

$$\Gamma^+[\mathbf{v}_k; \zeta_{\mathbf{v}}] \equiv \underbrace{\mathbf{v}_k \odot \exp\left(\frac{\varepsilon_{\mathbf{v}}^k}{2} s_{\mathbf{v}}^k(\zeta_{\mathbf{v}_k})\right)}_{\mathbf{v} \text{ scaling}} - \frac{\varepsilon_{\mathbf{v}}^k}{2} \left[ \underbrace{\partial_x S(x_k) \odot \exp\left(\varepsilon_{\mathbf{v}}^k q_{\mathbf{v}}^k(\zeta_{\mathbf{v}_k})\right)}_{\text{force scaling}} + \underbrace{t_{\mathbf{v}}^k(\zeta_{\mathbf{v}_k})}_{\text{translation}} \right]$$

$$\Lambda^+[\bar{\mathbf{x}}_k; \zeta_{\bar{\mathbf{x}}_k}] \equiv \underbrace{\bar{\mathbf{x}}_k \odot \exp\left(\varepsilon_{\bar{\mathbf{x}}}^k s_{\bar{\mathbf{x}}}^k(\zeta_{\bar{\mathbf{x}}_k})\right)}_{\bar{\mathbf{x}} \text{ scaling}} + \varepsilon_{\bar{\mathbf{x}}}^k \left[ \underbrace{v'_k \odot \exp\left(\varepsilon_{\bar{\mathbf{x}}}^k q_{\bar{\mathbf{x}}}^k(\zeta_{\bar{\mathbf{x}}_k})\right)}_{\mathbf{v} \text{ scaling}} + \underbrace{t_{\bar{\mathbf{x}}}^k(\zeta_{\bar{\mathbf{x}}_k})}_{\text{translation}} \right]$$