable for graphs: Time (hr)
## covariates: Weight (kg), Sex (-)
## reference class for covariate Sex : 0
## Dataset characteristics:
## number of subjects: 12
```

```

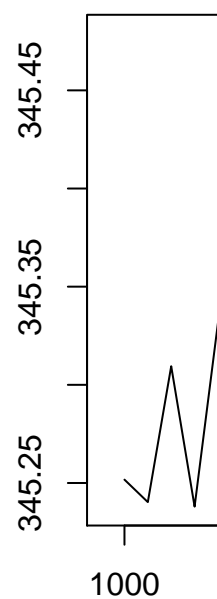
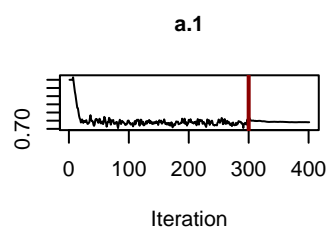
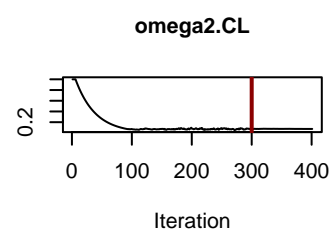
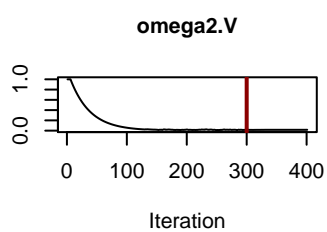
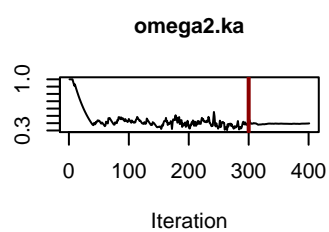
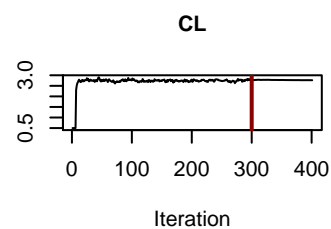
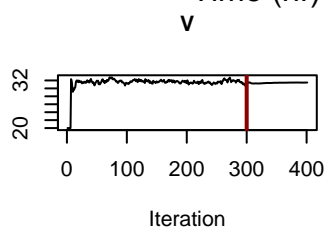
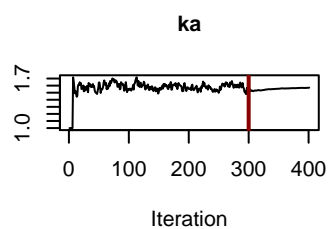
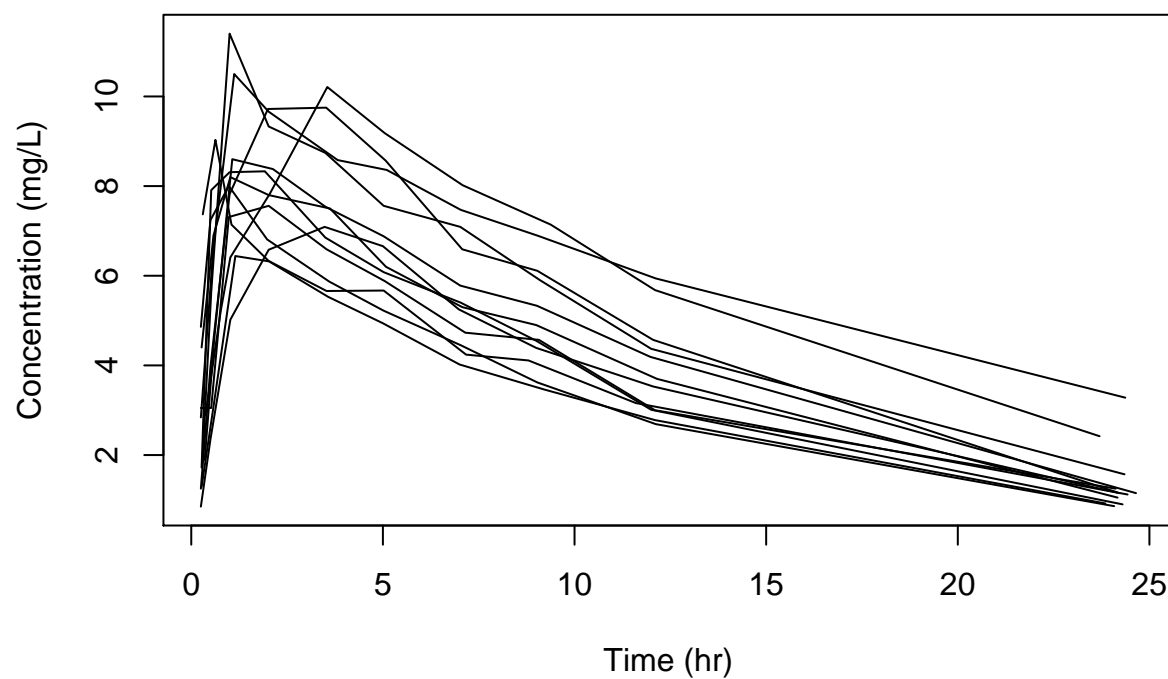
##      number of observations: 120
##      average/min/max nb obs: 10.00 / 10 / 10
## First 10 lines of data:
##      Id      Dose  Time Concentration Weight Sex mdv cens occ ytype
## 1      1 319.992 0.25          2.84   79.6   1  0    0  1    1
## 2      1 319.992 0.57          6.57   79.6   1  0    0  1    1
## 3      1 319.992 1.12         10.50   79.6   1  0    0  1    1
## 4      1 319.992 2.02          9.66   79.6   1  0    0  1    1
## 5      1 319.992 3.82          8.58   79.6   1  0    0  1    1
## 6      1 319.992 5.10          8.36   79.6   1  0    0  1    1
## 7      1 319.992 7.03          7.47   79.6   1  0    0  1    1
## 8      1 319.992 9.05          6.89   79.6   1  0    0  1    1
## 9      1 319.992 12.12         5.94   79.6   1  0    0  1    1
## 10     1 319.992 24.37          3.28   79.6   1  0    0  1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: One-compartment model with first-order absorption
## Model type: structural
## function(psi,id,xidep) {
##     dose<-xidep[,1]
##     tim<-xidep[,2]
##     ka<-psi[id,1]
##     V<-psi[id,2]
##     CL<-psi[id,3]
##     k<-CL/V
##     ypred<-dose*ka/(V*(ka-k))*(exp(-k*tim)-exp(-ka*tim))
##     return(ypred)
## }
## <bytecode: 0x564408b4f728>
## Nb of parameters: 3
##     parameter names: ka V CL
##     distribution:
##     Parameter Distribution Estimated
## [1,] ka      log-normal Estimated
## [2,] V      log-normal Estimated
## [3,] CL      log-normal Estimated
## Variance-covariance matrix:
##     ka V CL
## ka  1 0 0
## V   0 1 0
## CL  0 0 1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
##         ka V CL
## Pop.CondInit 1 20 0.5
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling

```

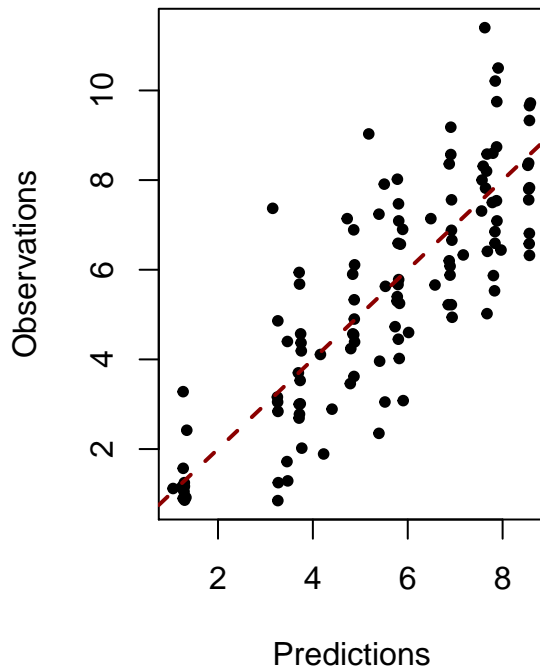
```

