# GRE Physics Study Notes v2

Courtesy of Nicole Duncan, transcribed by Jeren Suzuki  ${\it Last~Edited~18th~September~2013}$ 

# Contents

1	Hermitian Matrix	1
2	Doppler Effect	1
		1
3		1
4	The Structure of Hydrogen	2
5		2
6	Free Particle	2
7	Schrödinger's Equation	3
8		3
		3
		3
9		3
10		3
		3
		4
		4
11		4
12		4
13		4
14		4
$\frac{14}{15}$		$\frac{1}{4}$
$\frac{16}{16}$		$\frac{1}{4}$
17		4
18		5
19		5
20		5
21		5
22		5
		5
		5
23	- <del> </del>	5
24		6
25	The state of the s	6
26		6
27		6
28	Fermi	6
29		6
30	Multiplicity/States	7
31		7
32	Collisions	7
33	Springs/Single Harmonic Oscillator	7
34	Thin Films	7
35	Conductivity/Current Density	8
36	Resistance	8
37	Boltzmann Statistics	8
38	Density of State Distribution	8
39	·	8
40		8
41		9
42		9
43		9
44	•	9
45		9
46	· · ·	9
		9

48	High Pass	 10
49	Special Relativity	 10
	49.1 Time Dilation	 10
	49.2 Length Contraction	 10
	49.3 Invariant	 10
	49.4 Energy	 10
50	Finite Potential Well	 11
51	Fundamental Particles	 11
52	Single Slit Diffraction	 11
53	Double Slit	 11
54		11
55	Bragg	 11
56	Aperture Limited: Airy Disk: Diffraction Limit: Angular Resolution	11
57	Electrostatics	12
	57.1 Limits	12
	57.2 Motion Through a Capacitor, etc	12
	57.3 Dipole	12
	57.4 Current Density	 12
	57.5 Drift Speed	12
	57.6 Conductivity	12
58	·	12
00	58.1 Tesla	13
	58.2 Force	13
	58.3 Cyclotron	13
	58.4 Cycloid	13
	58.5 Examples	13
	58.5.1 Solenoid	13
	58.5.2 Ring	13
	58.5.3 Sheet of Current	13
	58.5.4 Toroid	13
	58.5.5 Dipole	13
59		14
60	Radiation	14
61	Maxwell's Equations	14
62		14
63		14
64		$\frac{14}{15}$
	Coordinate Systems	$\frac{15}{15}$
	·	
66 67		15
67 68	1	15
68	1 0	15
69 70		15
70 71	·	15
71	Polarizers	16
72	$lackbox{arphi}$	16
73	•	16
74		16
75 		16
76	•	16
77		16
	77.1 Concave	17
	77.2 Convex	17
78		17
79		17
80		17
81	Mixing Gases	 17

82	Equipartition Theorem	17
83	Degrees of Freedom	18
84	Simple Pendulum	18
85	Gravity	18
86	Drag Force	18
87	Selection Rules	18
88	Stationary States	18
89	Spectroscopic Notation	19
90	Matter Waves	19
91	Pipes/Tubes/Fixed and Open Ends	19
92	Solutions to Time-Independent Schrödinger's Equation	19
93	Physical Pendulum	19
94	Intrinsic Magnetic Moment	20
95	Equations of Motions	20
96	Moments of Inertia	20
97	Hermitian Matrix	20
98	Balancing Problem	20
99	Decay Rates	20
100	Interferometer	20
	Springs	21
	Speed of Sound	21
103	Commutator Identities	21
104	Motion in a Circle	21
	Specific Heat in a Solid	21
106	Doppler Shift	21
107	Fission	22
108	Wire Resistance	22
109	Spin Matrices	22
110	For What v Will a Car Stay on a Hill?	22
111	Böhr Model	22
112	Fluids	22
113	Gauss' with non-uniform	23
114	Capacitors	23
115	Diffraction Limit	23
116	Normal Modes	23
117	Radiation in Atoms	23
118	Ionization Energy	24
119	Binding Energy	24
120	Hierarchy of Forces	24
121	Pair Production	24
122	Spectral Lines	24
123	Photon Interactions with Matter	24
124	Neutron	25
125	Deuteron	25
126	Protium	25

#### 1 Hermitian Matrix

- 1. Square Matrix
- 2.  $A = A^{\dagger} \rightarrow$  the matrix is equal to its conjugate transpose
- 3. Entries on the diagonal are real
- 4. Sum of 2 Hermitian matrices is Hermitian
- 5. Product of 2 Hermitian matrices is Hermitian only if they commute
- 6. Eigenvalues are orthogonal
- 7. The determinant is real

### 2 Doppler Effect

$$f = f_0 \left[ \frac{v + v_s}{v + v_0} \right] \tag{1}$$

$$\Delta d \downarrow = \begin{cases} +v_s \\ -v_0 \end{cases}$$

towards e/o

$$\Delta d \uparrow = \begin{cases} -v_s \\ +v_0 \end{cases}$$

away from e/o

#### 2.1 Relativistic

$$\frac{f_0}{f} = \frac{\lambda}{\lambda_0} = \sqrt{\frac{1+\beta}{1-\beta}} , \beta = \frac{v}{c}$$
 (2)

# 3 Lagrangian and Hamiltonian

$$L = T - U \tag{3}$$

$$\frac{\partial L}{\partial x} - \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{x}} \right) = 0 \tag{4}$$

$$H = T + U \text{ iff } U \neq U(\dot{x}) , U \neq U(t)$$
(5)

$$\rho = \frac{\partial L}{\partial \dot{q}} \qquad \dot{q} = \frac{\partial H}{\partial \rho} \qquad \dot{p} = \frac{\partial H}{\partial q} \tag{6}$$

#### The Structure of Hydrogen 4

- 1. Fine: Spin/orbit + relativistic correction Breaks l degeneracy , preserves jwhy  $E_{2s} < E_{2p}$
- 2. Hyperfine: spin/spin coupling of  $e^-$ /nucleus Responsible for 21 cm line

$$\mu_p = \frac{ge}{2m_p} \langle \bar{s}_p \rangle \ \mu_e = -\frac{e}{m_e} \langle \bar{s}_e \rangle \tag{7}$$

$$E_{n'f} = \frac{\mu_0 g_p e^2}{3\pi m_p m_e a^3} \langle \bar{s}_p \cdot \bar{s}_e \rangle \tag{8}$$

