

LQR Controller for AUV Depth Regulation

Safa Bazrafshan

Independent Researcher

Email: safa.bazrafshan@gmail.com

ORCID: <https://orcid.org/0009-0004-4029-9550>

In this phase, an LQR (Linear Quadratic Regulator) controller was designed to regulate the depth of the AUV using a linearized model of the system. The purpose was to design a controller that minimizes a quadratic cost function while ensuring stability and performance.

System Model:

The linearized state-space representation is:

$$\dot{x} = Ax + Bu, \quad y = Cx$$

with the matrices:

- $A = \begin{bmatrix} 0 & 10 & -0.8 \end{bmatrix}$
- $B = \begin{bmatrix} 0 & 0.5 \end{bmatrix}$
- $C = \begin{bmatrix} 1 & 0 \end{bmatrix}$

LQR Design:

The controller minimizes the cost function:

$$J = \int_0^{\infty} (x^T Qx + u^T Ru) dt$$

With selected weights:

- $Q = \text{diag}(100, 1)$
- $R = 0.01$

Using MATLAB's `lqr` function, the optimal gain matrix K was obtained. The closed-loop control law is:

$$u = -Kx$$

Simulation Result:

The resulting depth response of the AUV shows excellent stability. The system remains at the zero-depth position with no oscillation, overshoot, or drift — confirming a well-tuned controller.

Figure_LQR Depth Response

