# Simulation suite - comparing results

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# 13/09/2022

# Setup

# Computational functions

Note to self: bias=mean(estimation errors)

- summary statistics
  - sample mean:

$$\bar{\theta} = \frac{1}{K} \sum_{k} \hat{\theta}_{k}$$

- sample variance

$$S_{\theta}^2 = var(\hat{\theta} - \bar{\theta}) = \frac{1}{K - 1} \sum_k (\hat{\theta}_k - \bar{\theta})^2$$

- absolute metrics
  - absolute bias
    - \* defined as the difference

$$E(\hat{\theta}) - \theta_0$$

\* estimated as

$$\bar{\theta} - \theta_0$$

- precision
  - \* defined as the variance of the estimates

$$E\left((\theta - E(\theta))^2\right)$$

\* estimated as

$$S_{\theta}^2$$

- accuracy (MSE)

\* defined as

$$MSE = E((\theta - \theta_0)^2)$$

\* estimated as

$$\frac{1}{K} \sum_{k} (\hat{\theta}_k - \bar{\theta})^2$$

\* RMSE: square root of MSE

$$RMSE = \sqrt{MSE}$$

- relative Bias
  - defined as the relative difference from true parameter in simhelpers

$$E(\hat{\theta})/\theta$$

- \* estimated as  $mean(\hat{\theta})/\theta_0$
- \* should be close to 1
- here, we define it as the relative difference from true parameter minus 1

$$E(\hat{\theta} - \theta)/\theta$$

\* estimated as

$$mean(\hat{\theta} - \theta_0)/\theta_0$$

- \* should be close to 0
- relative MSE
  - accuracy in relative terms
  - defined as

$$E((\hat{\theta}-\theta)^2)/\theta^2$$

- approximated as

$$((\bar{\theta}-\theta_0)^2+S_\theta^2)/\theta_0^2$$

- take square root to obtain the relative RMSE

Note **TODO**: install simhelpers package for computation of these metrics + the MC error

# Continuous data

#### Emax and Hill models

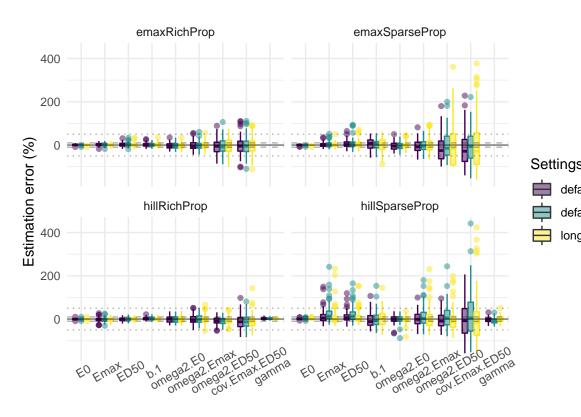
Data was simulated according to an Emax model or a Hill model (the first N=100 simulated datasets from the 200 simulated for the Pharm Res paper).

#### Settings

```
dataType <- "cont"
parpop<-c(5,30,500,3)
nampar<-c("E0","Emax","ED50","gamma")
omega<-diag(c(0.09,0.49,0.49))
omega[3,2]<-omega[2,3]<-0.245
respar<-c(0.1)</pre>
```

#### Simulation results

```
runDate <- '220913'
who <- "eco"
saemixVersion <-"cran31"
exampleName <- "doseResponsePlanProp"
runSettings <- c("defaultTrue", "defaultFalse", "longFalse")
runScenarios <- c("emaxRichProp", "emaxSparseProp", "hillRichProp", "hillSparseProp")</pre>
```



defa

defa

Version 3.1 on CRAN

Parameter

## pdf ##

Bias and accuracy of the estimates in the different settings and scenarios

% latex table generated in R 3.6.3 by x table 1.8-4 package % Thu Sep 15 10:04:55 2022

% latex table generated in R 3.6.3 by xtable 1.8-4 package % Thu Sep 15 10:04:55 2022 \begin{table}[ht]