3. Stark Effect: Atom in external E Not spin dependent  $H' = eE_z$  if  $E = E_z$ Hydrogen:

$$E_1' = \langle H' \rangle = eE \int_0^\infty d^3 r z |\Psi_{100}|^2 = 0$$
 (9)

4. Zeeman Effect: Atom in external BSpin/orbital angular momentum(l) + B coupling

$$H_z' = (\bar{\mu}_e + \bar{\mu}_s) \cdot B_{\text{ext}} \tag{10}$$

Weak:  $B_{\rm ext} \ll B_{\rm int}$   $E' \propto mj \rightarrow {\rm breaks~into~} 2j+1 {\rm ~levels}$ Strong:  $B_{\rm ext} \gg B_{\rm int}$  $E' = \mu_B B_{\text{ext}}(m_e + 2m_s)$ 

#### Particle in a Box 5

$$E_n = n^2 E_0 \tag{11}$$

$$E_0 = \frac{\hbar^2 k^2}{2m}$$

$$k = \frac{n\pi}{a}$$
(12)

$$k = \frac{n\pi}{a} \tag{13}$$

$$\Psi = \sqrt{\frac{2}{a}}\sin(kx) , p = \hbar k$$
 (14)

3D: 
$$E = \frac{\hbar^2}{2m} [k_x^2 + k_y^2 + k_z^2]$$
 (15)

#### Free Particle 6

$$\Psi = Ae^{i(kx - \omega t)} \tag{16}$$

$$\Delta p \Delta x = \frac{\hbar}{2} \tag{17}$$

$$\Delta x \Delta k \sim 1 \tag{18}$$

Packet moves with group velocity...  $v_g = \frac{\partial \omega}{\partial k}$ 

$$\Psi = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \Phi(k)e^{ikx}dk \qquad \Phi = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \Psi(x)e^{-ikx}dx$$
 (19)

#### 7 Schrödinger's Equation

$$\left(-\frac{\hbar^2}{2m}\nabla^2 + V\right)\Psi = i\hbar\frac{\partial\Psi}{\partial t} \tag{20}$$

Separable  $\Psi(x,t) = \Psi(x)\phi(t)$ 

$$\phi = e^{-iE_n t/\hbar} \tag{21}$$

#### 8 Index of Refraction

$$n = \frac{c}{v} = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}} \qquad v = v_\phi = \sqrt{\frac{1}{\epsilon \mu}}$$
 (22)

 $\lambda = \frac{\lambda_0}{n}$  inside a medium

#### 8.1 Cherenkov Radiation

A charged particle passing through a medium which travels faster than the speed of light in that medium will emit light

$$n = \frac{c}{v} \longrightarrow v_{\min} = \frac{c}{n} \tag{23}$$

#### 8.2 Bremsstrahlung Radiation

Continuous spectrum of radiation emitted when a charged particle is decelerated in a metal target

#### 9 Gauss' Laws

$$\int E \cdot da = \frac{Q_{\rm in}}{\epsilon_0} \to \nabla \cdot E = \frac{\rho_{\rm in}}{\epsilon_0}$$
 (24)

$$\int B \cdot da = 0 \to \nabla \cdot B = 0 \tag{25}$$

$$\int g \cdot da = 4\pi MG \to \nabla \cdot g = -4\pi G \rho_m \tag{26}$$

### 10 Damped Driven Oscillator

$$F = -\underbrace{kx}_{\text{spring}} - \underbrace{b\dot{x}}_{\text{damp}} + \underbrace{A\cos\theta}_{\text{driving}}, \omega = \sqrt{\frac{k}{m}}, \beta = \frac{b}{2m}$$
(27)

#### 10.1 Critically Damped $\rightarrow \omega = \beta$

$$X_e = Ae^{-\omega_0 t} + A_2 t e^{-\omega_0 t} \tag{28}$$

### 10.2 Overdamped $\rightarrow \omega < \beta$

$$X_o = Ae^{-\beta t}e^{-\omega''t}, \omega'' = \sqrt{\beta^2 - \omega_0^2}$$
 (29)

### 10.3 Underdamped $\rightarrow \omega > \beta$

$$X_u = Ae^{-\beta t}\cos(\omega' t + \phi) , \omega' = \sqrt{\omega_0^2 - \beta^2}$$
(30)

### 11 Traveling Wave Formalism

$$v_{\phi} = \frac{\omega}{k} \quad \psi = A\cos k(vt - x) = A\cos(\omega t - kx)$$
(31)

In one period,  $x - vt = 2\pi$ 

### 12 Maxwell Velocity Distribution

$$D(v) \propto v^2 e^{-E/kT} \tag{32}$$

#### 13 Mean Free Path

$$l = \frac{1}{n\sigma} \tag{33}$$

#### 14 Cross Section

$$N_s = N_i \frac{N_t}{A} \sigma \tag{34}$$

# 15 Particle Diffusion (Fick's Law)

$$J = -D\nabla n \tag{35}$$

## 16 Thermal Diffusion (Fourier's Law)

$$\phi = -\sigma \nabla T \tag{36}$$

# 17 Thermodynamic Identity

$$TdS - PdV + \mu dN = dU \tag{37}$$

### 18 Heat Capacity

$$C \equiv \frac{dQ}{dT} \tag{38}$$

$$C_p = \frac{dQ}{dT} = T\frac{dS}{dT}$$
  $C_v = \frac{dQ}{dT} = \frac{dU}{dT}$  (39)

At constant  $P,\,E$  lost to work  $\Rightarrow T_p < T_V \Rightarrow C_p > C_v$ 

### 19 Water

 $ho = 1 \text{ g/cm}^3, 1 \text{ L} = 1 \text{ kg}$ 

#### 20 Decay

$$\begin{array}{ccc} \frac{0}{4}\beta + \bar{\nu} & \frac{0}{1}\beta + \nu & \frac{2}{1}D \\ \frac{4}{2}\alpha & \frac{0}{0}\gamma & \frac{A}{2}X \end{array}$$

#### 21 Beats

$$f_0 = f_1 - f_2$$
,  $T_b = \frac{1}{f_1 - f_2}$ , occur when  $f_1 + f_2$  are close (40)

The tuned frequency:

$$f = \underbrace{n}_{\text{harmonic}} f_f \tag{41}$$

### 22 First Law of Thermodynamics

$$U = Q + W (42)$$

#### 22.1 Second Law of Thermodynamics

 ${\cal S}$  increases or stays the same for any cyclic process.

