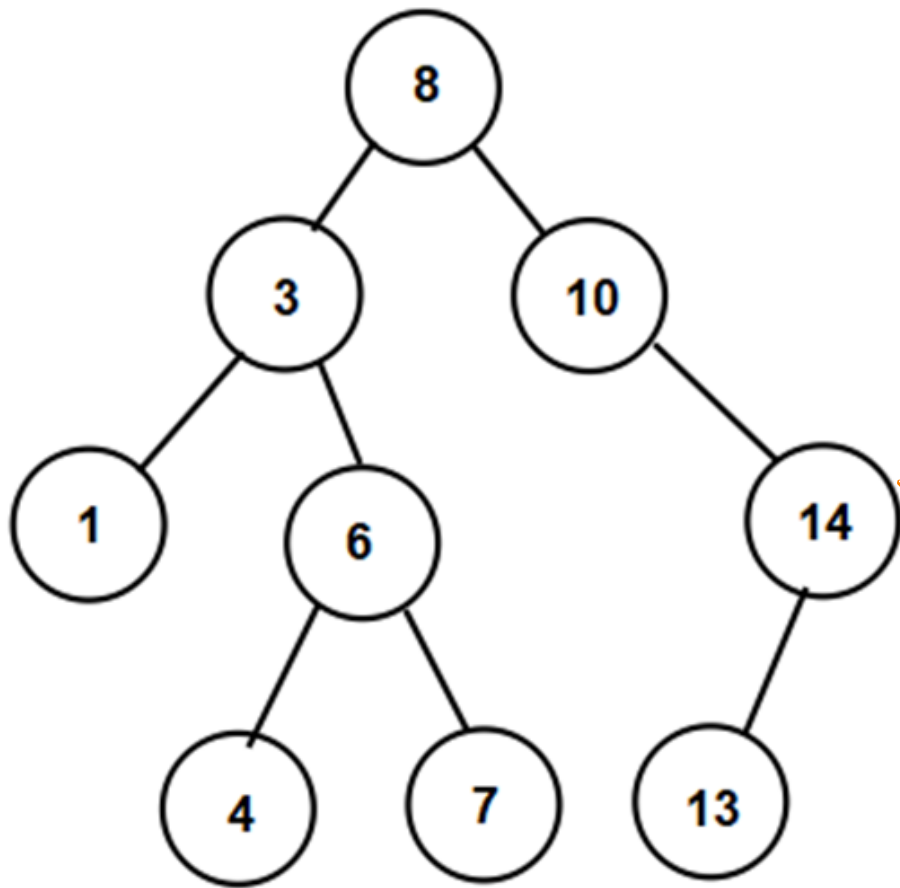
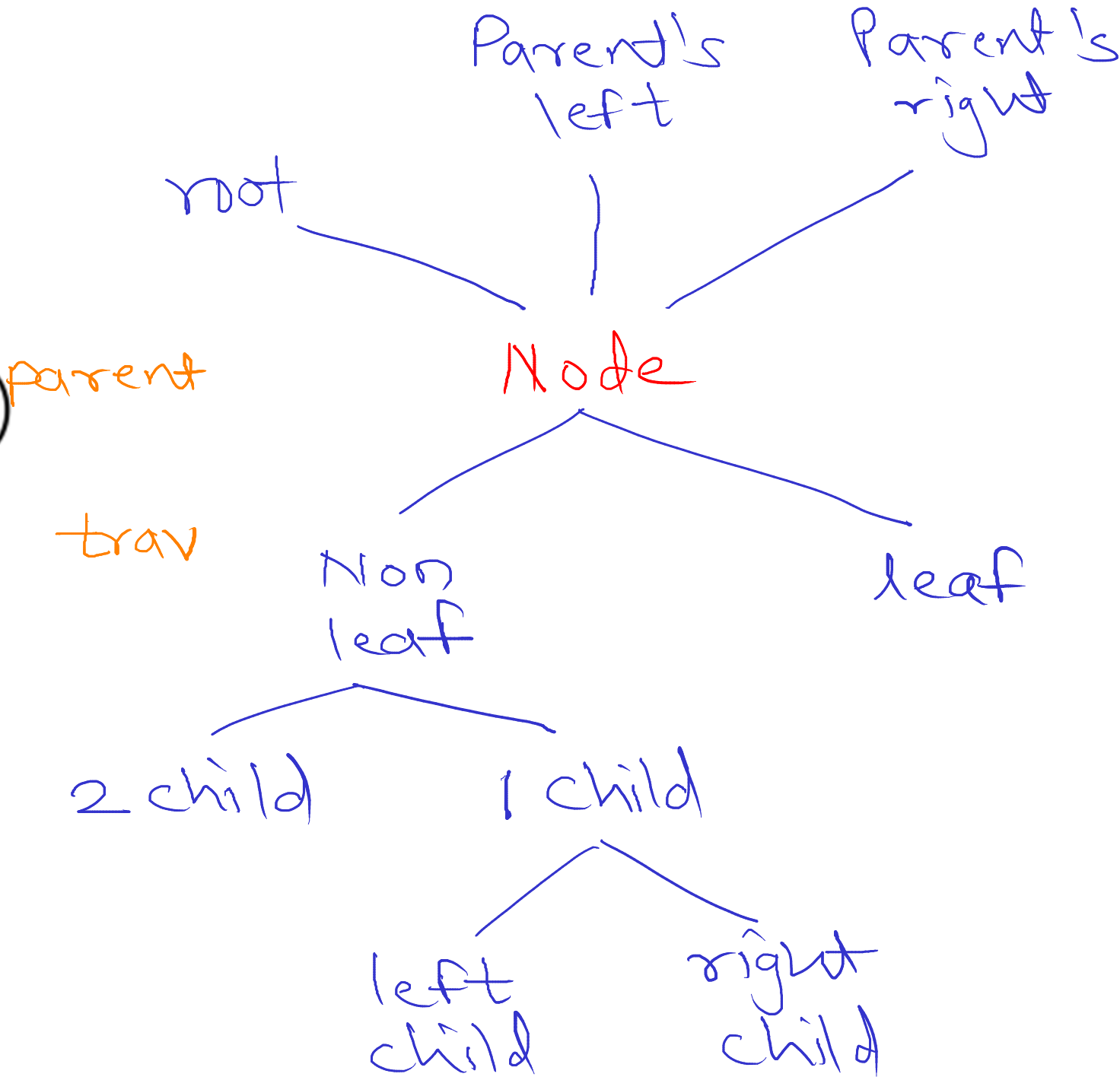


