



**POLITECNICO**  
MILANO 1863

DIPARTIMENTO DI ELETTRONICA  
INFORMAZIONE E BIOINGEGNERIA



**UNIVERSITÀ**  
DEGLI STUDI  
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# Capturing Medical Knowledge into a Safe and Trustworthy Digital Twin

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## Context

### Domain:

Medical Cyber-Physical Systems,  
e.g., mechanical ventilators

Requests from stakeholders:

safety of  
decisions

Challenges:  
component  
heterogeneity,  
uncertainty

trust in the  
system

Solution:

**Digital Twin**

risk assessment

training of  
medical staff

using...

## Stochastic Hybrid Automata (SHA)

locations with different  
behavior of variables

edges

labeled by...

channels  
(actions)

= events

flow conditions  
(parametrized ODEs)  
& stochastic  
parameter distributions

invariants  
(permanence conditions)

guards (necessary  
conditions)

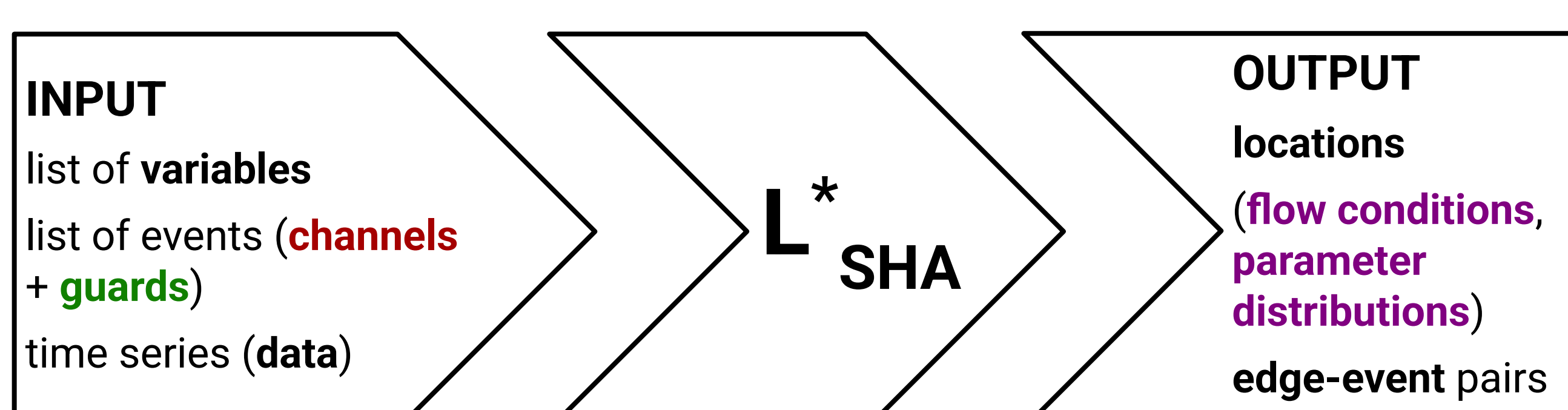
Advantages:

