

Testing examples in saemix 3.0 - discrete models

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Objective

Check saemix for discrete data models

Setup

- set up work directories
- two versions toggled by testMode
 - if testMode is FALSE, load the functions in R
 - if testMode is TRUE, load the library in a dev_mode environment
- aim: check the examples used in the online documentation
 - all examples must run without error

```
if(testMode) cat("Testing package\n") else cat("Loading libraries\n")
```

```
## Loading libraries
```

Testing library

Binary response model

- Toenail data
 - using the full model with 2 random effects (better than with only random effect on intercept according to AIC/BIC)
 - quick diagnostics using a simulation function
- **TODO**
 - add diagnostics (npd-categorical ?)
 - maybe check SE's with package by S. Ueckert

```
if(testMode)
  data(toenail.saemix) else
  toenail.saemix<-read.table(file.path(datDir, "toenail.saemix.tab"), header=TRUE)

saemix.data<-saemixData(name.data=toenail.saemix,name.group=c("id"),name.predictors=c("time","y"), name
                        name.covariates=c("treatment"),name.X=c("time"))
```

```
## [1] "treatment"
```

```
##
```

```
##
```

```
## The following SaemixData object was successfully created:
```

```
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset toenail.saemix
##   Structured data: y ~ time + y | id
##   X variable for graphs: time ()
##   covariates: treatment (-)
##   reference class for covariate treatment : 0

# Explore data
toe1 <- toenail.saemix %>%
  group_by(visit, treatment) %>%
  summarise(nev = sum(y), n=n()) %>%
  mutate(freq = nev/n, sd=sqrt((1-nev/n)/nev)) %>%
  mutate(lower=freq-1.96*sd, upper=freq+1.96*sd)

## `summarise()` has grouped output by 'visit'. You can override using the `.groups` argument.

toe1$lower[toe1$lower<0] <-0 # we should use a better approximation for CI
toe1$treatment <- factor(toe1$treatment, labels=c("A","B"))

plot1<-ggplot(toe1, aes(x=visit, y=freq, group=treatment)) + geom_line(aes(colour=treatment)) +
  geom_point(aes(colour=treatment)) +
  geom_ribbon(aes(ymin=lower, ymax=upper, fill=treatment), alpha=0.2) +
  ylim(c(0,1)) + theme_bw() + theme(legend.position = "top") +
  xlab("Visit number") + ylab("Observed frequency of infection")

# saemix model
binary.model<-function(psi,id,xidep) {
  tim<-xidep[,1]
  y<-xidep[,2]
  inter<-psi[id,1]
  slope<-psi[id,2]
  logit<-inter+slope*tim
  pevent<-exp(logit)/(1+exp(logit))
  logpdf<-rep(0,length(tim))
  P.obs = (y==0)*(1-pevent)+(y==1)*pevent
  logpdf <- log(P.obs)
  return(logpdf)
}

saemix.model<-saemixModel(model=binary.model,description="Binary model",
  modeltype="likelihood",
  psi0=matrix(c(0,-.5,0,0.5),ncol=2,byrow=TRUE,dimnames=list(NULL,c("theta1","theta2"),
  transform.par=c(0,0), covariate.model=c(0,1),covariance.model=matrix(c(1,0,0,1),2,2))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Binary model
## Model type: likelihood
## function(psi,id,xidep) {
##   tim<-xidep[,1]
```

```

## y<-xidep[,2]
## inter<-psi[id,1]
## slope<-psi[id,2]
## logit<-inter+slope*tim
## pevent<-exp(logit)/(1+exp(logit))
## logpdf<-rep(0,length(tim))
## P.obs = (y==0)*(1-pevent)+(y==1)*pevent
## logpdf <- log(P.obs)
## return(logpdf)
## }
## Nb of parameters: 2
## parameter names: theta1 theta2
## distribution:
## Parameter Distribution Estimated
## [1,] theta1 normal Estimated
## [2,] theta2 normal Estimated
## Variance-covariance matrix:
## theta1 theta2
## theta1 1 0
## theta2 0 1
## Covariate model:
## theta1 theta2
## [1,] 0 1
## Initial values
## theta1 theta2
## Pop.CondInit 0 -0.5
## Cov.CondInit 0 0.5

saemix.options<-list(seed=1234567,save=FALSE,save.graphs=FALSE, displayProgress=FALSE, nb.chains=10, fir

# saemix fit
binary.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ---- Data ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset toenail.saemix
## Structured data: y ~ time + y | id
## X variable for graphs: time ()
## covariates: treatment (-)
## reference class for covariate treatment : 0
## Dataset characteristics:
## number of subjects: 294
## number of observations: 1908
## average/min/max nb obs: 6.49 / 1 / 7
## First 10 lines of data:
## id time y y.1 treatment mdv cens occ ytype
## 1 1 0.0000000 1 1 1 0 0 1 1
## 2 1 0.8571429 1 1 1 0 0 1 1
## 3 1 3.5357143 1 1 1 0 0 1 1
## 4 1 4.5357143 0 0 1 0 0 1 1
## 5 1 7.5357143 0 0 1 0 0 1 1

```

```

## 6  1 10.0357143 0  0          1  0  0  1  1
## 7  1 13.0714286 0  0          1  0  0  1  1
## 8  2  0.0000000 0  0          0  0  0  1  1
## 9  2  0.9642857 0  0          0  0  0  1  1
## 10 2  2.0000000 1  1          0  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
##   Model function:  Binary model
##   Model type:    likelihood
## function(psi,id,xidep) {
##   tim<-xidep[,1]
##   y<-xidep[,2]
##   inter<-psi[id,1]
##   slope<-psi[id,2]
##   logit<-inter+slope*tim
##   pevent<-exp(logit)/(1+exp(logit))
##   logpdf<-rep(0,length(tim))
##   P.obs = (y==0)*(1-pevent)+(y==1)*pevent
##   logpdf <- log(P.obs)
##   return(logpdf)
## }
## <bytecode: 0x55e9dd526cd0>
##   Nb of parameters: 2
##       parameter names:  theta1 theta2
##       distribution:
##       Parameter Distribution Estimated
## [1,] theta1    normal      Estimated
## [2,] theta2    normal      Estimated
##   Variance-covariance matrix:
##       theta1 theta2
## theta1      1      0
## theta2      0      1
##   Covariate model:
##       [,1] [,2]
## treatment  0   1
##   Initial values
##       theta1 theta2
## Pop.CondInit    0  -0.5
## Cov.CondInit    0   0.5
## -----
## ----   Key algorithm options   ----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of log-likelihood by importance sampling
##   Number of iterations:  K1=300, K2=100
##   Number of chains:    10
##   Seed: 1234567
##   Number of MCMC iterations for IS: 5000
##   Simulations:
##       nb of simulated datasets used for npde: 1000
##       nb of simulated datasets used for VPC: 100
##   Input/output

```

```

##          save the results to a file: FALSE
##          save the graphs to files: FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter          Estimate
## [1,] theta1             -2.20
## [2,] theta2             -1.25
## [3,] beta_treatment(theta2) -0.47
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate
## theta1 omega2.theta1 59.3
## theta2 omega2.theta2  1.1
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.theta1 omega2.theta2
## omega2.theta1 1      0
## omega2.theta2 0      1
## -----
## ----- Statistical criteria -----
## -----
##
## Likelihood computed by importance sampling
##      -2LL= 1116.755
##      AIC = 1128.755
##      BIC = 1150.856
## -----

# simulate from model (nsim=100)
simulBinary<-function(psi,id,xidep) {
  tim<-xidep[,1]
  y<-xidep[,2]
  inter<-psi[id,1]
  slope<-psi[id,2]
  logit<-inter+slope*tim
  pevent<-1/(1+exp(-logit))
  ysim<-rbinom(length(tim),size=1, prob=pevent)
  return(ysim)
}

yfit<-binary.fit
nsim<-100
yfit <- simulateDiscreteSaemix(yfit, simulBinary, nsim=nsim)
simdat <-yfit@sim.data@datasim
simdat$visit<-rep(toenail.saemix$visit,nsim)
simdat$treatment<-rep(toenail.saemix$treatment,nsim)

# VPC-type diagnostic
ytab<-NULL

```

```
for(irep in 1:nsim) {
  xtab<-simdat[simdat$irep==irep,]
  xtab1 <- xtab %>%
    group_by(visit, treatment) %>%
    summarise(nev = sum(ysim), n=n()) %>%
    mutate(freq = nev/n)
  ytab<-rbind(ytab,xtab1[,c("visit", "freq", "treatment")])
}
```

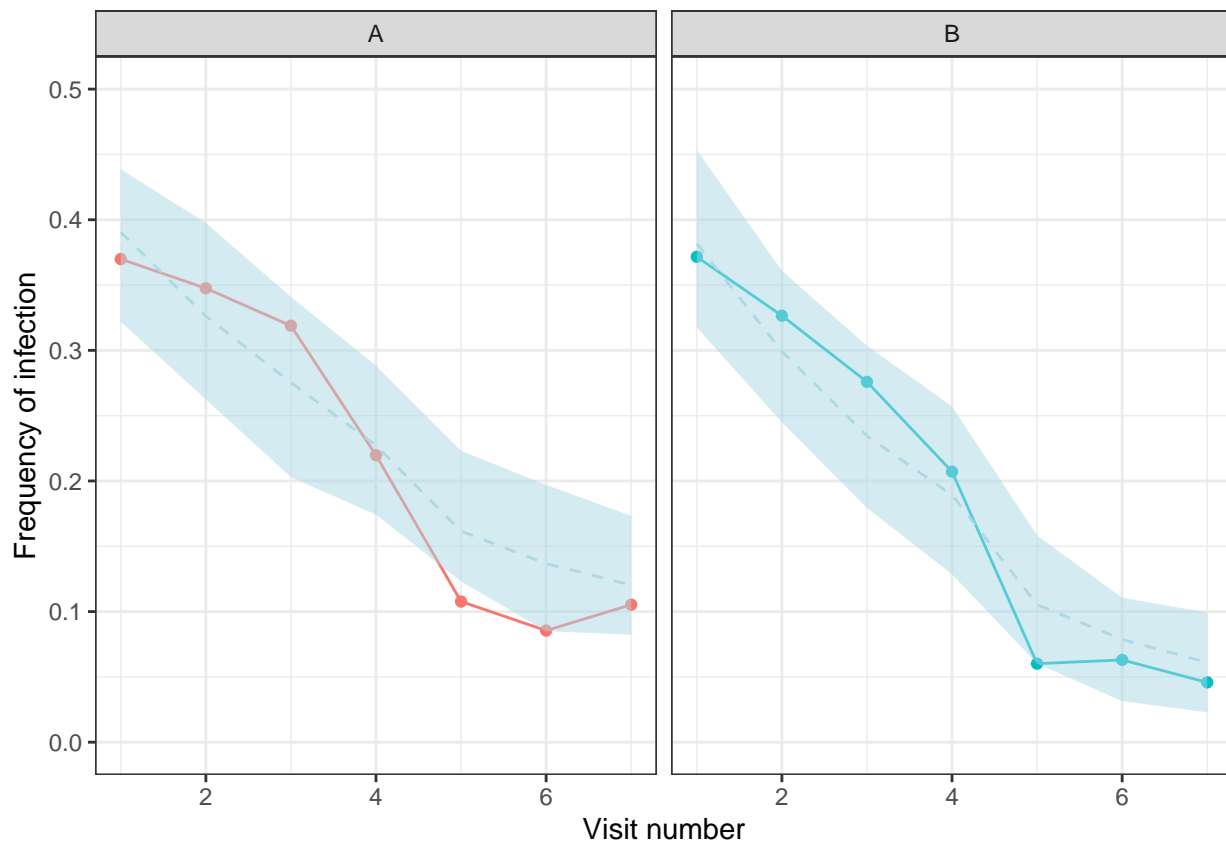
[illegible]


```
## `summarise()` has grouped output by 'visit'. You can override using the `.groups` argument.
gtab <- ytab %>%
  group_by(visit, treatment) %>%
  summarise(lower=quantile(freq, c(0.05)), median=quantile(freq, c(0.5)), upper=quantile(freq, c(0.95)),
    mutate(treatment=ifelse(treatment==1,"B","A"))

## `summarise()` has grouped output by 'visit'. You can override using the `.groups` argument.
gtab$freq<-1

plot2 <- ggplot(toe1, aes(x=visit, y=freq, group=treatment)) + geom_line(aes(colour=treatment)) +
  geom_point(aes(colour=treatment)) +
  geom_line(data=gtab, aes(x=visit, y=median), linetype=2, colour='lightblue') +
  geom_ribbon(data=gtab, aes(ymin=lower, ymax=upper), alpha=0.5, fill='lightblue') +
  ylim(c(0,0.5)) + theme_bw() + theme(legend.position = "none") + facet_wrap(~treatment) +
  xlab("Visit number") + ylab("Frequency of infection")

print(plot2)
```



Categorical response model

- Knee pain after 3, 7 and 10 days of treatment compared to baseline (time=0)
 - longitudinal ordinal model with 5 categories
 - similar results to Monolix in terms of parameter estimates
 - SE don't seem so off, but still higher than Monolix (but computed with linearisation anyway)
- Comparing the 3 covariate models - model with Age on alp1 and treatment on beta best


```

if(testMode)
  data(knee.saemix) else
    knee.saemix<-read.table(file.path(datDir, "knee.saemix.tab"), header=TRUE)

# Data
saemix.data<-saemixData(name.data=knee.saemix,name.group=c("id"),
                        name.predictors=c("y", "time"), name.X=c("time"),
                        name.covariates = c("Age","Sex","treatment","Age2"),
                        units=list(x="d",y="", covariates=c("yr","-","-", "yr2")))

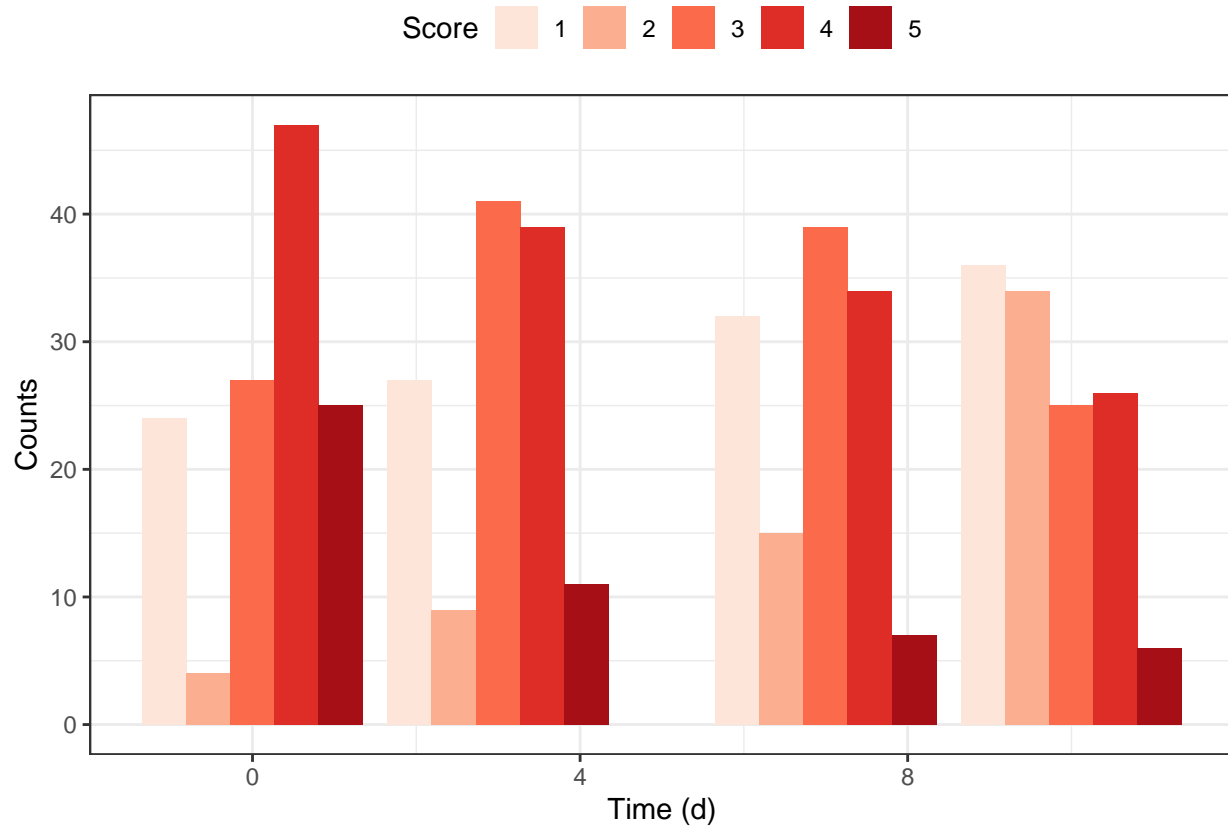
## Column name(s) do(es) not exist in the dataset, please check
## Remove columns 1 ( )
## No valid name given, attempting automatic recognition
## Automatic recognition of columns y successful
## [1] "Age"      "Sex"      "treatment" "Age2"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset knee.saemix
##   Structured data: y ~ y + time | id
##   X variable for graphs: time (d)
##   covariates: Age (yr), Sex (-), treatment (-), Age2 (yr2)
##   reference class for covariate Sex : 0
##   reference class for covariate treatment : 0

gtab <- knee.saemix %>%
  group_by(time, y) %>%
  summarise(n=length(y)) %>%
  mutate(y=as.factor(y))

## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.

ggplot(data = gtab, aes(x = time, y=n, group=y, fill=y)) +
  geom_bar(stat="identity", position = "dodge") + theme_bw() +
  scale_fill_brewer(palette = "Reds") + theme(legend.position = "top") +
  labs(fill = "Score" ) + xlab("Time (d)") + ylab("Counts")

```



```
# Model for ordinal responses
ordinal.model<-function(psi,id,xidep) {
  y<-xidep[,1]
  time<-xidep[,2]
  alp1<-psi[id,1]
  alp2<-psi[id,2]
  alp3<-psi[id,3]
  alp4<-psi[id,4]
  beta<-psi[id,5]

  logit1<-alp1 + beta*time
  logit2<-logit1+alp2
  logit3<-logit2+alp3
  logit4<-logit3+alp4
  pge1<-exp(logit1)/(1+exp(logit1))
  pge2<-exp(logit2)/(1+exp(logit2))
  pge3<-exp(logit3)/(1+exp(logit3))
  pge4<-exp(logit4)/(1+exp(logit4))
  pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
  logpdf <- log(pobs)

  return(logpdf)
}

# Fitting
covmodel2<-covmodel1<-matrix(data=0,ncol=5,nrow=4)
covmodel1[,1]<-1
```

```

covmodel1[,5]<-1
covmodel2[3,5]<-covmodel2[4,1]<-1

saemix.model<-saemixModel(model=ordinal.model,description="Ordinal categorical model",modeltype="likelihood",
                           psi0=matrix(c(0,0.2, 0.6, 3, 0.2),ncol=5,byrow=TRUE,dimnames=list(NULL,c("alp1","alp2","alp3","alp4","beta")),
                           transform.par=c(0,1,1,1,1),omega.init=diag(rep(1,5)), covariance.model = diag(5,1))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Ordinal categorical model
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,1]
##   time<-xidep[,2]
##   alp1<-psi[id,1]
##   alp2<-psi[id,2]
##   alp3<-psi[id,3]
##   alp4<-psi[id,4]
##   beta<-psi[id,5]
##
##   logit1<-alp1 + beta*time
##   logit2<-logit1+alp2
##   logit3<-logit2+alp3
##   logit4<-logit3+alp4
##   pge1<-exp(logit1)/(1+exp(logit1))
##   pge2<-exp(logit2)/(1+exp(logit2))
##   pge3<-exp(logit3)/(1+exp(logit3))
##   pge4<-exp(logit4)/(1+exp(logit4))
##   pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
##   logpdf <- log(pobs)
##
##   return(logpdf)
## }
## Nb of parameters: 5
##   parameter names: alp1 alp2 alp3 alp4 beta
##   distribution:
##   Parameter Distribution Estimated
## [1,] alp1      normal      Estimated
## [2,] alp2      log-normal   Estimated
## [3,] alp3      log-normal   Estimated
## [4,] alp4      log-normal   Estimated
## [5,] beta      log-normal   Estimated
## Variance-covariance matrix:
##   alp1 alp2 alp3 alp4 beta
## alp1  1    0    0    0    0
## alp2  0    0    0    0    0
## alp3  0    0    0    0    0
## alp4  0    0    0    0    0
## beta  0    0    0    0    1
## No covariate in the model.
## Initial values