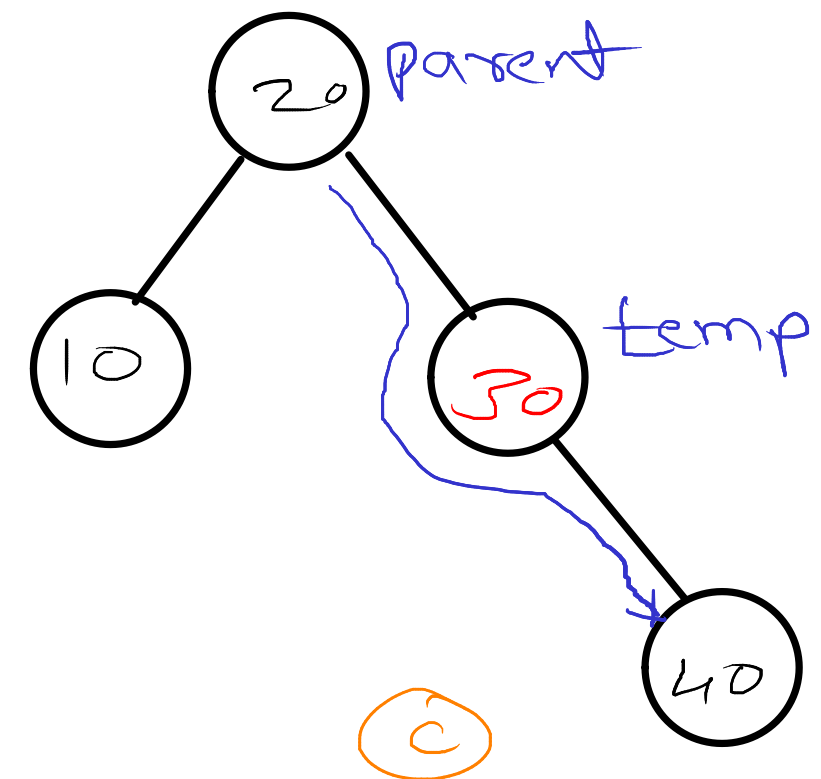
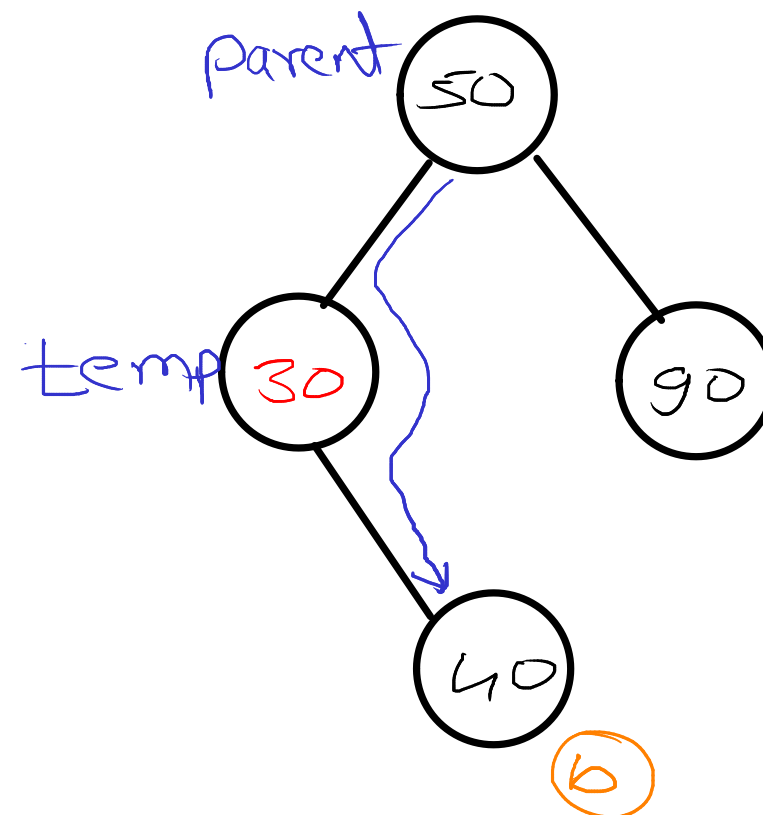
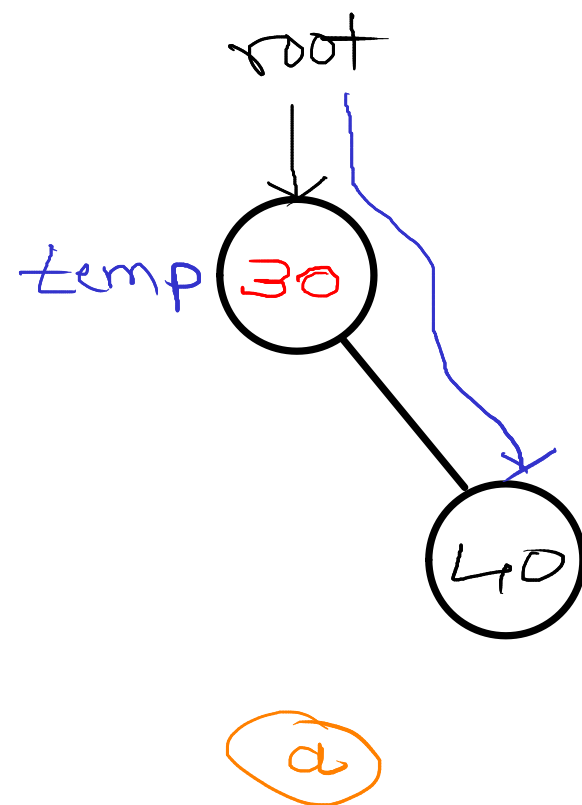
BST - Delete Node



Key = 4

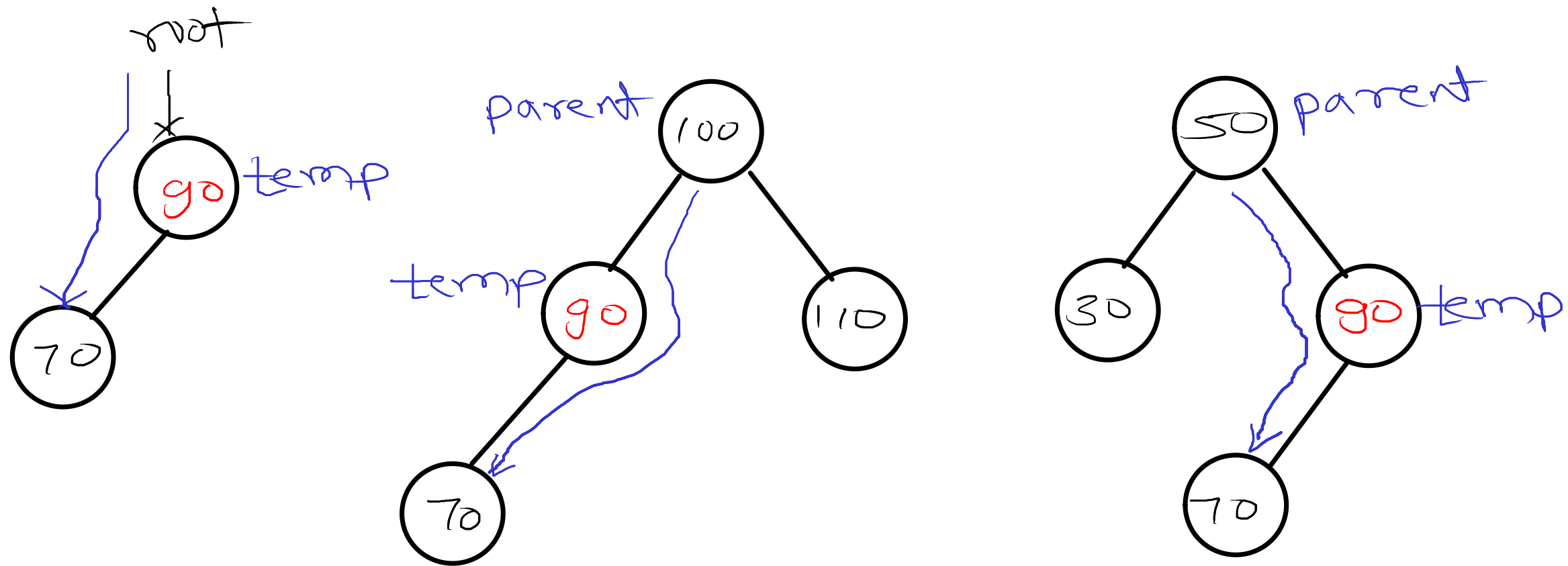


BST - Delete node which has single child (right child)