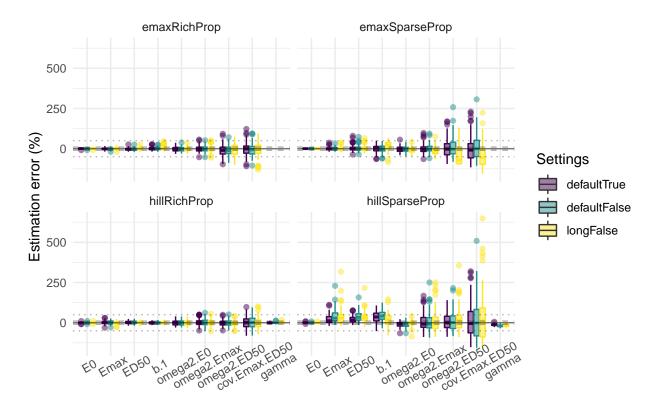
	param	true	bias	rrmse	bias	rrmse	bias	rrmse
1	emaxRichProp							
2	E0	5.00	0.84	0.12	0.90	0.12	0.78	0.12
3	Emax	30.00	1.61	0.53	1.82	0.53	0.66	0.53
4	ED50	500.00	1.79	0.89	2.26	0.92	0.18	0.91
5	b.1	0.10	0.86	0.75	0.93	0.76	1.45	1.12
6	omega 2.E0	0.09	-3.24	1.81	-3.11	1.83	-3.14	1.86
7	omega2.Emax	0.49	-1.86	3.55	-2.25	3.32	-2.11	3.38
8	omega2.ED50	0.49	-3.86	11.36	-3.52	12.32	-6.20	15.66
9	cov.Emax.ED50	0.24	-3.19	15.34	-3.56	15.42	-4.29	16.27
10	emaxSparseProp							
11	E0	5.00	0.60	0.10	0.62	0.12	0.31	0.13
12	Emax	30.00	1.03	1.01	2.52	1.50	1.21	1.06
13	ED50	500.00	4.74	3.26	6.34	5.06	3.40	3.22
14	b.1	0.10	4.94	7.18	0.71	5.42	0.83	9.97
15	omega 2.E0	0.09	-3.81	3.45	-4.15	2.94	-2.62	2.98
16	omega2.Emax	0.49	-6.22	7.60	-3.23	7.72	-0.15	12.29
17	omega2.ED50	0.49	-16.64	36.61	0.41	36.72	-0.85	102.73
18	cov.Emax.ED50	0.24	-21.36	58.87	-6.46	56.35	-0.22	137.87
19	hillRichProp							
20	E0	5.00	-0.42	0.12	-0.40	0.12	-0.38	0.12
21	Emax	30.00	-2.74	1.05	-2.66	1.03	-1.90	0.94
22	ED50	500.00	-1.07	0.73	-1.03	0.73	-0.04	0.70
23	gamma	3.00	2.35	0.31	2.29	0.28	1.45	0.23
24	b.1	0.10	1.87	0.59	2.26	0.63	-0.34	0.56
25	omega2.E0	0.09	-1.46	2.45	-1.70	2.49	-1.23	2.49
26	omega2.Emax	0.49	-1.27	3.79	-0.69	3.62	-0.25	3.70
27	omega2.ED50	0.49	-8.55	3.90	-8.25	3.73	-7.65	3.40
28	cov.Emax.ED50	0.24	-11.90	13.22	-10.98	12.75	-10.44	11.21
29	hill Sparse Prop							
30	E0	5.00	0.33	0.07	-0.18	0.07	0.47	0.08
31	Emax	30.00	11.91	10.49	24.72	22.79	7.81	15.43
32	ED50	500.00	10.63	6.69	22.44	16.46	7.07	8.99
33	gamma	3.00	-2.43	1.43	-7.90	2.39	0.64	2.25
34	b.1	0.10	-4.08	10.53	-0.55	11.32	4.95	12.80
35	omega 2.E0	0.09	-0.02	2.83	-0.40	2.89	-1.60	2.74
36	omega2.Emax	0.49	0.96	9.61	8.62	20.69	1.69	23.27
37	omega2.ED50	0.49	-2.68	15.91	9.66	27.09	-4.74	27.71
38	cov.Emax.ED50	0.24	-2.46	65.36	20.21	106.51	-3.39	123.68

