

Day- 4

odd \rightarrow input length

✓ Except one element, All elements appears twice. Find that element

$$2(n) + 1 \Rightarrow \text{odd}$$

$$\begin{array}{l} \textcircled{1} \\ \rightarrow O(n^2) \\ + \\ \rightarrow O(1) \end{array} \} \rightarrow \begin{array}{l} O(n \log n) \\ + \\ O(n) \end{array} \textcircled{2}$$

Input: ar[] = {7, 3, 5, 4, 5, 3, 4}

Output: 7

$$7 \rightarrow 1$$

$$3 \rightarrow 2$$

$$5 \rightarrow 2$$

$$4 \rightarrow 2$$

3 3 4 4 5 5 7
1 2 2 2 2 2 2

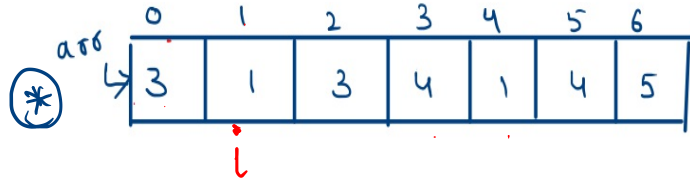
$$\frac{n}{2} + 1$$

\Rightarrow

key	v
7	1
3	2
5	2
4	2

$$\begin{array}{l} \downarrow \\ O(n) + O(n) \textcircled{3} \\ \rightarrow O(n) \checkmark \\ \downarrow \\ * O(n) + O(1) \end{array} \}$$

PS. $\left\{ \begin{array}{l} \text{temp} = \text{arr}[0] \\ \text{for}(i=1; i < n; i++) \\ \text{temp} = \text{temp} \wedge \text{arr}[i] \end{array} \right\}$ $O(n)$
 $+ O(1)$
 \Rightarrow
 $\text{temp} = \text{arr}[0]$
 Print(temp)



$\text{temp} = 3 \wedge 1 \wedge 3 \wedge 4 \wedge 1 \wedge 4 \wedge 5$
 $\underbrace{3 \wedge 1}_2$
 $0 \wedge 5 = 5$

$3 \rightarrow 11$
 $1 \rightarrow 01$
 $\hline 10 \Rightarrow 2$
 $2 \rightarrow 10$
 $3 \rightarrow 11$
 $\hline 01 \Rightarrow 1$
 $3 \wedge 1 \wedge 3 = 1$
 $0 \wedge 1 = 1$

→ Ex-OR operator $[\oplus]$
 \wedge

A	B	A+B	A·B	A⊕B
0	0	0	0	0 ✓
0	1	1	0	1 ✓
1	0	1	0	1 ✓
1	1	1	1	0 ✓

A, B are Boolean Variables
 $\rightarrow 0/1$

$0 \oplus x = x$
 $x \oplus x = 0$
 $0 \oplus 1 = 1$
 $0 \oplus 3 = 3$

EA

(*) Check given number is Even/Odd without using Arithmetic Operators ✓

$n \div 2 = 0 \rightarrow \text{even}$
 \uparrow else $\rightarrow \text{odd}$
 $*$

$\rightarrow +, *, -, \%, /$

$n_1 = 10 \Rightarrow (1010)_2$
 \uparrow

odd \rightarrow last bit : 1

$n_2 = 11 \Rightarrow (1011)_2$ *
 \uparrow } odd

even \rightarrow last bit : 0

$n_3 = 7 \Rightarrow (0111)_2$ *

$n_3 = 8 \Rightarrow (1000)_2$
 \uparrow

$n_1 = 10$ $n_1 \& 1$ 1010 $\& 0001$ <hr/> $0000 \Rightarrow 0$

$n_2 = 11 ; n_2 \& 1$

1	0	1	1
&	0	0	0
<hr/>			
0	0	0	1
<hr/>			

$\Rightarrow 1$

$n \& 1$
 $\rightarrow 0$ even
 $\rightarrow 1$ odd

✓ 2) Rotate array by d elements [left], anti-clock wise direction

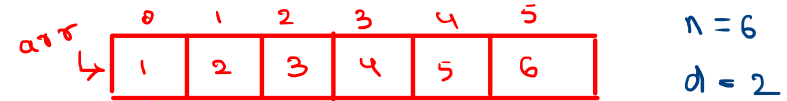
input:-

arr[6] = { 1,2,3,4,5,6 } and d=2

output :-

d=1 ==> 2,3,4,5,6,1 ✓

d=2 ==> 3,4,5,6,1,2 [final output]