#### 22.2 Third Law of Thermodynamics

$$S(T=0) = 1 \quad C_v \to 0 \text{ as } T \to 0 \tag{43}$$

# 23 Fundamental Assumption of Statistical Mechanics

All accessible microscopic states are equally likely

#### 24 Isothermal

Slow so T can equalize.

$$P_1 V_1 = P_2 V_2 \quad W = Nk \ln \left(\frac{V_i}{V_f}\right) \quad , W = -\int_{V_i}^{V_f} P dV \tag{44}$$

$$U = 0$$
 since  $\Delta T = 0$ ,  $U = \frac{f}{2}Nk\Delta T$  (45)

### 25 Adiabatic Compression

Fast, so no  $\Delta Q$  lost, like opening a soda can.

$$\Delta Q = 0 \to U = W \tag{46}$$

$$\Delta U = Nk\Delta T = W \tag{47}$$

$$\gamma = \frac{f+2}{f}, W = \frac{P_f V_f - P_i V_i}{1-\gamma}, V_f^{\gamma} P_f = V_i^{\gamma} P_i$$
(48)

#### 26 Heat

$$Q = TdS (49)$$

$$Q = mc\Delta T \tag{50}$$

$$Q = Pt (51)$$

$$U = Q + W (52)$$

# 27 Cyclotron

$$\omega = \frac{qB}{m}$$
  $F_c = F_B \to \frac{mv^2}{r} = qvB \to v = \frac{qBr}{m} = r\omega$  (53)

#### 28 Fermi

$$T_f = \frac{E}{k_B}$$
  $E_f = \frac{\hbar^2 k^2}{2m}$   $p = \hbar k$   $v_f = \frac{p_f}{m}$   $k_F = \left(\frac{3\pi^2 N}{\text{vol}}\right)^{1/3}$  (54)

$$p_f = \frac{2}{3} \frac{E_f}{v} \tag{55}$$

Degenerate Fermi gas: so cold that all states below  $E_F$  are occupied

### 29 Telescope

$$M = -\frac{f_{\text{object}}}{f_{\text{eye}}} = \frac{\theta_{\text{eye}}}{\theta_{\text{object}}}$$
 (56)

### 30 Multiplicity/States

Probability  $(\Omega_n) = \frac{\Omega_n}{\Omega_{all}}$  where  $\Omega$  is the multiplicity # of things.

- 1. Total # microstates: (# of states can be in) # of things
- 2. Ways to choose n things from N

$$\Omega\binom{N}{n} = \frac{N!}{(N-n)!n!} \tag{57}$$

#### 31 Rocket Motion

$$u\frac{dm}{dt} + M\frac{dv}{dt} = 0 (58)$$

$$v_f = v_0 + u \ln \left(\frac{M_i}{M_f}\right) \tag{59}$$

#### 32 Collisions

- 1. Momentum is always conserved  $p_i = p_f$ Don't forget to use (+) and (-) for before and after velocity collisions
- 2. KE and U conserved before or after collision only

3.

$$\epsilon = \underbrace{\frac{|v_1| + |v_2|}{|U_1| + |U_2|}}_{\text{before}} \tag{60}$$

- 4. Impulse  $J = F\Delta t = \Delta p = \Delta L$
- 5. Cross section  $N_s = N_I \frac{N_t}{A} \sigma$

### 33 Springs/Single Harmonic Oscillator

$$F = -kx \quad U = \frac{1}{2}kx^2 \quad \omega = \sqrt{\frac{k}{m}}$$
 (61)

$$ma = -kx = m\ddot{x} \tag{62}$$

$$E_{\text{tot}} = \frac{1}{2}kA^2$$
,  $A = \text{max amplitude}$  (63)

### 34 Thin Films

$$\Delta \phi = \begin{cases} 0 & n_2 < n_1 \\ \pi & n_2 > n_1 \end{cases} \qquad 2d = \begin{cases} n\lambda/2 & \Delta \phi_{\rm tot} = \pi \\ n\lambda & \Delta \phi_{\rm tot} = 0, 2\pi \end{cases}, \ n = \text{odd } \# \text{'s only}$$

### 35 Conductivity/Current Density

$$\bar{J} = ne\bar{v} = \sigma E \tag{64}$$

$$\sigma = \frac{ne^2\tau}{m} \tag{65}$$

#### 36 Resistance

$$R = \frac{\rho L}{A} \tag{66}$$

#### 37 Boltzmann Statistics

$$Z = \sum_{i} g_i e^{-E_i/kT} , g_i = \text{degeneracy of state } i$$
 (67)

$$p_s = \frac{g_s e^{-E_s/k_B t}}{Z} \qquad \frac{p_A}{p_B} = \frac{g_A}{g_B} \frac{e^{-A/kT}}{e^{-B/kT}} = \frac{g_A}{g_B} e^{(-A+B)/kT}$$
(68)

$$\langle \bar{X} \rangle = \frac{\sum_{i} e^{-E_i/kT}}{Z} \to \langle \bar{E} \rangle = \frac{1}{Z} \sum_{i} E_i e^{-E_i/kT}$$
 (69)

$$U = N\bar{E} \to \text{total Energy of system}$$
 (70)

### 38 Density of State Distribution

Fermions:

$$N_i = \frac{g_i}{e^{(E_i - \mu)/kT} + 1} \tag{71}$$

Bosons:

$$N_i = \frac{g_i}{e^{(E_i - \mu)/kT} - 1} \tag{72}$$

#### 39 Band Pass Filter

$$j\omega C + \frac{1}{j\omega L} = Z = \frac{-\omega^2 C L + 1}{j\omega L} \quad \omega_o = \frac{1}{\sqrt{LC}}$$
 (73)

### 40 Resonant Frequency

Inductor and capacitor in series:

$$j\omega L = \frac{1}{j\omega C} \to \omega_0^2 LC = 1 \to \omega = \frac{1}{\sqrt{LC}}$$
 (74)

Inductor and capacitor in parallel:

$$j\omega C + \frac{1}{j\omega L} = 0 \to j\omega C = \frac{1}{j\omega L} \to \omega = \frac{1}{\sqrt{LC}}$$
 (75)

#### 41 Central Force Motion

$$\begin{array}{ll} \mu = \frac{m_1 m_2}{m_1 + m_2} & R_{\rm CM} = \frac{\sum m_i r_i}{\sum m_i} & T = \frac{1}{2} \mu |\dot{r}|^2 \\ r_1 = \frac{m_2}{m_1 + m_2} r & r_2 = \frac{m_1}{m_1 + m_2} r & \bar{r} = \bar{r}_1 - \bar{r}_2 \end{array}$$