		CE	1		1. :		1	
	param	empSE	bias	rrmse	bias	rrmse	bias	rrmse
1	emaxRichProp	0.15	<b>F</b> 00	0.75		0.70	- 0-	0.74
2	E0	0.17	-5.80	0.75	-5.56	0.73	-5.65	0.74
3	Emax	2.14	6.82	1.79	8.02	1.86	4.04	1.34
4	ED50	46.36	-5.67	2.84	-5.78	3.01	-10.77	3.91
5	b.1	0.01	-19.58	4.24	-20.16	4.47	-33.72	11.74
6	omega 2.E0	0.01	16.69	4.70	15.90	4.44	15.28	4.22
7	omega2.Emax	0.09	-12.91	3.68	-9.85	2.97	-10.84	3.08
8	omega2.ED50	0.16	-34.20	13.69	-36.68	15.40	-44.38	21.35
9	cov.Emax.ED50	0.10	-21.09	6.53	-21.22	6.54	-24.00	7.63
10	emaxSparseProp							
11	E0	0.16	-7.32	1.03	-13.13	2.12	-18.42	3.81
12	Emax	3.00	-26.51	9.08	-36.51	15.45	-27.54	10.29
13	ED50	87.11	-28.47	11.06	-39.77	18.96	-30.24	12.80
14	b.1	0.03	-22.69	5.85	-11.70	2.15	-31.01	14.14
15	omega2.E0	0.02	-11.64	2.62	-4.94	1.50	-5.78	1.71
16	omega2.Emax	0.13	-27.48	9.84	-27.54	10.06	-43.19	20.72
17	omega2.ED50	0.29	-31.93	13.16	-30.55	12.38	-59.96	38.32
18	cov.Emax.ED50	0.18	-33.61	14.01	-31.39	12.85	-57.06	34.79
19	hillRichProp							
20	E0	0.17	-9.04	1.37	-9.51	1.46	-9.20	1.41
21	Emax	2.96	-18.12	5.33	-17.13	4.96	-13.58	3.90
22	ED50	42.47	-10.77	3.03	-10.60	2.97	-8.36	2.40
23	gamma	0.15	-22.38	6.29	-17.00	4.31	-17.10	4.33
24	b.1	0.01	-8.25	1.13	-10.28	1.51	-10.69	1.59
25	omega 2.E0	0.01	-4.18	2.17	-4.93	2.25	-5.17	2.26
26	omega2.Emax	0.10	-16.48	5.24	-14.15	4.52	-14.52	4.59
27	omega2.ED50	0.09	-19.77	6.20	-17.95	5.50	-13.98	4.22
28	cov.Emax.ED50	0.08	-29.44	10.55	-28.24	9.85	-22.88	7.19
29	hillSparseProp							
30	E0	0.13	-5.50	0.67	-4.59	0.59	-7.96	1.03
31	Emax	9.03	-57.46	38.02	-59.52	42.87	-67.18	52.36
32	ED50	117.86	-42.27	23.08	-50.08	32.46	-53.97	36.29
33	gamma	0.35	-17.82	6.92	-35.08	15.66	-29.57	13.34
34	b.1	0.03	12.25	9.35	6.22	5.24	6.64	6.06
35	omega2.E0	0.02	-12.25	4.30	-11.92	4.30	-6.07	4.13
36	omega2.Emax	0.15	-25.12	13.01	-37.22	24.61	-52.23	33.13
37	omega2.ED50	0.19	-34.67	14.34	-42.05	21.44	-50.44	28.26
38	cov.Emax.ED50	0.20	-34.46	14.72	-40.24	21.55	-52.55	30.86

\caption{Relative bias and relative RMSE (in %) on SE estimated by linearisation, compared to the empirical SE, in the example doseResponsePlanProp for settings:defaultTrue, defaultFalse, longFalse} \end{table}

# Tweaking the algorithm Keeping

```
runDate <- '220914'
who <- "eco"
saemixVersion <-"tweakSA"
exampleName <- "doseResponsePlanProp"
runSettings <- c("defaultTrue", "defaultFalse", "longFalse")
runScenarios <- c("emaxRichProp", "emaxSparseProp", "hillRichProp", "hillSparseProp")</pre>
```