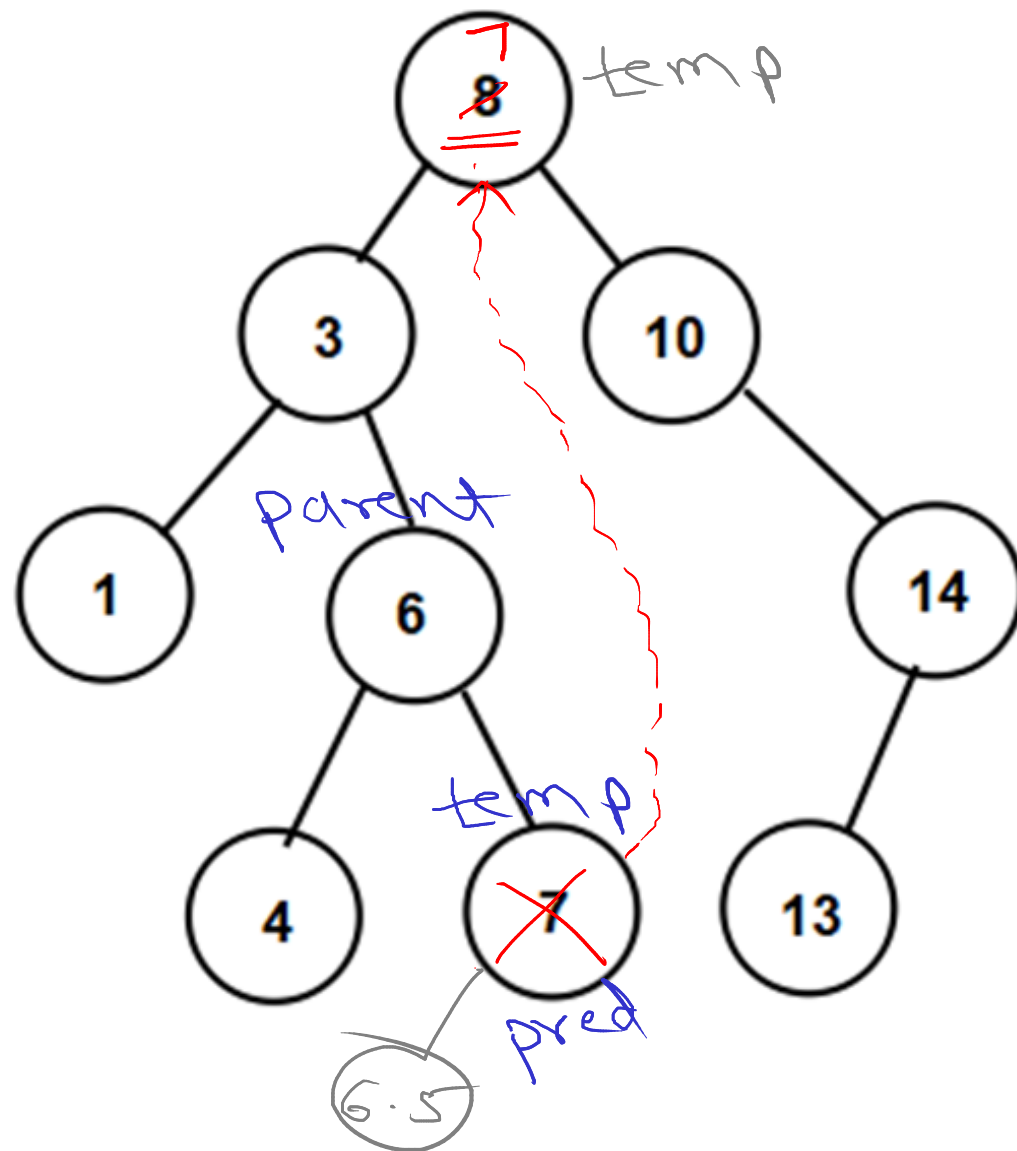
```
if(temp.left == null){  
    if(temp == root)           // root node  
        a    root = temp.right;  
    else if(temp == parent.left) // parent's left child  
        b    parent.left = temp.right;  
    else // if(temp == parent.right) // parent's right child  
        c    parent.right = temp.right;  
}
```

BST - Delete node which has single child (left child)



```
if(temp.right == null){  
    if(temp == root)                // root node  
        root = temp.left;  
    else if(temp == parent.left)    // parent's left child  
        parent.left = temp.left;  
    else // if(temp == parent.right) // parent's right child  
        parent.right = temp.left;  
}
```

BST - Delete node which has two childs



```
if(temp.left != null && temp.right != null){  
    //1. find predecessor with its parent  
    Node pred = temp.left;  
    parent = temp;  
    while(pred.right != null){  
        parent = pred;  
        pred = pred.right;  
    }  
    //2. replace data of temp by data of pred  
    temp.data = pred.data;  
    //3. mark pred for deletion  
    temp = pred;  
}
```

Inorder traversal :

