



**BITS Pilani**  
Hyderabad Campus

# Database Management Systems

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# Lecture Session-10

## Schema Refinement-2

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### ***Content***

- ☐ *3 NF and BCNF*
- ☐ *Decomposition requirements*
- ☐ *Lossless join decomposition*
- ☐ *Dependency preserving decomposition*
- ☐ *Examples*

# Recap of 1NF and 2 NF

## 1. First Normal Form (1NF)

It states that the domain of any attribute must include only atomic (single / simple/ individual) values.

In the example given below, under the column *Dloc* each row has more than one values.

Ex.: Dept

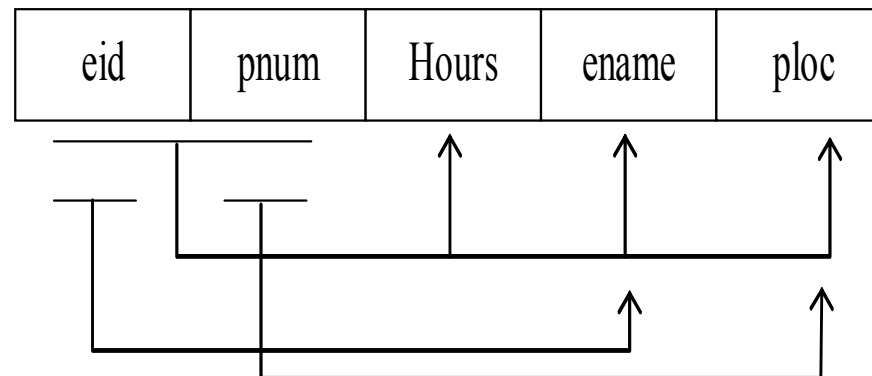
<i>DId</i>	<i>Dname</i>	<i>Dloc</i>
10	Engg	HYD CHENNAI
20	Mark	HYD MUMBAI

## 2. Second Normal Form (2NF)

It is based on *full functional dependency*.

$\{X \rightarrow A\}$  is fully functional if we remove any attribute from X then that FD does not hold anymore.

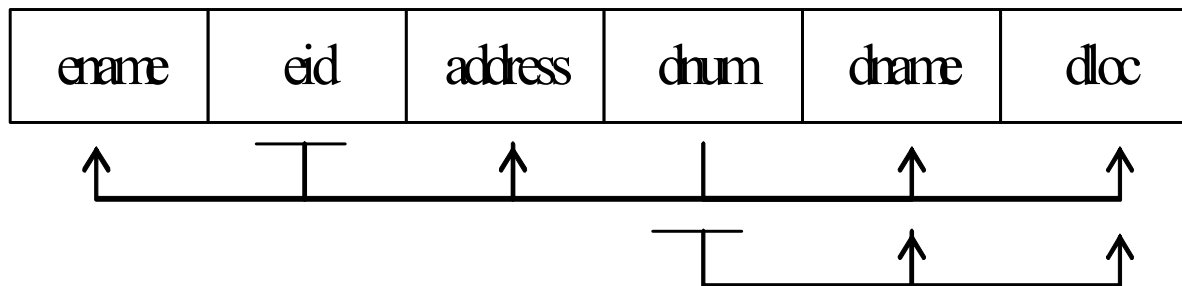
Condition for 2NF: All non-key attributes are fully functionally dependent on key (or) no non-key attribute should be dependent on part of key (partial dependency).



### 3. Third Normal form (3NF)

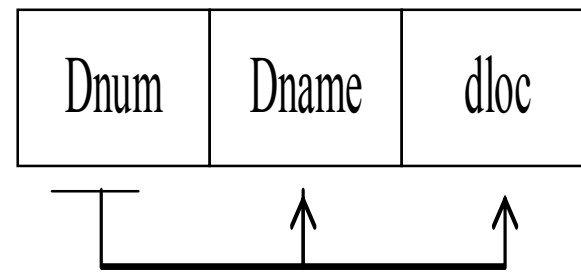
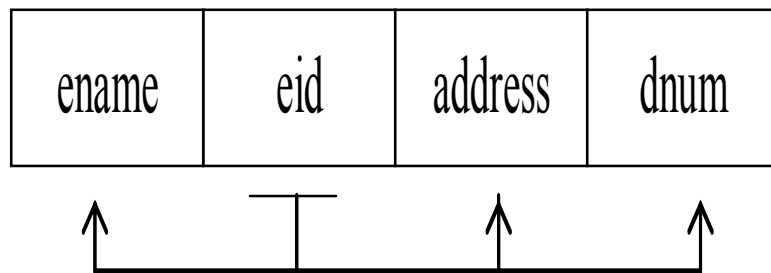
It is based on transitive dependency.

According to this, a relation should not have a non key attribute functionally determined by another non key attribute. i.e., there should be no transitive dependency.



Not in 3NF, because *Dname* is transitively dependent on *eid*.

Now we can decompose the above into 2 relations.