```

```

##          alp1 alp2 alp3 alp4 beta
## Pop.CondInit    0 0.2 0.6   3 0.2

saemix.model.cov1<-saemixModel(model=ordinal.model,description="Ordinal categorical model",modeltype="1",
                                psi0=matrix(c(0,0.2, 0.6, 3, 0.2),ncol=5,byrow=TRUE,dimnames=list(NULL,c(
                                transform.par=c(0,1,1,1,1),omega.init=diag(rep(1,5))), covariance.model = c(
                                covariate.model = covmodel1)

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function: Ordinal categorical model
##   Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,1]
##   time<-xidep[,2]
##   alp1<-psi[id,1]
##   alp2<-psi[id,2]
##   alp3<-psi[id,3]
##   alp4<-psi[id,4]
##   beta<-psi[id,5]
##
##   logit1<-alp1 + beta*time
##   logit2<-logit1+alp2
##   logit3<-logit2+alp3
##   logit4<-logit3+alp4
##   pge1<-exp(logit1)/(1+exp(logit1))
##   pge2<-exp(logit2)/(1+exp(logit2))
##   pge3<-exp(logit3)/(1+exp(logit3))
##   pge4<-exp(logit4)/(1+exp(logit4))
##   pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
##   logpdf <- log(pobs)
##
##   return(logpdf)
## }
##   Nb of parameters: 5
##       parameter names: alp1 alp2 alp3 alp4 beta
##       distribution:
##       Parameter Distribution Estimated
## [1,] alp1      normal      Estimated
## [2,] alp2      log-normal   Estimated
## [3,] alp3      log-normal   Estimated
## [4,] alp4      log-normal   Estimated
## [5,] beta      log-normal   Estimated
##   Variance-covariance matrix:
##       alp1 alp2 alp3 alp4 beta
## alp1    1    0    0    0    0
## alp2    0    0    0    0    0
## alp3    0    0    0    0    0
## alp4    0    0    0    0    0
## beta    0    0    0    0    1
##   Covariate model:
##       alp1 alp2 alp3 alp4 beta

```

```

## [1,] 1 0 0 0 1
## [2,] 1 0 0 0 1
## [3,] 1 0 0 0 1
## [4,] 1 0 0 0 1
## Initial values
## alp1 alp2 alp3 alp4 beta
## Pop.CondInit 0 0.2 0.6 3 0.2
## Cov.CondInit 0 0.0 0.0 0 0.0

saemix.model.cov2<-saemixModel(model=ordinal.model,description="Ordinal categorical model",modeltype="1",
                                psi0=matrix(c(0,0.2, 0.6, 3, 0.2),ncol=5,byrow=TRUE,dimnames=list(NULL,c(
                                transform.par=c(0,1,1,1,1),omega.init=diag(rep(1,5))), covariance.model =
                                covariate.model = covmodel2)

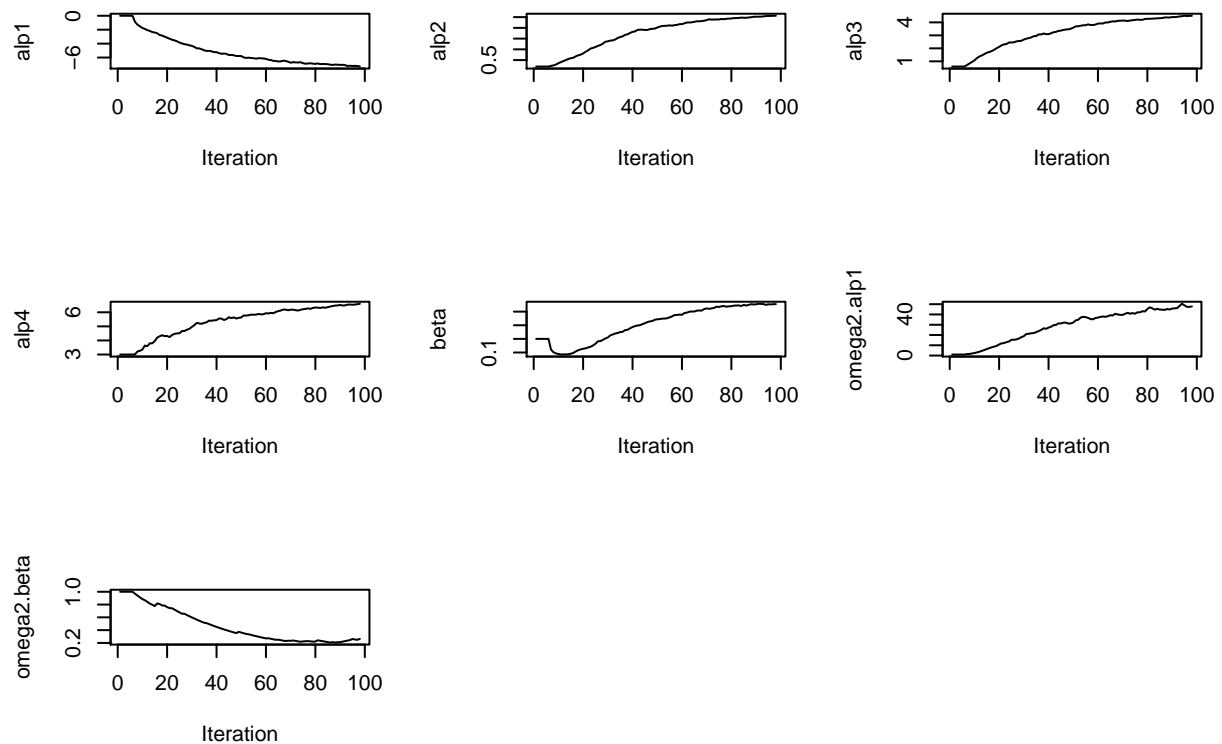
##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Ordinal categorical model
## Model type: likelihood
## function(psi,id,xidep) {
## y<-xidep[,1]
## time<-xidep[,2]
## alp1<-psi[id,1]
## alp2<-psi[id,2]
## alp3<-psi[id,3]
## alp4<-psi[id,4]
## beta<-psi[id,5]
##
## logit1<-alp1 + beta*time
## logit2<-logit1+alp2
## logit3<-logit2+alp3
## logit4<-logit3+alp4
## pge1<-exp(logit1)/(1+exp(logit1))
## pge2<-exp(logit2)/(1+exp(logit2))
## pge3<-exp(logit3)/(1+exp(logit3))
## pge4<-exp(logit4)/(1+exp(logit4))
## pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
## logpdf <- log(pobs)
##
## return(logpdf)
## }
## Nb of parameters: 5
## parameter names: alp1 alp2 alp3 alp4 beta
## distribution:
## Parameter Distribution Estimated
## [1,] alp1 normal Estimated
## [2,] alp2 log-normal Estimated
## [3,] alp3 log-normal Estimated
## [4,] alp4 log-normal Estimated
## [5,] beta log-normal Estimated
## Variance-covariance matrix:
## alp1 alp2 alp3 alp4 beta
## alp1 1 0 0 0 0

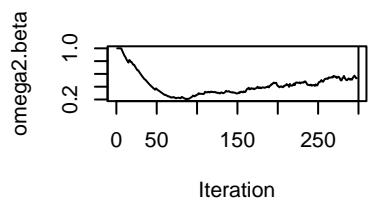
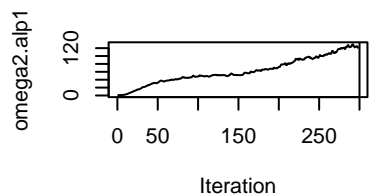
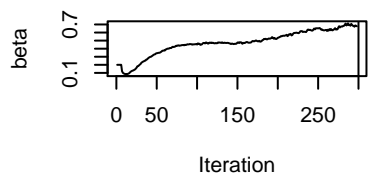
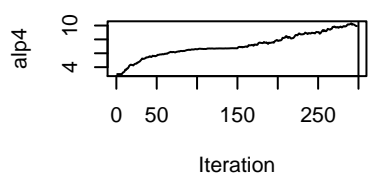
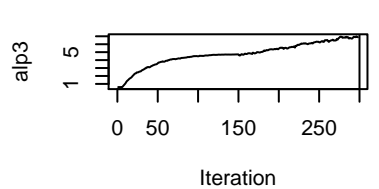
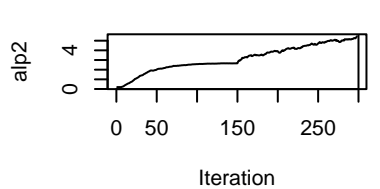
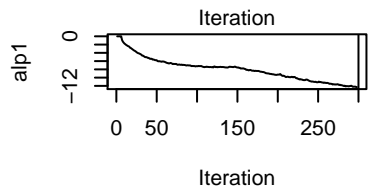
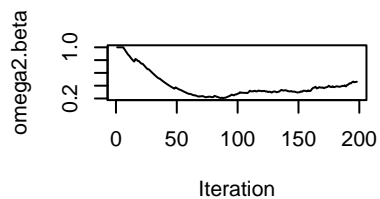
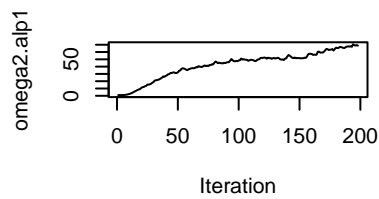
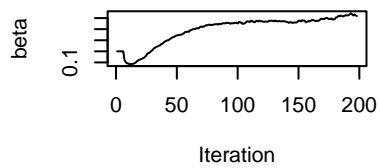
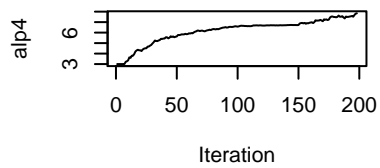
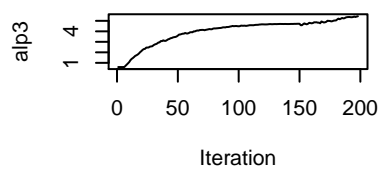
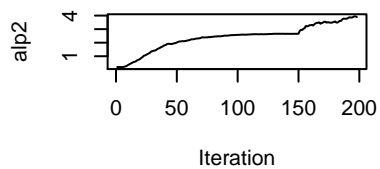
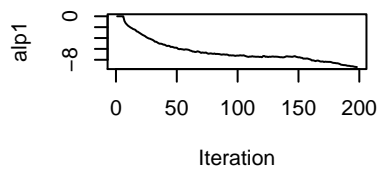
```

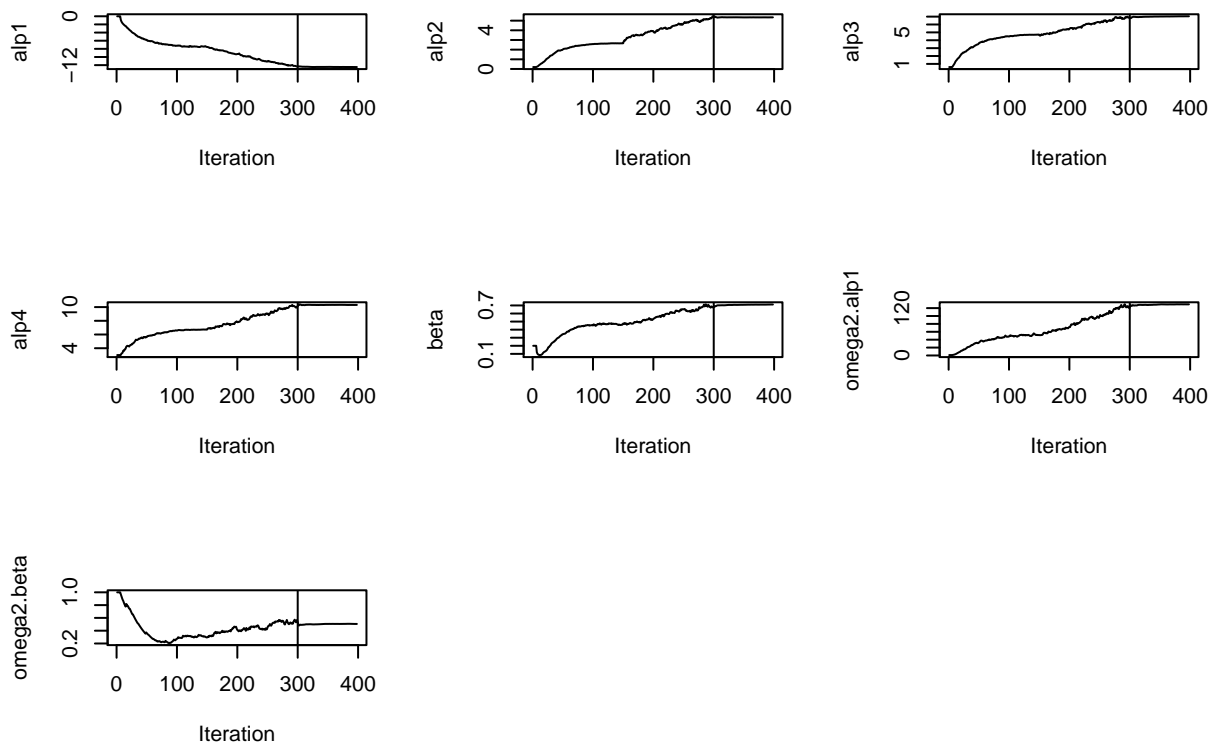
```
## alp2    0    0    0    0    0
## alp3    0    0    0    0    0
## alp4    0    0    0    0    0
## beta    0    0    0    0    1
## Covariate model:
##      alp1 alp2 alp3 alp4 beta
## [1,]    0    0    0    0    0
## [2,]    0    0    0    0    0
## [3,]    0    0    0    0    1
## [4,]    1    0    0    0    0
##      Initial values
##      alp1 alp2 alp3 alp4 beta
## Pop.CondInit    0 0.2 0.6  3 0.2
## Cov.CondInit    0 0.0 0.0  0 0.0
```

```
saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, nb.chains=10)
#saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, nb.chains=10, fim=FALSE)
```

```
ord.fit<-saemix(saemix.model,saemix.data,saemix.options)
```







```
## Error in solve.default(F0) :
##   le système est numériquement singulier : conditionnement de la réciproque = 3.8767e-17
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ---- Data ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset knee.saemix
##   Structured data: y ~ y + time | id
##   X variable for graphs: time (d)
##   covariates: Age (yr), Sex (-), treatment (-), Age2 (yr2)
##   reference class for covariate Sex : 0
##   reference class for covariate treatment : 0
## Dataset characteristics:
##   number of subjects: 127
##   number of observations: 508
##   average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
##   id y time y.1 Age Sex treatment Age2 mdv cens occ ytype
## 1 1 4 0 4 -2 1 0 4 0 0 1 1
## 2 1 4 3 4 -2 1 0 4 0 0 1 1
## 3 1 4 7 4 -2 1 0 4 0 0 1 1
## 4 1 4 10 4 -2 1 0 4 0 0 1 1
## 5 2 4 0 4 2 1 0 4 0 0 1 1
## 6 2 4 3 4 2 1 0 4 0 0 1 1
## 7 2 4 7 4 2 1 0 4 0 0 1 1
## 8 2 4 10 4 2 1 0 4 0 0 1 1
## 9 3 3 0 3 11 1 0 121 0 0 1 1
## 10 3 3 3 3 11 1 0 121 0 0 1 1
```



```

## -----
## -----      Model      -----
## -----
## Nonlinear mixed-effects model
##   Model function: Ordinal categorical model
##   Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,1]
##   time<-xidep[,2]
##   alp1<-psi[id,1]
##   alp2<-psi[id,2]
##   alp3<-psi[id,3]
##   alp4<-psi[id,4]
##   beta<-psi[id,5]
##
##   logit1<-alp1 + beta*time
##   logit2<-logit1+alp2
##   logit3<-logit2+alp3
##   logit4<-logit3+alp4
##   pge1<-exp(logit1)/(1+exp(logit1))
##   pge2<-exp(logit2)/(1+exp(logit2))
##   pge3<-exp(logit3)/(1+exp(logit3))
##   pge4<-exp(logit4)/(1+exp(logit4))
##   pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
##   logpdf <- log(pobs)
##
##   return(logpdf)
## }
## <bytecode: 0x55e9ded79f10>
##   Nb of parameters: 5
##     parameter names: alp1 alp2 alp3 alp4 beta
##     distribution:
##     Parameter Distribution Estimated
## [1,] alp1      normal      Estimated
## [2,] alp2      log-normal   Estimated
## [3,] alp3      log-normal   Estimated
## [4,] alp4      log-normal   Estimated
## [5,] beta      log-normal   Estimated
##   Variance-covariance matrix:
##     alp1 alp2 alp3 alp4 beta
## alp1    1    0    0    0    0
## alp2    0    0    0    0    0
## alp3    0    0    0    0    0
## alp4    0    0    0    0    0
## beta    0    0    0    0    1
##   No covariate in the model.
##   Initial values
##           alp1 alp2 alp3 alp4 beta
## Pop.CondInit    0 0.2 0.6   3 0.2
## -----
## -----   Key algorithm options   -----
## -----
##     Estimation of individual parameters (MAP)
##     Estimation of standard errors and linearised log-likelihood

```

```

## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 10
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##     nb of simulated datasets used for npde: 1000
##     nb of simulated datasets used for VPC: 100
## Input/output
##     save the results to a file: FALSE
##     save the graphs to files: FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
## Parameter Estimate SE CV(%)
## [1,] alp1 -12.47 1.96 16
## [2,] alp2 5.34 1.93 36
## [3,] alp3 7.05 1.56 22
## [4,] alp4 10.31 3.03 29
## [5,] beta 0.71 0.15 22
## -----
## ----- Variance of random effects -----
## -----
## Parameter Estimate SE CV(%)
## alp1 omega2.alp1 129.61 NA NA
## beta omega2.beta 0.51 NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
## omega2.alp1 omega2.beta
## omega2.alp1 1 0
## omega2.beta 0 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
## -2LL= 5970.576
## AIC = 5986.576
## BIC = 6009.33
##
## Likelihood computed by importance sampling
## -2LL= 864.4609
## AIC = 880.4609
## BIC = 903.2144
## -----
ord.fit.cov1<-saemix(saemix.model.cov1,saemix.data,saemix.options)

## Error in plot.new() : figure margins too large
## Error in plot.new() : figure margins too large
## Error in plot.new() : figure margins too large

```

```

## Error in plot.new() : figure margins too large
## Error in solve.default(F0) :
## routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset knee.saemix
## Structured data: y ~ y + time | id
## X variable for graphs: time (d)
## covariates: Age (yr), Sex (-), treatment (-), Age2 (yr2)
## reference class for covariate Sex : 0
## reference class for covariate treatment : 0
## Dataset characteristics:
## number of subjects: 127
## number of observations: 508
## average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
## id y time y.1 Age Sex treatment Age2 mdv cens occ ytype
## 1 1 4 0 4 -2 1 0 4 0 0 1 1
## 2 1 4 3 4 -2 1 0 4 0 0 1 1
## 3 1 4 7 4 -2 1 0 4 0 0 1 1
## 4 1 4 10 4 -2 1 0 4 0 0 1 1
## 5 2 4 0 4 2 1 0 4 0 0 1 1
## 6 2 4 3 4 2 1 0 4 0 0 1 1
## 7 2 4 7 4 2 1 0 4 0 0 1 1
## 8 2 4 10 4 2 1 0 4 0 0 1 1
## 9 3 3 0 3 11 1 0 121 0 0 1 1
## 10 3 3 3 3 11 1 0 121 0 0 1 1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Ordinal categorical model
## Model type: likelihood
## function(psi,id,xidep) {
## y<-xidep[,1]
## time<-xidep[,2]
## alp1<-psi[id,1]
## alp2<-psi[id,2]
## alp3<-psi[id,3]
## alp4<-psi[id,4]
## beta<-psi[id,5]
##
## logit1<-alp1 + beta*time
## logit2<-logit1+alp2
## logit3<-logit2+alp3
## logit4<-logit3+alp4
## pge1<-exp(logit1)/(1+exp(logit1))
## pge2<-exp(logit2)/(1+exp(logit2))
## pge3<-exp(logit3)/(1+exp(logit3))
## pge4<-exp(logit4)/(1+exp(logit4))