##      Number of iterations: K1=300, K2=100
##      Number of chains: 5
##      Seed: 632545
##      Number of MCMC iterations for IS: 5000
##      Simulations:
##          nb of simulated datasets used for npde: 1000
##          nb of simulated datasets used for VPC: 100
##      Input/output
##          save the results to a file: FALSE
##          save the graphs to files: FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] ka          1.57   0.304 19.3
## [2,] V          31.47   1.423  4.5
## [3,] CL          2.77   0.239  8.7
## [4,] a.1         0.74   0.057  7.7
## -----
## ----- Variance of random effects -----
## -----
##      Parameter Estimate SE      CV(%)
## ka omega2.ka 0.397   0.1790 45
## V  omega2.V  0.017   0.0096 58
## CL omega2.CL 0.074   0.0360 49
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.ka omega2.V omega2.CL
## omega2.ka 1          0          0
## omega2.V  0          1          0
## omega2.CL 0          0          1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 344.1136
##      AIC = 358.1136
##      BIC = 361.5079
##
## Likelihood computed by importance sampling
##      -2LL= 345.4329
##      AIC = 359.4329
##      BIC = 362.8273
## -----
plot(saemix.fit)

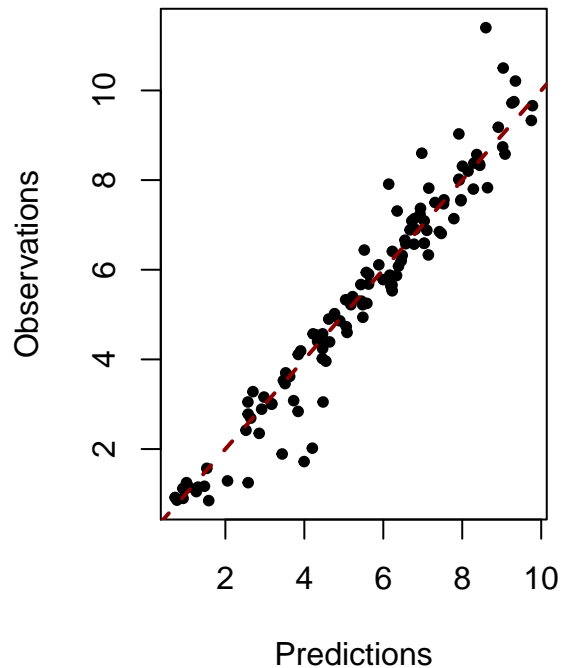
```



Population predictions



Individual predictions, MAP



```
# Model with covariates
saemix.model<-saemixModel(model=model1cpt,
  description="One-compartment model with first-order absorption",
  psi0=matrix(c(1.,20,0.5,0.1,0,-0.01),ncol=3,byrow=TRUE,
    dimnames=list(NULL, c("ka","V","CL"))),transform.par=c(1,1,1),
  covariate.model=matrix(c(0,0,1,0,0,0),ncol=3,byrow=TRUE),fixed.estim=c(1,1,1),
  covariance.model=matrix(c(1,0,0,0,1,1,0,1,1),ncol=3,byrow=TRUE),
  omega.init=matrix(c(1,0,0,0,1,0,0,0,1),ncol=3,byrow=TRUE),error.model="combination")

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: One-compartment model with first-order absorption
## Model type: structural
## function(psi,id,xidep) {
##   dose<-xidep[,1]
##   tim<-xidep[,2]
##   ka<-psi[id,1]
##   V<-psi[id,2]
##   CL<-psi[id,3]
##   k<-CL/V
##   ypred<-dose*ka/(V*(ka-k))*(exp(-k*tim)-exp(-ka*tim))
##   return(ypred)
## }
## <bytecode: 0x564408b4f728>
## Nb of parameters: 3
## parameter names: ka V CL
## distribution:
```

```

##      Parameter Distribution Estimated
## [1,] ka      log-normal Estimated
## [2,] V      log-normal Estimated
## [3,] CL      log-normal Estimated
##      Variance-covariance matrix:
##      ka V CL
## ka  1 0 0
## V   0 1 1
## CL  0 1 1
##      Error model: combined , initial values: a.1=1 b.1=1
##      Covariate model:
##      ka V CL
## [1,] 0 0 1
## [2,] 0 0 0
##      Initial values
##      ka V CL
## Pop.CondInit 1.0 20 0.50
## Cov.CondInit 0.1 0 -0.01

saemix.options<-list(seed=39546,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)
saemix.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset theo.saemix
##      Structured data: Concentration ~ Dose + Time | Id
##      X variable for graphs: Time (hr)
##      covariates: Weight (kg), Sex (-)
##      reference class for covariate Sex : 0
## Dataset characteristics:
##      number of subjects:      12
##      number of observations: 120
##      average/min/max nb obs: 10.00 / 10 / 10
## First 10 lines of data:
##      Id      Dose  Time Concentration Weight Sex mdv cens occ ytype
## 1      1 319.992 0.25          2.84   79.6  1  0  0  1  1
## 2      1 319.992 0.57          6.57   79.6  1  0  0  1  1
## 3      1 319.992 1.12         10.50   79.6  1  0  0  1  1
## 4      1 319.992 2.02          9.66   79.6  1  0  0  1  1
## 5      1 319.992 3.82          8.58   79.6  1  0  0  1  1
## 6      1 319.992 5.10          8.36   79.6  1  0  0  1  1
## 7      1 319.992 7.03          7.47   79.6  1  0  0  1  1
## 8      1 319.992 9.05          6.89   79.6  1  0  0  1  1
## 9      1 319.992 12.12         5.94   79.6  1  0  0  1  1
## 10     1 319.992 24.37          3.28   79.6  1  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
##      Model function: One-compartment model with first-order absorption
##      Model type: structural

```



```

## function(psi,id,xidep) {
##   dose<-xidep[,1]
##   tim<-xidep[,2]
##   ka<-psi[id,1]
##   V<-psi[id,2]
##   CL<-psi[id,3]
##   k<-CL/V
##   ypred<-dose*ka/(V*(ka-k))*(exp(-k*tim)-exp(-ka*tim))
##   return(ypred)
## }
## <bytecode: 0x564408b4f728>
##   Nb of parameters: 3
##     parameter names:  ka V CL
##     distribution:
##       Parameter Distribution Estimated
## [1,] ka      log-normal Estimated
## [2,] V      log-normal Estimated
## [3,] CL      log-normal Estimated
##   Variance-covariance matrix:
##     ka V CL
## ka  1 0  0
## V   0 1  1
## CL  0 1  1
##   Error model: combined , initial values: a.1=1 b.1=1
##   Covariate model:
##     [,1] [,2] [,3]
## Weight  0  0  1
##   Initial values
##           ka V   CL
## Pop.CondInit 1.0 20  0.50
## Cov.CondInit 0.1  0 -0.01
## -----
## ----   Key algorithm options   ----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of standard errors and linearised log-likelihood
##   Estimation of log-likelihood by importance sampling
##   Number of iterations:  K1=300, K2=100
##   Number of chains:  5
##   Seed:  39546
##   Number of MCMC iterations for IS:  5000
##   Simulations:
##     nb of simulated datasets used for npde:  1000
##     nb of simulated datasets used for VPC:  100
##   Input/output
##     save the results to a file:  FALSE
##     save the graphs to files:  FALSE
## -----
## ----                               Results                               ----
## -----
## -----   Fixed effects   -----
## -----
##   Parameter      Estimate SE      CV(%) p-value
## [1,] ka          1.5565  0.3050 19.6  -

```

