36-315: Statistical Graphics & Visualization

- · course objectives
 - learn useful principles for making appropriate statistical graphics.
 - critique existing graphs and remake better ones.
 - visualize statistical analyses to facilitate communication.
 - pinpoint the statistical claims you can/cannot make from graphics.
 - write and speak publicly about statistical graphics.
 - practice tidy data manipulation in R using the tidyverse
 - practice reproducible workflows with Quarto
- grammar of graphics defined and used in ggplot2
 - ▶ see 01lec.pdf
- goal of data visualization: show data, communicate a story
 - ▶ induce viewer to think about substance, not graphical methodology
 - make large, complex datasets more coherent
 - encourage comparison of different pieces of data
 - describe, explore, and identify relationships
 - avoid data distortion and data decoration
 - use consistent graph design
 - avoid graphs that lead to misleading conclusions!
- data types
 - quantitative
 - discrete
 - continuous
 - categorical (factor)
 - nominal
 - · no order
 - · e.g. race, species
 - ordinal
 - ordered!
 - ranking
 - DEFAULT IN R! manually define factor levels, or alpha. default
- area plots
 - ▶ pie chart (BAD!!!)
 - bar chart
 - stacked bar/spine chart (for variable comparison)
 - ► waffle charts????
 - ► rose diagrams (temporal or directional context can justify usage)
- something something "geom bar stat=identity" to "take y as is"
- α level CI is $\hat{x} \pm z_{1-\frac{\alpha}{2}} \cdot \text{SE}(\hat{x})$
- 1d chisq test: ${\cal H}_A$ is "at least one category differs"

chisq.test(table(penguins\$species))

- CI interpretation
 - ► If CIs don't overlap significant difference
 - ► If CIs overlap a little ambiguous
 - ► If CIs overlap → a lot no significant difference

- multiple testing:
 - ▶ have multiple pairwise comparisons via CI eyeballing? Type 1 error is now above 5%!!!
 - correct by inflating p values
 - ► Bonferroni Correction:
 - making K comparisons \longrightarrow reject iff $p \leq \frac{\alpha}{K}$.
 - easy to impl and popular but inflates p the most
 - CIs: plot $(1-\alpha)\%$ CIs \longrightarrow plot $(1-\frac{\alpha}{\kappa})\%$ CIs
- 2d chisq test: H_A is "A, B independent"

```
chisq.test(table(penguins$species, penguins$island))
```

- visualize this with mosaic plots
- mosaic plots: can shade by Pearson residuals
 - more positive p.r → more counts than expected, more neg is vice versa
 - we might reject null for the global chisq test but see all white residuals: can't reject null for individual local tests.
- 1d quant
 - boxplots: only summary stats: bad!
 - ▶ hist: see dist, bin width matters.
 - density curves: conditional dists
- estimation schools of thought:
 - ▶ parametric: assume dist, est params (eg MLE, 3623X)
 - ► nonparametric: make few assumptions, use whole dataset (density curves, regression lines??)
- · kernel density estimation
 - place lil dist on every x_i
 - usually normal, but many exist (fuck it triangle. things can help maintain strict left right dist bounds if needed)
 - bandwidth (higher is more smooth dist): ggplot alr uses Gaussian reference rule of thumb, set to $1.06 \cdot \sigma_{\text{sample}} \cdot n^{-1/5}$.
 - ▶ adjust bandwith via geom_density(adjust = <multiplier>)
- Kolmogorov-Smirnov (KS) Test
 - H_A : distributions different
 - stat: largest gap
 - ▶ 1 sample: compare ECDF to theoretical distribution

```
ks.test(
  x = penguins$flipper_length_mm,
  y = "pnorm",
  mean = flipper_length_mean,
  sd = flipper_length_sd
)
```

▶ 2 sample: compare two ECDFs

```
ks.test(rap_duration, y = rock_duration) # both straight up vec[int]
```

- Power: prob of reject when you're supposed to (null is false) increased by:
 - sample size
 - reduce variance/error
 - increase differences/effects
 - ► choose right test! i.e. KS is underpowered compared to t.test/Barlett (sensitive to non-normality)

t.test(sample_rap_duration, sample_pop_duration) # H_A : mean not all equal
bartlett.test(list(sample_rap_duration, sample_pop_duration)) # H_A: variances not
all equal