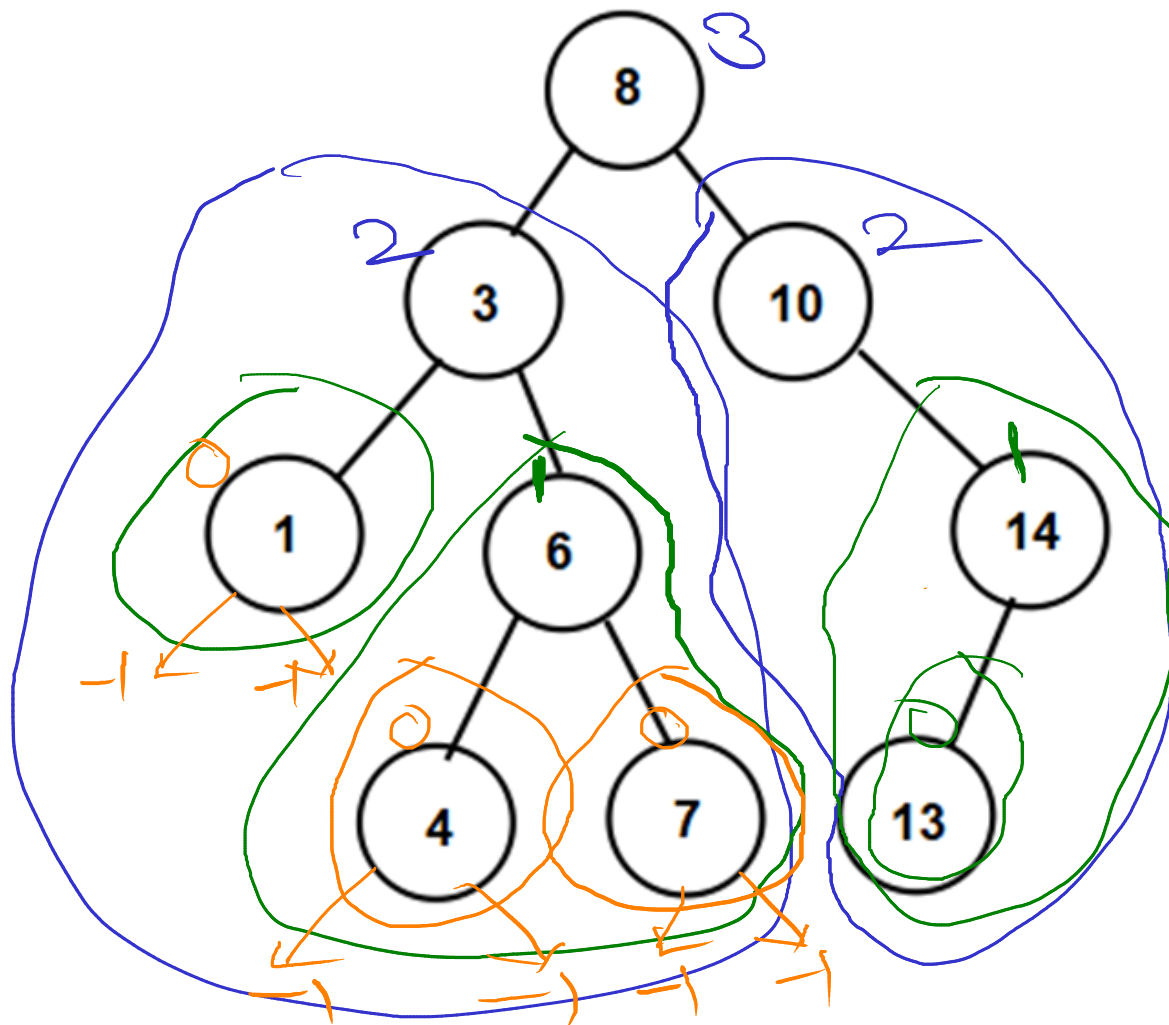
1 3 4 6 7 8 10 13 14

inorder
predecessor
left
extreme right

inorder
successor
right
extreme left

BST - Height

Height of tree = MAX(Height(left sub tree), Height(right sub tree)) + 1



//0. if left or right sub tree is absent

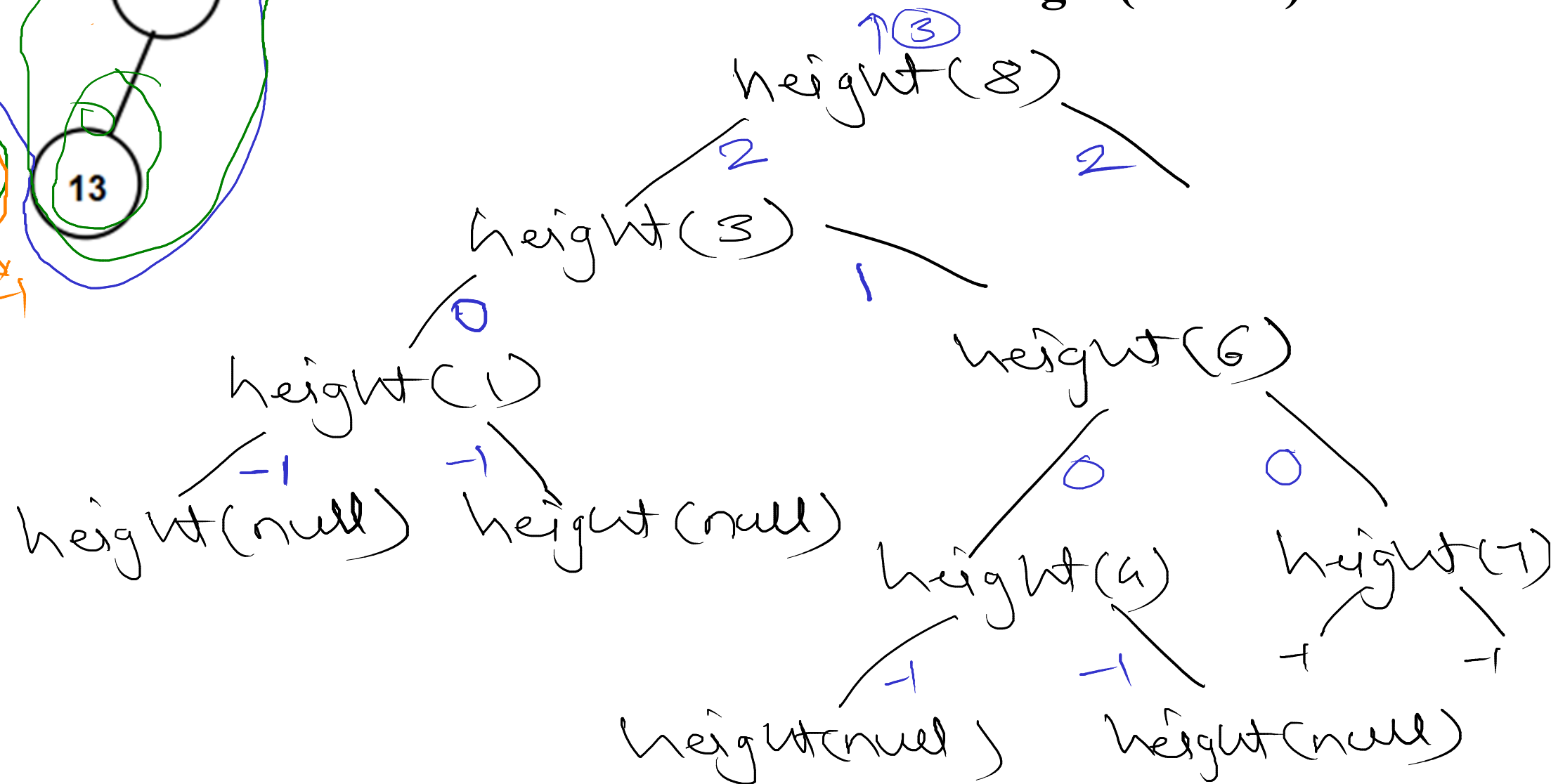
//then return -1

//1. find height of left subtree

//2. find height of right subtree

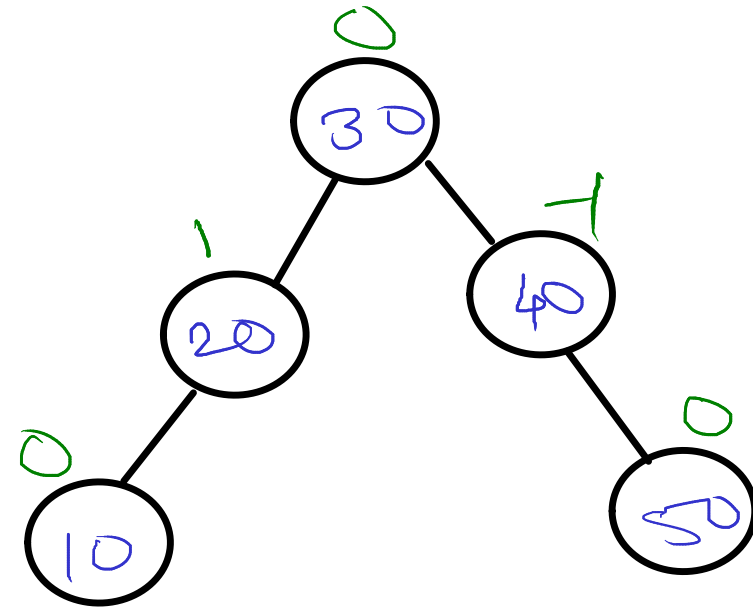
//3. find max height

//4. add one into max height(return)



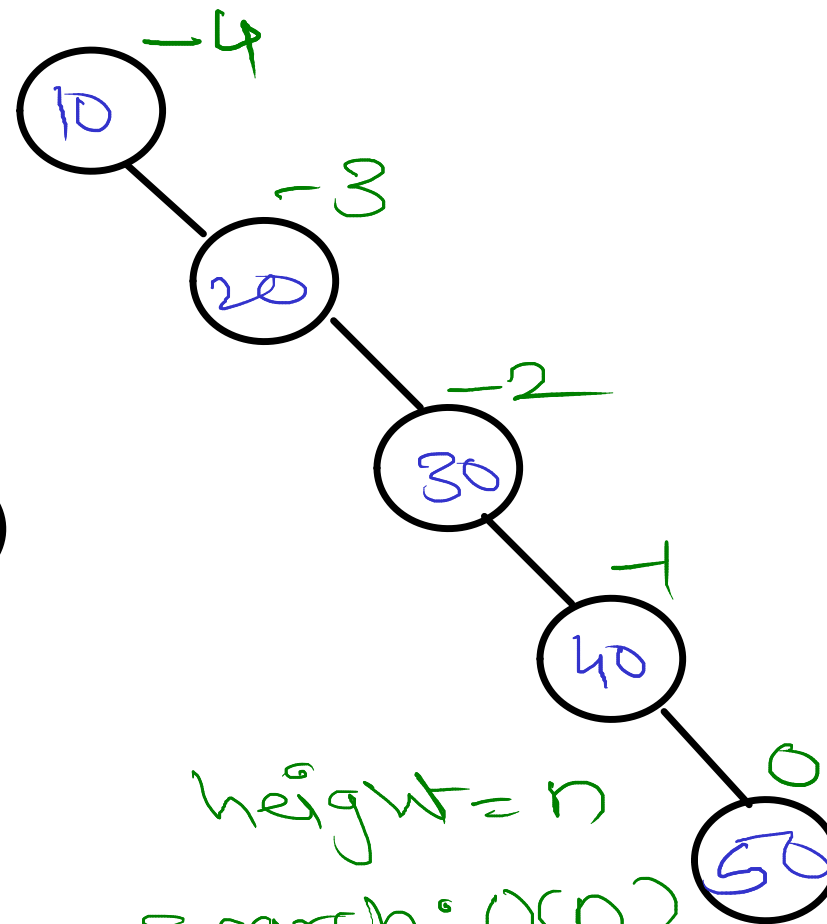