#### 42 Moments of Inertia

1. Hoop:  $MR^2$ 

2. Disk:  $\frac{1}{2}MR^2$ 

3. Solid Sphere:  $\frac{2}{3}MR^2$ 

4. Hollow Sphere:  $\frac{2}{5}MR^2$ 

5. Rod End:  $\frac{1}{3}ML^2$ 

6. Rod Middle:  $\frac{1}{12}ML^2$ 

### 43 Blackbody Radiation

$$T\lambda = 3 \text{ mm}K \quad P \propto T^4 \quad \rho \propto AT^4 \text{ (for photons)}$$
 (76)

#### 44 Heat Engine

$$e \le 1 - \frac{T_c}{T_h}$$
  $e = \frac{\text{benefit}}{\text{cost}} = \frac{W}{Q_h}$   $W = Q_h - Q_c$  (77)

### 45 Refrigerator

$$e \le \frac{T_c}{T_h - T_c}$$
  $e = \frac{\text{benefit}}{\text{cost}} = \frac{Q_c}{W}$  (78)

# 46 Space-Time Diagram

$$s^2 = x^2 - (ct)^2 (79)$$

1. s > 0 Spacelike  $\Delta t$  can equal 0, simultaneous events occur

2. s < 0 Timelike Events can occur at same point in space,  $\Delta x = 0$ , but not simultaneously  $\Delta t \neq 0$ 

3.  $\Delta s = 0$  Lightlike

#### 47 Low-Pass

RC or LR perpendicular to each other. For RC:

$$\frac{\frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} = \frac{1}{j\omega CR + 1} , \omega \to 0, \to 1$$
 (80)

For LR:

$$\frac{R}{R+j\omega L}, \omega \to 0, \to 1 \tag{81}$$

Square signals turn into wave-like signals with crests.

$$V_{\text{out}} = V_{\text{in}} \left( \frac{Z_2}{Z_1 + Z_2} \right) \tag{82}$$

Where  $Z_1$  and  $Z_2$  are on either side of a perpendicular  $V_{\rm out}$  with a  $V_{\rm in}$  leading into  $Z_1$ .

### 48 High Pass

CR or RL, turns square signals into signals where the flat tops of square turns into decaying to 0.

### 49 Special Relativity

$$\begin{array}{cccc} v/c & \gamma \\ .1 & 1.005 \\ .25 & 1.033 \\ .5 & 1.151 \\ .75 & 1.55 \\ .9 & 2.3 \end{array} \text{ Motion in } \hat{x}\text{:}$$

$$x = \gamma(x' + vt') \tag{83}$$

$$t = \gamma \left( t' + \frac{vx}{c^2} \right) \tag{84}$$

$$u_x' = \frac{u_x + v}{1 + \frac{u_x v}{c^2}} \tag{85}$$

$$u_z' = \frac{u_z}{\gamma \left(1 + \frac{u_x v}{c^2}\right)} \tag{86}$$

#### 49.1 Time Dilation

$$t' = \gamma t_0 \tag{87}$$

#### 49.2 Length Contraction

$$x' = \frac{x}{\gamma} \tag{88}$$

#### 49.3 Invariant

$$\Delta s^2 = \Delta x^2 - (ct)^2 \tag{89}$$

#### 49.4 Energy

$$E_r^2 = E_0^2 + (pc)^2$$
  $E_r \neq \frac{p_r^2}{2m}$   $E_r = \gamma E_0$   $p_r = \gamma mv = \gamma p$  (90)

#### 50 Finite Potential Well

$$E \propto n^2 \quad d \propto \frac{1}{\sqrt{V - E_n}} \to d \propto n$$
 (91)

#### 51 Fundamental Particles

1. Bosons:

Gauge Boson - Gluon - Strong

Photon - E&M

W,Z Bosons - a.k.a weak bosons

Higgs

Graviton

Pion

2. Fermions:

Quarks (Up, down, top, bottom, strange, charm)

Leptons (Electron, Muon, Tauon) and neutrino variants of each

3. Composite Fermions: Protons and Neutrons, etc.

### 52 Single Slit Diffraction

$$d\sin\theta = n\lambda$$
  $\theta = \text{angle between central max and first minimum}$  (92)

$$\tan \theta = \frac{y}{L} \text{ central max, width } \Delta y_{\text{max}} = \frac{2L\lambda}{d}$$
(93)

#### 53 Double Slit

$$d\sin\theta = n\lambda \quad \Delta y = L\tan\theta \tag{94}$$

### 54 Diffraction Grating

$$d\sin\theta = n\lambda$$
  $y = L\tan\theta = L\frac{\sin\theta}{\cos\theta} = \frac{Ln\lambda}{d\cos\theta}$  (95)

### 55 Bragg

$$2d\sin\theta = n\lambda$$
  $d = \frac{a}{\sqrt{l^2 + h^2 + k^2}}$ , letters are miller indices (96)

# 56 Aperture Limited: Airy Disk: Diffraction Limit: Angular Resolution

$$\sin \theta = \frac{1.22\lambda}{D}$$
,  $D = \text{diameter of aperture}$ ,  $\theta = \text{angular separation}$  (97)

#### 57 Electrostatics

$$F = \frac{kq_1q_2}{r^2} \quad \epsilon = k\epsilon_0 \quad k = 9 \times 10^9 \frac{\text{Nm}}{c^2}$$
 (98)

1. Sphere:  $\propto \frac{1}{r^2}$ 

2. Infinite Line:  $\propto \frac{1}{r}$ 

3. Infinite Plane doesn't fall off:  $E = \frac{\sigma}{2\epsilon_0}$ 

4. Ring:  $\propto \frac{x}{d^3}$ ,  $d = \sqrt{x^2 + R^2}$ 

5. Capacitor doesn't fall off:  $E_{\rm out}=0$  ,  $E_{\rm in}=\frac{\sigma}{\epsilon_0}$ 

#### 57.1 Limits

As  $x \to \infty$  all objects look like point objects. Sometimes use binomial approximation to get behavior at  $\infty$ ,  $(1+x)^n \sim 1 + nx$  for  $x \ll 1$ .

#### 57.2 Motion Through a Capacitor, etc.

Use kinematics equations F = ma = qE find V, a, t to get  $\theta$  deflection.

