

### Elliptic Cone

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 0$$

#### Traces

In plane  $z = p$ : an ellipse

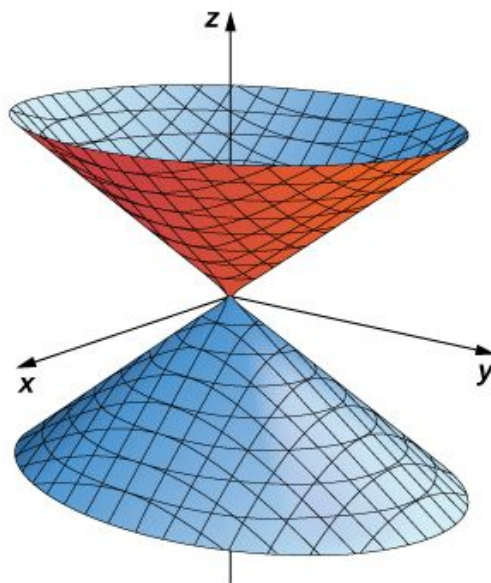
In plane  $y = q$ : a hyperbola

In plane  $x = r$ : a hyperbola

In the  $xz$  - plane: a pair of lines that intersect at the origin

In the  $yz$  - plane: a pair of lines that intersect at the origin

The axis of the surface corresponds to the variable with a negative coefficient. The traces in the coordinate planes parallel to the axis are intersecting lines.



### Elliptic Paraboloid

$$z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

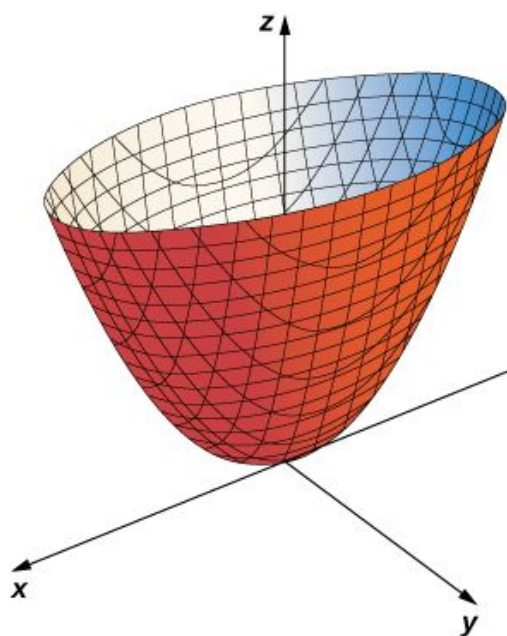
#### Traces

In plane  $z = p$ : an ellipse

In plane  $y = q$ : a parabola

In plane  $x = r$ : a parabola

The axis of the surface corresponds to the linear variable.



### Hyperbolic Paraboloid

$$z = \frac{x^2}{a^2} - \frac{y^2}{b^2}$$

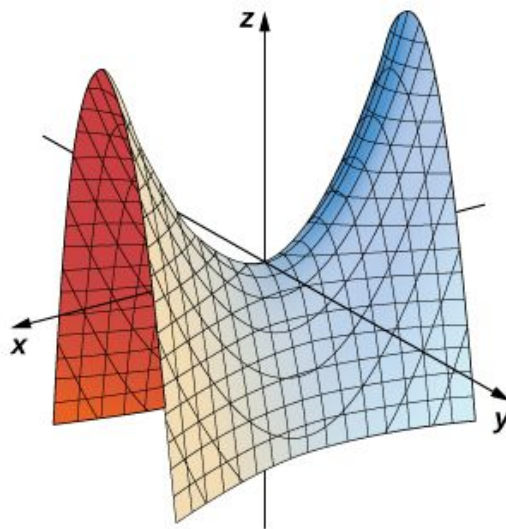
#### Traces

In plane  $z = p$ : a hyperbola

In plane  $y = q$ : a parabola

In plane  $x = r$ : a parabola

The axis of the surface corresponds to the linear variable.



**Ellipsoid**

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

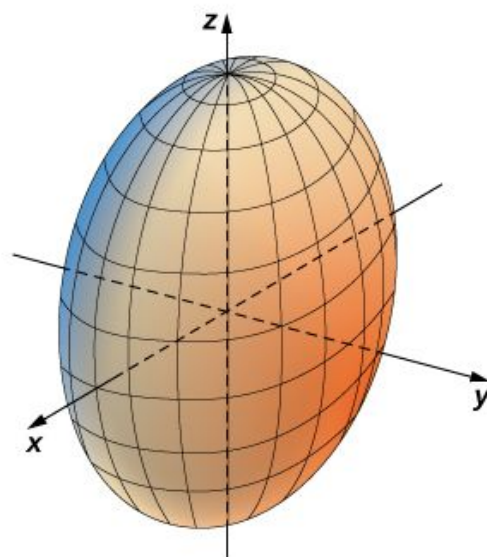
**Traces**

In plane  $z = p$ : an ellipse

In plane  $y = q$ : an ellipse

In plane  $x = r$ : an ellipse

If  $a = b = c$ , then this surface is a sphere.


**Hyperboloid of One Sheet**

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

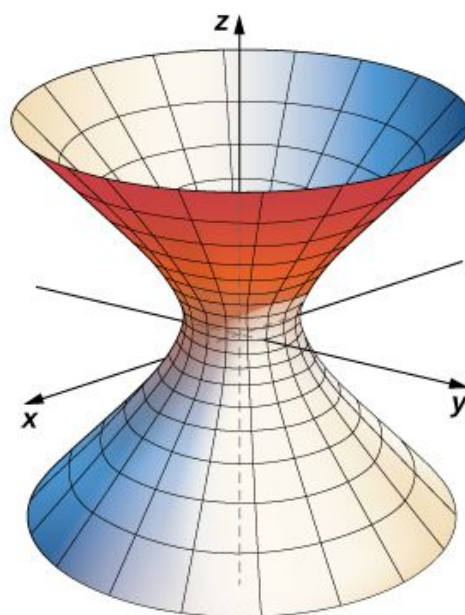
**Traces**

In plane  $z = p$ : an ellipse

In plane  $y = q$ : a hyperbola

In plane  $x = r$ : a hyperbola

In the equation for this surface, two of the variables have positive coefficients and one has a negative coefficient. The axis of the surface corresponds to the variable with the negative coefficient.


**Hyperboloid of Two Sheets**

$$\frac{z^2}{c^2} - \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

**Traces**

In plane  $z = p$ : an ellipse or the empty set (no trace)

In plane  $y = q$ : a hyperbola

In plane  $x = r$ : a hyperbola

In the equation for this surface, two of the variables have negative coefficients and one has a positive coefficient. The axis of the surface corresponds to the variable with a positive coefficient. The surface does not intersect the coordinate plane perpendicular to the axis.