Skewed BST

Keys : 30, 40, 20, 50, 10



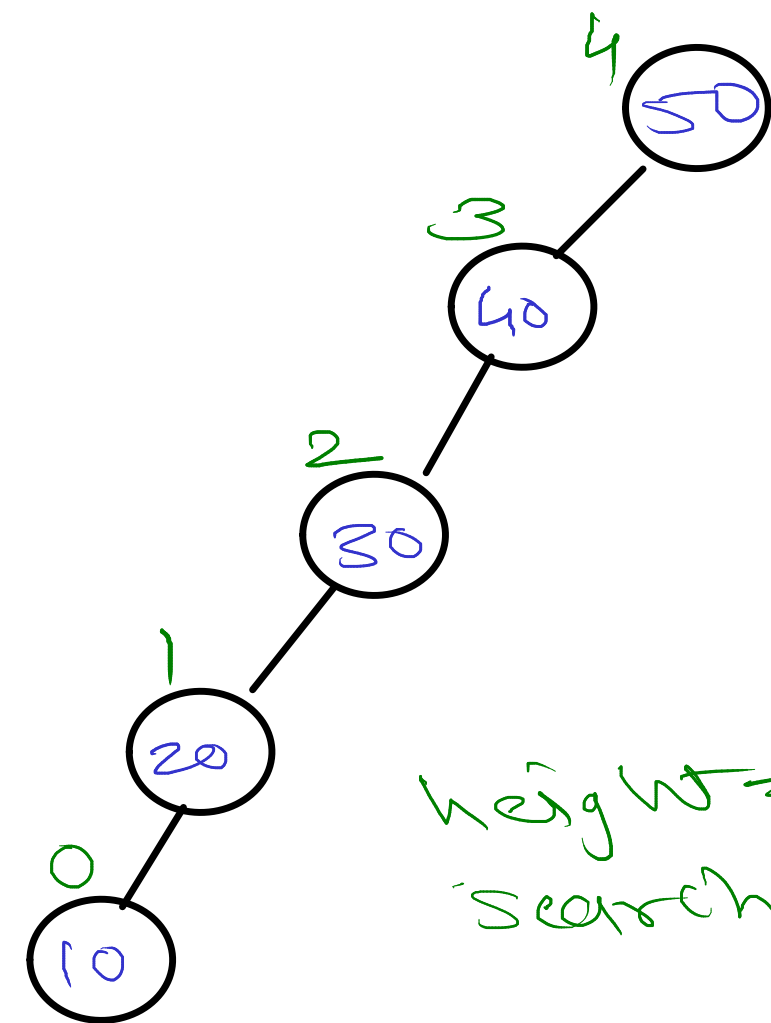
height = $\log n$
search : $O(\log n)$

Keys : 10, 20, 30, 40, 50



height = n
search : $O(n)$

Key : 50, 40, 30, 20, 10



height = n
search : $O(n)$

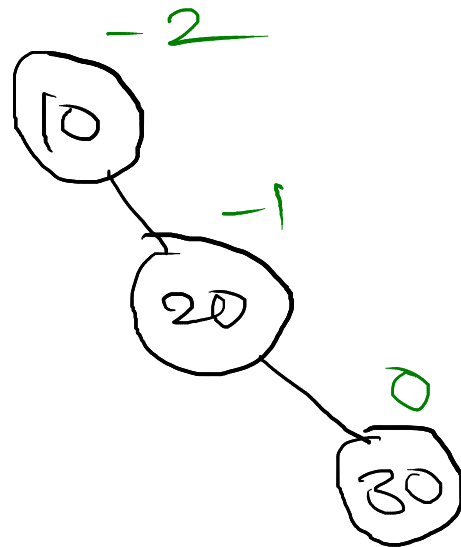
- if tree is growing in only one direction, it is called as skewed BST.
- if tree is growing in only right direction, it is called as right skewed BST.
- if tree is growing in only left direction, it is called as left skewed BST.