#### 57.3 Dipole

$$\bar{p} = q\bar{d}$$

$$\bar{E}_{\text{dipole}} = \begin{cases} \frac{2k\bar{p}}{r^3} & \text{axis of } \bar{d} \\ -\frac{k\bar{p}}{r^3} & \perp & \text{to } \bar{d} \end{cases}$$
(99)

#### 57.4 Current Density

$$J = nev_d$$
,  $I = JA = \frac{\text{current of cross section}}{m^2}$  (100)

#### 57.5 Drift Speed

$$J = \sigma E = \frac{ne^2 \tau}{m} E \to v_d = \frac{\sigma E}{ne} = \frac{e\tau E}{m}$$
 (101)

#### 57.6 Conductivity

$$\sigma = \frac{ne^2\tau}{m} \tag{102}$$

## 58 Magnetic Field

$$B = \frac{\mu_0 I}{4\pi} \frac{d\bar{l} \times \hat{r}}{r^2} , d\bar{l} = \text{length and direction}$$
 (103)

58.1 Tesla

$$T = \frac{N}{A \cdot m}$$
, current  $I = \int J \cdot da_{\perp}$  (104)

**58.2** Force

$$F = q\bar{v} \times \bar{B} = I(d\bar{l} \times \bar{B}) \tag{105}$$

58.3Cyclotron

$$E \parallel B \to \text{ Helical motion}$$
 (106)

$$v_{\parallel}B \rightarrow \text{Helical}$$
 (107)

$$v_{\parallel}B \rightarrow \text{Helical}$$
 (107)
$$\frac{mv^2}{r} = qvB \rightarrow F_c = F_m$$
 (108)

58.4 Cycloid

$$E \perp B$$
 (109)

#### 58.5 Examples

58.5.1Solenoid

$$B = \begin{cases} 0 & \text{outside} \\ \frac{\mu_0 I N}{L} & \text{inside} \end{cases}$$

58.5.2 Ring

$$B = \frac{\mu_0 I}{2R} \tag{110}$$

Any displacement along center of ring should reduce the this equation as  $x \to 0$ .

58.5.3 Sheet of Current

$$B = \begin{cases} -\frac{\mu_0}{2} & z > 0\\ \frac{\mu_0}{2} & z < 0 \end{cases}$$

Toroid 58.5.4

$$B = \begin{cases} 0 & \text{out} \\ \frac{\mu_0 I N}{2\pi R} & \text{in} \end{cases}$$

58.5.5 Dipole

$$B \propto \frac{\mu}{r^3}$$
,  $\mu = IA = \text{dipole moment}$  (111)

$$B \propto \frac{IA}{r^3}$$
, as  $x \to \infty$ , this is twice the field of a current loop (112)

### 59 Inductance

$$\Phi = LI \quad \epsilon = -\frac{d\Phi}{dt} \quad \Phi_B = \int B \cdot dA \tag{113}$$

$$W = \frac{1}{2}LI^2 \left( \text{corollary: cap } W = \frac{t}{2}CV^2 \right)$$
 (114)

$$I(t) = \frac{\epsilon_0}{R} \left[ 1 - e^{-(R/L)t} \right] \quad \tau = \frac{L}{R}$$
(115)

#### 60 Radiation

Electric Dipole Magnetic Dipole Point Charge  $P \propto q^2 d^2 \omega^4 \qquad P \propto I^2 \omega^4 \qquad P \propto q^2 a^2$   $P_{\rm max} \perp {\rm to} \ \hat{a}.$ 

#### 61 Maxwell's Equations

$$\nabla \cdot E = \frac{\rho_{\text{in}}}{\epsilon_0} \quad \nabla \times E = -\frac{\partial B}{\partial t}$$

$$\nabla \cdot B = 0 \quad \nabla \times B = \mu_0 J - \mu_0 \epsilon_0 \frac{\partial E}{\partial t}$$

$$\oint E \cdot dA = \frac{Q_{\text{in}}}{\epsilon_0} \quad \oint E \cdot dl = -\frac{\partial \Phi_B}{\partial t}$$

$$\oint B \cdot dA = 0 \quad \oint B \cdot dl = \mu_0 I + \mu_0 \epsilon_0 \frac{\partial \Phi_E}{\partial t}$$

### 62 Boundary Conditions

$$E_{\parallel} = 0$$
,  $B_{\perp} = 0$  for reflected waves  $E_{\text{tot}} = 0$   $B_{\text{tot}} = 2B_{\text{wave}}$  (116)

$$\epsilon_1 E_1^{\perp} - \epsilon_2 E_2^{\perp} = \sigma_F \quad E_1^{\parallel} = E_2^{\parallel} \tag{117}$$

$$B_1^{\perp} = B_2^{\perp} \quad \frac{B_1^{\parallel}}{\mu_1} - \frac{B_2^{\parallel}}{\mu_2} = k_f \times \hat{n}$$
 (118)

#### 63 E&M Fields

B/E are in phase and perpendicular

$$B_{+}0 = \frac{k}{\omega}E_{0} = \frac{1}{c}E_{0} \tag{119}$$

Energy Density 
$$\langle U \rangle = \frac{\epsilon_0}{2} E^2$$
 Intensity  $\langle I \rangle = \frac{1}{2} c \epsilon E^2$  (120)

Radiation Pressure 
$$p = \frac{\langle s \rangle}{c}$$
  $\bar{s} = \frac{\bar{E} \times \bar{B}}{\mu_0}$ ,  $\hat{s} = \text{propagation of } \frac{E}{\mu}$  (121)

### 64 Relativistic E&M

Processes change between frames, but outcome is same.

Example: Parallel Plate Capacitor:

$$\sigma_0 = \frac{Q}{A} \quad \sigma' = \frac{Q}{A'}$$
, length contracts,  $A' < A \rightarrow \sigma' > \sigma_0 \quad \sigma' = \gamma \sigma_0$  (122)

Also, 
$$A = lw$$
  $a' = \frac{l}{\gamma}w = \frac{lw}{\gamma}$  (123)

so, 
$$E_{\perp} = \gamma E_0$$
  $E_{\parallel} = E_{\parallel}$  (124)

### 65 Coordinate Systems

- 1. Cartesian:  $dl = \hat{x}dx + \hat{y}dy + \hat{z}dz$ , dV = dxdydz
- 2. Spherical:  $dl = \hat{r}dr + rd\theta\hat{\theta} + r\sin\theta d\phi\hat{\phi}$ ,  $dV = r^2\sin\theta dr d\phi d\theta$
- 3. Cylindrical:  $dl = \hat{s}ds + sd\phi\hat{\phi} + \hat{z}dz$ ,  $dV = sdsd\phi dz$