```

## [2,] V          31.6621  1.4946  4.7  -
## [3,] CL          4.4308  1.9206 43.3  -
## [4,] beta_Weight(CL) -0.0067  0.0061 91.3  0.14
## [5,] a.1         0.5734  0.1211 21.1  -
## [6,] b.1         0.0748  0.0223 29.8  -
## -----
## ----- Variance of random effects -----
## -----
##      Parameter Estimate SE    CV(%)
## ka    omega2.ka 0.412    0.179 44
## V      omega2.V  0.019    0.011 56
## CL      omega2.CL 0.064    0.031 48
## covar cov.V.CL  0.035    0.016 45
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.ka omega2.V omega2.CL
## omega2.ka 1      0      0
## omega2.V  0      1      1
## omega2.CL 0      1      1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 330.7213
##      AIC = 350.7213
##      BIC = 355.5704
##
## Likelihood computed by importance sampling
##      -2LL= 333.9945
##      AIC = 353.9945
##      BIC = 358.8436
## -----

```

Simulated PD

```

if(testMode) {
  data(PD1.saemix)
  data(PD2.saemix)
} else {
  PD1.saemix<-read.table(file.path(datDir, "PD1.saemix.tab"), header=TRUE)
  PD2.saemix<-read.table(file.path(datDir, "PD1.saemix.tab"), header=TRUE)
}

saemix.data<-saemixData(name.data=PD1.saemix,header=TRUE,name.group=c("subject"),
  name.predictors=c("dose"),name.response=c("response"),
  name.covariates=c("gender"), units=list(x="mg",y="-",covariates=c("-")))

## [1] "gender"
##
##
## The following SaemixData object was successfully created:
##

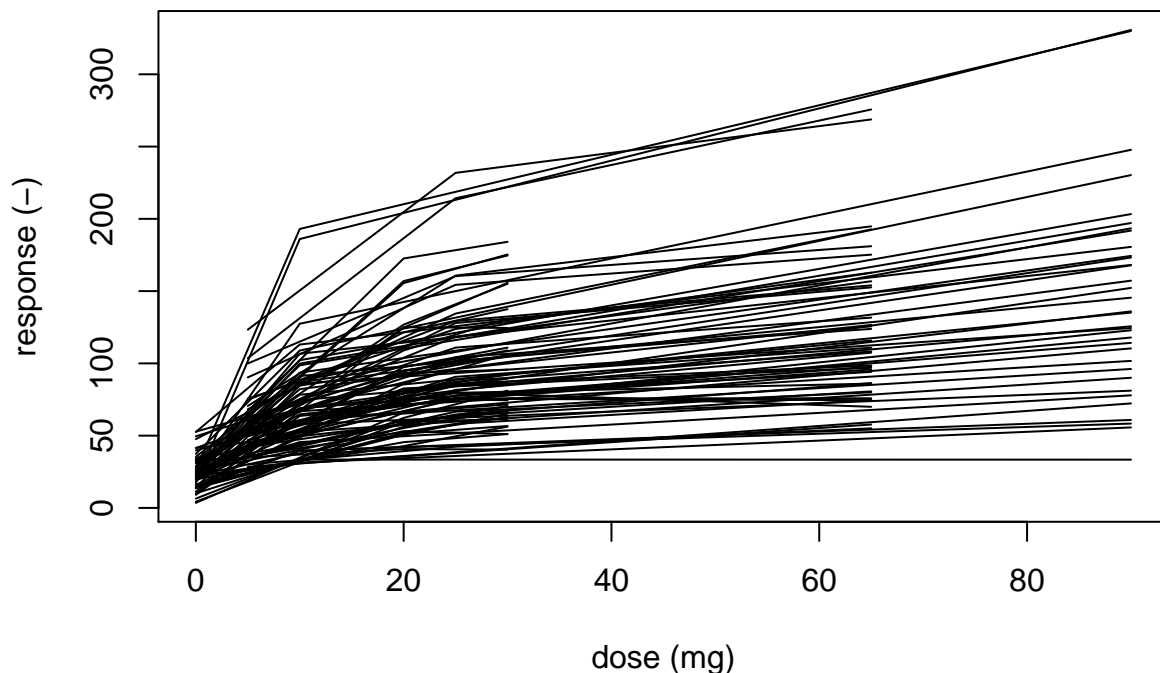
```

```
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset PD1.saemix
##   Structured data: response ~ dose | subject
##   Predictor: dose (mg)
##   covariates: gender (-)
##   reference class for covariate gender : 0

modelemax<-function(psi,id,xidep) {
  # input:
  #   psi : matrix of parameters (3 columns, E0, Emax, EC50)
  #   id : vector of indices
  #   xidep : dependent variables (same nb of rows as length of id)
  # returns:
  #   a vector of predictions of length equal to length of id
  dose<-xidep[,1]
  e0<-psi[id,1]
  emax<-psi[id,2]
  e50<-psi[id,3]
  f<-e0+emax*dose/(e50+dose)
  return(f)
}

# Plotting the data
plot(saemix.data,main="Simulated data PD1")
```

Simulated data PD1



```
# Compare models with and without covariates with LL by Importance Sampling
model1<-saemixModel(model=modelemax,description="Emax growth model",
  psi0=matrix(c(20,300,20,0,0,0),ncol=3,byrow=TRUE,dimnames=list(NULL,
    c("E0","Emax","EC50"))), transform.par=c(1,1,1),
```

```

covariate.model=matrix(c(0,0,0), ncol=3,byrow=TRUE),fixed.estim=c(1,1,1))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Emax growth model
## Model type: structural
## function(psi,id,xidep) {
## # input:
## # psi : matrix of parameters (3 columns, E0, Emax, EC50)
## # id : vector of indices
## # xidep : dependent variables (same nb of rows as length of id)
## # returns:
## # a vector of predictions of length equal to length of id
## dose<-xidep[,1]
## e0<-psi[id,1]
## emax<-psi[id,2]
## e50<-psi[id,3]
## f<-e0+emax*dose/(e50+dose)
## return(f)
## }
## Nb of parameters: 3
## parameter names: E0 Emax EC50
## distribution:
## Parameter Distribution Estimated
## [1,] E0 log-normal Estimated
## [2,] Emax log-normal Estimated
## [3,] EC50 log-normal Estimated
## Variance-covariance matrix:
## E0 Emax EC50
## E0 1 0 0
## Emax 0 1 0
## EC50 0 0 1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
## E0 Emax EC50
## Pop.CondInit 20 300 20
## Cov.CondInit 0 0 0

model2<-saemixModel(model=modelemax,description="Emax growth model",
psi0=matrix(c(20,300,20,0,0,0),ncol=3,byrow=TRUE,dimnames=list(NULL,
c("E0","Emax","EC50"))), transform.par=c(1,1,1),
covariate.model=matrix(c(0,0,1), ncol=3,byrow=TRUE),fixed.estim=c(1,1,1))

```

```

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Emax growth model
## Model type: structural

```

```

## function(psi,id,xidep) {
## # input:
## #   psi : matrix of parameters (3 columns, E0, Emax, EC50)
## #   id : vector of indices
## #   xidep : dependent variables (same nb of rows as length of id)
## # returns:
## #   a vector of predictions of length equal to length of id
##   dose<-xidep[,1]
##   e0<-psi[id,1]
##   emax<-psi[id,2]
##   e50<-psi[id,3]
##   f<-e0+emax*dose/(e50+dose)
##   return(f)
## }
##   Nb of parameters: 3
##     parameter names:  E0 Emax EC50
##     distribution:
##       Parameter Distribution Estimated
## [1,] E0          log-normal Estimated
## [2,] Emax        log-normal Estimated
## [3,] EC50        log-normal Estimated
##   Variance-covariance matrix:
##     E0 Emax EC50
## E0    1    0    0
## Emax  0    1    0
## EC50  0    0    1
##   Error model: constant , initial values: a.1=1
##   Covariate model:
##     E0 Emax EC50
## [1,]  0    0    1
##   Initial values
##     E0 Emax EC50
## Pop.CondInit 20  300  20
## Cov.CondInit  0    0    0