```

```

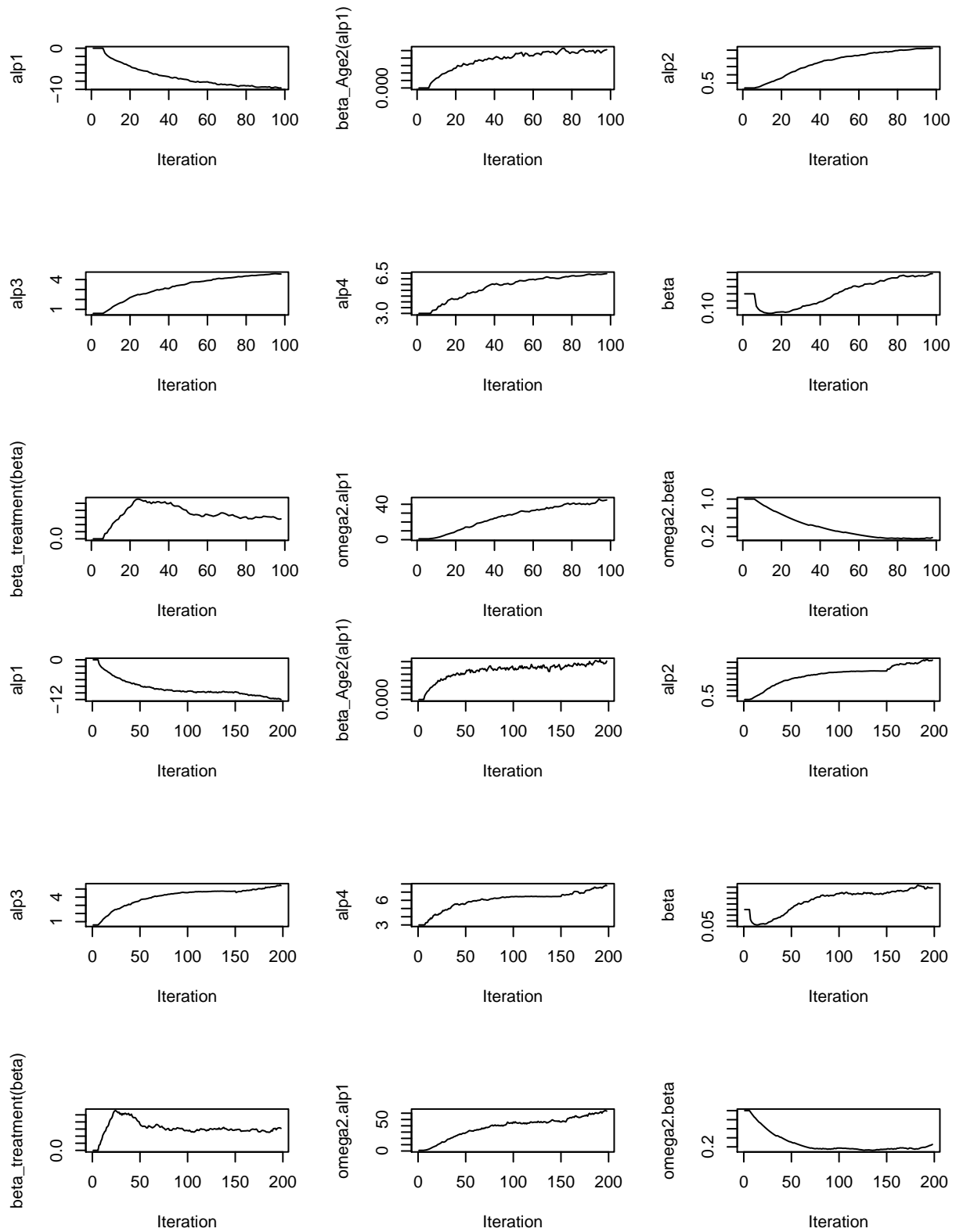
## pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
## logpdf <- log(pobs)
##
## return(logpdf)
## }
## <bytecode: 0x55e9ded79f10>
## Nb of parameters: 5
##      parameter names:  alp1 alp2 alp3 alp4 beta
##      distribution:
##      Parameter Distribution Estimated
## [1,] alp1      normal      Estimated
## [2,] alp2      log-normal   Estimated
## [3,] alp3      log-normal   Estimated
## [4,] alp4      log-normal   Estimated
## [5,] beta      log-normal   Estimated
## Variance-covariance matrix:
##      alp1 alp2 alp3 alp4 beta
## alp1    1    0    0    0    0
## alp2    0    0    0    0    0
## alp3    0    0    0    0    0
## alp4    0    0    0    0    0
## beta    0    0    0    0    1
## Covariate model:
##      [,1] [,2] [,3] [,4] [,5]
## Age      1    0    0    0    1
## Sex      1    0    0    0    1
## treatment 1    0    0    0    1
## Age2     1    0    0    0    1
## Initial values
##      alp1 alp2 alp3 alp4 beta
## Pop.CondInit    0 0.2 0.6  3 0.2
## Cov.CondInit    0 0.0 0.0  0 0.0
## psi1            0 0.0 0.0  0 0.0
## psi1            0 0.0 0.0  0 0.0
## psi1            0 0.0 0.0  0 0.0
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 10
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##      nb of simulated datasets used for npde: 1000
##      nb of simulated datasets used for VPC: 100
## Input/output
##      save the results to a file: FALSE
##      save the graphs to files: FALSE
## -----
## ---- Results ----
## -----

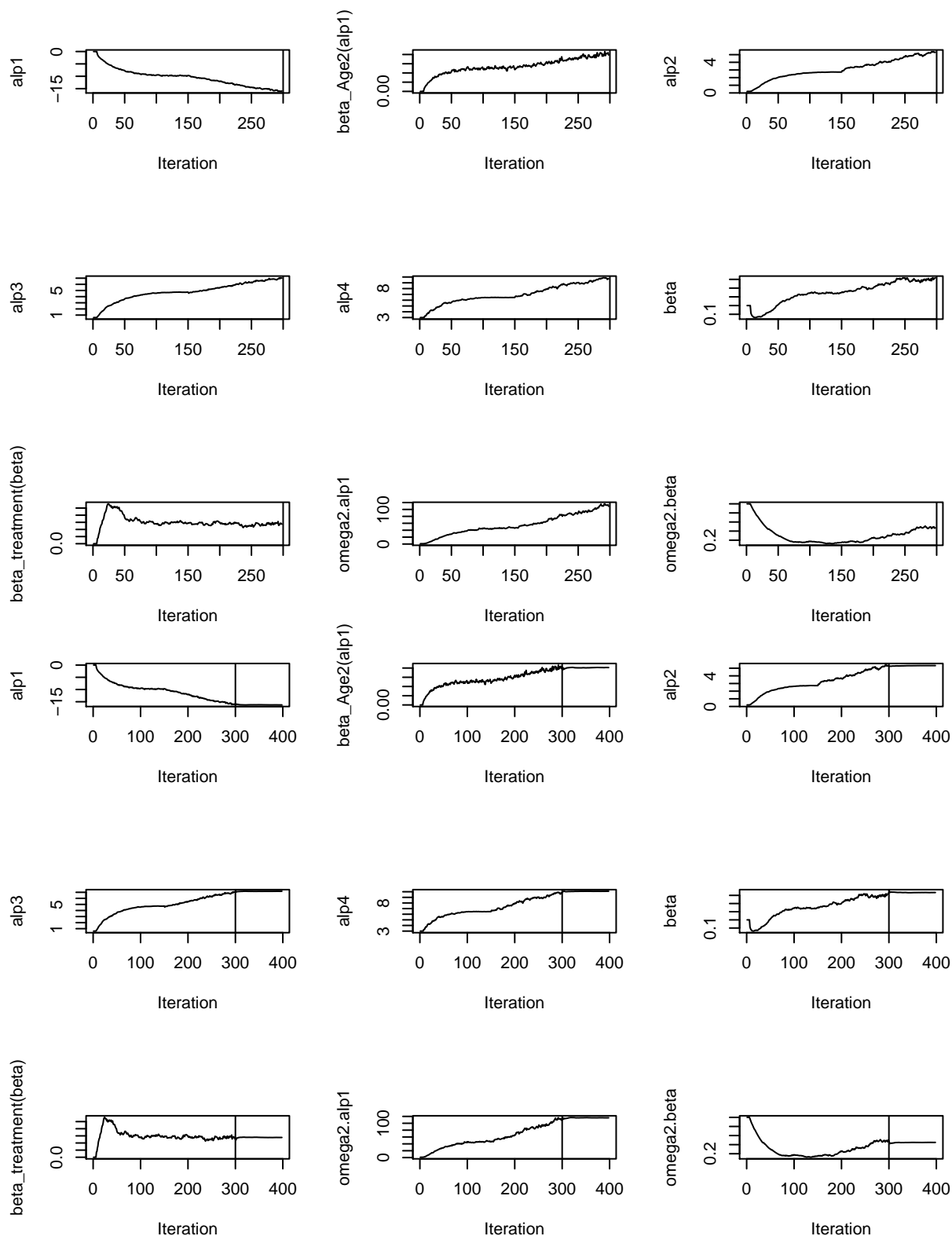
```

```

## ----- Fixed effects -----
## -----
##      Parameter      Estimate SE      CV(%) p-value
## [1,] alp1          -1.6e+01 3.4778   22   -
## [2,] beta_Age(alp1)  1.2e-01 0.1171   95  0.146
## [3,] beta_Sex(alp1) -6.9e-01 2.5495  370  0.394
## [4,] beta_treatment(alp1) 1.7e+00 2.1382  124  0.210
## [5,] beta_Age2(alp1)  3.4e-02 0.0166   49  0.021
## [6,] alp2          5.2e+00 1.8170   35   -
## [7,] alp3          6.9e+00 1.5416   22   -
## [8,] alp4          9.8e+00 2.8741   29   -
## [9,] beta          4.8e-01 0.2935   61   -
## [10,] beta_Age(beta) -1.6e-02 0.0229  142  0.240
## [11,] beta_Sex(beta)  3.4e-02 0.4957 1446  0.472
## [12,] beta_treatment(beta) 5.1e-01 0.4301   85  0.119
## [13,] beta_Age2(beta)  7.4e-04 0.0028  381  0.397
## -----
## ----- Variance of random effects -----
## -----
##      Parameter  Estimate SE CV(%)
## alp1 omega2.alp1 108.43  NA NA
## beta omega2.beta  0.41  NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.alp1 omega2.beta
## omega2.alp1 1      0
## omega2.beta 0      1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 5958.536
##      AIC = 5990.536
##      BIC = 6036.043
##
## Likelihood computed by importance sampling
##      -2LL= 840.4144
##      AIC = 872.4144
##      BIC = 917.9213
## -----
ord.fit.cov2<-saemix(saemix.model.cov2,saemix.data,saemix.options)

```





```
## Error in solve.default(F0) :
##   routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
```

```

## ----- Data -----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset knee.saemix
## Structured data: y ~ y + time | id
## X variable for graphs: time (d)
## covariates: Age (yr), Sex (-), treatment (-), Age2 (yr2)
## reference class for covariate Sex : 0
## reference class for covariate treatment : 0
## Dataset characteristics:
## number of subjects: 127
## number of observations: 508
## average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
## id y time y.1 Age Sex treatment Age2 mdv cens occ ytype
## 1 1 4 0 4 -2 1 0 4 0 0 1 1
## 2 1 4 3 4 -2 1 0 4 0 0 1 1
## 3 1 4 7 4 -2 1 0 4 0 0 1 1
## 4 1 4 10 4 -2 1 0 4 0 0 1 1
## 5 2 4 0 4 2 1 0 4 0 0 1 1
## 6 2 4 3 4 2 1 0 4 0 0 1 1
## 7 2 4 7 4 2 1 0 4 0 0 1 1
## 8 2 4 10 4 2 1 0 4 0 0 1 1
## 9 3 3 0 3 11 1 0 121 0 0 1 1
## 10 3 3 3 3 11 1 0 121 0 0 1 1
## -----
## ----- Model -----
## -----
## Nonlinear mixed-effects model
## Model function: Ordinal categorical model
## Model type: likelihood
## function(psi,id,xidep) {
## y<-xidep[,1]
## time<-xidep[,2]
## alp1<-psi[id,1]
## alp2<-psi[id,2]
## alp3<-psi[id,3]
## alp4<-psi[id,4]
## beta<-psi[id,5]
##
## logit1<-alp1 + beta*time
## logit2<-logit1+alp2
## logit3<-logit2+alp3
## logit4<-logit3+alp4
## pge1<-exp(logit1)/(1+exp(logit1))
## pge2<-exp(logit2)/(1+exp(logit2))
## pge3<-exp(logit3)/(1+exp(logit3))
## pge4<-exp(logit4)/(1+exp(logit4))
## pobs = (y==1)*pge1+(y==2)*(pge2 - pge1)+(y==3)*(pge3 - pge2)+(y==4)*(pge4 - pge3)+(y==5)*(1 - pge4)
## logpdf <- log(pobs)
##
## return(logpdf)
## }

```



```

## <bytecode: 0x55e9ded79f10>
##   Nb of parameters: 5
##       parameter names:  alp1 alp2 alp3 alp4 beta
##       distribution:
##       Parameter Distribution Estimated
## [1,] alp1      normal      Estimated
## [2,] alp2      log-normal   Estimated
## [3,] alp3      log-normal   Estimated
## [4,] alp4      log-normal   Estimated
## [5,] beta      log-normal   Estimated
##   Variance-covariance matrix:
##       alp1 alp2 alp3 alp4 beta
## alp1      1    0    0    0    0
## alp2      0    0    0    0    0
## alp3      0    0    0    0    0
## alp4      0    0    0    0    0
## beta      0    0    0    0    1
##   Covariate model:
##       [,1] [,2] [,3] [,4] [,5]
## treatment    0    0    0    0    1
## Age2          1    0    0    0    0
##   Initial values
##       alp1 alp2 alp3 alp4 beta
## Pop.CondInit    0 0.2 0.6   3 0.2
## Cov.CondInit    0 0.0 0.0   0 0.0
## psi1            0 0.0 0.0   0 0.0
## -----
## ----   Key algorithm options   ----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of standard errors and linearised log-likelihood
##   Estimation of log-likelihood by importance sampling
##   Number of iterations:  K1=300, K2=100
##   Number of chains:  10
##   Seed:  632545
##   Number of MCMC iterations for IS:  5000
##   Simulations:
##       nb of simulated datasets used for npde:  1000
##       nb of simulated datasets used for VPC:  100
##   Input/output
##       save the results to a file:  FALSE
##       save the graphs to files:  FALSE
## -----
## ----                               ----
## -----
## -----   Fixed effects   -----
## -----
##       Parameter      Estimate SE    CV(%) p-value
## [1,] alp1            -16.300 2.406 15    -
## [2,] beta_Age2(alp1)    0.041 0.014 33    0.0014
## [3,] alp2             5.340 1.814 34    -
## [4,] alp3             7.173 1.587 22    -
## [5,] alp4            10.079 3.010 30    -
## [6,] beta             0.535 0.176 33    -

```

```
## [7,] beta_treatment(beta) 0.554 0.347 63 0.0552
## -----
## ----- Variance of random effects -----
## -----
## Parameter Estimate SE CV(%)
## alp1 omega2.alp1 116.22 NA NA
## beta omega2.beta 0.45 NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
## omega2.alp1 omega2.beta
## omega2.alp1 1 0
## omega2.beta 0 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
## -2LL= 5980.122
## AIC = 6000.122
## BIC = 6028.564
##
## Likelihood computed by importance sampling
## -2LL= 843.57
## AIC = 863.57
## BIC = 892.0119
## -----
```

```
BIC(ord.fit)
```

```
## [1] 903.2144
```

```
BIC(ord.fit.cov1)
```

```
## [1] 917.9213
```

```
BIC(ord.fit.cov2)
```

```
## [1] 892.0119
```

```
# Comparing the 3 covariate models - model with Age2 on alp1 and treatment on beta best
compare.saemix(ord.fit, ord.fit.cov1, ord.fit.cov2)
```

```
## Likelihoods calculated by importance sampling
```

```
## AIC BIC BIC.cov
## 1 880.4609 903.2144 892.8407
## 2 872.4144 917.9213 907.5477
## 3 863.5700 892.0119 881.6382
```

```
#####
```

```
# But VPC not good
```

```
### Simulations for VPC
```

```
simulateOrdinal<-function(psi,id,xidep) {
  y<-xidep[,1]
  time<-xidep[,2]
  alp1<-psi[id,1]
  alp2<-psi[id,2]
  alp3<-psi[id,3]
```

```

alp4<-psi[id,4]
beta<-psi[id,5]

logit1<-alp1 + beta*time
logit2<-logit1+alp2
logit3<-logit2+alp3
logit4<-logit3+alp4
pge1<-exp(logit1)/(1+exp(logit1))
pge2<-exp(logit2)/(1+exp(logit2))
pge3<-exp(logit3)/(1+exp(logit3))
pge4<-exp(logit4)/(1+exp(logit4))
x<-runif(length(time))
ysim<-1+as.integer(x>pge1)+as.integer(x>pge2)+as.integer(x>pge3)+as.integer(x>pge4)
return(ysim)
}

nsim<-100
yfit<-ord.fit.cov2
yfit<-simulateDiscreteSaemix(yfit, simulateOrdinal, nsim=nsim)

simdat <-yfit@sim.data@datasim
simdat$time<-rep(yfit@data@data$time,nsim)
simdat$treatment<-rep(yfit@data@data$treatment,nsim)

ytab<-NULL
for(irep in 1:nsim) {
  xtab<-simdat[simdat$irep==irep,]
  xtab1 <- xtab %>%
    group_by(time, treatment, ysim) %>%
    summarise(n=length(ysim))
  ytab<-rbind(ytab,xtab1[,c("time","ysim","n","treatment")])
}

```

```

## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `groups` argument
## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `groups` argument
## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `groups` argument
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## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `groups` argument
## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `groups` argument

```

[illegible]

[illegible]

```
gtab <- ytab %>%
  group_by(time, treatment, ysim) %>%
  summarise(lower=quantile(n, c(0.05)), n=quantile(n, c(0.5)), upper=quantile(n, c(0.95))) %>%
  mutate(y=as.factor(ysim))
```

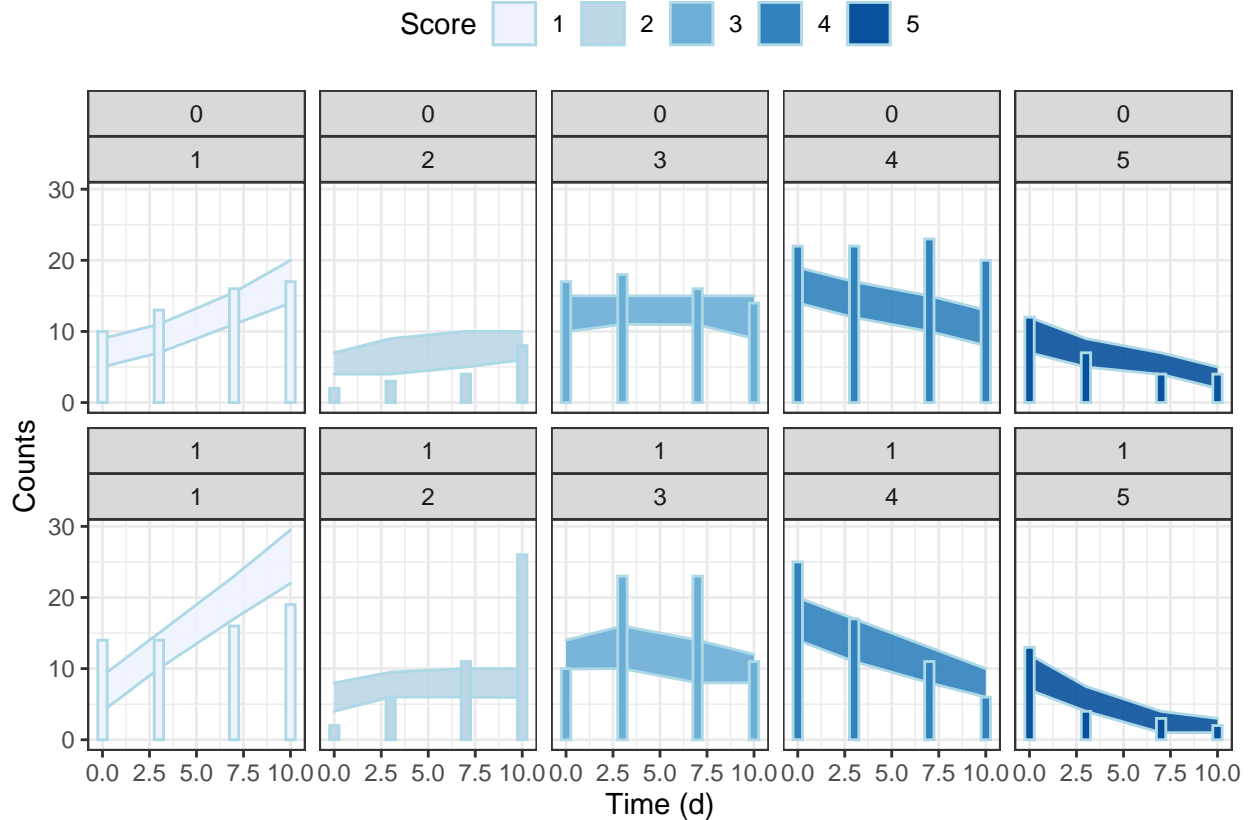
```
## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `.groups` argument
```

```
knee2 <- knee.saemix %>%
  group_by(time, treatment, y) %>%
  summarise(n=length(y)) %>%
  mutate(y=as.factor(y))
```

```
## `summarise()` has grouped output by 'time', 'treatment'. You can override using the `.groups` argument
```

```
kneevpc <- ggplot(data = knee2, aes(x = time, y=n, fill=y, group=treatment)) +
  geom_ribbon(data=gtab, aes(x=time, ymin=lower, ymax=upper), alpha=0.9, colour="lightblue") +
  geom_col(position = "dodge", width=0.5, colour="lightblue") + theme_bw() +
  scale_fill_brewer(palette = "Blues") + theme(legend.position = "top") +
  labs(fill = "Score") + xlab("Time (d)") + ylab("Counts") + facet_wrap(treatment~y, nrow=2)

print(kneevpc)
```



```
# VPC for median score in each group
knee3 <- knee.saemix %>%
  group_by(time, treatment) %>%
  summarise(mean=mean(y))
```

`summarise()` has grouped output by 'time'. You can override using the `.groups` argument.

```
ytab<-NULL
for(irep in 1:nsim) {
  xtab<-simdat[simdat$irep==irep,]
  xtab1 <- xtab %>%
    group_by(time, treatment) %>%
    summarise(mean=mean(ysim))
  ytab<-rbind(ytab,xtab1[,c("time","treatment","mean")])
}
```