conciseness

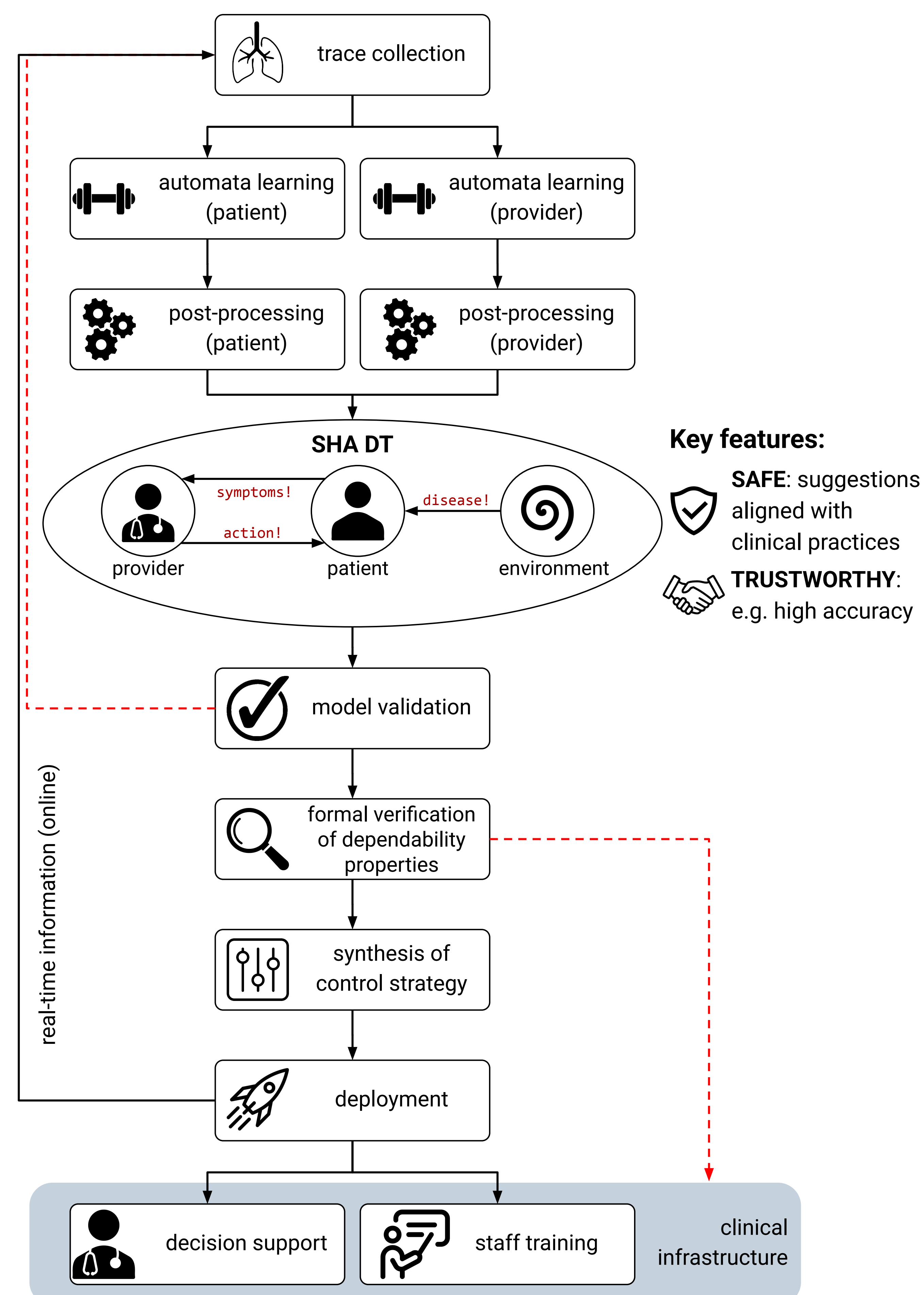
formal  
verification of  
properties

explainability

## Automata learning algorithms



## Proposed workflow



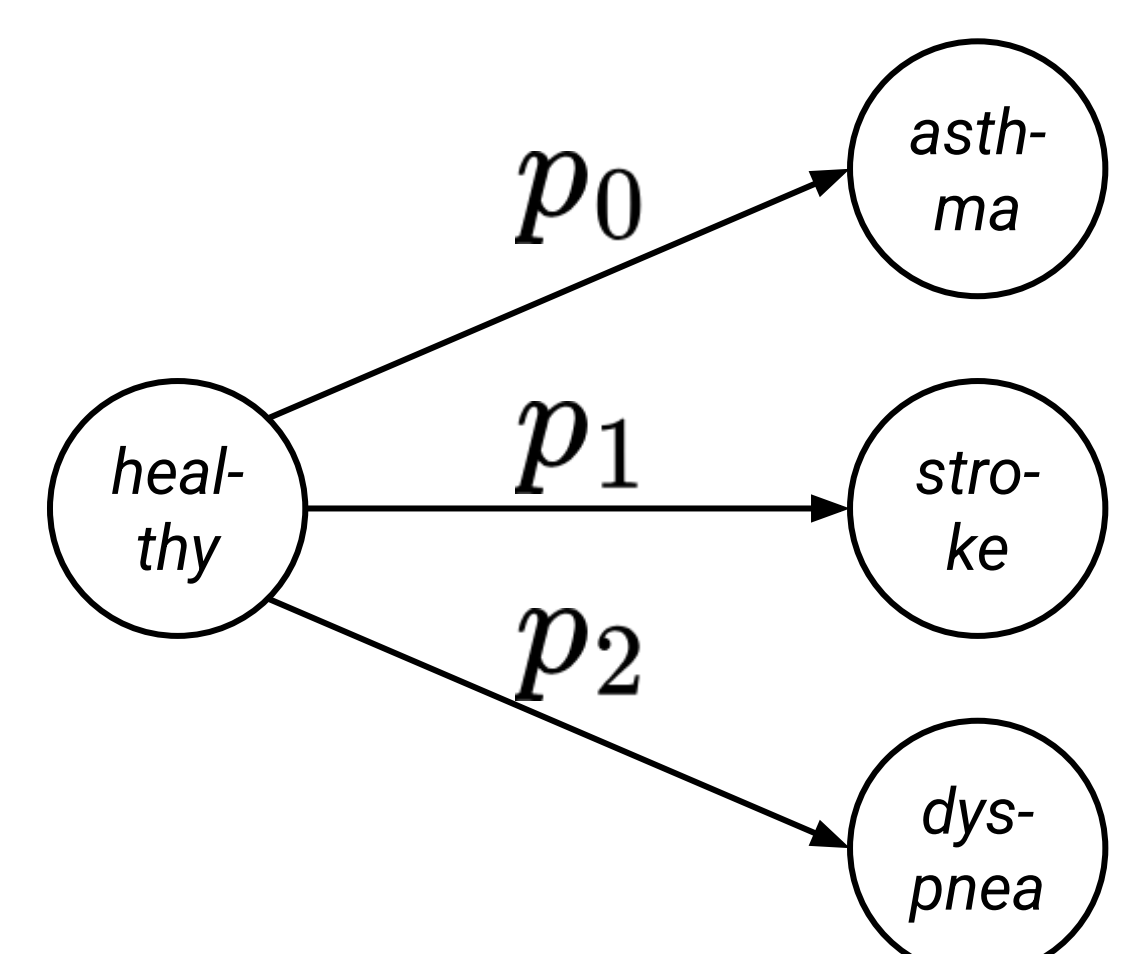
## SHA Bayesian extensions

For improved risk assessment

$$s \sim \text{Beta}(a, b)$$

$$y_i | s \stackrel{iid}{\sim} \text{Bernoulli}(s)$$

$$s | y_{1:n} \sim \text{Beta}(a_n, b_n)$$



Bayesian stress level models:

- flexible Beta distributions for different provider profiles
- models likelihood  $s$  of ignoring suggestions
- updates with real-time data  $y_i$

$$p_{0:2} \sim \text{Dir}(\alpha_{0:2})$$

transition probabilities  
between locations,  
modeled with  
Dirichlet distributions