# SE not computed as not needed for the test
saemix.options<-list(
  algorithms=c(0,1,1),nb.chains=3,seed=765754,
  nbiter.saemix=c(500,300),save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

fit1<-saemix(model1,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset PD1.saemix
##   Structured data: response ~ dose | subject
##   Predictor: dose (mg)
##   covariates: gender (-)
##   reference class for covariate gender :  0
## Dataset characteristics:
##   number of subjects:      100
##   number of observations: 300

```

```

##      average/min/max nb obs: 3.00 / 3 / 3
## First 10 lines of data:
##      subject dose response gender mdv cens occ ytype
## 1          1    0  11.2870      1  0    0  1    1
## 2          1   10  63.6114      1  0    0  1    1
## 3          1   90 122.9170      1  0    0  1    1
## 4          2    0  15.0514      1  0    0  1    1
## 5          2   10  39.5296      1  0    0  1    1
## 6          2   90  60.8522      1  0    0  1    1
## 7          3    0  25.5390      1  0    0  1    1
## 8          3   10  58.0035      1  0    0  1    1
## 9          3   90  81.1173      1  0    0  1    1
## 10         4    0  22.1446      1  0    0  1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Emax growth model
## Model type: structural
## function(psi,id,xidep) {
## # input:
## #   psi : matrix of parameters (3 columns, E0, Emax, EC50)
## #   id  : vector of indices
## #   xidep : dependent variables (same nb of rows as length of id)
## # returns:
## #   a vector of predictions of length equal to length of id
## dose<-xidep[,1]
## e0<-psi[id,1]
## emax<-psi[id,2]
## e50<-psi[id,3]
## f<-e0+emax*dose/(e50+dose)
## return(f)
## }
## <bytecode: 0x56440c8d8c98>
## Nb of parameters: 3
##   parameter names: E0 Emax EC50
##   distribution:
##   Parameter Distribution Estimated
## [1,] E0          log-normal Estimated
## [2,] Emax        log-normal Estimated
## [3,] EC50        log-normal Estimated
## Variance-covariance matrix:
##   E0 Emax EC50
## E0  1    0    0
## Emax 0    1    0
## EC50 0    0    1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
##           E0 Emax EC50
## Pop.CondInit 20  300  20
## -----
## ---- Key algorithm options ----
## -----

```

```

##      Estimation of individual parameters (MAP)
##      Estimation of standard errors and linearised log-likelihood
##      Estimation of log-likelihood by importance sampling
##      Number of iterations:  K1=500, K2=300
##      Number of chains:  3
##      Seed:  765754
##      Number of MCMC iterations for IS:  5000
##      Simulations:
##          nb of simulated datasets used for npde:  1000
##          nb of simulated datasets used for VPC:  100
##      Input/output
##          save the results to a file:  FALSE
##          save the graphs to files:  FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE   CV(%)
## [1,] E0          23.4   1.08 4.6
## [2,] Emax        107.2   6.09 5.7
## [3,] EC50         15.2   0.77 5.0
## [4,] a.1          4.8   0.42 8.8
## -----
## ----- Variance of random effects -----
## -----
##      Parameter   Estimate SE    CV(%)
## E0  omega2.E0    0.128   0.028 22
## Emax omega2.Emax 0.302   0.045 15
## EC50 omega2.EC50 0.071   0.027 38
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.E0 omega2.Emax omega2.EC50
## omega2.E0    1         0         0
## omega2.Emax  0         1         0
## omega2.EC50  0         0         1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 2463.063
##      AIC = 2477.063
##      BIC = 2495.299
##
## Likelihood computed by importance sampling
##      -2LL= 2466.154
##      AIC = 2480.154
##      BIC = 2498.39
## -----
fit2<-saemix(model2,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----

```

```

## ----- Data -----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset PD1.saemix
## Structured data: response ~ dose | subject
## Predictor: dose (mg)
## covariates: gender (-)
## reference class for covariate gender : 0
## Dataset characteristics:
## number of subjects: 100
## number of observations: 300
## average/min/max nb obs: 3.00 / 3 / 3
## First 10 lines of data:
## subject dose response gender mdv cens occ ytype
## 1 1 0 11.2870 1 0 0 1 1
## 2 1 10 63.6114 1 0 0 1 1
## 3 1 90 122.9170 1 0 0 1 1
## 4 2 0 15.0514 1 0 0 1 1
## 5 2 10 39.5296 1 0 0 1 1
## 6 2 90 60.8522 1 0 0 1 1
## 7 3 0 25.5390 1 0 0 1 1
## 8 3 10 58.0035 1 0 0 1 1
## 9 3 90 81.1173 1 0 0 1 1
## 10 4 0 22.1446 1 0 0 1 1
## -----
## ----- Model -----
## -----
## Nonlinear mixed-effects model
## Model function: Emax growth model
## Model type: structural
## function(psi,id,xidep) {
## # input:
## # psi : matrix of parameters (3 columns, E0, Emax, EC50)
## # id : vector of indices
## # xidep : dependent variables (same nb of rows as length of id)
## # returns:
## # a vector of predictions of length equal to length of id
## dose<-xidep[,1]
## e0<-psi[id,1]
## emax<-psi[id,2]
## e50<-psi[id,3]
## f<-e0+emax*dose/(e50+dose)
## return(f)
## }
## <bytecode: 0x56440c8d8c98>
## Nb of parameters: 3
## parameter names: E0 Emax EC50
## distribution:
## Parameter Distribution Estimated
## [1,] E0 log-normal Estimated
## [2,] Emax log-normal Estimated
## [3,] EC50 log-normal Estimated
## Variance-covariance matrix:

```



```

##      E0 Emax EC50
## E0      1      0      0
## Emax     0      1      0
## EC50     0      0      1
## Error model: constant , initial values: a.1=1
## Covariate model:
##      [,1] [,2] [,3]
## gender     0     0     1
## Initial values
##      E0 Emax EC50
## Pop.CondInit 20 300 20
## Cov.CondInit 0  0  0
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=500, K2=300
## Number of chains: 3
## Seed: 765754
## Number of MCMC iterations for IS: 5000
## Simulations:
##      nb of simulated datasets used for npde: 1000
##      nb of simulated datasets used for VPC: 100
## Input/output
##      save the results to a file: FALSE
##      save the graphs to files: FALSE
## -----
## ---- Results ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter      Estimate SE    CV(%) p-value
## [1,] E0              23.24  1.072  4.6 -
## [2,] Emax            107.20  6.120  5.7 -
## [3,] EC50             11.45  0.980  8.6 -
## [4,] beta_gender(EC50)  0.39  0.099 25.6 4.7e-05
## [5,] a.1              4.72  0.407  8.6 -
## -----
## ----- Variance of random effects -----
## -----
##      Parameter Estimate SE    CV(%)
## E0  omega2.E0  0.129  0.028 22
## Emax omega2.Emax 0.307  0.045 15
## EC50 omega2.EC50 0.052  0.022 43
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.E0 omega2.Emax omega2.EC50
## omega2.E0  1      0      0
## omega2.Emax 0      1      0
## omega2.EC50 0      0      1
## -----

```

```
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 2448.635
##      AIC = 2464.635
##      BIC = 2485.477
##
## Likelihood computed by importance sampling
##      -2LL= 2452.279
##      AIC = 2468.279
##      BIC = 2489.121
## -----
wstat<-(-2)*(fit1["results"]["ll.is"]-fit2["results"]["ll.is"])
cat("LRT test for covariate effect on EC50: p-value=",1-pchisq(wstat,1),"\n")