`summarise()` has grouped output by 'time'. You can override using the `.groups` argument.

```
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
```

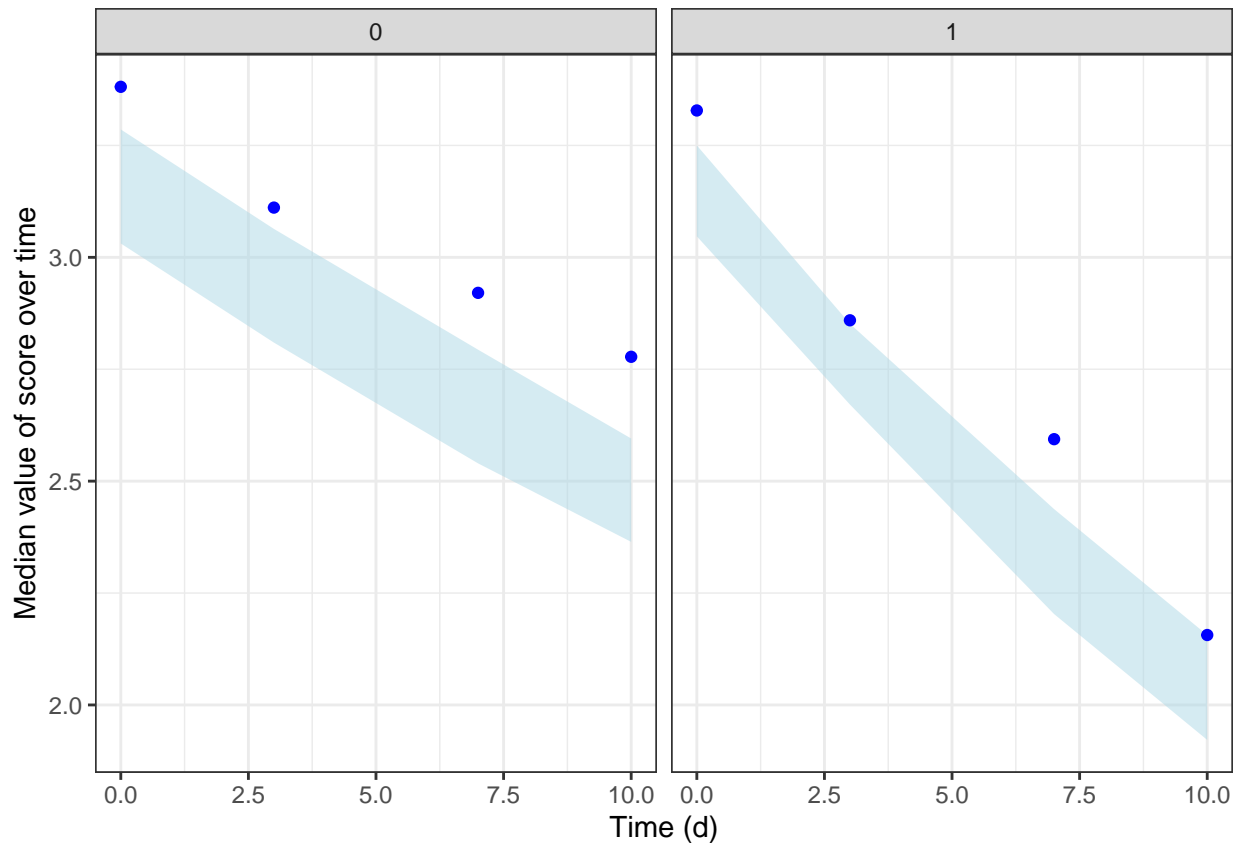
[illegible]

[illegible]

```
gtab <- ytab %>%
  group_by(time, treatment) %>%
  summarise(lower=quantile(mean, c(0.05)), mean=median(mean), upper=quantile(mean, c(0.95)))
```

```
## `summarise()` has grouped output by 'time'. You can override using the `.groups` argument.
```

```
kneeMedvpc <- ggplot(data = knee3, aes(x = time, y=mean, group=treatment)) +  
  geom_ribbon(data=gtab, aes(x=time, ymin=lower, ymax=upper), alpha=0.5, fill="lightblue") +  
  geom_point(colour='blue') + theme_bw() +  
  scale_fill_brewer(palette = "Blues") + theme(legend.position = "top") +  
  labs(fill = "Score") + xlab("Time (d)") + ylab("Median value of score over time") + facet_wrap(~trea  
  
print(kneeMedvpc)
```

Count data model

- Epilepsy
 - dataset epil from MASS
 - very basic model with only one parameter
- Drinking patterns amongst students (David Atkins from tutorial)
 - dataset rapi.saemix
 - lambda parameter from Poisson model with a time-effect, gender effects on both intercept and slope
 - different models can be adjusted to the data, accounting for overdispersion

Epilepsy data

```
epilepsy<-MASS:::epil
saemix.data<-saemixData(name.data=epilepsy, name.group=c("subject"),
                        name.predictors=c("period","y"),name.response=c("y"),
                        name.covariates=c("trt","base", "age"),
                        units=list(x="2-week",y="",covariates=c("", "", "yr")))
```

```
## [1] "trt" "base" "age"
```

```
##
```

```
##
```

```
## The following SaemixData object was successfully created:
```

```
##
```

```
## Object of class SaemixData
```

```
## longitudinal data for use with the SAEM algorithm
```

```

## Dataset epilepsy
##   Structured data: y ~ period + y | subject
##   X variable for graphs: period (2-week)
##   covariates: trt (), base (), age (yr)
##   reference class for covariate trt : placebo

## Poisson model with one parameter
countmodel.poisson<-function(psi,id,xidep) {
  y<-xidep[,2]
  lambda<-psi[id,1]
  logp <- -lambda + y*log(lambda) - log(factorial(y))
  return(logp)
}

# Adding a period effect
countmodel.periodpoi<-function(psi,id,xidep) {
  tim <- xidep[,1]
  y<-xidep[,2]
  lam<-psi[id,1]
  betaT<-psi[id,2]
  lambda<-lam*exp(beta*log(tim))
  logp <- -lambda + y*log(lambda) - log(factorial(y))
  return(logp)
}

## Generalised Poisson model
countmodel.genpoisson<-function(psi,id,xidep) {
  y<-xidep[,1]
  delta<-psi[id,1]
  lambda<-psi[id,2]
  logp <- -lambda
  pos.ind <- which(y>0)
  lp1 <-log(lambda) + (y-1)*log(lambda+y*delta) - (lambda+y*delta) - log(factorial(y))
  logp[pos.ind] <- lp1[pos.ind]
  return(logp)
}

## Poisson model with Zero-Inflation
countmodel.zip<-function(psi,id,xidep) {
  y<-xidep[,2]
  lambda<-psi[id,1]
  p0<-psi[id,2]
  logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y))
  logp0 <- log(p0+(1-p0)*exp(-lambda))
  logp[y==0]<-logp0[y==0]
  return(logp)
}

saemix.model.poi<-saemixModel(model=countmodel.poisson,description="count model Poisson",modeltype="lik",
                             psi0=matrix(c(0.5),ncol=1,byrow=TRUE,dimnames=list(NULL, c("lambda"))),
                             transform.par=c(1))

##
##
## The following SaemixModel object was successfully created:

```

```

##
## Nonlinear mixed-effects model
## Model function: count model Poisson
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## Nb of parameters: 1
##   parameter names: lambda
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda    log-normal    Estimated
## Variance-covariance matrix:
##   lambda
## lambda      1
## No covariate in the model.
## Initial values
##   lambda
## Pop.CondInit    0.5

saemix.model.zip<-saemixModel(model=countmodel.zip,description="count model ZIP",modeltype="likelihood",
                             psi0=matrix(c(0.5,0.2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","p0")),
                             transform.par=c(1,3), #omega.init=matrix(c(0.5,0,0,0.3),ncol=2,byrow=TRUE),
                             covariance.model=matrix(c(1,0,0,0),ncol=2,byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: count model ZIP
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   p0<-psi[id,2]
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y))
##   logp0 <- log(p0+(1-p0)*exp(-lambda))
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## Nb of parameters: 2
##   parameter names: lambda p0
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda    log-normal    Estimated
## [2,] p0        logit         Estimated
## Variance-covariance matrix:
##   lambda p0
## lambda    1  0
## p0         0  0
## No covariate in the model.

```

```

##      Initial values
##      lambda p0
## Pop.CondInit    0.5 0.2

saemix.model.gp<-saemixModel(model=countmodel.zip,description="Generalised Poisson model",modeltype="li
                             psi0=matrix(c(0.5,0.2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("delta","l
                             transform.par=c(1,1), #omega.init=matrix(c(0.5,0,0,0.3),ncol=2,byrow=TRUE
                             covariance.model=matrix(c(1,0,0,0),ncol=2,byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Generalised Poisson model
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   p0<-psi[id,2]
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y))
##   logp0 <- log(p0+(1-p0)*exp(-lambda))
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## Nb of parameters: 2
##   parameter names: delta lambda
##   distribution:
##   Parameter Distribution Estimated
## [1,] delta      log-normal Estimated
## [2,] lambda     log-normal Estimated
## Variance-covariance matrix:
##   delta lambda
## delta      1      0
## lambda     0      0
## No covariate in the model.
## Initial values
##   delta lambda
## Pop.CondInit    0.5    0.2

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

poisson.fit<-saemix(saemix.model.poi,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ---- Data ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset epilepsy
## Structured data: y ~ period + y | subject
## X variable for graphs: period (2-week)
## covariates: trt (), base (), age (yr)
## reference class for covariate trt : placebo

```

```

## Dataset characteristics:
##   number of subjects:      59
##   number of observations: 236
##   average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
##   subject period y y.1      trt base age mdv cens occ ytype
## 1         1      1 5    5 placebo 11 31  0   0  1    1
## 2         1      2 3    3 placebo 11 31  0   0  1    1
## 3         1      3 3    3 placebo 11 31  0   0  1    1
## 4         1      4 3    3 placebo 11 31  0   0  1    1
## 5         2      1 3    3 placebo 11 30  0   0  1    1
## 6         2      2 5    5 placebo 11 30  0   0  1    1
## 7         2      3 3    3 placebo 11 30  0   0  1    1
## 8         2      4 3    3 placebo 11 30  0   0  1    1
## 9         3      1 2    2 placebo  6 25  0   0  1    1
## 10        3      2 4    4 placebo  6 25  0   0  1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
##   Model function: count model Poisson
##   Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## <bytecode: 0x55e9dc358bf0>
##   Nb of parameters: 1
##     parameter names: lambda
##     distribution:
##       Parameter Distribution Estimated
## [1,] lambda    log-normal    Estimated
##   Variance-covariance matrix:
##     lambda
## lambda      1
##   No covariate in the model.
##   Initial values
##     lambda
## Pop.CondInit    0.5
## -----
## ----   Key algorithm options   ----
## -----
##   Estimation of individual parameters (MAP)
##   Estimation of standard errors and linearised log-likelihood
##   Estimation of log-likelihood by importance sampling
##   Number of iterations: K1=300, K2=100
##   Number of chains: 1
##   Seed: 632545
##   Number of MCMC iterations for IS: 5000
##   Simulations:
##     nb of simulated datasets used for npde: 1000
##     nb of simulated datasets used for VPC: 100

```

```

##      Input/output
##      save the results to a file: FALSE
##      save the graphs to files: FALSE
## -----
##      Results
## -----
##      Fixed effects
## -----
##      Parameter Estimate SE    CV(%)
## [1,] lambda      5.1      0.71 14
## -----
##      Variance of random effects
## -----
##      Parameter      Estimate SE    CV(%)
## lambda omega2.lambda 0.9      0.21 23
## -----
##      Correlation matrix of random effects
## -----
##      omega2.lambda
## omega2.lambda 1
## -----
##      Statistical criteria
## -----
## Likelihood computed by linearisation
##      -2LL= 60096.92
##      AIC = 60102.92
##      BIC = 60109.15
##
## Likelihood computed by importance sampling
##      -2LL= 1402.095
##      AIC = 1408.095
##      BIC = 1414.327
## -----
genpoisson.fit<-saemix(saemix.model.gp,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
##      Data
## -----
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset epilepsy
##      Structured data: y ~ period + y | subject
##      X variable for graphs: period (2-week)
##      covariates: trt (), base (), age (yr)
##      reference class for covariate trt : placebo
## Dataset characteristics:
##      number of subjects:      59
##      number of observations: 236
##      average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
##      subject period y y.1      trt base age mdv cens occ ytype
## 1      1      1 5    5 placebo  11 31   0   0   1    1
## 2      1      2 3    3 placebo  11 31   0   0   1    1

```

```

## 3      1      3 3      3 placebo  11 31  0  0  1  1
## 4      1      4 3      3 placebo  11 31  0  0  1  1
## 5      2      1 3      3 placebo  11 30  0  0  1  1
## 6      2      2 5      5 placebo  11 30  0  0  1  1
## 7      2      3 3      3 placebo  11 30  0  0  1  1
## 8      2      4 3      3 placebo  11 30  0  0  1  1
## 9      3      1 2      2 placebo   6 25  0  0  1  1
## 10     3      2 4      4 placebo   6 25  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Generalised Poisson model
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   p0<-psi[id,2]
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y))
##   logp0 <- log(p0+(1-p0)*exp(-lambda))
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## <bytecode: 0x55e9de3c01a0>
## Nb of parameters: 2
##   parameter names: delta lambda
##   distribution:
##   Parameter Distribution Estimated
## [1,] delta      log-normal Estimated
## [2,] lambda     log-normal Estimated
## Variance-covariance matrix:
##   delta lambda
## delta      1      0
## lambda     0      0
## No covariate in the model.
## Initial values
##   delta lambda
## Pop.CondInit  0.5    0.2
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##   nb of simulated datasets used for npde: 1000
##   nb of simulated datasets used for VPC: 100
## Input/output
##   save the results to a file: FALSE
##   save the graphs to files: FALSE

```

```

## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] delta      5.314   0.747 14
## [2,] lambda     0.041   0.024 58
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE      CV(%)
## delta omega2.delta 0.86      0.21 24
## -----
## ----- Correlation matrix of random effects -----
## -----
##              omega2.delta
## omega2.delta 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 60647.88
##      AIC = 60655.88
##      BIC = 60664.19
##
## Likelihood computed by importance sampling
##      -2LL= 1381.329
##      AIC = 1389.329
##      BIC = 1397.639
## -----
zippoisson.fit<-saemix(saemix.model.zip,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----- Data -----
## -----
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset epilepsy
##      Structured data: y ~ period + y | subject
##      X variable for graphs: period (2-week)
##      covariates: trt (), base (), age (yr)
##      reference class for covariate trt : placebo
## Dataset characteristics:
##      number of subjects:      59
##      number of observations: 236
##      average/min/max nb obs: 4.00 / 4 / 4
## First 10 lines of data:
##      subject period y y.1      trt base age mdv cens occ ytype
## 1      1      1 5    5 placebo  11 31   0   0   1    1
## 2      1      2 3    3 placebo  11 31   0   0   1    1
## 3      1      3 3    3 placebo  11 31   0   0   1    1
## 4      1      4 3    3 placebo  11 31   0   0   1    1

```



```

## 5      2      1 3      3 placebo  11 30  0  0  1  1
## 6      2      2 5      5 placebo  11 30  0  0  1  1
## 7      2      3 3      3 placebo  11 30  0  0  1  1
## 8      2      4 3      3 placebo  11 30  0  0  1  1
## 9      3      1 2      2 placebo   6 25  0  0  1  1
## 10     3      2 4      4 placebo   6 25  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: count model ZIP
## Model type: likelihood
## function(psi,id,xidep) {
##   y<-xidep[,2]
##   lambda<-psi[id,1]
##   p0<-psi[id,2]
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y))
##   logp0 <- log(p0+(1-p0)*exp(-lambda))
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## <bytecode: 0x55e9de3c01a0>
## Nb of parameters: 2
##   parameter names: lambda p0
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda    log-normal Estimated
## [2,] p0        logit      Estimated
## Variance-covariance matrix:
##   lambda p0
## lambda    1  0
## p0        0  0
## No covariate in the model.
## Initial values
##   lambda p0
## Pop.CondInit  0.5 0.2
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##   nb of simulated datasets used for npde: 1000
##   nb of simulated datasets used for VPC: 100
## Input/output
##   save the results to a file: FALSE
##   save the graphs to files: FALSE
## -----
## ----          Results          ----

```

```
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] lambda      5.320   0.748 14
## [2,] p0          0.041   0.024 58
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE      CV(%)
## lambda omega2.lambda 0.86      0.21 24
## -----
## ----- Correlation matrix of random effects -----
## -----
##              omega2.lambda
## omega2.lambda 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 61045.94
##      AIC = 61053.94
##      BIC = 61062.25
##
## Likelihood computed by importance sampling
##      -2LL= 1381.314
##      AIC = 1389.314
##      BIC = 1397.624
## -----
```

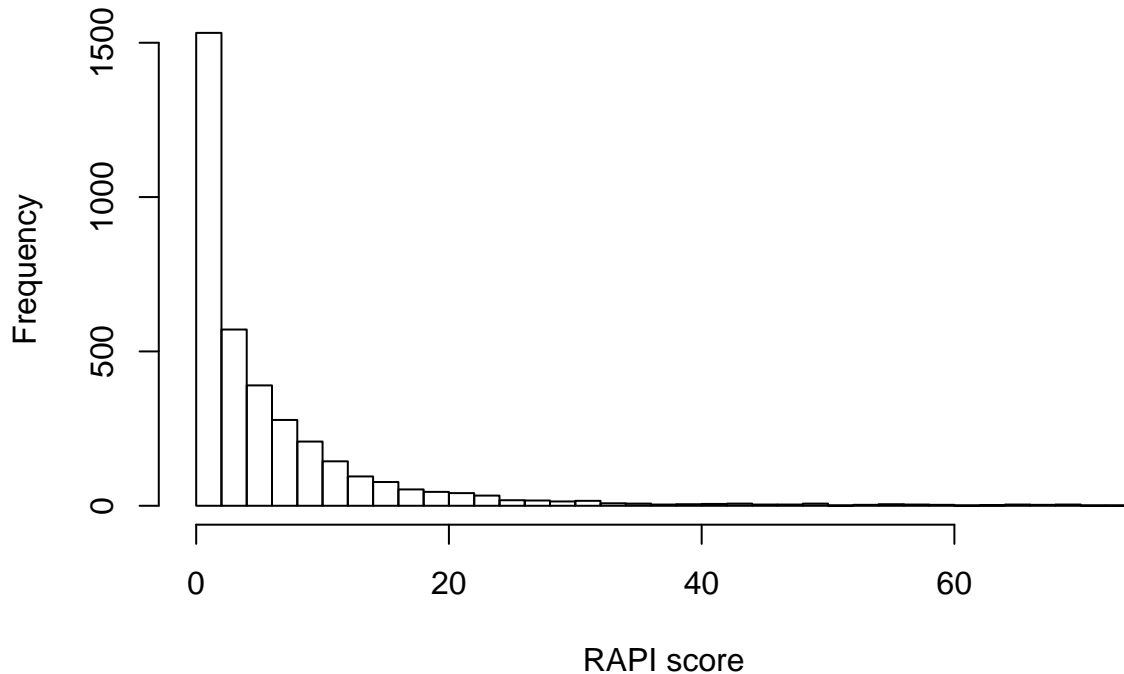
RAPI

```
if(testMode)
  data(rapi.saemix) else
  rapi.saemix<-read.table(file.path(datDir, "rapi.saemix.tab"), header=TRUE)

# Data
saemix.data<-saemixData(name.data=rapi.saemix, name.group=c("id"),
                        name.predictors=c("time", "rapi"), name.response=c("rapi"),
                        name.covariates=c("gender"),
                        units=list(x="months", y="", covariates=c("")))

## [1] "gender"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##      Structured data: rapi ~ time + rapi | id
##      X variable for graphs: time (months)
##      covariates: gender ()
##      reference class for covariate gender : Men
```

```
hist(rapi.saemix$rapi, main="", xlab="RAPI score", breaks=30)
```



```
## Models
# Poisson with a time effect
count.poisson<-function(psi,id,xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
  intercept<-psi[id,1]
  slope<-psi[id,2]
  lambda<- exp(intercept + slope*time)
  logp <- -lambda + y*log(lambda) - log(factorial(y))
  return(logp)
}

## ZIP Poisson model with time effect
count.poissonzip<-function(psi,id,xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
  intercept<-psi[id,1]
  slope<-psi[id,2]
  p0<-psi[id,3] # Probability of zero's
  lambda<- exp(intercept + slope*time)
  logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
  logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
  logp[y==0]<-logp0[y==0]
  return(logp)
}

## Generalized Poisson model with time effect
count.genpoisson<-function(psi,id,xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
```

```

    intercept<-psi[id,1]
    slope<-psi[id,2]
    lambda<- exp(intercept + slope*time)
    delta<-psi[id,3]
    logp <- log(lambda) + (y-1)*log(lambda+y*delta) - lambda - y*delta - log(factorial(y))
    return(logp)
}

## Negative binomial model with time effect
count.NB<-function(psi,id,xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
  intercept<-psi[id,1]
  slope<-psi[id,2]
  k<-psi[id,3]
  lambda<- exp(intercept + slope*time)
  logp <- log(factorial(y+k-1)) - log(factorial(y)) - log(factorial(k-1)) + y*log(lambda) - y*log(lambda+delta)
  return(logp)
}

# Fits
## Poisson
### Model without covariate
saemix.model.poi<-saemixModel(model=count.poisson,description="Count model Poisson",modeltype="likelihood",
                             psi0=matrix(c(log(5),0.01),ncol=2,byrow=TRUE,dimnames=list(NULL, c("intercept","slope")),
                             transform.par=c(0,0), omega.init=diag(c(0.5, 0.5)))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  Count model Poisson
##   Model type:     likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
##   Nb of parameters: 2
##       parameter names:  intercept slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal          Estimated
## [2,] slope      normal          Estimated
##   Variance-covariance matrix:
##       intercept slope
## intercept      1      0
## slope          0      1
##   No covariate in the model.