### Condition for 3NF

For each FD,  $X \rightarrow A$  in database

- i) X must be a superkey or
- ii) A is key attribute



## BCNF (Boyce Codd Normal Form)

It is a stricter form of 3NF

### Condition

For each FD  $X \rightarrow A$   
X must be a superkey

**4<sup>th</sup> NF:** Is based on multivalued dependency

**5<sup>th</sup> NF:** Is based on join dependency normally database designers go up to 3NF only, and 4NF & 5NF are beyond the scope of our discussion.

# Decomposition and Desirable properties

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As we have seen, decomposition (of a bigger relation  $R$  into smaller ones), is a major step in the process of normalization.

But during this activity of decomposition, we need to make sure that the decomposition is *lossless* and *dependency preserving*





# Loss-less join Decomposition

Let  $C$  represent a set of constraints on the database. A decomposition  $\{R_1, R_2, R_3, \dots, R_n\}$  of a relation schema  $R$  is a lossless join decomposition for  $R$  if all relation instances  $r$  on  $R$  that are legal under  $C$ .

$$r = \Pi_{R_1}(r) \ * \ \Pi_{R_2}(r) \ * \ \dots \ * \ \Pi_{R_n}(r)$$

$\Pi_{R_1}(r)$  = projection of  $r$  on  $R_1$

$r$  – relation instance in  $R$

$F$  = FDs on  $R$

(or)  $\{R\} \rightarrow \{R_1, R_2\}$

# Test for Lossless join property

(a)  $R = \{SSN, ENAME, PNUMBER, PNAME, PLOCATION, HOURS\}$   $D = \{R_1, R_2\}$

$R_1 = EMP\_LOCS = \{ENAME, PLOCATION\}$

$R_2 = EMP\_PROJ1 = \{SSN, PNUMBER, HOURS, PNAME, PLOCATION\}$

$F = \{SSN \rightarrow ENAME; PNUMBER \rightarrow \{PNAME, PLOCATION\}; \{SSN, PNUMBER\} \rightarrow HOURS\}$

	SSN	ENAME	PNUMBER	PNAME	PLOCATION	HOURS
$R_1$	$b_{11}$	$a_2$	$b_{13}$	$b_{14}$	$a_5$	$b_{16}$
$R_2$	$a_1$	$b_{22}$	$a_3$	$a_4$	$a_5$	$a_6$

(no changes to matrix after applying functional dependencies)

- (c)  $R = \{SSN, ENAME, PNUMBER, PNAME, PLOCATION, HOURS\}$   $D = \{R_1, R_2, R_3\}$   
 $R_1 = EMP = \{SSN, ENAME\}$   
 $R_2 = PROJ = \{PNUMBER, PNAME, PLOCATION\}$   
 $R_3 = WORKS\_ON = \{SSN, PNUMBER, HOURS\}$

$F = \{SSN \rightarrow \{ENAME, PNUMBER\}; PNUMBER \rightarrow \{PNAME, PLOCATION\}; \{SSN, PNUMBER\} \rightarrow HOURS\}$

	SSN	ENAME	PNUMBER	PNAME	PLOCATION	HOURS
$R_1$	$a_1$	$a_2$	$b_{13}$	$b_{14}$	$b_{15}$	$b_{16}$
$R_2$	$b_{21}$	$b_{22}$	$a_3$	$a_4$	$a_5$	$b_{26}$
$R_3$	$a_1$	$b_{32}$	$a_3$	$b_{34}$	$b_{35}$	$a_6$

(original matrix S at start of algorithm)

	SSN	ENAME	PNUMBER	PNAME	PLOCATION	HOURS
$R_1$	$a_1$	$a_2$	$b_{13}$	$b_{14}$	$b_{15}$	$b_{16}$
$R_2$	$b_{21}$	$b_{22}$	$a_3$	$a_4$	$a_5$	$b_{26}$
$R_3$	$a_1$	<del><math>b_{32}</math></del> $a_2$	$a_3$	<del><math>b_{34}</math></del> $a_4$	<del><math>b_{35}</math></del> $a_5$	$a_6$

(matrix S after applying the first two functional dependencies - last row is all "a" symbols, so we stop)

# Dependency Preserving Decomposition

Given a set of dependencies  $F$  on  $R$ , the projection of  $F$  on  $R_i$  denoted by

(where  $R_i$  is a subset of  $R$ ); is the set of FDs  $X \rightarrow Y$  in  $F^+$  such that the attributes in  $X \cup Y$  are contained in  $R_i$ .

$$\left( \Pi_{R_1}(F) \cup \Pi_{R_2}(F) \cup \dots, \Pi_{R_m}(F) \right)^+ = F^+$$

Then it is dependency preserving decomposition.

$\Pi_{R_1}(f)$  - is projection of  $F$  on  $R_1$ .



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This dependency preserving condition makes sure that no FD in original relation is lost as a result of decomposition. The FDs represent constraints (business logic).

**Note:**

- Not every BCNF is dependency preserving
- Limited amount of redundancy in 3NF in the form of transitive dependency is better than losing FDs as result of bringing 3NF to BCNF.



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## ***Summary***

- ✓ *Recap of 2NF*
- ✓ *What is 3NF and BCNF*
- ✓ *Decomposition into 3NF and BCNF*
- ✓ *Lossless join decomposition*
- ✓ *Dependency preserving decomposition*