## LRT test for covariate effect on EC50: p-value= 0.0001954234
```

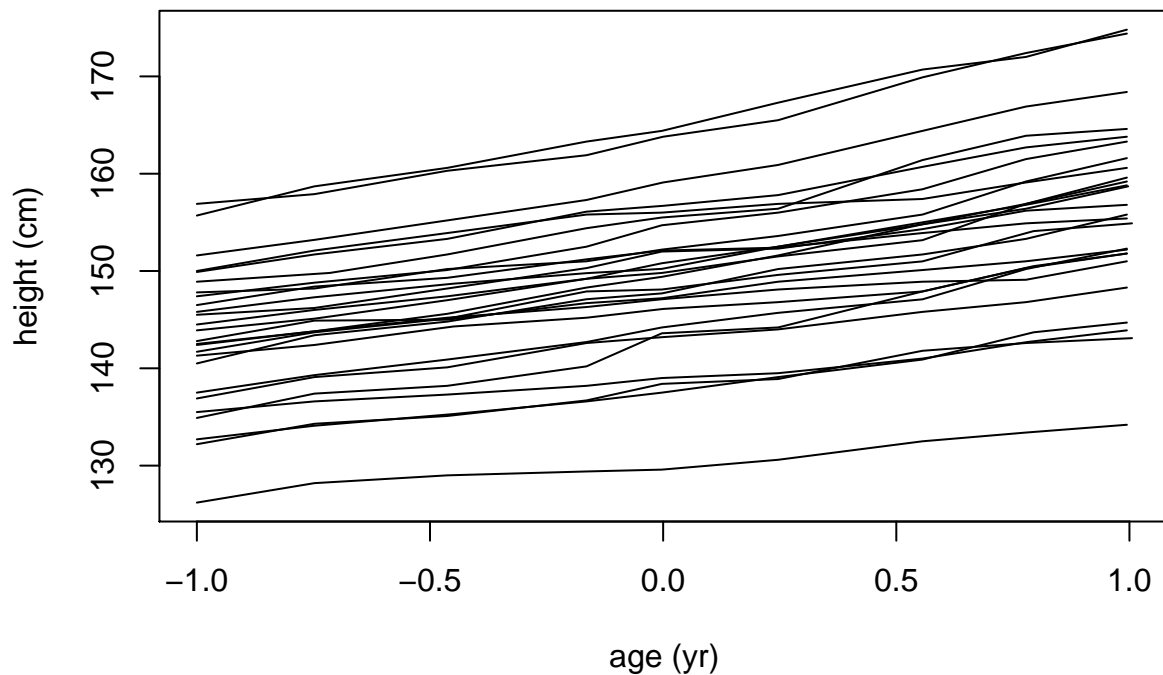
Oxford boys

```
if(testMode)
  data(oxboys.saemix) else
  oxboys.saemix<-read.table(file.path(datDir, "oxboys.saemix.tab"), header=TRUE)

saemix.data<-saemixData(name.data=oxboys.saemix,header=TRUE,
  name.group=c("Subject"),name.predictors=c("age"),name.response=c("height"),
  units=list(x="yr",y="cm"))

##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset oxboys.saemix
##      Structured data: height ~ age | Subject
##      Predictor: age (yr)

# plot the data
plot(saemix.data)
```



```
growth.linear<-function(psi,id,xidep) {
  x<-xidep[,1]
  base<-psi[id,1]
  slope<-psi[id,2]
  f<-base+slope*x
  return(f)
}
saemix.model<-saemixModel(model=growth.linear,description="Linear model",
  psi0=matrix(c(140,1),ncol=2,byrow=TRUE,dimnames=list(NULL,c("base","slope"))),
  transform.par=c(1,0),covariance.model=matrix(c(1,1,1,1),ncol=2,byrow=TRUE),
  error.model="constant")
```

```
##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  Linear model
##   Model type:     structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   base<-psi[id,1]
##   slope<-psi[id,2]
##   f<-base+slope*x
##   return(f)
## }
##   Nb of parameters: 2
##       parameter names:  base slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] base      log-normal      Estimated
```

```

## [2,] slope      normal      Estimated
## Variance-covariance matrix:
##      base slope
## base      1      1
## slope      1      1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
##      base slope
## Pop.CondInit 140      1

saemix.options<-list(algorithms=c(1,1,1),nb.chains=1,seed=201004,
  save=FALSE,save.graphs=FALSE, displayProgress=FALSE)
saemix.fit<-saemix(saemix.model,saemix.data,saemix.options)

## The number of subjects is small, increasing the number of chains to 2 to improve convergence
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset oxboys.saemix
## Structured data: height ~ age | Subject
## Predictor: age (yr)
## Dataset characteristics:
## number of subjects:      26
## number of observations: 234
## average/min/max nb obs: 9.00 / 9 / 9
## First 10 lines of data:
## Subject      age height mdv cens occ ytype
## 1          1 -1.0000 140.5  0   0  1     1
## 2          1 -0.7479 143.4  0   0  1     1
## 3          1 -0.4630 144.8  0   0  1     1
## 4          1 -0.1643 147.1  0   0  1     1
## 5          1 -0.0027 147.7  0   0  1     1
## 6          1  0.2466 150.2  0   0  1     1
## 7          1  0.5562 151.7  0   0  1     1
## 8          1  0.7781 153.3  0   0  1     1
## 9          1  0.9945 155.8  0   0  1     1
## 10         2 -1.0000 136.9  0   0  1     1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Linear model
## Model type: structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   base<-psi[id,1]
##   slope<-psi[id,2]
##   f<-base+slope*x
##   return(f)
## }
## <bytecode: 0x564408cd3d40>

```

```

##   Nb of parameters: 2
##       parameter names:  base slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] base      log-normal  Estimated
## [2,] slope     normal      Estimated
##   Variance-covariance matrix:
##       base slope
## base      1      1
## slope     1      1
##   Error model: constant , initial values: a.1=1
##   No covariate in the model.
##   Initial values
##       base slope
## Pop.CondInit  140      1
## -----
## ----   Key algorithm options   ----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of standard errors and linearised log-likelihood
##   Estimation of log-likelihood by importance sampling
##   Number of iterations:  K1=300, K2=100
##   Number of chains:  2
##   Seed:  201004
##   Number of MCMC iterations for IS:  5000
##   Simulations:
##       nb of simulated datasets used for npde:  1000
##       nb of simulated datasets used for VPC:  100
##   Input/output
##       save the results to a file:  FALSE
##       save the graphs to files:  FALSE
## -----
## ----                               Results                               ----
## -----
## ----- Fixed effects -----
## -----
##       Parameter Estimate SE      CV(%)
## [1,] base      149.16   1.563  1.0
## [2,] slope      6.51   0.331  5.1
## [3,] a.1        0.66   0.035  5.2
## -----
## ----- Variance of random effects -----
## -----
##       Parameter      Estimate SE      CV(%)
## base omega2.base    0.0029  0.00079  28
## slope omega2.slope  2.7361  0.79109  29
## covar cov.base.slope 0.0564  0.02087  37
## -----
## ----- Correlation matrix of random effects -----
## -----
##       omega2.base omega2.slope
## omega2.base  1.00      0.64
## omega2.slope 0.64      1.00
## -----

```

```
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 726.5422
##      AIC = 738.5422
##      BIC = 746.0908
##
## Likelihood computed by importance sampling
##      -2LL= 726.5619
##      AIC = 738.5619
##      BIC = 746.1105
## -----
```

Cow

```
if(testMode)
  data(cow.saemix) else
  cow.saemix<-read.table(file.path(datDir, "cow.saemix.tab"), header=TRUE)

saemix.data<-saemixData(name.data=cow.saemix,header=TRUE,name.group=c("cow"),
  name.predictors=c("time"),name.response=c("weight"),
  name.covariates=c("birthyear","twin","birthrank"),
  units=list(x="days",y="kg",covariates=c("yr","-","-")))

## [1] "birthyear" "twin"      "birthrank"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset cow.saemix
##   Structured data: weight ~ time | cow
##   Predictor: time (days)
##   covariates: birthyear (yr), twin (-), birthrank (-)
##   reference class for covariate twin : 1

growthcow<-function(psi,id,xidep) {
  x<-xidep[,1]
  a<-psi[id,1]
  b<-psi[id,2]
  k<-psi[id,3]
  f<-a*(1-b*exp(-k*x))
  return(f)
}

saemix.model<-saemixModel(model=growthcow,
  description="Exponential growth model",
  psi0=matrix(c(700,0.9,0.02,0,0,0),ncol=3,byrow=TRUE,
    dimnames=list(NULL,c("A","B","k"))),transform.par=c(1,1,1),fixed.estim=c(1,1,1),
  covariate.model=matrix(c(0,0,0),ncol=3,byrow=TRUE),
  covariance.model=matrix(c(1,0,0,0,1,0,0,0,1),ncol=3,byrow=TRUE),
  omega.init=matrix(c(1,0,0,0,1,0,0,0,1),ncol=3,byrow=TRUE),error.model="constant")