```

```

##      Initial values
##              intercept slope
## Pop.CondInit  1.609438  0.01
### Gender effect on intercept and slope
saemix.model.poi.cov2<-saemixModel(model=count.poisson,description="Count model Poisson",modeltype="lik
                                psi0=matrix(c(log(5),0.01),ncol=2,byrow=TRUE,dimnames=list(NULL, c("
                                transform.par=c(0,0), omega.init=diag(c(0.5, 0.5)),
                                covariance.model =matrix(data=1, ncol=2, nrow=2),
                                covariate.model=matrix(c(1,1), ncol=2, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  Count model Poisson
##   Model type:     likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
##   Nb of parameters: 2
##       parameter names:  intercept slope
##       distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
##   Variance-covariance matrix:
##           intercept slope
## intercept      1      1
## slope          1      1
##   Covariate model:
##       intercept slope
## [1,]          1      1
##   Initial values
##           intercept slope
## Pop.CondInit  1.609438  0.01
## Cov.CondInit  0.000000  0.00

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

### Fit with saemix
poisson.fit<-saemix(saemix.model.poi,saemix.data,saemix.options)

## Error in solve.default(F0) :
##   routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----

```

```

## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##   Structured data: rapi ~ time + rapi | id
##   X variable for graphs: time (months)
##   covariates: gender ()
##   reference class for covariate gender : Men
## Dataset characteristics:
##   number of subjects:      818
##   number of observations: 3616
##   average/min/max nb obs: 4.42 / 1 / 5
## First 10 lines of data:
##   id time rapi rapi.1 gender mdv cens occ ytype
## 1  1  0  0  0  Men  0  0  1  1
## 2  1  6  0  0  Men  0  0  1  1
## 3  1 18  0  0  Men  0  0  1  1
## 4  2  0  3  3  Women 0  0  1  1
## 5  2  6  6  6  Women 0  0  1  1
## 6  2 12  5  5  Women 0  0  1  1
## 7  2 18  4  4  Women 0  0  1  1
## 8  2 24  5  5  Women 0  0  1  1
## 9  3  0  9  9  Men  0  0  1  1
## 10 3 12  1  1  Men  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
##   Model function: Count model Poisson
##   Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## <bytecode: 0x55e9e5cf2928>
##   Nb of parameters: 2
##   parameter names: intercept slope
##   distribution:
##   Parameter Distribution Estimated
## [1,] intercept normal Estimated
## [2,] slope normal Estimated
##   Variance-covariance matrix:
##   intercept slope
## intercept 1 0
## slope 0 1
##   No covariate in the model.
##   Initial values
##   intercept slope
## Pop.CondInit 1.609438 0.01

```

```

## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##     nb of simulated datasets used for npde: 1000
##     nb of simulated datasets used for VPC: 100
## Input/output
##     save the results to a file: FALSE
##     save the graphs to files: FALSE
## -----
## ---- Results ----
## -----
## ----- Fixed effects -----
## -----
## Parameter Estimate SE CV(%)
## [1,] intercept 1.577 0.041 2.6
## [2,] slope -0.033 0.036 107.6
## -----
## ----- Variance of random effects -----
## -----
## Parameter Estimate SE CV(%)
## intercept omega2.intercept 0.9039 NA NA
## slope omega2.slope 0.0039 NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
## omega2.intercept omega2.slope
## omega2.intercept 1 0
## omega2.slope 0 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
## -2LL= 475787.9
## AIC = 475797.9
## BIC = 475821.4
##
## Likelihood computed by importance sampling
## -2LL= 21486.75
## AIC = 21496.75
## BIC = 21520.29
## -----
poisson.fit.cov2<-saemix(saemix.model.poi.cov2,saemix.data,saemix.options)

## Error in solve.default(F0) :
## routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Error in data.frame(name = namallpar, estimate = estpar, se = estSE) :

```

```

## arguments imply differing number of rows: 10, 11
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
## Structured data: rapi ~ time + rapi | id
## X variable for graphs: time (months)
## covariates: gender ()
## reference class for covariate gender : Men
## Dataset characteristics:
## number of subjects:      818
## number of observations: 3616
## average/min/max nb obs: 4.42 / 1 / 5
## First 10 lines of data:
## id time rapi rapi.1 gender mdv cens occ ytype
## 1  1  0  0  0  Men  0  0  1  1
## 2  1  6  0  0  Men  0  0  1  1
## 3  1 18  0  0  Men  0  0  1  1
## 4  2  0  3  3  Women 0  0  1  1
## 5  2  6  6  6  Women 0  0  1  1
## 6  2 12  5  5  Women 0  0  1  1
## 7  2 18  4  4  Women 0  0  1  1
## 8  2 24  5  5  Women 0  0  1  1
## 9  3  0  9  9  Men  0  0  1  1
## 10 3 12  1  1  Men  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Count model Poisson
## Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## <bytecode: 0x55e9e5cf2928>
## Nb of parameters: 2
## parameter names: intercept slope
## distribution:
## Parameter Distribution Estimated
## [1,] intercept normal Estimated
## [2,] slope normal Estimated
## Variance-covariance matrix:
## intercept slope
## intercept 1 1
## slope 1 1

```



```

## Covariate model:
##      [,1] [,2]
## gender    1    1
##      Initial values
##              intercept slope
## Pop.CondInit 1.609438 0.01
## Cov.CondInit 0.000000 0.00
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##      nb of simulated datasets used for npde: 1000
##      nb of simulated datasets used for VPC: 100
## Input/output
##      save the results to a file: FALSE
##      save the graphs to files: FALSE
## -----
## ---- Results ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter      Estimate
## [1,] intercept      1.683
## [2,] beta_gender(intercept) -0.196
## [3,] slope          -0.022
## [4,] beta_gender(slope)  -0.017
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate
## intercept omega2.intercept 0.9179
## slope      omega2.slope    0.0039
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.intercept omega2.slope
## omega2.intercept 1.00      -0.14
## omega2.slope    -0.14      1.00
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by importance sampling
##      -2LL= 21454.94
##      AIC = 21470.94
##      BIC = 21508.59
## -----

```

```
exp(poisson.fit@results@fixed.effects)
```

```
## [1] 4.8394604 0.9673886
```

```
exp(poisson.fit.cov2@results@fixed.effects)
```

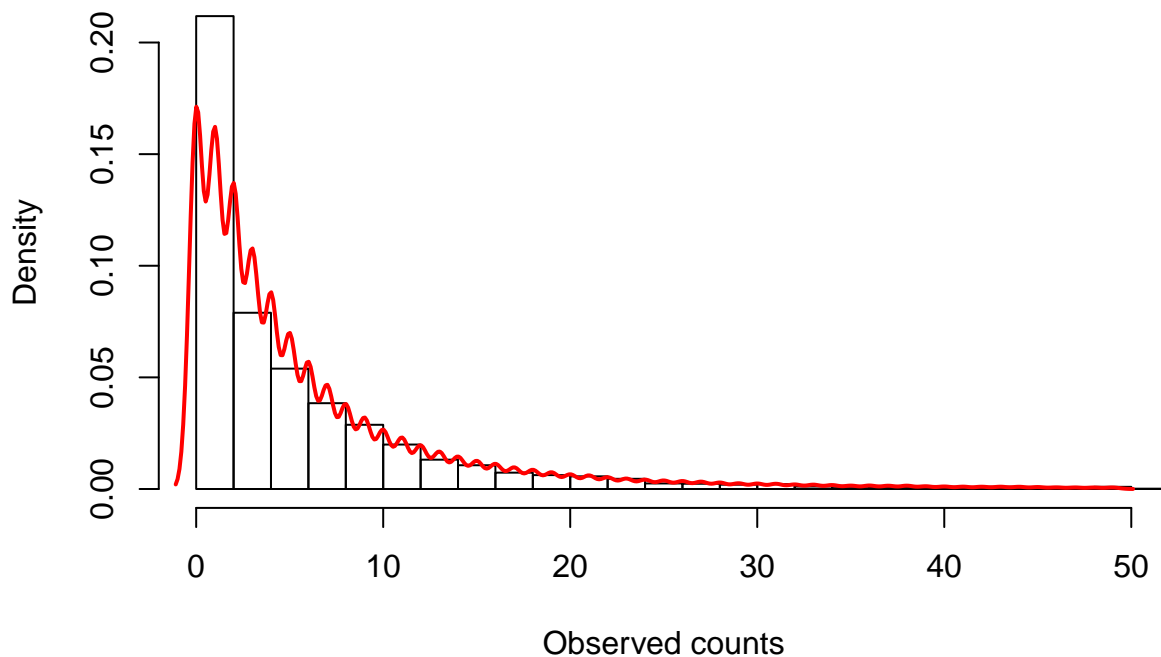
```
## [1] 5.3842360 0.8217414 0.9780800 0.9833256
```

```
### Simulations
```

```
saemix.simulatePoisson<-function(psi, id, xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
  intercept<-psi[id,1]
  slope<-psi[id,2]
  lambda<- exp(intercept + slope*time)
  y<-rpois(length(time), lambda=lambda)
  return(y)
}
```

```
yfit1<-simulateDiscreteSaemix(poisson.fit.cov2, saemix.simulatePoisson, 100)
```

```
hist(yfit1@data@data$rapi, xlim=c(0,50), freq=F, breaks=30, xlab="Observed counts", main="")
lines(density(yfit1@sim.data@datasim$ysim[yfit1@sim.data@datasim$ysim<50]), lwd = 2, col = 'red')
```



```
cat("Observed proportion of 0's", length(yfit1@data@data$rapi[yfit1@data@data$rapi==0])/yfit1@data@ntot)
```

```
## Observed proportion of 0's 0.2090708
```

```
cat("      Poisson model, p=", length(yfit1@sim.data@datasim$ysim[yfit1@sim.data@datasim$ysim==0])/length(yfit1@sim.data@datasim$ysim))
```

```
##      Poisson model, p= 0.1518501
```

Overdispersion

```

## ZIP
### base model
saemix.model.zip<-saemixModel(model=count.poissonzip,description="count model ZIP",modeltype="likelihood",
                             psi0=matrix(c(1.5, 0.01, 0.2),ncol=3,byrow=TRUE,dimnames=list(NULL, c("intercept", "slope", "p0")),
                             transform.par=c(0,0,3), covariance.model=diag(c(1,1,0)), omega.init=diag(c(1,1,0)))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  count model ZIP
##   Model type:  likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
##   Nb of parameters: 3
##       parameter names:  intercept slope p0
##       distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0          logit       Estimated
##   Variance-covariance matrix:
##           intercept slope p0
## intercept      1      0  0
## slope           0      1  0
## p0              0      0  0
##   No covariate in the model.
##   Initial values
##           intercept slope p0
## Pop.CondInit      1.5  0.01 0.2

### ZIP Poisson with gender on both intercept
saemix.model.zip.cov1<-saemixModel(model=count.poissonzip,description="count model ZIP",modeltype="likelihood",
                                   psi0=matrix(c(1.5, 0.01, 0.2),ncol=3,byrow=TRUE,dimnames=list(NULL, c("intercept", "slope", "p0")),
                                   transform.par=c(0,0,3), covariance.model=diag(c(1,1,0)), omega.init=diag(c(1,1,0)),
                                   covariate.model = matrix(c(1,0,0),ncol=3, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  count model ZIP
##   Model type:  likelihood

```

```

## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
##   Nb of parameters: 3
##       parameter names:  intercept slope p0
##       distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0         logit        Estimated
##   Variance-covariance matrix:
##           intercept slope p0
## intercept      1      0  0
## slope           0      1  0
## p0              0      0  0
##   Covariate model:
##           intercept slope p0
## [1,]           1      0  0
##   Initial values
##           intercept slope p0
## Pop.CondInit      1.5  0.01 0.2
## Cov.CondInit       0.0  0.00 0.0

### ZIP Poisson with gender on both intercept and slope
saemix.model.zip.cov2<-saemixModel(model=count.poissonzip,description="count model ZIP",modeltype="likelihood",
                                   psi0=matrix(c(1.5, 0.01, 0.2),ncol=3,byrow=TRUE,dimnames=list(NULL, c("intercept", "slope", "p0"))),
                                   transform.par=c(0,0,3), covariance.model=diag(c(1,1,0)), omega.init=c(1,1,1),
                                   covariate.model = matrix(c(1,1,0),ncol=3, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function:  count model ZIP
##   Model type:  likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]

```

```

##   return(logp)
## }
##   Nb of parameters: 3
##       parameter names:  intercept slope p0
##       distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0         logit       Estimated
##   Variance-covariance matrix:
##       intercept slope p0
## intercept      1      0  0
## slope          0      1  0
## p0             0      0  0
##   Covariate model:
##       intercept slope p0
## [1,]      1      1  0
##   Initial values
##       intercept slope p0
## Pop.CondInit      1.5  0.01 0.2
## Cov.CondInit      0.0  0.00 0.0

zippoisson.fit<-saemix(saemix.model.zip,saemix.data,saemix.options)

## Error in solve.default(F0) :
##   routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##   Structured data: rapi ~ time + rapi | id
##   X variable for graphs: time (months)
##   covariates: gender ()
##   reference class for covariate gender : Men
## Dataset characteristics:
##   number of subjects:      818
##   number of observations: 3616
##   average/min/max nb obs: 4.42 / 1 / 5
## First 10 lines of data:
##   id time rapi rapi.1 gender mdv cens occ ytype
## 1  1    0    0      0   Men   0    0    1    1
## 2  1    6    0      0   Men   0    0    1    1
## 3  1   18    0      0   Men   0    0    1    1
## 4  2    0    3      3 Women   0    0    1    1
## 5  2    6    6      6 Women   0    0    1    1
## 6  2   12    5      5 Women   0    0    1    1
## 7  2   18    4      4 Women   0    0    1    1
## 8  2   24    5      5 Women   0    0    1    1
## 9  3    0    9      9   Men   0    0    1    1
## 10 3   12    1      1   Men   0    0    1    1
## -----
## ----          Model          ----

```

```

## -----
## Nonlinear mixed-effects model
## Model function: count model ZIP
## Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## <bytecode: 0x55e9dd608e88>
## Nb of parameters: 3
##   parameter names: intercept slope p0
##   distribution:
##   Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0         logit        Estimated
## Variance-covariance matrix:
##           intercept slope p0
## intercept      1      0  0
## slope           0      1  0
## p0              0      0  0
## No covariate in the model.
## Initial values
##           intercept slope p0
## Pop.CondInit      1.5  0.01 0.2
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000
## Simulations:
##   nb of simulated datasets used for npde: 1000
##   nb of simulated datasets used for VPC: 100
## Input/output
##   save the results to a file: FALSE
##   save the graphs to files: FALSE
## -----
## ---- Results ----
## -----
## ----- Fixed effects -----
## -----

```

```

##      Parameter Estimate SE      CV(%)
## [1,] intercept  1.657   0.0425   2.6
## [2,] slope     -0.029   0.0357 123.5
## [3,] p0        0.076   0.0085  11.2
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE CV(%)
## intercept omega2.intercept 0.7977  NA NA
## slope      omega2.slope     0.0032  NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.intercept omega2.slope
## omega2.intercept 1          0
## omega2.slope     0          1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 459470.4
##      AIC = 459482.4
##      BIC = 459510.7
##
## Likelihood computed by importance sampling
##      -2LL= 20479.88
##      AIC = 20491.88
##      BIC = 20520.12
## -----
zippoisson.fit.cov1<-saemix(saemix.model.zip.cov1,saemix.data,saemix.options)

## Error in solve.default(F0) :
## routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ---- Data ----
## -----
## Object of class SaemixData
## longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
## Structured data: rapi ~ time + rapi | id
## X variable for graphs: time (months)
## covariates: gender ()
## reference class for covariate gender : Men
## Dataset characteristics:
## number of subjects: 818
## number of observations: 3616
## average/min/max nb obs: 4.42 / 1 / 5
## First 10 lines of data:
## id time rapi rapi.1 gender mdv cens occ ytype
## 1 1 0 0 0 Men 0 0 1 1
## 2 1 6 0 0 Men 0 0 1 1
## 3 1 18 0 0 Men 0 0 1 1
## 4 2 0 3 3 Women 0 0 1 1

```

```

## 5  2  6  6  6  Women  0  0  1  1
## 6  2 12  5  5  Women  0  0  1  1
## 7  2 18  4  4  Women  0  0  1  1
## 8  2 24  5  5  Women  0  0  1  1
## 9  3  0  9  9   Men   0  0  1  1
## 10 3 12  1  1   Men   0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: count model ZIP
## Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## <bytecode: 0x55e9dd608e88>
## Nb of parameters: 3
##   parameter names: intercept slope p0
##   distribution:
##   Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0         logit        Estimated
## Variance-covariance matrix:
##   intercept slope p0
## intercept      1    0  0
## slope          0    1  0
## p0             0    0  0
## Covariate model:
##   [,1] [,2] [,3]
## gender  1  0  0
## Initial values
##   intercept slope p0
## Pop.CondInit      1.5 0.01 0.2
## Cov.CondInit      0.0 0.00 0.0
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545
## Number of MCMC iterations for IS: 5000

```



```

##      Simulations:
##      nb of simulated datasets used for npde: 1000
##      nb of simulated datasets used for VPC: 100
##      Input/output
##      save the results to a file: FALSE
##      save the graphs to files: FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter          Estimate SE      CV(%) p-value
## [1,] intercept          1.786  0.0638   3.6 -
## [2,] beta_gender(intercept) -0.226  0.0852  37.7 0.004
## [3,] slope              -0.029  0.0357 123.4 -
## [4,] p0                  0.076  0.0085  11.2 -
## -----
## ----- Variance of random effects -----
## -----
##      Parameter          Estimate SE CV(%)
## intercept omega2.intercept 0.7849  NA NA
## slope      omega2.slope    0.0033  NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.intercept omega2.slope
## omega2.intercept 1      0
## omega2.slope     0      1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 454429.7
##      AIC = 454443.7
##      BIC = 454476.6
##
## Likelihood computed by importance sampling
##      -2LL= 20469.41
##      AIC = 20483.41
##      BIC = 20516.35
## -----
zippoisson.fit.cov2<-saemix(saemix.model.zip.cov2,saemix.data,saemix.options)

## Error in solve.default(F0) :
## routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----                      Data                      ----
## -----
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##      Structured data: rapi ~ time + rapi | id
##      X variable for graphs: time (months)

```

```

##      covariates: gender ()
##      reference class for covariate gender : Men
## Dataset characteristics:
##      number of subjects:      818
##      number of observations: 3616
##      average/min/max nb obs: 4.42 / 1 / 5
## First 10 lines of data:
##      id time rapi rapi.1 gender mdv cens occ ytype
## 1  1  0  0  0  Men  0  0  1  1
## 2  1  6  0  0  Men  0  0  1  1
## 3  1  18  0  0  Men  0  0  1  1
## 4  2  0  3  3  Women  0  0  1  1
## 5  2  6  6  6  Women  0  0  1  1
## 6  2  12  5  5  Women  0  0  1  1
## 7  2  18  4  4  Women  0  0  1  1
## 8  2  24  5  5  Women  0  0  1  1
## 9  3  0  9  9  Men  0  0  1  1
## 10 3  12  1  1  Men  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: count model ZIP
## Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   p0<-psi[id,3] # Probability of zero's
##   lambda<- exp(intercept + slope*time)
##   logp <- log(1-p0) -lambda + y*log(lambda) - log(factorial(y)) # Poisson
##   logp0 <- log(p0+(1-p0)*exp(-lambda)) # Zeroes
##   logp[y==0]<-logp0[y==0]
##   return(logp)
## }
## <bytecode: 0x55e9dd608e88>
## Nb of parameters: 3
##      parameter names: intercept slope p0
##      distribution:
##      Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## [3,] p0         logit        Estimated
## Variance-covariance matrix:
##      intercept slope p0
## intercept      1  0  0
## slope          0  1  0
## p0             0  0  0
## Covariate model:
##      [,1] [,2] [,3]
## gender  1  1  0
## Initial values
##      intercept slope p0