Balanced BST

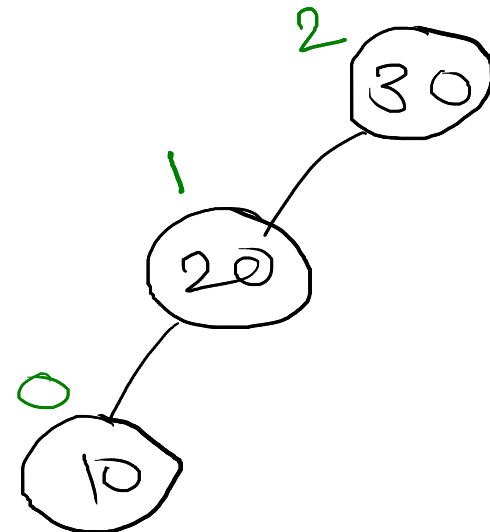
$$\text{Balance Factor} = \text{height}(\text{left sub tree}) - \text{height}(\text{right sub tree})$$

- tree is balanced if balance factor of all the nodes is either -1, 0 or +1
- balance factor = {-1, 0, +1}

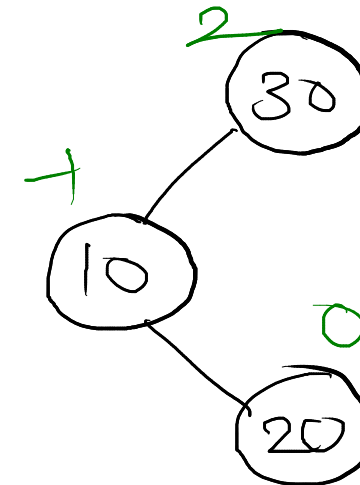
Keys : 10, 20, 30



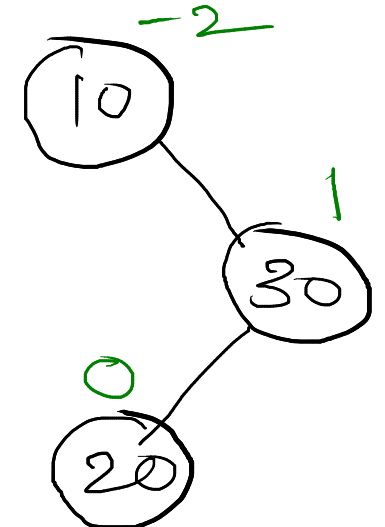
Keys : 30, 20, 10



Keys : 30, 10, 20

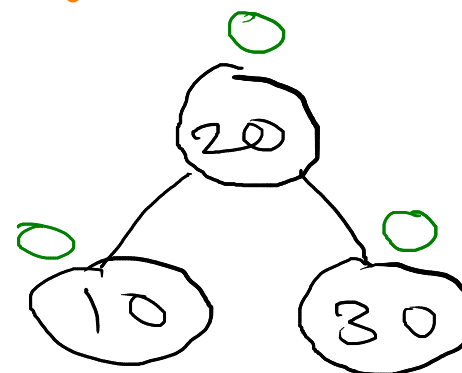


Keys : 10, 30, 20



Keys : 20, 10, 30

Keys : 20, 30, 10

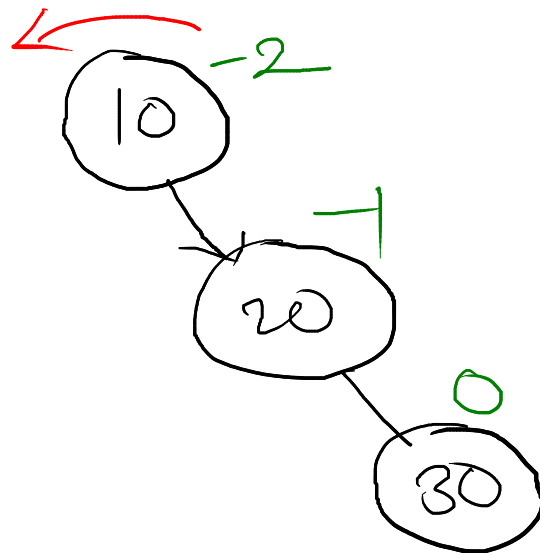


Balanced BST

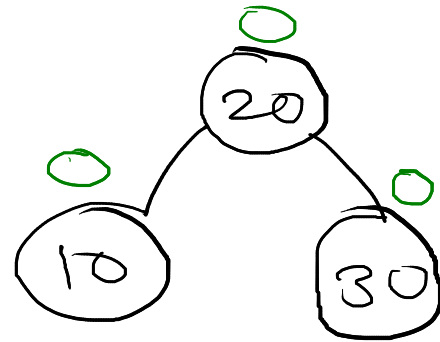