##
```

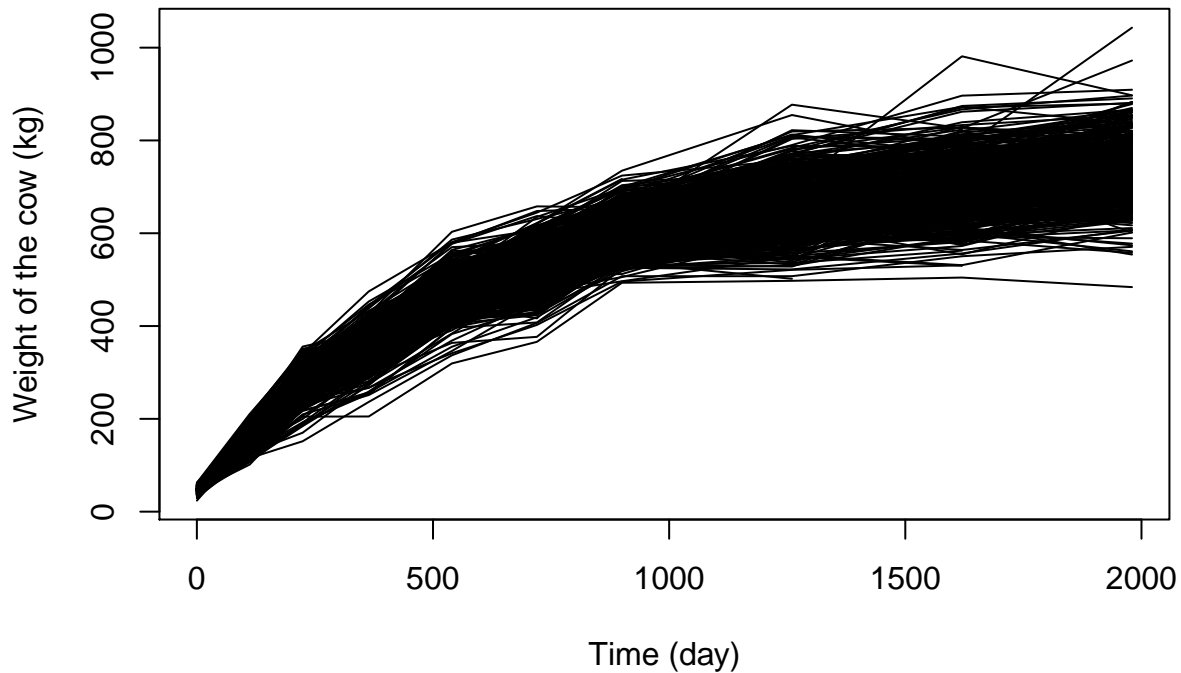
```

##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function: Exponential growth model
##   Model type: structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   a<-psi[id,1]
##   b<-psi[id,2]
##   k<-psi[id,3]
##   f<-a*(1-b*exp(-k*x))
##   return(f)
## }
##   Nb of parameters: 3
##     parameter names:  A B k
##     distribution:
##       Parameter Distribution Estimated
## [1,] A          log-normal Estimated
## [2,] B          log-normal Estimated
## [3,] k          log-normal Estimated
##   Variance-covariance matrix:
##     A B k
## A 1 0 0
## B 0 1 0
## k 0 0 1
##   Error model: constant , initial values: a.1=1
##     No covariate in the model.
##     Initial values
##           A   B   k
## Pop.CondInit 700 0.9 0.02
## Cov.CondInit  0 0.0 0.00

saemix.options<-list(algorithms=c(1,1,1),nb.chains=1,nbiter.saemix=c(200,100),
                     seed=4526,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

# Plotting the data
plot(saemix.data,xlab="Time (day)",ylab="Weight of the cow (kg)")

```



```
saemix.fit<-saemix(saemix.model,saemix.data,saemix.options)
```

```
## Nonlinear mixed-effects model fit by the SAEM algorithm
```

```
## -----
##      Data
## -----
```

```
## Object of class SaemixData
```

```
##   longitudinal data for use with the SAEM algorithm
```

```
## Dataset cow.saemix
```

```
##   Structured data: weight ~ time | cow
```

```
##   Predictor: time (days)
```

```
##   covariates: birthyear (yr), twin (-), birthrank (-)
```

```
##   reference class for covariate twin : 1
```

```
## Dataset characteristics:
```

```
##   number of subjects: 560
```

```
##   number of observations: 5455
```

```
##   average/min/max nb obs: 9.74 / 7 / 10
```

```
## First 10 lines of data:
```

```
##      cow time weight birthyear twin birthrank mdv cens occ ytype
```

## 1	1988005	0	44.0	1988	1	3	0	0	1	1
## 2	1988005	112	173.4	1988	1	3	0	0	1	1
## 3	1988005	224	292.8	1988	1	3	0	0	1	1
## 4	1988005	364	364.6	1988	1	3	0	0	1	1
## 5	1988005	540	490.4	1988	1	3	0	0	1	1
## 6	1988005	720	522.0	1988	1	3	0	0	1	1
## 7	1988005	900	601.1	1988	1	3	0	0	1	1
## 8	1988005	1260	698.1	1988	1	3	0	0	1	1
## 9	1988005	1620	657.7	1988	1	3	0	0	1	1
## 10	1988005	1980	776.7	1988	1	3	0	0	1	1

```
## -----
```



```

## -----      Model      -----
## -----
## Nonlinear mixed-effects model
##   Model function: Exponential growth model
##   Model type: structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   a<-psi[id,1]
##   b<-psi[id,2]
##   k<-psi[id,3]
##   f<-a*(1-b*exp(-k*x))
##   return(f)
## }
## <bytecode: 0x56440e7c2fa0>
##   Nb of parameters: 3
##     parameter names:  A B k
##     distribution:
##     Parameter Distribution Estimated
## [1,] A      log-normal Estimated
## [2,] B      log-normal Estimated
## [3,] k      log-normal Estimated
##   Variance-covariance matrix:
##   A B k
## A 1 0 0
## B 0 1 0
## k 0 0 1
##   Error model: constant , initial values: a.1=1
##   No covariate in the model.
##   Initial values
##           A   B   k
## Pop.CondInit 700 0.9 0.02
## -----
## -----      Key algorithm options      -----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of standard errors and linearised log-likelihood
##   Estimation of log-likelihood by importance sampling
##   Number of iterations:  K1=200, K2=100
##   Number of chains:  1
##   Seed: 4526
##   Number of MCMC iterations for IS: 5000
##   Simulations:
##     nb of simulated datasets used for npde: 1000
##     nb of simulated datasets used for VPC: 100
##   Input/output
##     save the results to a file: FALSE
##     save the graphs to files: FALSE
## -----
## -----      Results      -----
## -----
## -----      Fixed effects      -----
## -----
##   Parameter Estimate SE      CV(%)
## [1,] A      7.5e+02 2.9e+00 0.38

```

```
## [2,] B          9.4e-01  1.2e-03 0.13
## [3,] k          1.6e-03  1.2e-05 0.72
## [4,] a.1        2.7e+01  3.0e-01 1.12
## -----
## ----- Variance of random effects -----
## -----
## Parameter Estimate SE      CV(%)
## A omega2.A  6.4e-03  4.4e-04   7.0
## B omega2.B  4.7e-05  5.2e-05 110.7
## k omega2.k  1.4e-02  1.4e-03   9.8
## -----
## ----- Correlation matrix of random effects -----
## -----
##          omega2.A omega2.B omega2.k
## omega2.A 1          0          0
## omega2.B 0          1          0
## omega2.k 0          0          1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 53732
##      AIC = 53746
##      BIC = 53776.29
##
## Likelihood computed by importance sampling
##      -2LL= 53731.51
##      AIC = 53745.51
##      BIC = 53775.8
## -----
```

Wheat yield