```

```

## Pop.CondInit      1.5  0.01 0.2
## Cov.CondInit      0.0  0.00 0.0
## -----
## ----    Key algorithm options    ----
## -----
##      Estimation of individual parameters (MAP)
##      Estimation of standard errors and linearised log-likelihood
##      Estimation of log-likelihood by importance sampling
##      Number of iterations:  K1=300, K2=100
##      Number of chains:  1
##      Seed:  632545
##      Number of MCMC iterations for IS:  5000
##      Simulations:
##          nb of simulated datasets used for npde:  1000
##          nb of simulated datasets used for VPC:  100
##      Input/output
##          save the results to a file:  FALSE
##          save the graphs to files:  FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter              Estimate SE      CV(%) p-value
## [1,] intercept              1.773  0.0637   3.6 -
## [2,] beta_gender(intercept) -0.197  0.0853  43.3 0.011
## [3,] slope                  -0.020  0.0552 270.1 -
## [4,] beta_gender(slope)     -0.016  0.0724 460.4 0.414
## [5,] p0                     0.075  0.0085  11.2 -
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE CV(%)
## intercept omega2.intercept 0.7826  NA NA
## slope      omega2.slope    0.0033  NA NA
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.intercept omega2.slope
## omega2.intercept 1          0
## omega2.slope    0          1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 458502.9
##      AIC = 458518.9
##      BIC = 458556.5
##
## Likelihood computed by importance sampling
##      -2LL= 20459.27
##      AIC = 20475.27
##      BIC = 20512.93
## -----

```

Simulations

```
saemix.simulatePoissonZIP<-function(psi, id, xidep) {
  time<-xidep[,1]
  y<-xidep[,2]
  intercept<-psi[id,1]
  slope<-psi[id,2]
  p0<-psi[id,3] # Probability of zero's
  lambda<- exp(intercept + slope*time)
  prob0<-rbinom(length(time), size=1, prob=p0)
  y<-rpois(length(time), lambda=lambda)
  y[prob0==1]<-0
  return(y)
}
```

```
yfit2<-simulateDiscreteSaemix(zippoisson.fit.cov2, saemix.simulatePoissonZIP, 100)
```

```
par(mfrow=c(1,3))
```

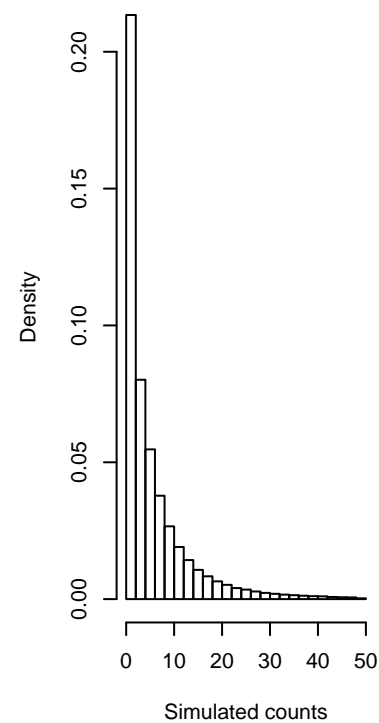
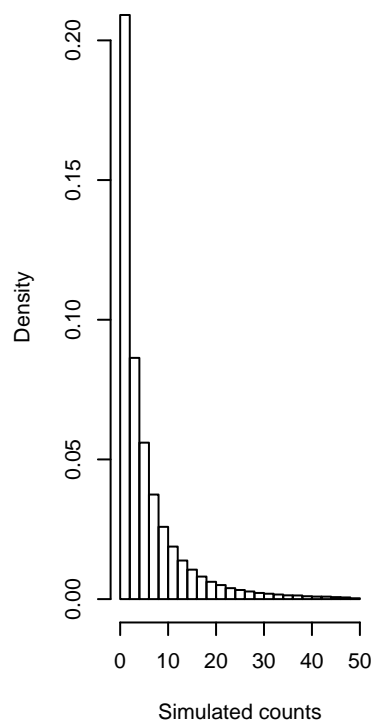
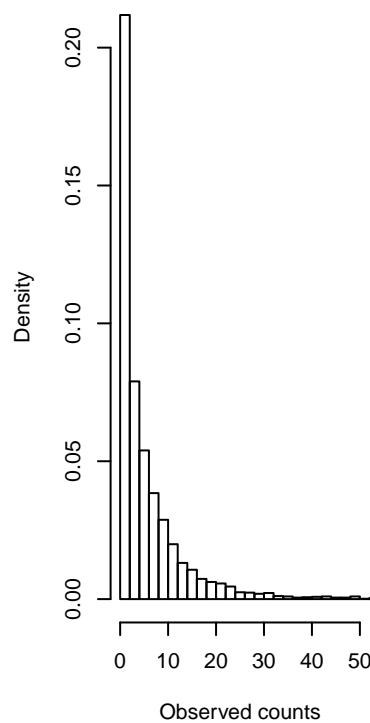
```
hist(yfit1@data@data$rapi, xlim=c(0,50), freq=F, breaks=30, xlab="Observed counts", main="")
```

```
hist(yfit1@sim.data@datasim$ysim[yfit1@sim.data@datasim$ysim<50], xlim=c(0,50), freq=F, breaks=20, xlab="Simulated counts", main="")
```

```
hist(yfit2@sim.data@datasim$ysim[yfit2@sim.data@datasim$ysim<50], xlim=c(0,50), freq=F, breaks=20, xlab="Simulated counts", main="")
```

Poisson model

ZIP model



Hurdle model

Hurdle - 2 models

```
saemix.data1<-saemixData(name.data=rapi.saemix[rapi.saemix$rapi>0,], name.group=c("id"),
  name.predictors=c("time", "rapi"), name.response=c("rapi"),
  name.covariates=c("gender"),
```

```

units=list(x="week",y="",covariates=c("")))

## [1] "gender"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix[rapi.saemix$rapi > 0, ]
##   Structured data: rapi ~ time + rapi | id
##   X variable for graphs: time (week)
##   covariates: gender ()
##   reference class for covariate gender : Men

rapi.saemix$y0<-as.integer(rapi.saemix$rapi>0)
saemix.data0<-saemixData(name.data=rapi.saemix, name.group=c("id"),
                        name.predictors=c("time","y0"),name.response=c("y0"),
                        name.covariates=c("gender"),
                        units=list(x="week",y="",covariates=c("")))

## [1] "gender"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##   Structured data: y0 ~ time + y0 | id
##   X variable for graphs: time (week)
##   covariates: gender ()
##   reference class for covariate gender : Men

# Fit Binomial model to saemix.data0
binary.model<-function(psi,id,xidep) {
  tim<-xidep[,1]
  y<-xidep[,2]
  inter<-psi[id,1]
  slope<-psi[id,2]
  logit<-inter+slope*tim
  pevent<-exp(logit)/(1+exp(logit))
  logpdf<-rep(0,length(tim))
  P.obs = (y==0)*(1-pevent)+(y==1)*pevent
  logpdf <- log(P.obs)
  return(logpdf)
}

saemix.hurdle0<-saemixModel(model=binary.model,description="Binary model",
                           modeltype="likelihood",
                           psi0=matrix(c(-1.5,-.1,0,0),ncol=2,byrow=TRUE,dimnames=list(NULL,c("theta1"
                           transform.par=c(0,0), covariate.model=c(1,1),
                           covariance.model=matrix(c(1,0,0,1),ncol=2), omega.init=diag(c(1,0.3)))

##

```

```

##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function: Binary model
##   Model type: likelihood
## function(psi,id,xidep) {
##   tim<-xidep[,1]
##   y<-xidep[,2]
##   inter<-psi[id,1]
##   slope<-psi[id,2]
##   logit<-inter+slope*tim
##   pevent<-exp(logit)/(1+exp(logit))
##   logpdf<-rep(0,length(tim))
##   P.obs = (y==0)*(1-pevent)+(y==1)*pevent
##   logpdf <- log(P.obs)
##   return(logpdf)
## }
##   Nb of parameters: 2
##       parameter names:  theta1 theta2
##       distribution:
##       Parameter Distribution Estimated
## [1,] theta1    normal      Estimated
## [2,] theta2    normal      Estimated
##   Variance-covariance matrix:
##       theta1 theta2
## theta1      1      0
## theta2      0      1
##   Covariate model:
##       theta1 theta2
## [1,]      1      1
##   Initial values
##       theta1 theta2
## Pop.CondInit  -1.5  -0.1
## Cov.CondInit   0.0   0.0

saemix.options<-list(seed=1234567,save=FALSE,save.graphs=FALSE, displayProgress=FALSE, nb.chains=10, fir

hurdlefit0<-saemix(saemix.hurdle0,saemix.data0,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix
##   Structured data: y0 ~ time + y0 | id
##   X variable for graphs: time (week)
##   covariates: gender ()
##   reference class for covariate gender : Men
## Dataset characteristics:
##   number of subjects:      818
##   number of observations: 3616
##   average/min/max nb obs: 4.42 / 1 / 5

```

```

## First 10 lines of data:
##   id time y0 y0.1 gender mdv cens occ ytype
## 1   1    0  0    0   Men    0    0  1    1
## 2   1    6  0    0   Men    0    0  1    1
## 3   1   18  0    0   Men    0    0  1    1
## 4   2    0  1    1  Women    0    0  1    1
## 5   2    6  1    1  Women    0    0  1    1
## 6   2   12  1    1  Women    0    0  1    1
## 7   2   18  1    1  Women    0    0  1    1
## 8   2   24  1    1  Women    0    0  1    1
## 9   3    0  1    1   Men    0    0  1    1
## 10  3   12  1    1   Men    0    0  1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Binary model
## Model type: likelihood
## function(psi,id,xidep) {
##   tim<-xidep[,1]
##   y<-xidep[,2]
##   inter<-psi[id,1]
##   slope<-psi[id,2]
##   logit<-inter+slope*tim
##   pevent<-exp(logit)/(1+exp(logit))
##   logpdf<-rep(0,length(tim))
##   P.obs = (y==0)*(1-pevent)+(y==1)*pevent
##   logpdf <- log(P.obs)
##   return(logpdf)
## }
## <bytecode: 0x55e9db532fe0>
## Nb of parameters: 2
##   parameter names: theta1 theta2
##   distribution:
##   Parameter Distribution Estimated
## [1,] theta1    normal      Estimated
## [2,] theta2    normal      Estimated
## Variance-covariance matrix:
##   theta1 theta2
## theta1    1    0
## theta2    0    1
## Covariate model:
##   [,1] [,2]
## gender    1    1
## Initial values
##   theta1 theta2
## Pop.CondInit -1.5 -0.1
## Cov.CondInit  0.0  0.0
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100

```

```

##      Number of chains: 10
##      Seed: 1234567
##      Number of MCMC iterations for IS: 5000
##      Simulations:
##          nb of simulated datasets used for npde: 1000
##          nb of simulated datasets used for VPC: 100
##      Input/output
##          save the results to a file: FALSE
##          save the graphs to files: FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter          Estimate
## [1,] theta1              2.696
## [2,] beta_gender(theta1) -0.062
## [3,] theta2              -0.029
## [4,] beta_gender(theta2) -0.034
## -----
## ----- Variance of random effects -----
## -----
##      Parameter          Estimate
## theta1 omega2.theta1 2.3052
## theta2 omega2.theta2 0.0072
## -----
## ----- Correlation matrix of random effects -----
## -----
##              omega2.theta1 omega2.theta2
## omega2.theta1 1              0
## omega2.theta2 0              1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by importance sampling
##      -2LL= 3248.691
##      AIC = 3262.691
##      BIC = 3295.639
## -----

```

```

# proportion of 0's in the data
rapi.tab <- table(rapi.saemix$rapi == 0)
rapi.tab/sum(rapi.tab)

```

```

##
##      FALSE      TRUE
## 0.7909292 0.2090708

```

```

# Fit Poisson model to saemix.data1

```

```

saemix.hurdle1.cov2<-saemixModel(model=count.poisson,description="Count model Poisson",modeltype="likel
                                psi0=matrix(c(log(5),0.01),ncol=2,byrow=TRUE,dimnames=list(NULL, c("in
                                transform.par=c(0,0), omega.init=diag(c(0.5, 0.5)),
                                covariance.model =matrix(data=1, ncol=2, nrow=2),
                                covariate.model=matrix(c(1,1), ncol=2, byrow=TRUE))

```



```

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function: Count model Poisson
##   Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## <bytecode: 0x55e9e5cf2928>
##   Nb of parameters: 2
##     parameter names: intercept slope
##     distribution:
##       Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
##   Variance-covariance matrix:
##     intercept slope
## intercept      1      1
## slope          1      1
##   Covariate model:
##     intercept slope
## [1,]      1      1
##   Initial values
##     intercept slope
## Pop.CondInit  1.609438  0.01
## Cov.CondInit  0.000000  0.00

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)

hurdlefit1<-saemix(saemix.hurdle1.cov2,saemix.data1,saemix.options)

## Error in solve.default(F0) :
##   routine Lapack dgesv : le système est exactement singulier : U[2,2] = 0
## Error in data.frame(name = namallpar, estimate = estpar, se = estSE) :
##   arguments imply differing number of rows: 10, 11
## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset rapi.saemix[rapi.saemix$rapi > 0, ]
##   Structured data: rapi ~ time + rapi | id
##   X variable for graphs: time (week)
##   covariates: gender ()
##     reference class for covariate gender : Men
## Dataset characteristics:

```

```

##      number of subjects:      802
##      number of observations: 2860
##      average/min/max nb obs: 3.57 / 1 / 5
## First 10 lines of data:
##      id time rapi rapi.1 gender mdv cens occ ytype
## 4      2    0    3      3 Women    0    0    1    1
## 5      2    6    6      6 Women    0    0    1    1
## 6      2   12    5      5 Women    0    0    1    1
## 7      2   18    4      4 Women    0    0    1    1
## 8      2   24    5      5 Women    0    0    1    1
## 9      3    0    9      9   Men    0    0    1    1
## 10     3   12    1      1   Men    0    0    1    1
## 12     4    0    3      3 Women    0    0    1    1
## 13     4    6    2      2 Women    0    0    1    1
## 14     5    0   35     35 Women    0    0    1    1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Count model Poisson
## Model type: likelihood
## function(psi,id,xidep) {
##   time<-xidep[,1]
##   y<-xidep[,2]
##   intercept<-psi[id,1]
##   slope<-psi[id,2]
##   lambda<- exp(intercept + slope*time)
##   logp <- -lambda + y*log(lambda) - log(factorial(y))
##   return(logp)
## }
## <bytecode: 0x55e9e5cf2928>
## Nb of parameters: 2
##   parameter names: intercept slope
##   distribution:
##   Parameter Distribution Estimated
## [1,] intercept normal      Estimated
## [2,] slope      normal      Estimated
## Variance-covariance matrix:
##       intercept slope
## intercept      1    1
## slope          1    1
## Covariate model:
##       [,1] [,2]
## gender    1    1
## Initial values
##       intercept slope
## Pop.CondInit 1.609438 0.01
## Cov.CondInit 0.000000 0.00
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling

```

```

##      Number of iterations:  K1=300, K2=100
##      Number of chains:      1
##      Seed: 632545
##      Number of MCMC iterations for IS: 5000
##      Simulations:
##          nb of simulated datasets used for npde: 1000
##          nb of simulated datasets used for VPC: 100
##      Input/output
##          save the results to a file: FALSE
##          save the graphs to files:  FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter      Estimate
## [1,] intercept      1.8656
## [2,] beta_gender(intercept) -0.1972
## [3,] slope          -0.0059
## [4,] beta_gender(slope)  -0.0085
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate
## intercept omega2.intercept 0.6000
## slope      omega2.slope    0.0017
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.intercept omega2.slope
## omega2.intercept 1.00      -0.32
## omega2.slope    -0.32      1.00
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by importance sampling
##      -2LL= 17628.18
##      AIC = 17644.18
##      BIC = 17681.67
## -----

```

```
summary(hurdlefit0)
```

```

## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate
## 1      theta1      2.696
## 2 beta_gender(theta1) -0.062
## 3      theta2     -0.029
## 4 beta_gender(theta2) -0.034
## -----
## ----- Variance of random effects -----
## -----

```

```
##           Parameter Estimate
## theta1 omega2.theta1    2.3052
## theta2 omega2.theta2    0.0072
## -----
## ----- Correlation matrix of random effects -----
## -----
##           omega2.theta1 omega2.theta2
## omega2.theta1 1.00          0.00
## omega2.theta2 0.00          1.00
## -----
## ----- Statistical criteria -----
## -----
##
## Likelihood computed by importance sampling
##      -2LL= 3248.691
##      AIC = 3262.691
##      BIC = 3295.639
## -----
```

```
summary(hurdlefit1)
```

```
## -----
## ----- Fixed effects -----
## -----
##           Parameter Estimate
## 1          intercept    1.8656
## 2 beta_gender(intercept) -0.1972
## 3              slope   -0.0059
## 4    beta_gender(slope) -0.0085
## -----
## ----- Variance of random effects -----
## -----
##           Parameter Estimate
## intercept omega2.intercept  0.6000
## slope      omega2.slope     0.0017
## -----
## ----- Correlation matrix of random effects -----
## -----
##           omega2.intercept omega2.slope
## omega2.intercept 1.00          -0.32
## omega2.slope     -0.32          1.00
## -----
## ----- Statistical criteria -----
## -----
##
## Likelihood computed by importance sampling
##      -2LL= 17628.18
##      AIC = 17644.18
##      BIC = 17681.67
## -----
```

```
# Table form - compare to column B in Table 2
yfit0<-hurdlefit0
yfit1<-hurdlefit1
```

```
rr.tab<-data.frame(param=c("intercept", "beta.Male.inter", "slope", "beta.Male.slope", "omega.inter", "omega.slope", "poissonNoZero", "logistic"),
  poissonNoZero=c(yfit1@results@fixed.effects, c(sqrt(diag(yfit1@results@omega))))),
  logistic=c(yfit0@results@fixed.effects, c(sqrt(diag(yfit0@results@omega)))))

print(rr.tab)
```

```
##           param poissonNoZero    logistic
## 1      intercept    1.865583452  2.69565710
## 2 beta.Male.inter  -0.197211376 -0.06199618
## 3           slope  -0.005943599 -0.02895852
## 4 beta.Male.slope -0.008525854 -0.03367309
## 5      omega.inter    0.774608111  1.51828371
## 6      omega.slope    0.041313987  0.08465239
```

Time-to-event

TTE model - simulated data

TTE data simulated according to a Weibull model, hazard defined by shape (β) and scale (λ) as:

$$h(t) = \frac{\beta}{\lambda} \left(\frac{t}{\lambda} \right)^{\beta-1}$$

```
# Simulating TTE data
set.seed(12345)

nsuj<-50
xtim<-c(0)
tte.data<-data.frame(id=rep(1:nsuj,each=length(xtim)),time=rep(xtim,nsuj))
psiM<-data.frame(lambda=seq(1.6,2,length.out=length(unique(tte.data$id))),beta = 2)

simul.tte<-function(psi,id,xidep) {
  T<-xidep
  N <- nrow(psi)
  Nj <- length(T)
  censoringtime = 3
  lambda <- psi[id,1]
  beta <- psi[id,2]
  obs <-rep(0,length(T))
  for (i in (1:N)){
    obs[id==i] <- rweibull(n=length(id[id==i]), shape=beta[i], scale=lambda[i])
  }
  obs[obs>censoringtime]<-censoringtime
  return(obs)
}

preds <- simul.tte(psiM, tte.data$id, tte.data[,c("time")])
tte.data$y<-0
tte.data$tlat<-preds
dat1<-tte.data[,c("id","time","y")]
dat2<-tte.data[,c("id","tlat","y")]
dat2$y<-as.integer(dat2$tlat>0 & dat2$tlat<3)
colnames(dat2)[2]<-"time"
```

```

tte.data<-rbind(dat1,dat2)
tte.data<-tte.data[order(tte.data$id, tte.data$time),]
tte.psiM<-psiM

# Simulate T from Weibull (check)
if(FALSE) {
  lambda<-2
  beta<-2
  nsim<-5000
  # By hand
  q1<-runif(nsim)
  # tevent<-lambda*exp(log(q1)/beta)
  tevent<-lambda*exp(log(-log(q1))/beta)
  tevent<-sort(tevent)
  # plot(tevent, exp(-(tevent/lambda)^beta))
  tevent2<-sort(rweibull(nsim, shape=beta, scale=lambda))
  plot(tevent, tevent2)
  abline(0,1)
}

saemix.data<-saemixData(name.data=tte.data, name.group=c("id"),
  name.predictors=c("time"), name.response="y")

##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset tte.data
##   Structured data: y ~ time | id
##   Predictor: time ()

tte.model<-function(psi,id,xidep) {
  T<-xidep[,1]
  N <- nrow(psi)
  Nj <- length(T)
  # censoringtime = 6
  censoringtime = max(T)
  lambda <- psi[id,1]
  beta <- psi[id,2]
  init <- which(T==0)
  cens <- which(T==censoringtime)
  ind <- setdiff(1:Nj, append(init,cens))
  hazard <- (beta/lambda)*(T/lambda)^(beta-1)
  H <- (T/lambda)^beta
  logpdf <- rep(0,Nj)
  logpdf[cens] <- -H[cens] + H[cens-1]
  logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind])
  return(logpdf)
}

saemix.model<-saemixModel(model=tte.model,description="time model",modeltype="likelihood",

