

Horspool's Algorithm

Case 1 If there are no c 's in the pattern—e.g., c is letter S in our example—we can safely shift the pattern by its entire length (if we shift less, some character of the pattern would be aligned against the text's character c that is known not to be in the pattern):

$$\begin{array}{ccccccccccc}
 s_0 & & \dots & & & & S & & \dots & & s_{n-1} \\
 & & & & & & \parallel & & & & \\
 & & & & & & \text{B} & \text{A} & \text{R} & \text{B} & \text{E} & \text{R} \\
 & & & & & & & & & & & \text{B} & \text{A} & \text{R} & \text{B} & \text{E} & \text{R}
 \end{array}$$

Case 2 If there are occurrences of character c in the pattern but it is not the last one there—e.g., c is letter B in our example—the shift should align the rightmost occurrence of c in the pattern with the c in the text:

$$\begin{array}{ccccccccccc}
 s_0 & & \dots & & & & B & & & \dots & s_{n-1} \\
 & & & & & & \diagdown & & & & \\
 & & & & & & & & & & \\
 & & & & & & B & A & R & B & E & R \\
 & & & & & & & & & & \\
 & & & & & & & & & & B & A & R & B & E & R
 \end{array}$$

Case 3 If c happens to be the last character in the pattern but there are no c 's among its other $m - 1$ characters—e.g., c is letter R in our example—the situation is similar to that of Case 1 and the pattern should be shifted by the entire pattern's length m :

s_0	...		M	E	R	...	s_{n-1}				
			X								
		L	E	A	D	E	R				
						L	E	A	D	E	R

Case 4 Finally, if c happens to be the last character in the pattern and there are other c 's among its first $m - 1$ characters—e.g., c is letter R in our example—the situation is similar to that of Case 2 and the rightmost occurrence of c among the first $m - 1$ characters in the pattern should be aligned with the text's c :

s_0	...		A	R	...	s_{n-1}			
			X						
		R	E	O	R	D	E	R	
			R	E	O	R	D	E	R

ALGORITHM *ShiftTable*($P[0..m - 1]$)

//Fills the shift table used by Horspool's and Boyer-Moore algorithms

//Input: Pattern $P[0..m - 1]$ and an alphabet of possible characters

//Output: $Table[0..size - 1]$ indexed by the alphabet's characters and

// filled with shift sizes computed by formula (7.1)

for $i \leftarrow 0$ **to** $size - 1$ **do** $Table[i] \leftarrow m$

for $j \leftarrow 0$ **to** $m - 2$ **do** $Table[P[j]] \leftarrow m - 1 - j$

return $Table$

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character c	A	B	C	D	E	F	...	R	...	Z	_
shift $t(c)$	4	2	6	6	1	6	6	3	6	6	6

ALGORITHM *HorspoolMatching*($P[0..m - 1]$, $T[0..n - 1]$)

//Implements Horspool's algorithm for string matching

//Input: Pattern $P[0..m - 1]$ and text $T[0..n - 1]$

//Output: The index of the left end of the first matching substring

// or -1 if there are no matches

ShiftTable($P[0..m - 1]$) //generate *Table* of shifts

$i \leftarrow m - 1$ //position of the pattern's right end

while $i \leq n - 1$ **do**

$k \leftarrow 0$ //number of matched characters

while $k \leq m - 1$ **and** $P[m - 1 - k] = T[i - k]$ **do**

$k \leftarrow k + 1$

if $k = m$

return $i - m + 1$

else $i \leftarrow i + \text{Table}[T[i]]$

return -1

character c	A	B	C	D	E	F	...	R	...	Z	_
shift $t(c)$	4	2	6	6	1	6	6	3	6	6	6

The actual search in a particular text proceeds as follows:

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J I M _ S A W _ M E _ I N _ A _ B A R B E R S H O P
B A R B E R                B A R B E R
      B A R B E R          B A R B E R
            B A R B E R      B A R B E R

```



Boyer-Moore Algorithm

bad- symbol shift.

$$d_1 = \max\{t_1(c) - k, 1\}.$$

BAOBAB

c	A	B	C	D	...	0	...	Z	_
$t_1(c)$	1	2	6	6	6	3	6	6	6

The good-suffix table is filled as follows:

k	pattern	d_2
1	ABC <u><u>B</u></u> A <u>B</u>	2
2	<u>A</u> BCB <u>A</u> <u>B</u>	4
3	<u>A</u> BC <u>B</u> A <u>B</u>	4
4	<u>A</u> BC <u>B</u> A <u>B</u>	4
5	<u>A</u> BC <u>B</u> A <u>B</u>	4

k	pattern	d_2
1	BAO <u><u>B</u></u> A <u>B</u>	2
2	<u>B</u> AOB <u>A</u> <u>B</u>	5
3	<u>B</u> AOB <u>A</u> <u>B</u>	5
4	<u>B</u> A <u>O</u> B <u>A</u> <u>B</u>	5
5	<u>B</u> A <u>O</u> B <u>A</u> <u>B</u>	5

The Boyer-Moore algorithm

- Step 1** For a given pattern and the alphabet used in both the pattern and the text, construct the bad-symbol shift table as described earlier.
- Step 2** Using the pattern, construct the good-suffix shift table as described earlier.
- Step 3** Align the pattern against the beginning of the text.
- Step 4** Repeat the following step until either a matching substring is found or the pattern reaches beyond the last character of the text. Starting with the last character in the pattern, compare the corresponding characters in the pattern and the text until either all m character pairs are matched (then stop) or a mismatching pair is encountered after $k \geq 0$ character pairs are matched successfully. In the latter case, retrieve the entry $t_1(c)$ from the c 's column of the bad-symbol table where c is the text's mismatched character. If $k > 0$, also retrieve the corresponding d_2 entry from the good-suffix table. Shift the pattern to the right by the

number of positions computed by the formula

$$d = \begin{cases} d_1 & \text{if } k = 0, \\ \max\{d_1, d_2\} & \text{if } k > 0, \end{cases}$$

where $d_1 = \max\{t_1(c) - k, 1\}$.

B E S S _ K N E W _ A B O U T _ B A O B A B S

$$d_1 = t_1(K) - 0 = 6$$

$$d_1 = t_1(_) - 2 = 4 \quad \text{B} \quad \text{A} \quad 0 \quad \text{B} \quad \text{A} \quad \text{B}$$

$$d_1 = t_1(_) - 1 = 5$$

$$d = \max\{5, 2\} = 5$$

FIGURE 7.3 Example of string matching with the Boyer-Moore algorithm.