d=1 2 3 4 5 6 1

d=2 3 4 5 6 1 2 (*) o/p

$$n = 6, \quad d = \frac{7}{*}$$



6



1

$$d = d \% n$$

$a[5]$ \rightarrow

0	1	2	3	4	5
1	2	3	4	5	6

4 5 6 1 2 3

Brute-Force :-

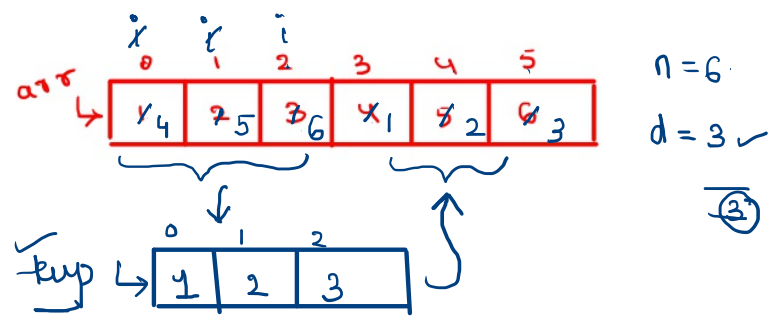
$\rightarrow d = d \% n$

① take temp array of size d

② copy first d elements of given array into temp array $\rightarrow d$ times

③ shift ^{last} $n-d$ elements to left, using a for loop [arr[i] = arr[i+d]] $\rightarrow n-d$

④ put all elements of temp array to last d positions in given array $\checkmark \rightarrow d$



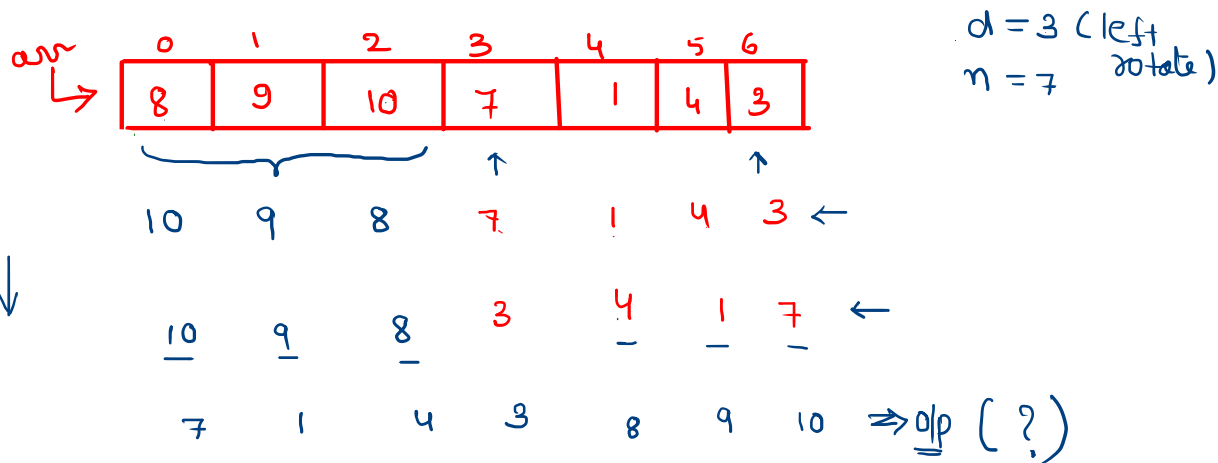
$O(n)$
 $+$
 $O(d)$
 $\rightarrow O(n)$

$d = n$

Multiple-sub-arrays-reverse

$O(d)$
 \rightarrow ① reverse(arr, 0, d-1) 0 to 2
 $O(n-d)$
 \rightarrow ② reverse(arr, d, n-1) 3 to 6
 $O(n)$
 \rightarrow ③ reverse(arr, 0, n-1) 0 to 6
 $\hookrightarrow arr \Rightarrow o/p$

$\rightarrow O(n)$
 $+$
 $O(1)$



(2-ptg + swap)

arr

0	1	2	3	4	5	6
8 3	9 4	10 1	7	10 1	9 4	8 3
L	L	L	L	R	R	R

```
while(l < r)
{
```

```
}
```

reverse
arr
⇒

3 4 1 7 10 9 8

O(n) ⇒ reverse(arr, L, r)

```
{
```

```
}
```

arr

0	1	2	3	4	5	6
8	9	10	7	1	4	3

* Home work : please do for same problem, clock wise

→ Notes

arr[6] = { 1,2,3,4,5,6 } and d=2



d=1 ==> 6,1,2,3,4,5 ✓

* d=2 ==> 5,6,1,2,3,4 [final output]



* Write an efficient program to find the sum of contiguous subarray within a one-dimensional array of numbers that has the largest sum.