```
if(testMode)
  data(yield.saemix) else
  yield.saemix<-read.table(file.path(datDir, "yield.saemix.tab"), header=TRUE)
saemix.data<-saemixData(name.data=yield.saemix,header=TRUE,name.group=c("site"),
  name.predictors=c("dose"),name.response=c("yield"),
  name.covariates=c("soil.nitrogen"),units=list(x="kg/ha",y="t/ha",covariates=c("kg/ha")))

## [1] "soil.nitrogen"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset yield.saemix
##   Structured data: yield ~ dose | site
##   Predictor: dose (kg/ha)
##   covariates: soil.nitrogen (kg/ha)
```

```

# Model: linear + plateau
yield.LP<-function(psi,id,xidep) {
  x<-xidep[,1]
  ymax<-psi[id,1]
  xmax<-psi[id,2]
  slope<-psi[id,3]
  f<-ymax+slope*(x-xmax)
  #' cat(length(f)," ",length(ymax),"\\n")
  f[x>xmax]<-ymax[x>xmax]
  return(f)
}
saemix.model<-saemixModel(model=yield.LP,description="Linear plus plateau model",
  psi0=matrix(c(8,100,0.2,0,0,0),ncol=3,byrow=TRUE,dimnames=list(NULL,
    c("Ymax","Xmax","slope"))),covariate.model=matrix(c(0,0,0),ncol=3,byrow=TRUE),
  transform.par=c(0,0,0),covariance.model=matrix(c(1,0,0,0,1,0,0,0,1),ncol=3,
    byrow=TRUE),error.model="constant")

```

```

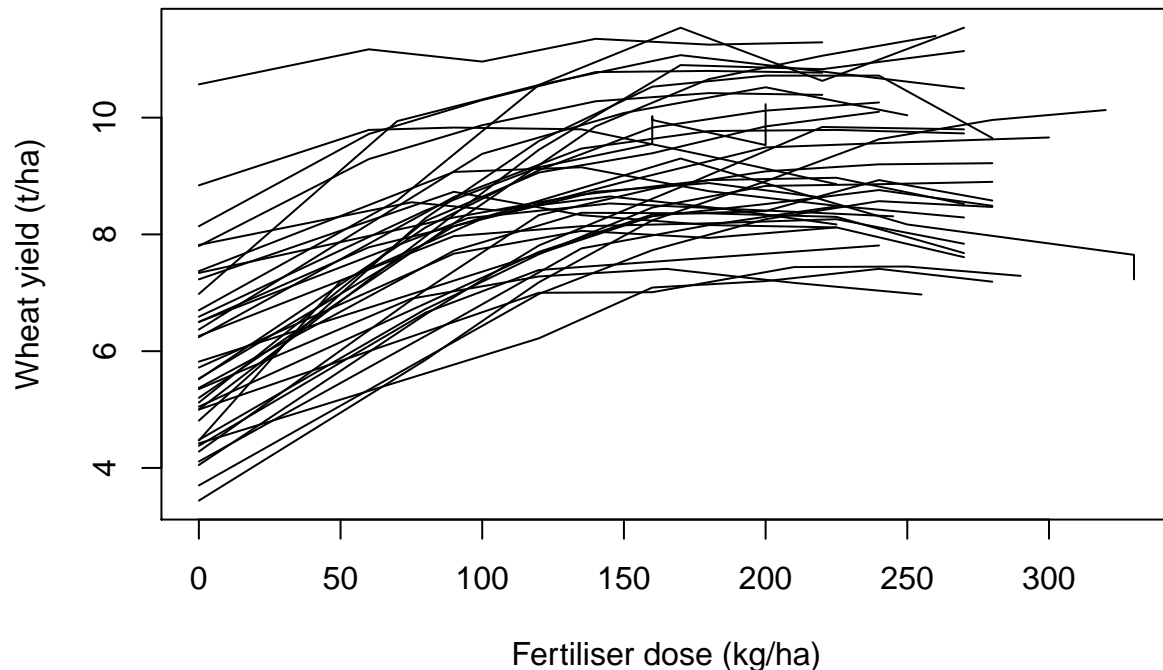
##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  Linear plus plateau model
##   Model type:     structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   ymax<-psi[id,1]
##   xmax<-psi[id,2]
##   slope<-psi[id,3]
##   f<-ymax+slope*(x-xmax)
##   #' cat(length(f)," ",length(ymax),"\\n")
##   f[x>xmax]<-ymax[x>xmax]
##   return(f)
## }
##   Nb of parameters: 3
##       parameter names:  Ymax Xmax slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] Ymax      normal      Estimated
## [2,] Xmax      normal      Estimated
## [3,] slope     normal      Estimated
##   Variance-covariance matrix:
##       Ymax Xmax slope
## Ymax      1    0    0
## Xmax      0    1    0
## slope     0    0    1
##   Error model: constant , initial values: a.1=1
##   No covariate in the model.
##   Initial values
##       Ymax Xmax slope
## Pop.CondInit      8 100  0.2
## Cov.CondInit      0  0  0.0

```

```
saemix.options<-list(algorithms=c(1,1,1),nb.chains=1,seed=666,
  save=FALSE,save.graphs=FALSE, displayProgress=FALSE)
```

```
# Plotting the data
```

```
plot(saemix.data,xlab="Fertiliser dose (kg/ha)", ylab="Wheat yield (t/ha)")
```



```
saemix.fit<-saemix(saemix.model,saemix.data,saemix.options)
```

```
## The number of subjects is small, increasing the number of chains to 2 to improve convergence
## Nonlinear mixed-effects model fit by the SAEM algorithm
```

```
## -----
## ---- Data ----
## -----
```

```
## Object of class SaemixData
```

```
## longitudinal data for use with the SAEM algorithm
```

```
## Dataset yield.saemix
```

```
## Structured data: yield ~ dose | site
```

```
## Predictor: dose (kg/ha)
```

```
## covariates: soil.nitrogen (kg/ha)
```

```
## Dataset characteristics:
```

```
## number of subjects: 37
```

```
## number of observations: 224
```

```
## average/min/max nb obs: 6.05 / 5 / 8
```

```
## First 10 lines of data:
```

```
## site dose yield soil.nitrogen mdv cens occ ytype
## 1 1901 0 6.70 70 0 0 1 1
## 2 1901 70 8.58 70 0 0 1 1
## 3 1901 120 10.56 70 0 0 1 1
## 4 1901 170 11.54 70 0 0 1 1
## 5 1901 220 10.63 70 0 0 1 1
```

```

## 6 1901 270 11.54          70 0 0 1 1
## 7 1902 0 6.98            80 0 0 1 1
## 8 1902 70 9.94           80 0 0 1 1
## 9 1902 120 10.56         80 0 0 1 1
## 10 1902 170 11.07        80 0 0 1 1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Linear plus plateau model
## Model type: structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   ymax<-psi[id,1]
##   xmax<-psi[id,2]
##   slope<-psi[id,3]
##   f<-ymax+slope*(x-xmax)
##   #' cat(length(f)," ",length(ymax),"\\n")
##   f[x>xmax]<-ymax[x>xmax]
##   return(f)
## }
## <bytecode: 0x56440c409800>
## Nb of parameters: 3
##   parameter names: Ymax Xmax slope
##   distribution:
##   Parameter Distribution Estimated
## [1,] Ymax      normal      Estimated
## [2,] Xmax      normal      Estimated
## [3,] slope     normal      Estimated
## Variance-covariance matrix:
##   Ymax Xmax slope
## Ymax   1    0    0
## Xmax   0    1    0
## slope  0    0    1
## Error model: constant , initial values: a.1=1
## No covariate in the model.
## Initial values
##           Ymax Xmax slope
## Pop.CondInit   8 100 0.2
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 2
## Seed: 666
## Number of MCMC iterations for IS: 5000
## Simulations:
##   nb of simulated datasets used for npde: 1000
##   nb of simulated datasets used for VPC: 100
## Input/output
## save the results to a file: FALSE

```