Rotations

RR Imbalance

Keys : 10, 20, 30

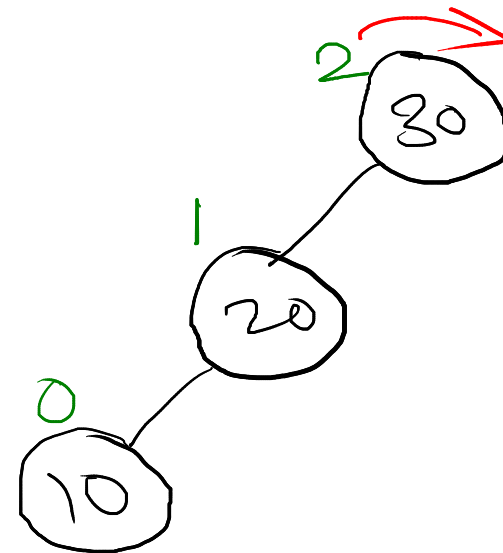


Left Rotation

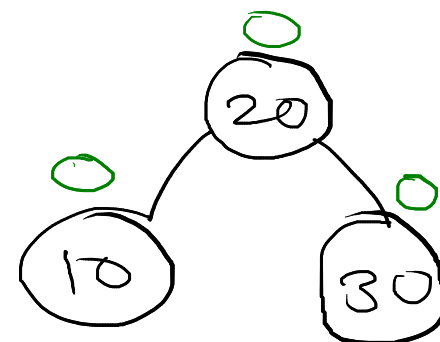


LL Imbalance

Keys : 30, 20, 10

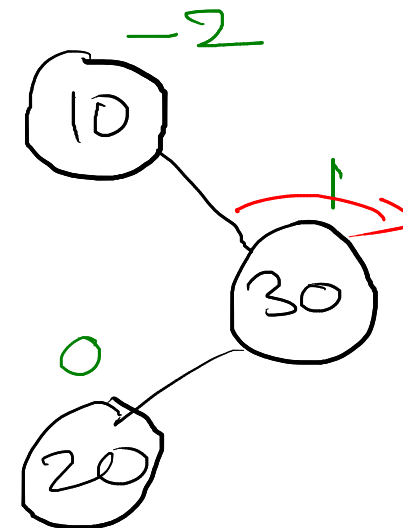


Right Rotation

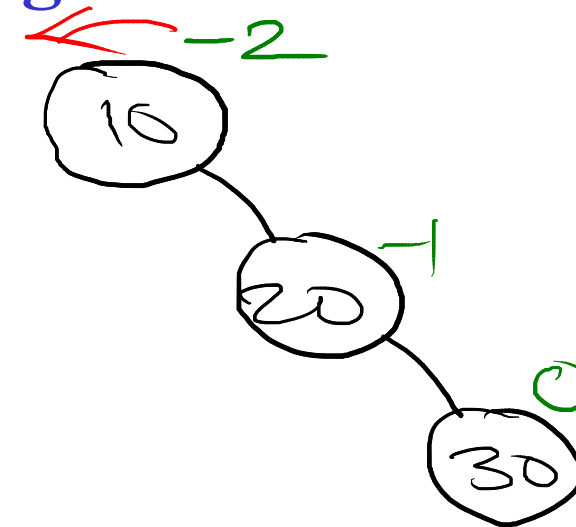


RL Imbalance

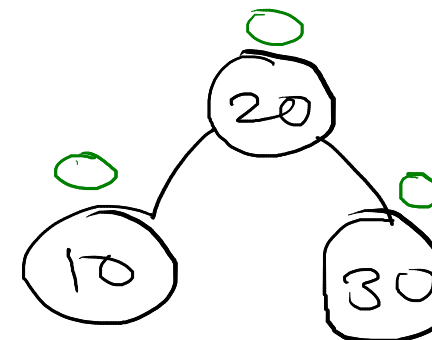
Keys : 10, 30, 20



Right Rotation

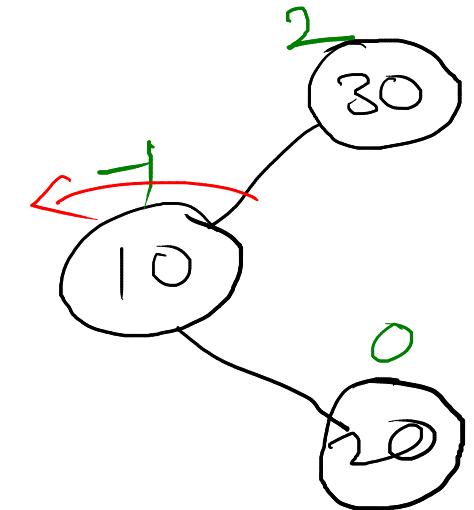


Left Rotation

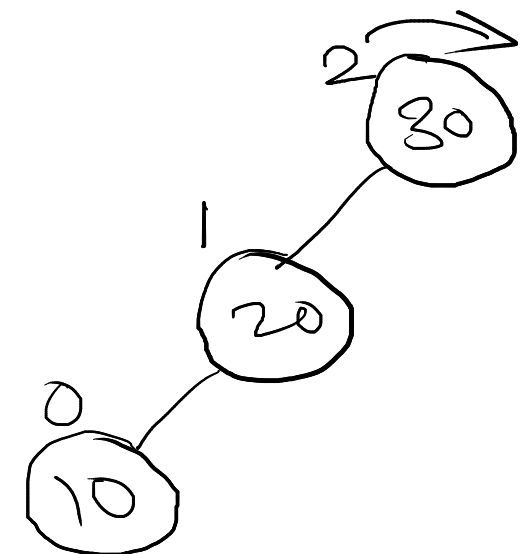


LR Imbalance

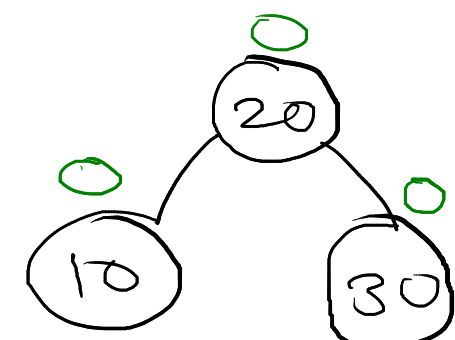
Keys : 30, 10, 20



Left Rotation



Right Rotation