#### 66 Positronium

$$\mu = \frac{m_e}{2} \to E_p = \frac{E_H}{2} \quad E_{pos} = \frac{-13.6 \text{ eV}}{2} \quad E_p = \frac{-6.8}{n^2}$$
 (125)

### 67 Free Expansion

$$W = 0 , \quad Q = 0 , \quad \Delta S > 0 , \quad \Delta S = Nk \ln \left(\frac{V_i}{V_f}\right)$$
 (126)

### 68 Entropy

$$S = k \ln(\Omega) \quad , Q = TdS \quad S_{\text{tot}} = S_A + S_B \tag{127}$$

### 69 P/N Junctions

- 1. n donate  $e^-$  to CB
- 2. p donate holes to VB

# 70 Wave Velocity

Group Velocity 
$$v_g = \frac{\partial \omega}{\partial k}$$
 phase  $v_\phi = \frac{\omega}{k} = \sqrt{\frac{1}{\epsilon \mu}} = \frac{\lambda}{T}$  (128)

#### 71 Polarizers

- 1.  $I = I_0 \cos^2 \theta$  for plane polarized
- 2.  $I = \frac{I_0}{2}$  for natural light

# 72 Heisenberg

$$\sigma_p \sigma_x \ge \frac{\hbar}{2} \quad \sigma_A \sigma_B \ge \frac{1}{2i} \langle [\hat{A}, \hat{B}] \rangle$$
 (129)

### 73 Compton Effect

Elastic scattering of photons - shows particle nature of light

$$\Delta \lambda = \lambda_c (1 - \cos \theta) \quad \lambda_c = \frac{hc}{E_0} = \frac{h}{mc}$$
 (130)

#### 74 Photoelectric Effect

$$KE_{\text{max}} = E_p - \Phi = \hbar\omega - \Phi = \frac{hc}{\lambda} - \Phi = hf - \Phi$$
 (131)

Energy of photon 
$$=\frac{hc}{\lambda} = hf = \frac{h}{2\pi}\omega = \hbar\omega$$
 (132)

Einstein's Equation:  $eV = hf - \Phi$ , V = (-) value which  $e^-$  can be stopped from hitting the cathode,  $I \to 0$  (133)

#### 75 Phonon

Displacement from equilibrium values of plane spacing

$$E_{\rm phonon} = \hbar\omega$$
 (134)

### 76 Superconductor

- 1. Meissner: B = 0 inside  $S_c$
- 2.  $\rho \to 0$  at critical temp
- 3.  $\lambda_c$  penetration depth measures how far B penetrates before  $\to 0$   $B = B_0 e^{-x/\lambda_c}$

#### 77 Mirrors

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \to d_i = \frac{d_o f}{f - d_o} \tag{135}$$

$$M = \frac{h_i}{h_o} = -\frac{d_i}{d_o} \quad f = \frac{R}{2} \tag{136}$$

Rays go through center and continues in a straight line and goes parallel then through focal point.

#### 77.1 Concave

Converging Mirror, what most diagrams are of

#### 77.2 Convex

Diverging Mirror. Images always smaller, virtual, and upright. They cover a wide field of view.

### 78 Reflection/Refraction

Snell's Law:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \tag{137}$$

$$\theta_i = \theta_r$$
,  $\theta$  measured relative to normal (138)

For total internal reflection:

$$n_1 \sin \theta_1 = n_2 \sin 90 \tag{139}$$

$$\sin \theta_1 = \frac{n_2}{n_1} \tag{140}$$

$$n = \frac{c}{v} = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}} \qquad \epsilon = k \epsilon_0 \qquad \frac{n_1}{n_2} = \frac{v_2}{v_1}$$
(141)

#### 79 Bloch's Theorem

 $\Psi$  solutions to Schrödinger's Equation are plane waves modulated by a function with the periodicity of the lattice

#### 80 Stern-Gerlach

Expected 2s+1 states, saw 2s+1=2 states. Implied that  $H=-\gamma \bar{S}\cdot \bar{B}$ 

### 81 Mixing Gases

$$\begin{cases} \text{if } A \neq B & \Delta s = \Delta s_A + \Delta s_B \\ \text{if } A = B & \Delta s = 0 \text{ since } \Delta \ln(\Omega) \sim 0 \text{ since } \Omega = \text{ large } \# \end{cases}$$

# 82 Equipartition Theorem

$$U = \frac{f}{2}NkT \tag{142}$$

f = # quadratic terms in Hamiltonian (not degrees of freedom, but in general they're equal).

$$kT \sim \frac{1}{40} \text{ eV } @ \text{ room temperature}$$
 (143)

### 83 Degrees of Freedom

- 1. A quadratic term in PE or KE
- 2. Translational  $(\frac{mv^2}{r})$
- 3. Rotational  $(I\omega^2)$
- 4. Vibrational (Counts as 2)  $(kx^2, mv^2)$

### 84 Simple Pendulum

$$\omega = \sqrt{\frac{g}{l}} \qquad \theta = \theta_{\text{max}} \sin(\omega t) \tag{144}$$

### 85 Gravity

$$F_g = \frac{Gm_1m_2}{r^2} = mg \quad \text{Kepler: } T^2 \propto a^3$$
 (145)

Escape velocity:

$$F_c = F_g \to mg = \frac{mv^2}{r} \to v = \sqrt{gr} \tag{146}$$

Gauss:

$$\int g \cdot dA = -4\pi G \int dM_{\rm in} \to \int g \cdot dA = -4\pi G M_{\rm in}$$
(147)

### 86 Drag Force

$$F_D \propto v^n$$
 air:  $F_D \propto v^2$  (148)

Terminal velocity 
$$F_D = F_g \to v = \sqrt{\frac{g}{k}}$$
 (149)

$$F_D = mkv^2 (150)$$

### 87 Selection Rules

$$\Delta l = \pm 1$$
  $\Delta m = \pm 1, 0$   $\Delta s$  no rule  $\Delta n \ge 1$  (151)

### 88 Stationary States

$$\langle \Psi | \Psi \rangle$$
 is not a function of time (152)

#### 89 Spectroscopic Notation

$$^{2s+1}L_j \tag{153}$$

- 1. Spin isn't always  $\frac{1}{2}$
- 2. L = orbital angular momentum
- 3. j = s + L = total angular momentum

$$L = \begin{cases} s & 0 \\ p & 1 \\ d & 2 \\ f & 3 \end{cases}$$

#### 90 **Matter Waves**

$$p = \hbar k \qquad k = \frac{2\pi}{\lambda} \qquad p = \frac{h}{\lambda} \to \lambda = \frac{h}{p}$$
 (154)