# Parameter

## pdf ## 2

Bias and accuracy of the estimates in the different settings and scenarios % latex table generated in R 3.6.3 by xtable 1.8-4 package % Thu Sep 15  $10:04:59\ 2022$  % latex table generated in R 3.6.3 by xtable 1.8-4 package % Thu Sep 15  $10:04:59\ 2022$  \begin{table}[ht]

	param	true	bias	rrmse	bias	rrmse	bias	rrmse
1	emaxRichProp							
2	E0	5.00	0.69	0.11	0.68	0.11	0.79	0.12
3	Emax	30.00	-0.86	0.51	-1.24	0.48	0.96	0.58
4	ED50	500.00	-2.44	0.80	-3.11	0.78	0.78	0.90
5	b.1	0.10	0.41	0.82	0.03	0.75	2.06	1.57
6	omega2.E0	0.09	-3.01	1.86	-2.93	1.89	-3.22	1.80
7	omega2.Emax	0.49	-1.56	3.35	-2.00	3.06	-2.40	3.74
8	omega2.ED50	0.49	-8.87	12.05	-9.94	10.52	-7.78	19.02
9	cov.Emax.ED50	0.24	-4.68	14.71	-6.11	13.39	-6.15	21.05
10	emaxSparseProp							
11	E0	5.00	0.46	0.12	0.47	0.11	0.85	0.11
12	Emax	30.00	0.23	1.05	0.73	1.14	-1.34	1.11
13	ED50	500.00	1.44	3.40	1.61	3.14	1.55	2.83
14	b.1	0.10	0.74	6.17	-1.14	5.34	17.03	11.17
15	omega2.E0	0.09	-4.21	3.63	-3.81	3.06	-6.00	3.32
16	omega2.Emax	0.49	-1.15	8.52	0.19	7.45	-11.67	9.31
17	omega2.ED50	0.49	2.04	34.62	10.52	41.27	-42.28	61.16
18	cov.Emax.ED50	0.24	-0.41	56.58	6.86	55.22	-43.44	78.41
19	hillRichProp							
20	E0	5.00	-0.54	0.12	-0.52	0.12	-0.55	0.12
21	Emax	30.00	1.92	1.30	2.38	1.28	0.06	1.02
22	ED50	500.00	2.28	0.98	2.53	0.94	1.18	0.82
23	gamma	3.00	0.27	0.20	0.29	0.20	0.65	0.20
24	b.1	0.10	-0.80	0.63	-0.76	0.55	-1.24	0.58
25	omega2.E0	0.09	-1.16	2.56	-1.08	2.56	-1.08	2.52
26	omega2.Emax	0.49	1.85	3.87	2.47	4.34	0.95	3.76
27	omega2.ED50	0.49	-2.04	3.23	-0.98	4.02	-3.95	3.50
28	cov.Emax.ED50	0.24	1.27	12.12	3.22	14.25	-2.88	12.13
29	hill Sparse Prop							
30	E0	5.00	-0.27	0.08	-0.55	0.09	-0.72	0.08
31	Emax	30.00	21.43	11.64	37.64	29.24	37.18	34.80
32	ED50	500.00	20.63	8.15	38.87	24.08	35.95	22.45
33	gamma	3.00	-12.77	2.02	-19.26	4.18	-16.66	3.37
34	b.1	0.10	33.16	22.38	43.06	28.12	17.12	18.05
35	omega2.E0	0.09	-9.48	3.60	-9.98	4.18	-2.27	3.46
36	omega2.Emax	0.49	5.70	27.28	3.62	33.02	7.75	42.69
37	omega2.ED50	0.49	8.76	28.81	11.58	37.24	17.18	54.36
38	cov.Emax.ED50	0.24	17.22	134.48	16.92	156.32	26.61	230.42