```

```

psi0=matrix(c(1,2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","beta"))),
transform.par=c(1,1),covariance.model=matrix(c(1,0,0,1),ncol=2, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: time model
## Model type: likelihood
## function(psi,id,xidep) {
## T<-xidep[,1]
## N <- nrow(psi)
## Nj <- length(T)
## # censoringtime = 6
## censoringtime = max(T)
## lambda <- psi[id,1]
## beta <- psi[id,2]
## init <- which(T==0)
## cens <- which(T==censoringtime)
## ind <- setdiff(1:Nj, append(init,cens))
## hazard <- (beta/lambda)*(T/lambda)^(beta-1)
## H <- (T/lambda)^beta
## logpdf <- rep(0,Nj)
## logpdf[cens] <- -H[cens] + H[cens-1]
## logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind])
## return(logpdf)
## }
## Nb of parameters: 2
## parameter names: lambda beta
## distribution:
## Parameter Distribution Estimated
## [1,] lambda log-normal Estimated
## [2,] beta log-normal Estimated
## Variance-covariance matrix:
## lambda beta
## lambda 1 0
## beta 0 1
## No covariate in the model.
## Initial values
## lambda beta
## Pop.CondInit 1 2

saemix.model<-saemixModel(model=tte.model,description="time model",modeltype="likelihood",
psi0=matrix(c(1,2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","beta"))),
transform.par=c(1,1),covariance.model=matrix(c(1,0,0,0),ncol=2, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: time model
## Model type: likelihood

```

```

## function(psi,id,xidep) {
##   T<-xidep[,1]
##   N <- nrow(psi)
##   Nj <- length(T)
##   # censoringtime = 6
##   censoringtime = max(T)
##   lambda <- psi[id,1]
##   beta <- psi[id,2]
##   init <- which(T==0)
##   cens <- which(T==censoringtime)
##   ind <- setdiff(1:Nj, append(init,cens))
##   hazard <- (beta/lambda)*(T/lambda)^(beta-1)
##   H <- (T/lambda)^beta
##   logpdf <- rep(0,Nj)
##   logpdf[cens] <- -H[cens] + H[cens-1]
##   logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind])
##   return(logpdf)
## }
##   Nb of parameters: 2
##       parameter names:  lambda beta
##       distribution:
##       Parameter Distribution Estimated
## [1,] lambda    log-normal  Estimated
## [2,] beta      log-normal  Estimated
##   Variance-covariance matrix:
##       lambda beta
## lambda      1    0
## beta        0    0
##   No covariate in the model.
##   Initial values
##       lambda beta
## Pop.CondInit      1    2

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)
tte.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset tte.data
##   Structured data: y ~ time | id
##   Predictor: time ()
## Dataset characteristics:
##   number of subjects:      50
##   number of observations: 100
##   average/min/max nb obs: 2.00 / 2 / 2
## First 10 lines of data:
##   id      time y mdv cens occ ytype
## 1    1 0.0000000 0  0    0  1      1
## 51   1 0.9152915 1  0    0  1      1
## 2    2 0.0000000 0  0    0  1      1
## 52   2 0.5857074 1  0    0  1      1

```



```

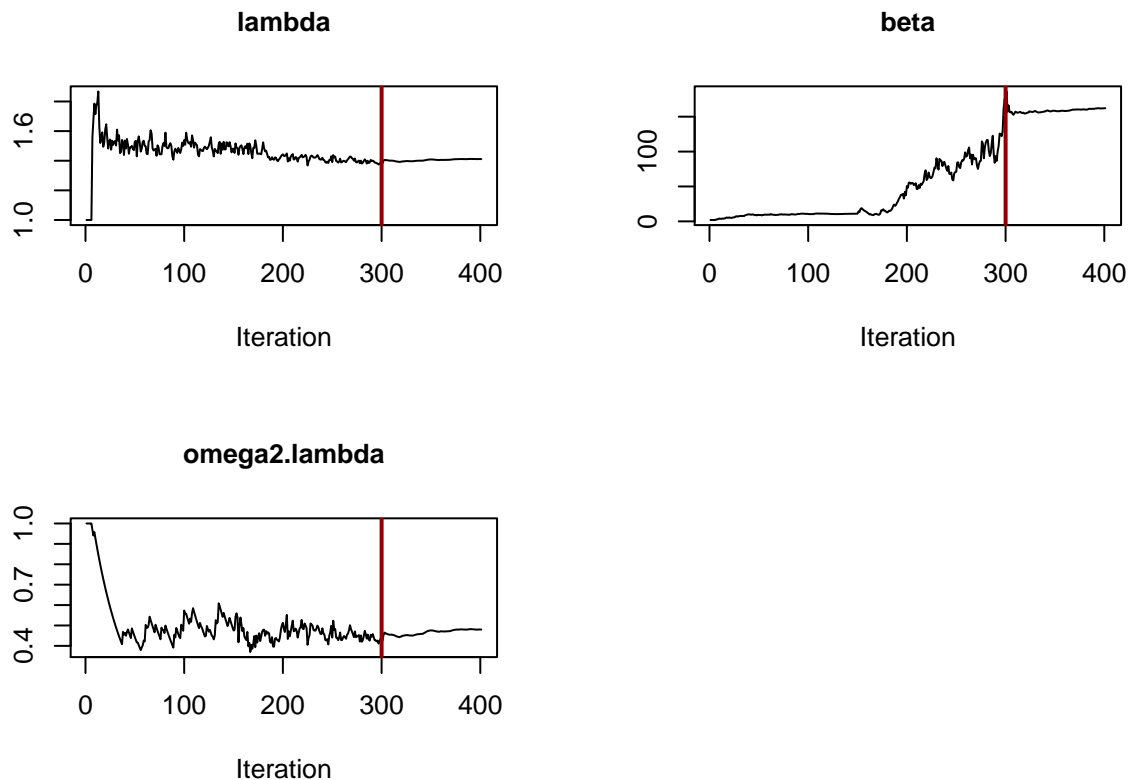
## 3 3 0.0000000 0 0 0 1 1
## 53 3 0.8447454 1 0 0 1 1
## 4 4 0.0000000 0 0 0 1 1
## 54 4 0.5648408 1 0 0 1 1
## 5 5 0.0000000 0 0 0 1 1
## 55 5 1.4458047 1 0 0 1 1
## -----
## ---- Model ----
## -----
## Nonlinear mixed-effects model
## Model function: time model
## Model type: likelihood
## function(psi,id,xidep) {
##   T<-xidep[,1]
##   N <- nrow(psi)
##   Nj <- length(T)
##   # censoringtime = 6
##   censoringtime = max(T)
##   lambda <- psi[id,1]
##   beta <- psi[id,2]
##   init <- which(T==0)
##   cens <- which(T==censoringtime)
##   ind <- setdiff(1:Nj, append(init,cens))
##   hazard <- (beta/lambda)*(T/lambda)^(beta-1)
##   H <- (T/lambda)^beta
##   logpdf <- rep(0,Nj)
##   logpdf[cens] <- -H[cens] + H[cens-1]
##   logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind])
##   return(logpdf)
## }
## <bytecode: 0x55e9df7a8478>
## Nb of parameters: 2
##   parameter names: lambda beta
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda log-normal Estimated
## [2,] beta log-normal Estimated
## Variance-covariance matrix:
##   lambda beta
## lambda 1 0
## beta 0 0
## No covariate in the model.
## Initial values
##   lambda beta
## Pop.CondInit 1 2
## -----
## ---- Key algorithm options ----
## -----
## Estimation of individual parameters (MAP)
## Estimation of standard errors and linearised log-likelihood
## Estimation of log-likelihood by importance sampling
## Number of iterations: K1=300, K2=100
## Number of chains: 1
## Seed: 632545

```

```

##      Number of MCMC iterations for IS: 5000
##      Simulations:
##          nb of simulated datasets used for npde: 1000
##          nb of simulated datasets used for VPC: 100
##      Input/output
##          save the results to a file: FALSE
##          save the graphs to files: FALSE
## -----
## ----- Results -----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] lambda      1.4      0.58  41
## [2,] beta      162.2     5675.89 3500
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate SE      CV(%)
## lambda omega2.lambda 0.48      0.21  44
## -----
## ----- Correlation matrix of random effects -----
## -----
##      omega2.lambda
## omega2.lambda 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 573.0104
##      AIC = 581.0104
##      BIC = 588.6585
##
## Likelihood computed by importance sampling
##      -2LL= 122.2899
##      AIC = 130.2899
##      BIC = 137.938
## -----
plot(tte.fit, plot.type="convergence")

```



TTE model - lung cancer

- create dataset for saemix (once) using the lung data from the survival package
- changes
 - saemix format: added time=0
 - created one column for status (dead or alive, recoded as 1/0) and one for censoring (0/1)
 - removed subjects with missing age, institution, sex, or ph scores (ecog and karno)

Checks

- The **Surv** function from the **survival** package creates a survival object for use as the response in a model formula.
 - one entry for each subject that is the survival time, which is followed by a + if the subject was censored
 - transform lung.saemix in the Surv format to check the survival function w/r saemix fit
- Weibull model
 - parametric survival function

$$S(t) = e^{-\left(\frac{t}{\lambda}\right)^\beta}$$

- Also tried computing a SE for $S(t)$ using the delta-method where the vector of derivatives for the survival function of Weibull model are:

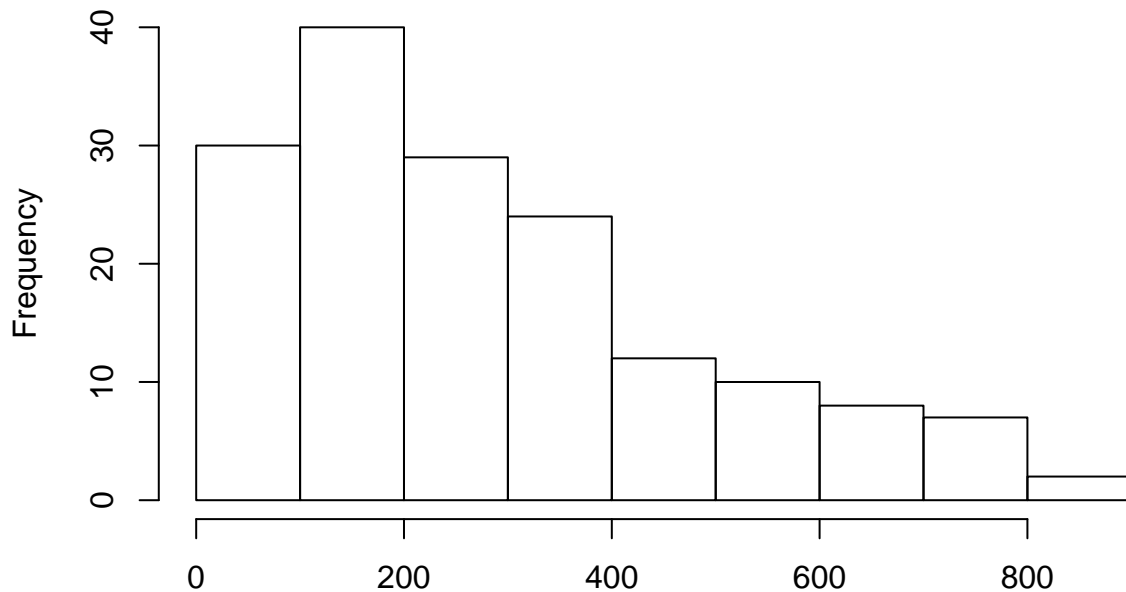
$$\begin{pmatrix} \frac{\delta S}{\delta \lambda} \\ \frac{\delta S}{\delta \beta} \end{pmatrix} = \begin{pmatrix} \frac{\beta}{\lambda} \left(\frac{t}{\lambda}\right)^\beta e^{-\left(\frac{t}{\lambda}\right)^\beta} \\ -\ln\left(\frac{t}{\lambda}\right) \left(\frac{t}{\lambda}\right)^\beta e^{-\left(\frac{t}{\lambda}\right)^\beta} \end{pmatrix}$$

- works pretty well compared to the non-parametric KM estimate

```
if(testMode)
  data(lung.saemix) else
```

```
lung.saemix<-read.table(file.path(datDir, "lung.saemix.tab"), header=TRUE)
hist(lung.saemix$time[lung.saemix$status==1])
```

Histogram of lung.saemix\$time[lung.saemix\$status == 1]



lung.saemix\$time[lung.saemix\$status == 1]

```
# Note: missing data in pat.karno, wt.loss and meal.cal
if(FALSE)
  print(summary(lung.saemix))

saemix.data<-saemixData(name.data=lung.saemix,header=TRUE,name.group=c("id"),
  name.predictors=c("time","status","cens"),name.response=c("status"),
  name.covariates=c("age", "sex", "ph.ecog", "ph.karno", "pat.karno", "wt.loss", "meal.cal"),
  units=list(x="days",y="",covariates=c("yr","", "-", "%", "%", "cal", "pounds")))

## [1] "age"      "sex"      "ph.ecog"  "ph.karno" "pat.karno" "wt.loss"
## [7] "meal.cal"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset lung.saemix
##   Structured data: status ~ time + status + cens | id
##   X variable for graphs: time (days)
##   covariates: age (yr), sex (), ph.ecog (-), ph.karno (%), pat.karno (%), wt.loss (cal), meal.cal
##   reference class for covariate sex : 0

weibulltte.model<-function(psi,id,xidep) {
  T<-xidep[,1]
  y<-xidep[,2] # events (1=event, 0=no event)
```

```

cens<-which(xidep[,3]==1) # censoring times (subject specific)
init <- which(T==0)
lambda <- psi[id,1] # Parameters of the Weibull model
beta <- psi[id,2]
Nj <- length(T)

ind <- setdiff(1:Nj, append(init,cens)) # indices of events
hazard <- (beta/lambda)*(T/lambda)^(beta-1) # ln(H')
H <- (T/lambda)^beta # ln(H)
logpdf <- rep(0,Nj) # ln(l(T=0))=0
logpdf[cens] <- -H[cens] + H[cens-1] # ln(l(T=censoring time))
logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind]) # ln(l(T=event time))
return(logpdf)
}

saemix.model<-saemixModel(model=weibulltte.model,description="time model",modeltype="likelihood",
  psi0=matrix(c(1,2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","beta"))),
  transform.par=c(1,1),covariance.model=matrix(c(1,0,0,0),ncol=2, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: time model
## Model type: likelihood
## function(psi,id,xidep) {
## T<-xidep[,1]
## y<-xidep[,2] # events (1=event, 0=no event)
## cens<-which(xidep[,3]==1) # censoring times (subject specific)
## init <- which(T==0)
## lambda <- psi[id,1] # Parameters of the Weibull model
## beta <- psi[id,2]
## Nj <- length(T)
##
## ind <- setdiff(1:Nj, append(init,cens)) # indices of events
## hazard <- (beta/lambda)*(T/lambda)^(beta-1) # ln(H')
## H <- (T/lambda)^beta # ln(H)
## logpdf <- rep(0,Nj) # ln(l(T=0))=0
## logpdf[cens] <- -H[cens] + H[cens-1] # ln(l(T=censoring time))
## logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind]) # ln(l(T=event time))
## return(logpdf)
## }
## Nb of parameters: 2
## parameter names: lambda beta
## distribution:
## Parameter Distribution Estimated
## [1,] lambda log-normal Estimated
## [2,] beta log-normal Estimated
## Variance-covariance matrix:
## lambda beta
## lambda 1 0
## beta 0 0
## No covariate in the model.

```

```

##      Initial values
##      lambda beta
## Pop.CondInit      1      2

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, displayProgress=FALSE)
tte.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##      longitudinal data for use with the SAEM algorithm
## Dataset lung.saemix
##      Structured data: status ~ time + status + cens | id
##      X variable for graphs: time (days)
##      covariates: age (yr), sex (), ph.ecog (-), ph.karno (%), pat.karno (%), wt.loss (cal), meal.cal
##      reference class for covariate sex : 0
## Dataset characteristics:
##      number of subjects:      225
##      number of observations: 450
##      average/min/max nb obs: 2.00 / 2 / 2
## First 10 lines of data:
##      id time status cens status.1 age sex ph.ecog ph.karno pat.karno wt.loss
## 1  1  0  0  0  0  74  0  1  90  100  NA
## 2  1 306  1  0  1  74  0  1  90  100  NA
## 3  2  0  0  0  0  68  0  0  90  90  15
## 4  2 455  1  0  1  68  0  0  90  90  15
## 5  3  0  0  0  0  56  0  0  90  90  15
## 6  3 1010 0  1  0  56  0  0  90  90  15
## 7  4  0  0  0  0  57  0  1  90  60  11
## 8  4 210  1  0  1  57  0  1  90  60  11
## 9  5  0  0  0  0  60  0  0  100 90  0
## 10 5 883  1  0  1  60  0  0  100 90  0
##      meal.cal mdv cens.1 occ ytype
## 1  1175  0  0  1  1
## 2  1175  0  0  1  1
## 3  1225  0  0  1  1
## 4  1225  0  0  1  1
## 5  NA  0  0  1  1
## 6  NA  0  0  1  1
## 7  1150  0  0  1  1
## 8  1150  0  0  1  1
## 9  NA  0  0  1  1
## 10 NA  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
##      Model function: time model
##      Model type: likelihood
## function(psi,id,xidep) {
##      T<-xidep[,1]
##      y<-xidep[,2] # events (1=event, 0=no event)
##      cens<-which(xidep[,3]==1) # censoring times (subject specific)

```

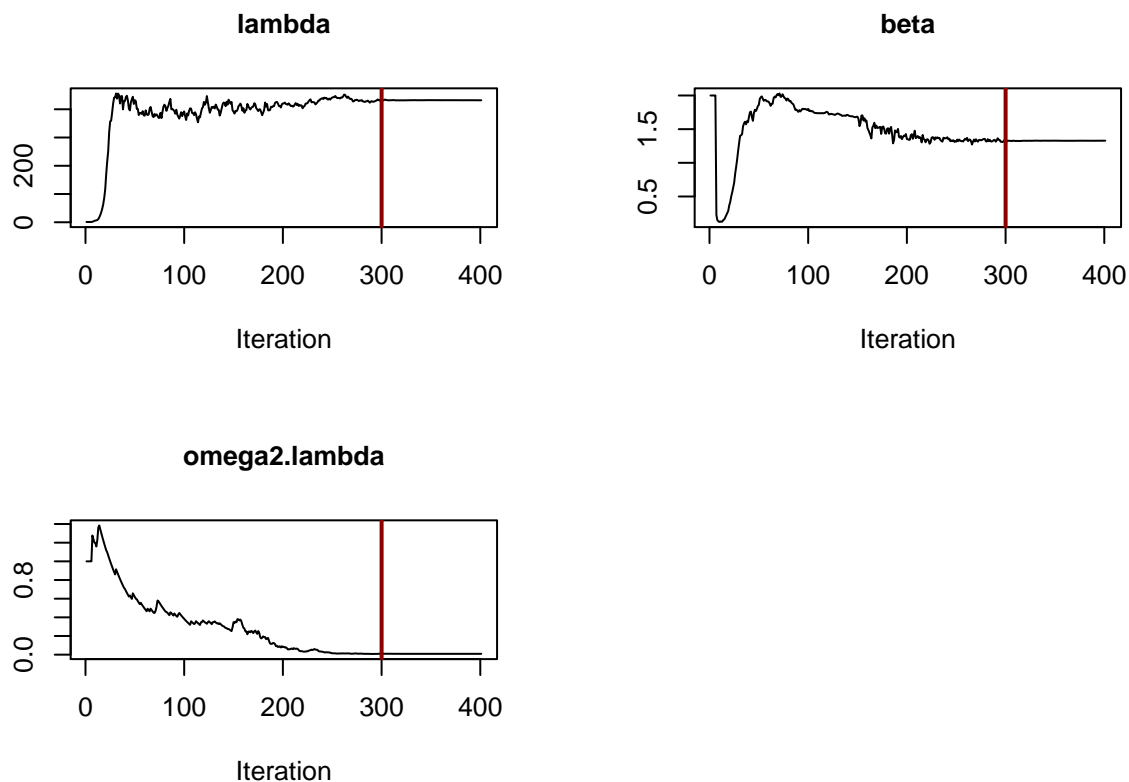
```

##  init <- which(T==0)
##  lambda <- psi[id,1] # Parameters of the Weibull model
##  beta <- psi[id,2]
##  Nj <- length(T)
##
##  ind <- setdiff(1:Nj, append(init,cens)) # indices of events
##  hazard <- (beta/lambda)*(T/lambda)^(beta-1) # ln(H')
##  H <- (T/lambda)^beta # ln(H)
##  logpdf <- rep(0,Nj) # ln(l(T=0))=0
##  logpdf[cens] <- -H[cens] + H[cens-1] # ln(l(T=censoring time))
##  logpdf[ind] <- -H[ind] + H[ind-1] + log(hazard[ind]) # ln(l(T=event time))
##  return(logpdf)
## }
## <bytecode: 0x55e9e4ee0798>
##  Nb of parameters: 2
##      parameter names:  lambda beta
##      distribution:
##      Parameter Distribution Estimated
## [1,] lambda    log-normal  Estimated
## [2,] beta      log-normal  Estimated
##  Variance-covariance matrix:
##      lambda beta
## lambda      1    0
## beta        0    0
##      No covariate in the model.
##      Initial values
##      lambda beta
## Pop.CondInit      1    2
## -----
## ----  Key algorithm options  ----
## -----
##      Estimation of individual parameters (MAP)
##      Estimation of standard errors and linearised log-likelihood
##      Estimation of log-likelihood by importance sampling
##      Number of iterations:  K1=300, K2=100
##      Number of chains:  1
##      Seed:  632545
##      Number of MCMC iterations for IS:  5000
##      Simulations:
##      nb of simulated datasets used for npde:  1000
##      nb of simulated datasets used for VPC:  100
##      Input/output
##      save the results to a file:  FALSE
##      save the graphs to files:  FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter Estimate SE      CV(%)
## [1,] lambda    431.8    51.60 12
## [2,] beta       1.3     0.19 14
## -----
## ----- Variance of random effects -----