#### 91 Pipes/Tubes/Fixed and Open Ends

1. Closed on both ends:

Ends are nodes,  $\sin kx$  dependence,  $\Psi = A \sin kx \cos \omega t$  $\lambda = \frac{2L}{n}$  longest  $\lambda$  is 2L

2. Open on both ends:

Ends are antinodes,  $\cos kx$  dependence

$$\lambda = \frac{2L}{n}$$
  $\Psi = A\cos kx \cos \omega t$ 

3. Closed/Open ends:

Node/Antinode Longest  $\lambda = 4L$  (so  $\frac{1}{4}\lambda$  can fit end to end)

$$\lambda = \frac{4L}{2n-1} \text{ (-1 if } n \text{ starts at 1)}$$
 
$$\Psi = A \sin kx \cos \omega t$$

#### 92 Solutions to Time-Independent Schrödinger's Equation

$$\langle H \rangle = \sum_{n} |C_n|^2 E_n = C_1 E_1 + C_2 E_2 + \cdots, \sum_{n} |C_N|^2 = 1$$
 (155)

$$\operatorname{Prob}(a < x < b) = \int_{a}^{b} |\Psi(x)|^{2} dx \to \text{ area under the } |\Psi|^{2} \text{ vs } x \text{ graph}$$
 (156)

#### Physical Pendulum 93

$$\tau = I\alpha = I\dot{\omega} = mg\sin\theta L_{\rm cm} = \bar{r}\times\bar{F} \tag{157}$$

$$\ddot{\theta} = \frac{mgL_{\rm CM}}{I}\theta \to \omega = \sqrt{\frac{mgL_{\rm CM}}{I}} , \quad L_{\rm CM} = \text{the distance from the pivot point to the center of mass}$$
 (158)

#### 94 Intrinsic Magnetic Moment

$$\bar{\mu}_s = \frac{gq}{2m}\bar{s}$$
 m is dominant factor (159)

#### 95 Equations of Motions

Look for boundary values I(s) given x(t) and y(t). Differentiate and see which one yields  $v_0$ 

#### 96 Moments of Inertia

The moment of an object stretched along the axis of rotation doesn't change

$$I_{\rm disk} = I_{\rm cylinder} \tag{160}$$

The moment of a cuboid:

$$I = \frac{M}{12}(x^2 + y^2) \tag{161}$$

"Twin Plate", y=0 so  $I_z=\frac{M}{12}x^2.$  Then,  $I_z=\frac{1}{12}(2d)^2=\frac{M}{3}d^2$ 

#### 97 Hermitian Matrix

Real eigenvalues, square

$$A = A^{T} = A^{*T}$$
 the entries are equal to their conjugate transpose (162)

All diagonals must be real. The sum of two Hermitian matrices is also Hermitian.

$$\langle f|\hat{A}f\rangle = \langle \hat{A}f|f\rangle \Rightarrow A = A^*$$
 (163)

### 98 Balancing Problem

Easiest to use center of mass.

Center of Mass = 
$$\frac{\sum m_i r_i}{\sum m_i}$$
 one mass is at  $-r$  (164)

### 99 Decay Rates

$$\frac{dA}{dt} = -kA \to A = A_0 e^{-kt}; \frac{A}{A_0} = \frac{1}{2} = e^{-kt} \to t_{1/2} = \frac{\ln(2)}{k}$$
(165)

#### 100 Interferometer

Fringe shifts occur for changing distance or  $\lambda$ .

$$2d = m\lambda$$
  $d = \text{change in distance}$   $\lambda = \Delta\lambda$   $\lambda_{\text{gas}} = \frac{\lambda_{\text{vac}}}{n}$  (166)

In a tube where gas  $\rightarrow$  vacuum:

$$2d = m(\lambda_{\text{gas}} - \lambda_{\text{vac}}) = m\lambda_{\text{vac}} \left(\frac{1}{n} - 1\right)$$
(167)

#### 101 Springs

Add like capacitors. Makes sense because in series they can stretch more so F = kx must be decreased, in parallel, they stretch less so  $k \uparrow$  for the same force.

Springs in series: 
$$\frac{1}{k_{\text{tot}}} = \frac{1}{k_1} + \frac{1}{k_2}$$
 (168)

Springs in parallel: 
$$k = k_1 + k_2$$
 (169)

### 102 Speed of Sound

In an ideal gas:  $v \propto \sqrt{T}$ 

#### 103 Commutator Identities

$$[A,B] = -[B,A] \tag{170}$$

$$[AB, C] = A[B, C] + [A, C]B$$
 (171)

$$[A, BC] = B[A, C] + [A, B]C$$
 (172)

### 104 Motion in a Circle

Always  $a_{\text{radial}}$  component. Only  $a_{\text{tan}}$  if  $v_{\text{tan}}$  changes.

$$F = \frac{mv^2}{r} = ma_r \to a_r = \frac{v^2}{r} \tag{173}$$

$$a_r = r \times \alpha \qquad v = r \times \omega \tag{174}$$

### 105 Specific Heat in a Solid

#### 1. Einstein Model:

Treats atoms as harmonic oscillators, 3N total harmonic oscillators and they all have the same energy (frequency) using Bose-Einstein statistics

#### 2. Debye:

Also 3N harmonic oscillators. Assigns a range of energies (frequencies) and treats the lattice vibrations as phonons in a box

#### 3. Dulong-Petit:

High temperature, uses equipartition theorem with harmonic oscillators (f = 6, c = 3Nk). Debye and Einstein models reduce to this in the high T limit.