param         empSE         bias         rrmse         bias         rrmse         bias           1         emaxRichProp         2         E0         0.16         -4.61         0.65         -4.77         0.67         -5.49	0.72
2 E0 0.16 -4.61 0.65 -4.77 0.67 -5.49	
3 Emax 2.13 4.43 1.49 7.42 1.75 -0.36	
4 ED50 42.93 -4.55 2.86 -1.89 2.51 -9.45	3.92
5 b.1 0.01 -23.53 5.93 -20.74 4.71 -43.56	19.31
6 omega2.E0 0.01 14.87 4.13 13.80 3.82 17.42	4.95
7 omega2.Emax 0.09 -10.96 3.18 -7.14 2.47 -15.21	4.13
8 omega2.ED50 0.16 -37.10 15.60 -32.40 12.41 -49.61	26.14
9 cov.Emax.ED50 0.09 -21.15 6.46 -17.63 5.05 -33.19	12.75
10 emaxSparseProp	
11 E0 0.17 -15.94 2.94 -11.22 1.67 -7.77	1.07
12 Emax 3.08 -28.33 10.23 -30.33 11.07 -33.10	13.03
13 ED50 91.88 -32.91 14.01 -29.33 11.68 -30.68	12.86
14 b.1 0.02 -15.07 3.49 -8.50 1.96 -29.23	11.22
15 omega2.E0 0.02 -14.56 3.34 -7.27 1.78 -5.00	1.60
16 omega2.Emax 0.14 -31.07 12.15 -25.70 9.04 -33.63	13.88
17 omega2.ED50 0.29 -27.14 10.49 -30.61 12.42 -44.53	22.71
18 cov.Emax.ED50 0.18 -30.62 12.43 -28.11 11.00 -40.64	19.62
19 hillRichProp	
20 E0 0.17 -8.62 1.31 -8.53 1.30 -9.15	
21 Emax 3.38 -22.95 7.14 -20.87 6.49 -16.38	4.67
22 ED50 48.16 -16.30 4.40 -13.48 3.81 -11.96	3.28
23 gamma 0.13 -18.96 4.80 -18.98 4.78 -16.84	3.94
24 b.1 0.01 -16.38 3.13 -10.15 1.47 -12.55	
25 omega2.E0 0.01 -6.54 2.41 -6.39 2.40 -5.84	
26 omega2.Emax 0.10 -13.76 4.40 -17.76 5.83 -13.90	4.45
27 omega2.ED50 0.09 -14.64 4.38 -23.09 7.58 -18.33	5.63
28 cov.Emax.ED50 0.09 -25.15 8.24 -30.00 11.11 -26.68	9.03
29 hillSparseProp	
30 E0 0.14 -9.29 1.27 -10.46 1.49 -6.24	0.82
31 Emax 7.96 -40.59 21.33 -43.27 28.92 -54.36	39.25
32 ED50 98.63 -14.78 8.05 -23.68 15.19 -31.79	19.20
33 gamma 0.19 33.21 15.63 8.86 4.64 -3.74	3.58
34 b.1 0.03 18.92 6.94 28.28 11.09 -3.36	2.40
35 omega2.E0 0.01 7.26 4.13 3.04 2.52 -10.11	
36 omega2.Emax 0.25 -46.78 26.10 -40.61 25.35 -50.54	32.20
37 omega2.ED50 0.26 -43.81 21.38 -42.63 21.63 -54.87	33.05
38 cov.Emax.ED50 0.28 -48.86 26.57 -44.31 24.69 -56.69	36.04

 $\label{lem:caption} $$ \operatorname{RMSE} (in \%) \ on \ SE \ estimated by linearisation, compared to the empirical SE, in the example doseResponsePlanProp for settings: defaultTrue, defaultFalse, longFalse $$ \ \end{table} $$$ 