```

##          save the graphs to files: FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] Ymax          8.89  0.176  2.0
## [2,] Xmax         19.75  5.089 25.8
## [3,] slope          0.15  0.037 24.7
## [4,] a.1           0.71  0.041  5.8
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE      CV(%)
## Ymax  omega2.Ymax  1.0e+00  0.2659   25
## Xmax  omega2.Xmax  5.3e+01 38.0311  72
## slope omega2.slope 9.2e-06  0.0018 19486
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.Ymax omega2.Xmax omega2.slope
## omega2.Ymax  1          0          0
## omega2.Xmax  0          1          0
## omega2.slope 0          0          1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 616.5701
##      AIC = 630.5701
##      BIC = 641.8466
##
## Likelihood computed by importance sampling
##      -2LL= 616.5048
##      AIC = 630.5048
##      BIC = 641.7812
## -----
# Comparing the likelihoods obtained by linearisation and importance sampling
# to the likelihood obtained by Gaussian Quadrature
saemix.fit<-llgq.saemix(saemix.fit)
{
  cat("LL by Importance sampling, LL_IS=",saemix.fit["results"]["ll.is"],"\n")
  cat("LL by linearisation, LL_lin=",saemix.fit["results"]["ll.lin"],"\n")
  cat("LL by Gaussian Quadrature, LL_GQ=",saemix.fit["results"]["ll.gq"],"\n")
}

## LL by Importance sampling, LL_IS= -308.2524
## LL by linearisation, LL_lin= -308.2851
## LL by Gaussian Quadrature, LL_GQ= -308.2772
# Testing for an effect of covariate soil.nitrogen on Xmax
saemix.model2<-saemixModel(model=yield.LP,description="Linear plus plateau model",
  psi0=matrix(c(8,100,0.2,0,0,0),ncol=3,byrow=TRUE,dimnames=list(NULL,

```

```

      c("Ymax", "Xmax", "slope"))), covariate.model=matrix(c(0,1,0), ncol=3, byrow=TRUE),
      transform.par=c(0,0,0), covariance.model=matrix(c(1,0,0,0,1,0,0,0,1), ncol=3,
      byrow=TRUE), error.model="constant")

```

```

##
##
## The following SaemixModel object was successfully created:
##

```

```

## Nonlinear mixed-effects model
##   Model function:  Linear plus plateau model
##   Model type:     structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   ymax<-psi[id,1]
##   xmax<-psi[id,2]
##   slope<-psi[id,3]
##   f<-ymax+slope*(x-xmax)
##   #' cat(length(f)," ",length(ymax),"\n")
##   f[x>xmax]<-ymax[x>xmax]
##   return(f)
## }
## <bytecode: 0x56440c409800>
##   Nb of parameters: 3
##       parameter names:  Ymax Xmax slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] Ymax      normal      Estimated
## [2,] Xmax      normal      Estimated
## [3,] slope     normal      Estimated
##   Variance-covariance matrix:
##       Ymax Xmax slope
## Ymax      1    0    0
## Xmax      0    1    0
## slope     0    0    1
##   Error model: constant , initial values: a.1=1
##   Covariate model:
##       Ymax Xmax slope
## [1,]    0    1    0
##   Initial values
##       Ymax Xmax slope
## Pop.CondInit    8 100 0.2
## Cov.CondInit    0  0 0.0

```

```

saemix.fit2<-saemix(saemix.model2,saemix.data,saemix.options)

```

```

## The number of subjects is small, increasing the number of chains to 2 to improve convergence
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset yield.saemix
##   Structured data: yield ~ dose | site

```

```

## Predictor: dose (kg/ha)
## covariates: soil.nitrogen (kg/ha)
## Dataset characteristics:
##   number of subjects:      37
##   number of observations: 224
##   average/min/max nb obs: 6.05 / 5 / 8
## First 10 lines of data:
##   site dose yield soil.nitrogen mdv cens occ ytype
## 1 1901    0 6.70          70  0  0  1    1
## 2 1901   70 8.58          70  0  0  1    1
## 3 1901  120 10.56         70  0  0  1    1
## 4 1901  170 11.54         70  0  0  1    1
## 5 1901  220 10.63         70  0  0  1    1
## 6 1901  270 11.54         70  0  0  1    1
## 7 1902    0 6.98          80  0  0  1    1
## 8 1902   70 9.94          80  0  0  1    1
## 9 1902  120 10.56         80  0  0  1    1
## 10 1902  170 11.07         80  0  0  1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Linear plus plateau model
## Model type: structural
## function(psi,id,xidep) {
##   x<-xidep[,1]
##   ymax<-psi[id,1]
##   xmax<-psi[id,2]
##   slope<-psi[id,3]
##   f<-ymax+slope*(x-xmax)
##   #' cat(length(f)," ",length(ymax),"\\n")
##   f[x>xmax]<-ymax[x>xmax]
##   return(f)
## }
## <bytecode: 0x56440c409800>
## Nb of parameters: 3
##   parameter names: Ymax Xmax slope
##   distribution:
##   Parameter Distribution Estimated
## [1,] Ymax      normal      Estimated
## [2,] Xmax      normal      Estimated
## [3,] slope     normal      Estimated
## Variance-covariance matrix:
##   Ymax Xmax slope
## Ymax   1    0    0
## Xmax   0    1    0
## slope  0    0    1
## Error model: constant , initial values: a.1=1
## Covariate model:
##           [,1] [,2] [,3]
## soil.nitrogen  0    1    0
## Initial values
##           Ymax Xmax slope
## Pop.CondInit  8  100  0.2

```



```

## Cov.CondInit    0    0    0.0
## -----
## ----    Key algorithm options    ----
## -----
##      Estimation of individual parameters (MAP)
##      Estimation of standard errors and linearised log-likelihood
##      Estimation of log-likelihood by importance sampling
##      Number of iterations:  K1=300, K2=100
##      Number of chains:  2
##      Seed:  666
##      Number of MCMC iterations for IS:  5000
##      Simulations:
##          nb of simulated datasets used for npde:  1000
##          nb of simulated datasets used for VPC:  100
##      Input/output
##          save the results to a file:  FALSE
##          save the graphs to files:  FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter              Estimate SE      CV(%) p-value
## [1,] Ymax                   9.184   0.1919  2.1  -
## [2,] Xmax                   218.403  15.7188  7.2  -
## [3,] beta_soil.nitrogen(Xmax) -1.106   0.1715 15.5  5.8e-11
## [4,] slope                   0.026   0.0012  4.7  -
## [5,] a.1                     0.302   0.0192  6.4  -
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE      CV(%)
## Ymax  omega2.Ymax  1.3e+00  3.2e-01 24
## Xmax  omega2.Xmax  1.0e+03  2.9e+02 28
## slope omega2.slope 2.9e-05  1.1e-05 38
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.Ymax  omega2.Xmax  omega2.slope
## omega2.Ymax  1           0           0
## omega2.Xmax  0           1           0
## omega2.slope 0           0           1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 389.099
##      AIC = 405.099
##      BIC = 417.9863
##
## Likelihood computed by importance sampling
##      -2LL= 380.8696
##      AIC = 396.8696
##      BIC = 409.7569

```

```
## -----
# BIC for the two models
{
  cat("Model without covariate, BIC=",saemix.fit["results"]["bic.is"],"\n")
  cat("Model with covariate, BIC=",saemix.fit2["results"]["bic.is"],"\n")
  pval<-1-pchisq(-2*saemix.fit["results"]["ll.is"]+2*saemix.fit2["results"]["ll.is"],1)
  cat("          LRT: p=",pval,"\n")
}

## Model without covariate, BIC= 641.7812
## Model with covariate, BIC= 409.7569
##          LRT: p= 0
```

Exiting

```
if(testMode) {
  dev_mode()
}
```