### 106 Doppler Shift

$$f = f_0 \left( \frac{1 + v_s}{1 + v_0} \right) \qquad \frac{\lambda}{\lambda_0} = \frac{f_0}{f} = \sqrt{\frac{1 + \beta}{1 - \beta}} , \beta = \frac{v}{c}$$
 (175)

The "redshift":  $z = \frac{\lambda_0 - \lambda}{\lambda} = \frac{f - f_0}{f}$ 

#### 107 Fission

Conservation of energy, binding energy of nucleus is always (-), like  $e^-$  binding energy.

$$-BE_i + KE_i = -BE_f + KE_f \tag{176}$$

#### 108 Wire Resistance

$$R = \frac{\rho L}{A} \tag{177}$$

### 109 Spin Matrices

$$S_i \psi = \frac{\hbar}{2} \sigma_i \psi \tag{178}$$

For example, eigenstate of  $S_x$  with  $-\frac{\hbar}{2}$  and  $\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ 

$$\frac{1}{\sqrt{2}}(|\uparrow\rangle - |\downarrow\rangle) = \frac{1}{\sqrt{2}} \left[ \begin{pmatrix} 1\\0 \end{pmatrix} - \begin{pmatrix} 0\\1 \end{pmatrix} \right] = \frac{1}{\sqrt{2}} \left[ \begin{pmatrix} 1\\-1 \end{pmatrix} \right] \tag{179}$$

$$\begin{pmatrix} 1 \\ -1 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} -1 \\ 1 \end{pmatrix} \to S_x \psi = \frac{\hbar}{2} \left( \frac{1}{\sqrt{2}} \right) \begin{pmatrix} -1 \\ 1 \end{pmatrix} = -\frac{\hbar}{2} \left( \frac{1}{\sqrt{2}} \right) \begin{pmatrix} -1 \\ 1 \end{pmatrix} = -\frac{\hbar}{2} \psi \tag{180}$$

$$|\uparrow\rangle = \begin{pmatrix} 1\\0 \end{pmatrix} \qquad |\downarrow\rangle = \begin{pmatrix} 0\\1 \end{pmatrix} \tag{181}$$

### 110 For What v Will a Car Stay on a Hill?

$$F_c = F_g \qquad \frac{mv^2}{r} = mg \tag{182}$$

### 111 Böhr Model

- 1.  $e^-$  have classical motions
- 2.  $\Delta E = hf$
- 3. Angular momentum quantized  $L = n\hbar$
- $4. E_n = -\frac{Z^2 E_0}{n^2} \qquad E_n \propto \mu$
- 5.  $\Delta E = E_0 \left( \frac{1}{n_f^2} \frac{1}{n_i^2} \right) \to \frac{1}{\lambda} = R_y \left( \frac{1}{n_f^2} \frac{1}{n_i^2} \right) , R_y = 1 \times 10^7 \text{ m}^{-1}$
- 6. Positronium:  $\mu = \frac{m_e}{2} \rightarrow E_p = \frac{E_0}{2n^2}$

### 112 Fluids

Equilibrium when  $F_A = F_B$ , where F = mg.

#### 113 Gauss' with non-uniform

Must integrate.

$$\rho = Ar^2 \quad dV = 4\pi r^2 dr \quad \int E \cdot dA = \frac{Q_{\rm in}}{\epsilon_0} = \frac{\int \rho dV}{\epsilon_0} = \frac{\int Ar^2 4 \ pir^2 dr}{\epsilon_0} = \frac{A4\pi r^5}{5\epsilon_0}$$
(183)

#### 114 Capacitors

In series,  $Q_1 = Q_2$  while in parallel,  $V_1 = V_2$ 

### 115 Diffraction Limit

$$\sin \theta = \frac{1.22\lambda}{d}$$
  $d = \text{diameter of lens}$  (184)

#### 116 Normal Modes

- 1. Highest normal mode frequency when out of phase
- 2. Use limits if possible, with  $M \to \infty$
- 3. # frequency = # masses
- 4. If odd # masses, one  $\omega$  will be  $\omega_0$ , others above and below

For two hanging masses connected by a spring,

In phase: 
$$\omega = \sqrt{\frac{g}{l}}$$
 spring's  $\Delta x = 0$  (185)

Out of phase: 
$$\omega = \sqrt{\frac{2k}{m} + \frac{g}{l}}$$
 (186)

For three masses connected by two springs with the mass in the middle larger than the equal masses on the sides:

$$\omega = \sqrt{\frac{k}{m}}$$
, like attached to a wall (187)

Side masses are in phase, middle mass is out of phase,  $\omega = \sqrt{\frac{2k}{m}}$ .

For 2 masses connected by 3 springs with the side masses connected to a wall:

In phase: 
$$\Delta x_1 = \Delta x_2$$
 and  $k'$  isn't expanded,  $\omega = \sqrt{\frac{k}{m}}$  (188)

Out of phase: 
$$\Delta x_1 = -\Delta x_2$$
 and center of mass  $k'$  stays in place  $\omega = \sqrt{\frac{k + 2k'}{m}}$  (189)

#### 117 Radiation in Atoms

#### 118 Ionization Energy

E required to liberate the outermost  $e^-$ . On the periodic table, increases in the +y, +x direction.

### 119 Binding Energy

How tightly bound nucleons are

- 1. Peak at Fe/N  $\rightarrow$  elements  $Z < Z_{\rm FE}$  undergo Fusion,  $Z > Z_{\rm Fe}$  undergo fission to release energy
- 2. When BE/nucleon increases, in reaction, energy is released
- 3. The mass of a nucleus is always less than the  $\sum$  particle's masses
- 4. "More tightly bound" = less mass/nucleon, more BE/nucleon
- 5. Created by the strong force
- 6. Energy given off in fusion/fission is the  $\Delta E$  between fuel and products

### 120 Hierarchy of Forces

- 1. Strong
- 2. E&M
- 3. Weak
- 4. Gravity

#### 121 Pair Production

- 1. Creation of elementary particle and anti-particle from photon
- 2. Cannot occur in free space, usually near a nucleus or other photon
- 3. For  $e^-$ , the photon E must exceed twice the rest energy of the  $e^-, \approx 1 \text{ MeV}$
- 4. If 2 photons, 500 keV
- 5. Dominates at high E

## 122 Spectral Lines

- 1. Less dense gas  $\rightarrow$  more sharp and precise lines don't lose E due to collisions
- 2. Sodium doublet created by spin/orbit coupling, more pronounced in an external B

#### 123 Photon Interactions with Matter

- 1. Compton Effect: low E, elastic scattering  $< 10^6$  MeV
- 2. Photoelectric Effect: mid  $E_{\gamma} < 10^7 \text{ MeV}$
- 3. Pair Production: high  $E_{\gamma} > 10^6 \text{ MeV}$

### 124 Neutron

A fermion with:

$${}_{0}^{1}n \tag{190}$$

Decay: 
$${}_{0}^{1}n \to {}_{1}^{1}p^{+} + {}_{-1}^{1}e + \bar{\nu}$$
 (191)

Capture: 
$${}_{1}^{1}p^{+} + {}_{-1}^{1} e \rightarrow {}_{0}^{1} n + \bar{\nu}$$
 (192)

### 125 Deuteron

"Heavy Hydrogen",  $^2_1 H.$  Also, a boson.

# 126 Protium

A proton,  ${}^1_1H$ , Hydrogen nucleus, a fermion