	param	true	bias	rmse	precision	bias	rmse	precision	bias	rmse	precision
<del>1</del>	emaxRichProp	true	Dias	Tillse	precision	Dias	Timse	precision	Dias	Timse	precision
2	E0	5.00	0.04	0.17	0.17	0.04	0.17	0.17	0.04	0.17	0.17
3	Emax	30.00	0.04 $0.48$	2.18	2.14	0.04 $0.55$	$\frac{0.17}{2.17}$	2.11	0.04 $0.20$	$\frac{0.17}{2.17}$	2.17
4	ED50	500.00	8.97	46.99	46.36	11.32	47.84	46.71	0.20 $0.89$	47.55	47.78
5	b.1	0.10	0.00	0.01	0.01	0.00	0.01	0.01	0.00	0.01	0.01
6	omega2.E0	0.10	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
7	omega2.Emax	0.09 $0.49$	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
8	omega2.ED50	0.49 $0.49$	-0.01	0.03 $0.16$	0.03	-0.01	0.03 $0.17$	0.03 $0.17$	-0.01	0.09 $0.19$	0.09
9	cov.Emax.ED50	0.49 $0.24$	-0.02	0.10	0.10	-0.02	0.17	0.17	-0.03	0.19 $0.10$	0.19
10	emaxSparseProp	0.24	-0.01	0.10	0.10	-0.01	0.10	0.10	-0.01	0.10	0.10
11	E0	5.00	0.03	0.16	0.16	0.03	0.17	0.17	0.02	0.18	0.18
12	Emax	30.00	0.03	3.00	3.00	0.03 $0.76$	3.66	3.59	0.02 $0.36$	3.08	3.07
13	ED50	500.00	23.72	89.86	87.11	31.68	112.00	107.97	16.99	89.29	88.10
14	b.1	0.10	0.00	0.03	0.03	0.00	0.02	0.02	0.00	0.03	0.03
15	omega2.E0	0.10	-0.00	0.03 $0.02$	0.03	-0.00	0.02 $0.02$	0.02	-0.00	0.03 $0.02$	0.03 $0.02$
16	omega2.Emax	0.09 $0.49$	-0.00	0.02 $0.13$	0.02 $0.13$	-0.00	0.02 $0.14$	0.01 $0.14$	-0.00	0.02 $0.17$	0.02 $0.17$
17	omega2.ED50	0.49 $0.49$	-0.03	0.13 $0.30$	0.13	0.02	0.14 $0.30$	0.14	-0.00	0.17 $0.49$	0.17 $0.50$
18	cov.Emax.ED50	0.49 $0.24$	-0.05	0.30 $0.19$	0.29	-0.02	0.30 $0.18$	0.30	-0.00	0.49 $0.29$	0.30 $0.29$
19	hillRichProp	0.24	-0.05	0.19	0.16	-0.02	0.16	0.16	-0.00	0.29	0.29
20	E0	5.00	-0.02	0.17	0.17	-0.02	0.17	0.17	-0.02	0.17	0.17
$\frac{20}{21}$	Emax	30.00	-0.02	3.06	2.96	-0.02	3.03	2.94	-0.02	2.89	$\frac{0.17}{2.85}$
$\frac{21}{22}$	ED50	500.00	-5.33	42.59	$\frac{2.90}{42.47}$	-0.30 -5.17	42.59	42.49	-0.22	41.73	41.94
$\frac{22}{23}$	gamma	3.00	0.07	0.17	0.15	0.07	0.16	0.14	0.22	0.14	0.14
$\frac{23}{24}$	b.1	0.10	0.07	$0.17 \\ 0.01$	0.13 $0.01$	0.07	0.10 $0.01$	0.14 $0.01$	-0.00	0.14 $0.01$	0.14 $0.01$
$\frac{24}{25}$	omega2.E0	0.10 $0.09$	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
$\frac{25}{26}$	omega2.Emax	0.09 $0.49$	-0.00	0.01 $0.09$	0.01 $0.10$	-0.00	0.01 $0.09$	0.01 $0.09$	-0.00	0.01 $0.09$	0.01 $0.09$
$\frac{20}{27}$	omega2.ED50	0.49 $0.49$	-0.01 -0.04	0.09 $0.10$	0.10	-0.00 -0.04	0.09	0.09	-0.00 -0.04	0.09	0.09 $0.08$
28	cov.Emax.ED50	0.49 $0.24$	-0.04	0.10 $0.09$	0.09 $0.08$	-0.04 -0.03	0.09		-0.04	0.09 $0.08$	0.08
$\frac{28}{29}$	hillSparseProp	0.24	-0.05	0.09	0.08	-0.05	0.09	0.08	-0.05	0.08	0.08
$\frac{29}{30}$	E0	5.00	0.02	0.13	0.13	-0.01	0.13	0.13	0.02	0.14	0.14
30		30.00		9.67		$\frac{-0.01}{7.42}$		12.25		11.73	
$\frac{31}{32}$	Emax ED50		3.57	9.67 $128.75$	9.03	$\frac{7.42}{112.22}$	$14.27 \\ 202.14$		$2.34 \\ 35.34$		11.55 $145.70$
		500.00	53.14		117.86			168.98		149.22	
33	gamma	3.00	-0.07	0.36	0.35	-0.24	0.46	0.40	0.02	0.45	0.45
34	b.1	0.10	-0.00	0.03	0.03	-0.00	0.03	0.03	0.00	0.04	0.04
$\frac{35}{36}$	omega2.E0	0.09	-0.00	0.02	0.02	-0.00	0.02	0.02	-0.00	0.01	0.01
36	omega2.Emax	0.49	0.00	0.15	0.15	0.04	0.22	0.22	0.01	0.24	0.24
37	omega2.ED50	0.49	-0.01	0.19	0.19	0.05	0.25	0.25	-0.02	0.26	0.26
38	cov.Emax.ED50	0.24	-0.01	0.20	0.20	0.05	0.25	0.25	-0.01	0.27	0.27