```

```
## -----
##      Parameter      Estimate SE   CV(%)
## lambda omega2.lambda 0.009   0.17 1858
## -----
## ----- Correlation matrix of random effects -----
## -----
##              omega2.lambda
## omega2.lambda 1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by linearisation
##      -2LL= 5189.352
##      AIC = 5197.352
##      BIC = 5211.017
##
## Likelihood computed by importance sampling
##      -2LL= 2269.357
##      AIC = 2277.357
##      BIC = 2291.021
## -----
```

```
plot(tte.fit, plot.type="convergence")
```



```
ypred<-predict(tte.fit)

# Use survival package to assess Survival curve
if(TRUE) {
  library(survival)
  lung.surv<-lung.saemix[lung.saemix$time>0,]
```



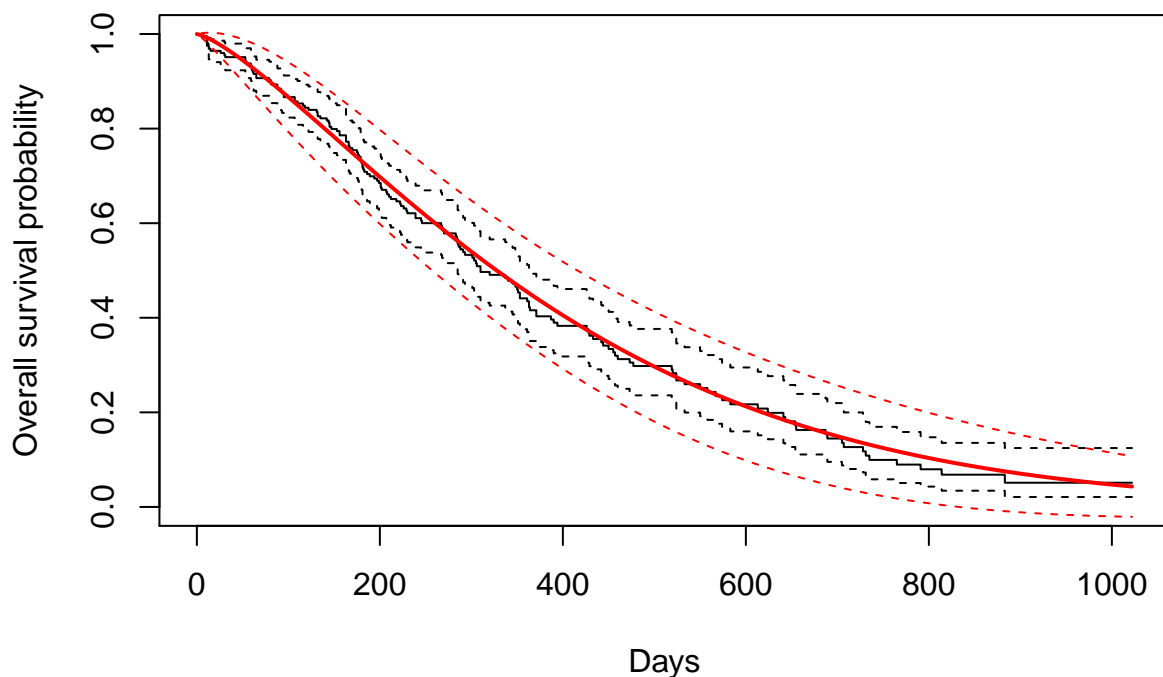
```

lung.surv$status<-lung.surv$status+1
Surv(lung.surv$time, lung.surv$status) # 1=censored, 2=dead
f1 <- survfit(Surv(time, status) ~ 1, data = lung.surv)
xtim<-seq(0,max(lung.saemix$time), length.out=200)
estpar<-tte.fit@results@fixed.effects
estse<-tte.fit@results@se.fixed
ypred<-exp(-(xtim/estpar[1])^(estpar[2]))

# Computing SE for the survival curve based on linearised FIM (probably not a good idea) through the de
invfim<-solve(tte.fit@results@fim[1:2,1:2])
xcal<- (xtim/estpar[1])^estpar[2]
dsdbeta<- -log(xtim/estpar[1]) * xcal *exp(-xcal)
dsdalpha<- estpar[2]/estpar[1] * xcal *exp(-xcal)
xmat<-rbind(dsdalpha, dsdbeta)
# x1<-t(xmat[,1:3]) %%% invfim %%% xmat[,1:3]
sesurv<-rep(0,length(xcal))
for(i in 1:length(xcal))
  sesurv[i]<-sqrt(t(xmat[,i]) %%% invfim %%% xmat[,i])
plot(f1, xlab = "Days", ylab = "Overall survival probability")
lines(xtim,ypred, col="red",lwd=2)
lines(xtim,ypred+1.96*sesurv, col="red",lwd=1, lty=2)
lines(xtim,ypred-1.96*sesurv, col="red",lwd=1, lty=2)

# ypred2<-exp(-(xtim/(estpar[1]-1.96*sqrt(invfim[1,1]))^(estpar[2]+1.96*sqrt(invfim[2,2]))))
# ypred3<-exp(-(xtim/(estpar[1]+1.96*sqrt(invfim[1,1]))^(estpar[2]+1.96*sqrt(invfim[2,2]))))
# lines(xtim,ypred2, col="blue",lwd=1, lty=2)
# lines(xtim,ypred3, col="blue",lwd=1, lty=2)
}

```



RTTE model

- again difficult to find real data
- simulated data
 - Exemple simulé de Belhal **TODO**
 - data from the Monolix documentation: absolutely no indication where the data comes from (weibull_data.txt for the weibullRTTE.mlxtran project in the demo)
- search for real data
 - asked Ulrika Simonsson for the RTTE data on post-operative pain (Pain Medicine 2015)
 - data on events in Gaucher disease used for the ENSAI workshops (but few events)
 - discretised PCA events during warfarin treatment ? (from the warfarin PK/PD) (but threshold ?)

```
# Simulating RTTE data by simulating from U(0,1) and inverting the cdf
simul.rtte.unif<-function(psi) { # xidep, id not important, we only use psi
  censoringtime <- 3
  maxevents <- 30
  lambda <- psi[,1]
  beta <- psi[,2]
  simdat<-NULL
  N<-nrow(psi)
  for(i in 1:N) {
    eventTimes<-c(0)
    T<-0
    Vj<-runif(1)
    # T <- (-log(Vj)*lambda[i])^(beta[i])
    T<-lambda[i]*(-log(Vj))^(1/beta[i])
    nev<-0
    while (T < censoringtime & nev<maxevents){
      eventTimes <- c(eventTimes, T)
      nev<-nev+1
      Vj<-runif(1)
      # T <- T+(-log(Vj)*lambda[i])^(beta[i])
      # T<-(-log(Vj)*lambda[i] + T^(1/beta[i]))^(beta[i])
      T<-lambda[i]*(-log(Vj) + (T/lambda[i])^(beta[i]))^(1/beta[i])
    }
    if(nev==maxevents) {
      message("Reached maximum number of events\n")
    }
    eventTimes<-c(eventTimes, censoringtime)
    cens<-rep(1,length(eventTimes))
    cens[1]<-cens[length(cens)]<-0
    simdat<-rbind(simdat,
                  data.frame(id=i, T=eventTimes, status=cens))
  }
  return(simdat)
}
```

```
# Subjects
set.seed(12345)
param<-c(2, 1.5, 0.5)
# param<-c(4, 1.2, 0.3)
omega<-c(0.25,0.25)
nsuj<-200
risk<-rep(0,nsuj)
```

```

risk[(nsuj/2+1):nsuj]<-1
psiM<-data.frame(lambda=param[1]*exp(rnorm(nsuj,sd=omega[1])), beta=param[2]*exp(param[3]*risk+rnorm(nsuj,sd=omega[2])),
simdat <- simul.rtte.unif(psiM)

## Reached maximum number of events
simdat$risk<-as.integer(simdat$id>(nsuj/2))

# Simulate T from Weibull (check)
if(FALSE) {
  lambda<-2
  beta<-2
  nsim<-5000
  # By hand
  q1<-runif(nsim)
  # tevent<-lambda*exp(log(q1)/beta)
  tevent<-lambda*exp(log(-log(q1))/beta)
  tevent<-sort(tevent)
  # plot(tevent, exp(-(tevent/lambda)^beta))
  tevent2<-sort(rweibull(nsim, shape=beta, scale=lambda))
  plot(tevent, tevent2)
  abline(0,1)
}

saemix.data<-saemixData(name.data=simdat, name.group=c("id"), name.predictors=c("T"), name.response="status")

## [1] "risk"
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset simdat
##   Structured data: status ~ T | id
##   Predictor: T ()
##   covariates: risk (-)
##   reference class for covariate risk : 0

rtte.model<-function(psi,id,xidep) {
  T<-xidep[,1]
  N <- nrow(psi) # nb of subjects
  Nj <- length(T) # nb of events (including 0 and censoring times)
  # censoringtime = 6
  censoringtime = max(T) # same censoring for everyone
  lambda <- psi[id,1]
  beta <- psi[id,2]
  tinit <- which(T==0) # indices of beginning of observation period
  tcens <- which(T==censoringtime) # indices of censored events
  tevent <- setdiff(1:Nj, append(tinit,tcens)) # indices of non-censored event times
  hazard <- (beta/lambda)*(T/lambda)^(beta-1)
  H <- (T/lambda)^beta
  logpdf <- rep(0,Nj)
  logpdf[tcens] <- -H[tcens] + H[tcens-1]
}

```

```

logpdf[tevent] <- -H[tevent] + H[tevent-1] + log(hazard[tevent])
return(logpdf)
}

saemix.model.base<-saemixModel(model=rtte.model,description="Repeated TTE model",modeltype="likelihood",
                                psi0=matrix(c(1,2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","beta")),
                                transform.par=c(1,1),covariance.model=matrix(c(1,0,0,1),ncol=2, byrow=TRUE))

##
##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
## Model function: Repeated TTE model
## Model type: likelihood
## function(psi,id,xidep) {
##   T<-xidep[,1]
##   N <- nrow(psi) # nb of subjects
##   Nj <- length(T) # nb of events (including 0 and censoring times)
##   # censoringtime = 6
##   censoringtime = max(T) # same censoring for everyone
##   lambda <- psi[id,1]
##   beta <- psi[id,2]
##   tinit <- which(T==0) # indices of beginning of observation period
##   tcens <- which(T==censoringtime) # indices of censored events
##   tevent <- setdiff(1:Nj, append(tinit,tcens)) # indices of non-censored event times
##   hazard <- (beta/lambda)*(T/lambda)^(beta-1)
##   H <- (T/lambda)^beta
##   logpdf <- rep(0,Nj)
##   logpdf[tcens] <- -H[tcens] + H[tcens-1]
##   logpdf[tevent] <- -H[tevent] + H[tevent-1] + log(hazard[tevent])
##   return(logpdf)
## }
## Nb of parameters: 2
##   parameter names: lambda beta
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda    log-normal    Estimated
## [2,] beta      log-normal    Estimated
##   Variance-covariance matrix:
##       lambda beta
## lambda      1    0
## beta        0    1
##   No covariate in the model.
##   Initial values
##       lambda beta
## Pop.CondInit      1    2

saemix.model<-saemixModel(model=rtte.model,description="Repeated TTE model",modeltype="likelihood",
                            psi0=matrix(c(1,2),ncol=2,byrow=TRUE,dimnames=list(NULL, c("lambda","beta")),
                            transform.par=c(1,1),covariate.model=matrix(c(0,1),ncol=2),
                            covariance.model=matrix(c(1,0,0,1),ncol=2, byrow=TRUE))

##

```

```

##
## The following SaemixModel object was successfully created:
##
## Nonlinear mixed-effects model
##   Model function: Repeated TTE model
##   Model type: likelihood
## function(psi,id,xidep) {
##   T<-xidep[,1]
##   N <- nrow(psi) # nb of subjects
##   Nj <- length(T) # nb of events (including 0 and censoring times)
##   # censoringtime = 6
##   censoringtime = max(T) # same censoring for everyone
##   lambda <- psi[id,1]
##   beta <- psi[id,2]
##   tinit <- which(T==0) # indices of beginning of observation period
##   tcens <- which(T==censoringtime) # indices of censored events
##   tevent <- setdiff(1:Nj, append(tinit,tcens)) # indices of non-censored event times
##   hazard <- (beta/lambda)*(T/lambda)^(beta-1)
##   H <- (T/lambda)^beta
##   logpdf <- rep(0,Nj)
##   logpdf[tcens] <- -H[tcens] + H[tcens-1]
##   logpdf[tevent] <- -H[tevent] + H[tevent-1] + log(hazard[tevent])
##   return(logpdf)
## }
##   Nb of parameters: 2
##       parameter names:  lambda beta
##       distribution:
##       Parameter Distribution Estimated
## [1,] lambda    log-normal    Estimated
## [2,] beta      log-normal    Estimated
##   Variance-covariance matrix:
##       lambda beta
## lambda      1    0
## beta        0    1
##   Covariate model:
##       lambda beta
## [1,]      0    1
##   Initial values
##       lambda beta
## Pop.CondInit      1    2
## Cov.CondInit      0    0

saemix.options<-list(seed=632545,save=FALSE,save.graphs=FALSE, fim=FALSE, displayProgress=FALSE)
rtte.fit<-saemix(saemix.model,saemix.data,saemix.options)

## Nonlinear mixed-effects model fit by the SAEM algorithm
## -----
## ----          Data          ----
## -----
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset simdat
##   Structured data: status ~ T | id
##   Predictor: T ()
##   covariates: risk (-)

```

```

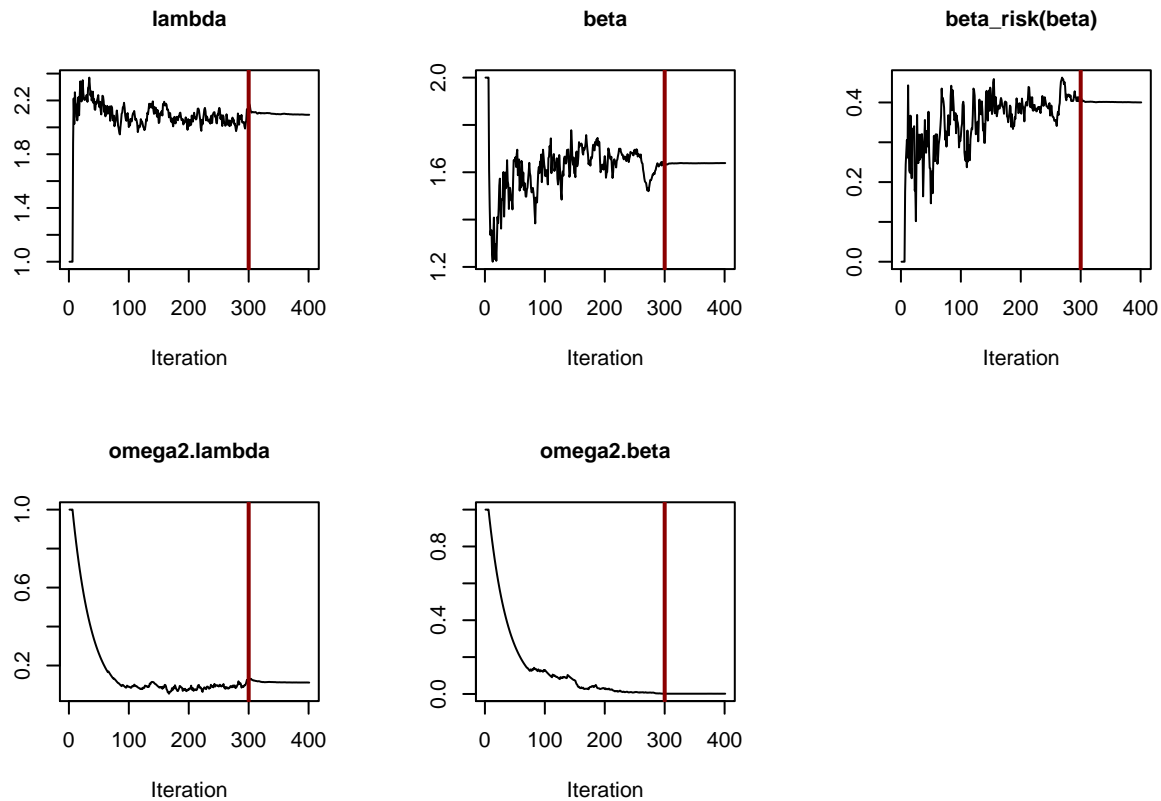
##      reference class for covariate risk : 0
## Dataset characteristics:
##      number of subjects:      200
##      number of observations: 967
##      average/min/max nb obs: 4.83 / 2 / 32
## First 10 lines of data:
##      id      T status risk mdv cens occ ytype
## 1  1 0.0000000      0  0  0  0  1  1
## 2  1 0.7520145      1  0  0  0  1  1
## 3  1 0.8775847      1  0  0  0  1  1
## 4  1 2.4331650      1  0  0  0  1  1
## 5  1 3.0000000      0  0  0  0  1  1
## 6  2 0.0000000      0  0  0  0  1  1
## 7  2 1.3712351      1  0  0  0  1  1
## 8  2 3.0000000      0  0  0  0  1  1
## 9  3 0.0000000      0  0  0  0  1  1
## 10 3 2.8564910      1  0  0  0  1  1
## -----
## ----          Model          ----
## -----
## Nonlinear mixed-effects model
## Model function: Repeated TTE model
## Model type: likelihood
## function(psi,id,xidep) {
##   T<-xidep[,1]
##   N <- nrow(psi) # nb of subjects
##   Nj <- length(T) # nb of events (including 0 and censoring times)
##   # censoringtime = 6
##   censoringtime = max(T) # same censoring for everyone
##   lambda <- psi[id,1]
##   beta <- psi[id,2]
##   tinit <- which(T==0) # indices of beginning of observation period
##   tcens <- which(T==censoringtime) # indices of censored events
##   tevent <- setdiff(1:Nj, append(tinit,tcens)) # indices of non-censored event times
##   hazard <- (beta/lambda)*(T/lambda)^(beta-1)
##   H <- (T/lambda)^beta
##   logpdf <- rep(0,Nj)
##   logpdf[tcens] <- -H[tcens] + H[tcens-1]
##   logpdf[tevent] <- -H[tevent] + H[tevent-1] + log(hazard[tevent])
##   return(logpdf)
## }
## <bytecode: 0x55e9de24a7d0>
## Nb of parameters: 2
##   parameter names:  lambda beta
##   distribution:
##   Parameter Distribution Estimated
## [1,] lambda    log-normal Estimated
## [2,] beta      log-normal Estimated
## Variance-covariance matrix:
##   lambda beta
## lambda      1  0
## beta        0  1
## Covariate model:
##   [,1] [,2]

```

```

## risk    0    1
##      Initial values
##              lambda beta
## Pop.CondInit      1    2
## Cov.CondInit      0    0
## -----
## ----      Key algorithm options      ----
## -----
##      Estimation of individual parameters (MAP)
##      Estimation of log-likelihood by importance sampling
##      Number of iterations:  K1=300, K2=100
##      Number of chains:  1
##      Seed:  632545
##      Number of MCMC iterations for IS:  5000
##      Simulations:
##          nb of simulated datasets used for npde:  1000
##          nb of simulated datasets used for VPC:  100
##      Input/output
##          save the results to a file:  FALSE
##          save the graphs to files:  FALSE
## -----
## ----                      Results                      ----
## -----
## ----- Fixed effects -----
## -----
##      Parameter      Estimate
## [1,] lambda          2.1
## [2,] beta            1.6
## [3,] beta_risk(beta) 0.4
## -----
## ----- Variance of random effects -----
## -----
##      Parameter      Estimate
## lambda omega2.lambda 0.1125
## beta  omega2.beta    0.0015
## -----
## ----- Correlation matrix of random effects -----
## -----
##              omega2.lambda omega2.beta
## omega2.lambda 1              0
## omega2.beta   0              1
## -----
## ----- Statistical criteria -----
## -----
## Likelihood computed by importance sampling
##      -2LL= 690.2485
##      AIC = 702.2485
##      BIC = 722.0384
## -----
plot(rtte.fit, plot.type="convergence")

```



```
saemix.data<-saemixData(name.data=tte.data, name.group=c("id"),
  name.predictors=c("time"), name.response="y")
```

```
##
##
## The following SaemixData object was successfully created:
##
## Object of class SaemixData
##   longitudinal data for use with the SAEM algorithm
## Dataset tte.data
##   Structured data: y ~ time | id
##   Predictor: time ()
```

Exiting

```
if(testMode) {
  dev_mode()
}
```