Largest Subarray Sum Problem

(*)

-2	-3	4	-1	-2	1	5	-3
0	1	2	3	4	5	6	7

$$4 + (-1) + (-2) + 1 + 5 = 7$$

Maximum Contiguous Array Sum is 7

max_sum = 0 → here

Local_sum = 0

① B.F

{Unit - 2}

n → # of sub-Array's

Sum → ^{arr}

0	1	2
1	2	3

$$\frac{n(n+1)}{2} \Rightarrow O(n^2)$$

$$\hookrightarrow O(n^2) \times O(n)$$

⇒

1

2

3

 → length (1) O(n³)

1	2
---	---

2	3
---	---

 → length (2) (*)

1	2	3
---	---	---

 → length (3)

$$\frac{n(n+1)}{2}$$

$$n=3$$

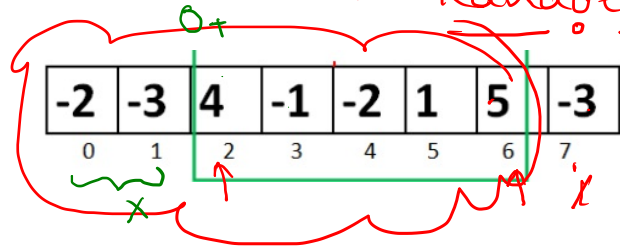
$$n=4$$

$$\begin{array}{r} 3 + 2 + 1 = 6 \\ \hline \checkmark 4 + \checkmark 3 + \checkmark 2 + \checkmark 1 = (10) \end{array}$$

Brute-Force

Kanade's Algo:

Int. Min Value



i
x

• SUM = -2 4 7 ✓

⇒ SUM

• curr_sum = 0 -2 0

-3 0 4 3 1 2 7 4

function fun(arr[], n)

{

sum = -infinity ✓ -∞

curr_sum = 0 ✓

for(i=0; i<n; i++)

{

curr_sum = curr_sum + arr[i] ✓

if(curr_sum > sum)

sum = curr_sum ✓

if(curr_sum < 0)

curr_sum = 0 ✓

}

return sum ✓

}

⑦

CS = 0
-2
L -3
-5
L

Search an element in row-wise, column-wise sorted

2D array

Input: `mat[4][4] = { {10, 20, 30, 40},
 {15, 25, 35, 45},
 {27, 29, 37, 48},
 {32, 33, 39, 50}};`

$\left. \begin{matrix} \text{ } \\ \text{ } \\ \text{ } \\ \text{ } \end{matrix} \right\} \text{matrix}$

$x = 29$

Output: Found at (2, 1)

Explanation: Element at (2,1) is 29

Input : `mat[4][4] = { {10, 20, 30, 40},
 {15, 25, 35, 45},
 {27, 29, 37, 48},
 {32, 33, 39, 50}};`

$x = 100$

Output : Element not found

Explanation: Element 100 is not found

$O(n \times m)$
 $+ O(1) \rightarrow ?$

	0	1	2	3
0	10	20	30	40
1	15	25	35	45
2	27	29	37	48
3	32	33	39	50

	0	1	2	3
0	10	20	30	40
1	15	25	35	45
2	27	29	37	48
3	32	33	39	50

$\frac{O(n*m)}{\rightarrow}$

$O(m+n)$

row
col } sorted

key = 29

$\rightarrow = / > / <$

arr[i][j] v/s key

key < arr[i][j]

j--

key > arr[i][j]

i++

key == arr[i][j]
return



```
search(int[][] mat,int n, int x)  
{
```

⇒ n x n

```
    int i = 0, j = n - 1;  
    while (i < n && j >= 0)  
    {  
        if (mat[i][j] == x)  
        {  
            print("element found"); ✓  
            return;  
        }  
        if (mat[i][j] > x)  
            j--; ✓  
        else  
            i++; ✓  
    }  
    print("element is not found");  
    return;  
}
```