 $\label{thm:continuity:continuity:equal} Table~1:~Bias,~precision~and~accurary~in~the~example~doseResponsePlanProp~for~settings:defaultTrue,~defaultFalse,~longFalse$ 

	param	true	bias	rmse	precision	bias	rmse	precision	bias	rmse	precision
1	emaxRichProp										
2	E0	5.00	0.03	0.17	0.16	0.03	0.17	0.16	0.04	0.17	0.17
3	Emax	30.00	-0.26	2.13	2.13	-0.37	2.08	2.05	0.29	2.28	2.27
4	ED50	500.00	-12.22	44.42	42.93	-15.57	43.89	41.24	3.89	47.10	47.18
5	b.1	0.10	0.00	0.01	0.01	0.00	0.01	0.01	0.00	0.01	0.01
6	omega2.E0	0.09	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
7	omega2.Emax	0.49	-0.01	0.09	0.09	-0.01	0.09	0.09	-0.01	0.09	0.09
8	omega2.ED50	0.49	-0.04	0.17	0.16	-0.05	0.16	0.15	-0.04	0.21	0.21
9	cov.Emax.ED50	0.24	-0.01	0.09	0.09	-0.01	0.09	0.09	-0.02	0.11	0.11
10	emaxSparseProp										
11	E0	5.00	0.02	0.18	0.17	0.02	0.17	0.17	0.04	0.17	0.16
12	Emax	30.00	0.07	3.06	3.08	0.22	3.19	3.20	-0.40	3.14	3.13
13	ED50	500.00	7.18	91.70	91.88	8.06	88.16	88.23	7.76	83.69	83.75
14	b.1	0.10	0.00	0.02	0.02	-0.00	0.02	0.02	0.02	0.03	0.03
15	omega2.E0	0.09	-0.00	0.02	0.02	-0.00	0.02	0.02	-0.01	0.02	0.02
16	omega2.Emax	0.49	-0.01	0.14	0.14	0.00	0.13	0.13	-0.06	0.15	0.14
17	omega2.ED50	0.49	0.01	0.29	0.29	0.05	0.31	0.31	-0.21	0.38	0.32
18	cov.Emax.ED50	0.24	-0.00	0.18	0.18	0.02	0.18	0.18	-0.11	0.22	0.19
19	hillRichProp										
20	E0	5.00	-0.03	0.17	0.17	-0.03	0.17	0.17	-0.03	0.17	0.17
21	Emax	30.00	0.58	3.41	3.38	0.71	3.38	3.32	0.02	3.01	3.03
22	ED50	500.00	11.38	49.26	48.16	12.66	48.37	46.92	5.88	45.01	44.85
23	gamma	3.00	0.01	0.13	0.13	0.01	0.13	0.13	0.02	0.13	0.13
24	b.1	0.10	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
25	omega2.E0	0.09	-0.00	0.01	0.01	-0.00	0.01	0.01	-0.00	0.01	0.01
26	omega2.Emax	0.49	0.01	0.10	0.10	0.01	0.10	0.10	0.00	0.09	0.09
27	omega2.ED50	0.49	-0.01	0.09	0.09	-0.00	0.10	0.10	-0.02	0.09	0.09
28	cov.Emax.ED50	0.24	0.00	0.08	0.09	0.01	0.09	0.09	-0.01	0.08	0.09
29	hill Sparse Prop										
30	E0	5.00	-0.01	0.14	0.14	-0.03	0.15	0.15	-0.04	0.14	0.14
31	Emax	30.00	6.43	10.21	7.96	11.29	16.18	11.65	11.15	17.65	13.74
32	ED50	500.00	103.13	142.36	98.63	194.37	244.92	149.77	179.74	236.38	154.30
33	gamma	3.00	-0.38	0.43	0.19	-0.58	0.61	0.21	-0.50	0.55	0.23
34	b.1	0.10	0.03	0.05	0.03	0.04	0.05	0.03	0.02	0.04	0.04
35	omega2.E0	0.09	-0.01	0.02	0.01	-0.01	0.02	0.02	-0.00	0.02	0.02
36	omega2.Emax	0.49	0.03	0.25	0.25	0.02	0.28	0.28	0.04	0.32	0.32
37	omega2.ED50	0.49	0.04	0.26	0.26	0.06	0.30	0.29	0.08	0.36	0.35
38	cov.Emax.ED50	0.24	0.04	0.28	0.28	0.04	0.30	0.30	0.07	0.37	0.37

 $\label{thm:continuity:continuit$