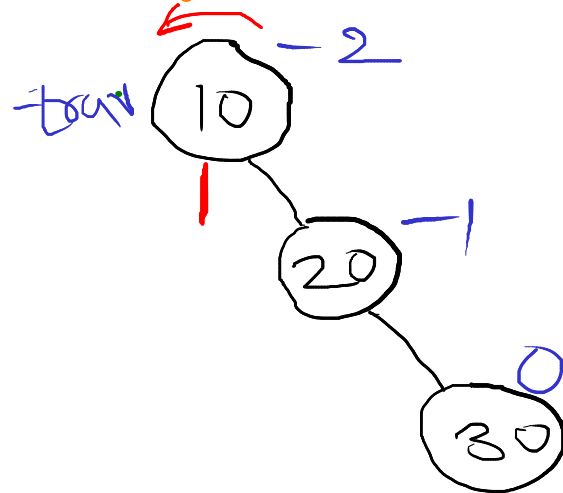


Single Roatation

Double Rotations

RR Imbalance

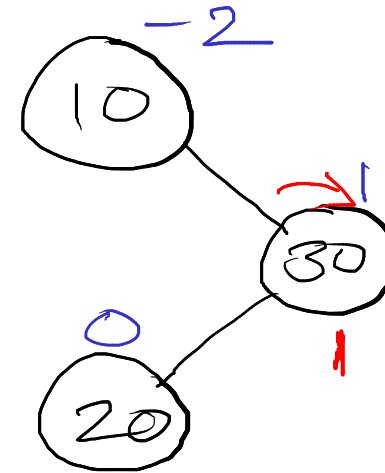
Keys : 10, 20, 30



bf < -1 §§
val > trav.right.data

RL Imbalance

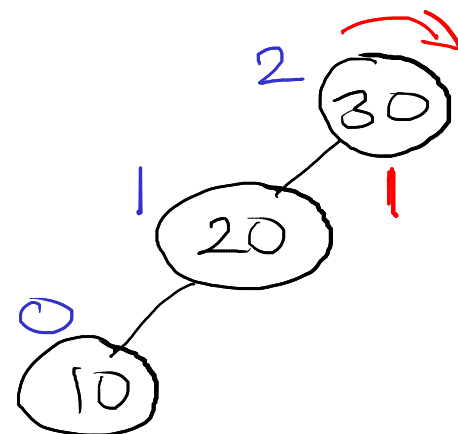
Keys : 10, 30, 20



bf < -1 §§
val < trav.right.data

LL Imbalance

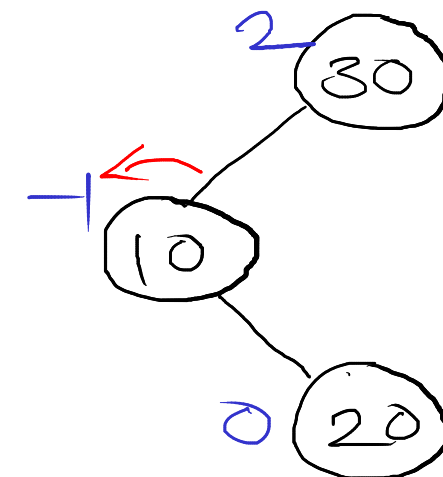
Keys : 30, 20, 10



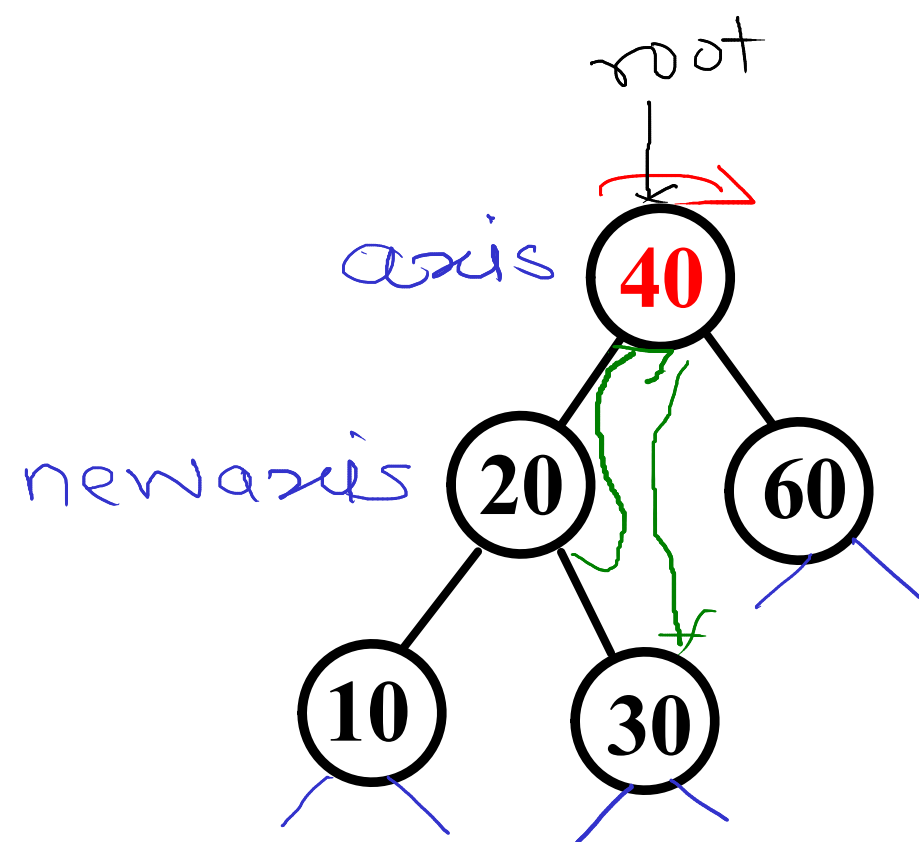
bf > 1 §§
val < trav.left.data

LR Imbalance

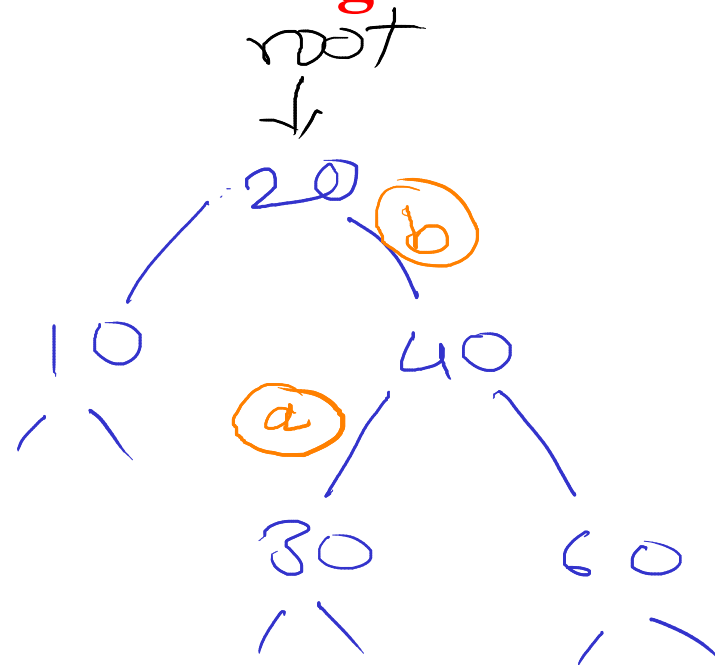
Keys : 30, 10, 20



bf > 1 §§
val > trav.left.data

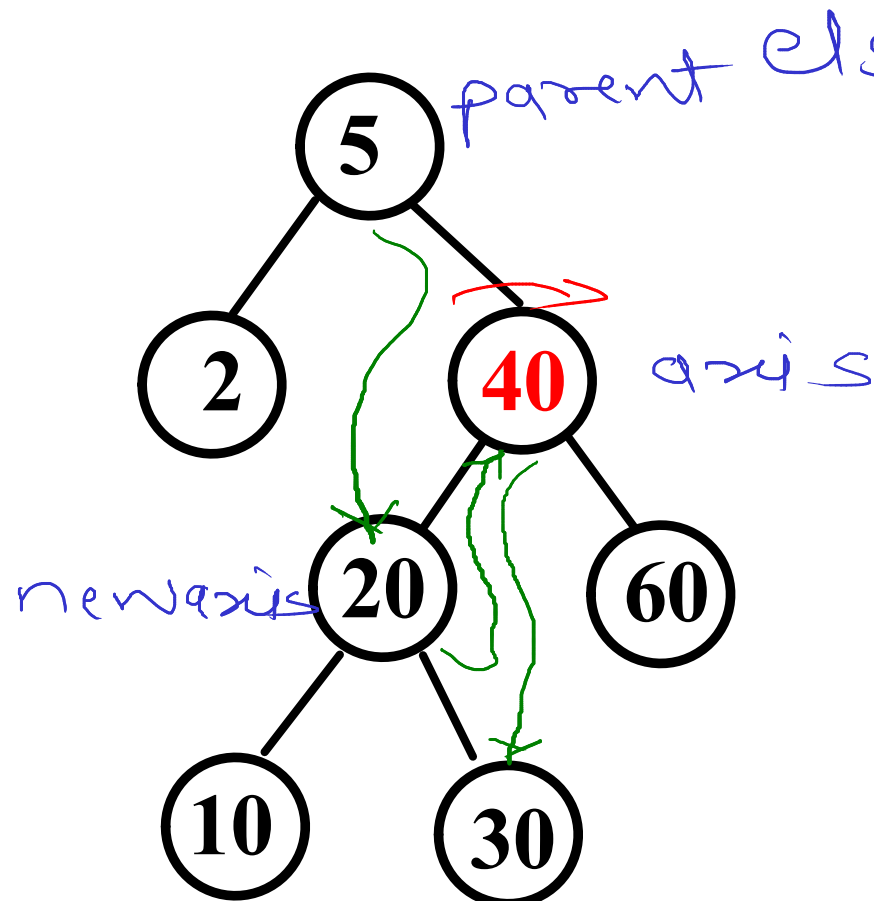
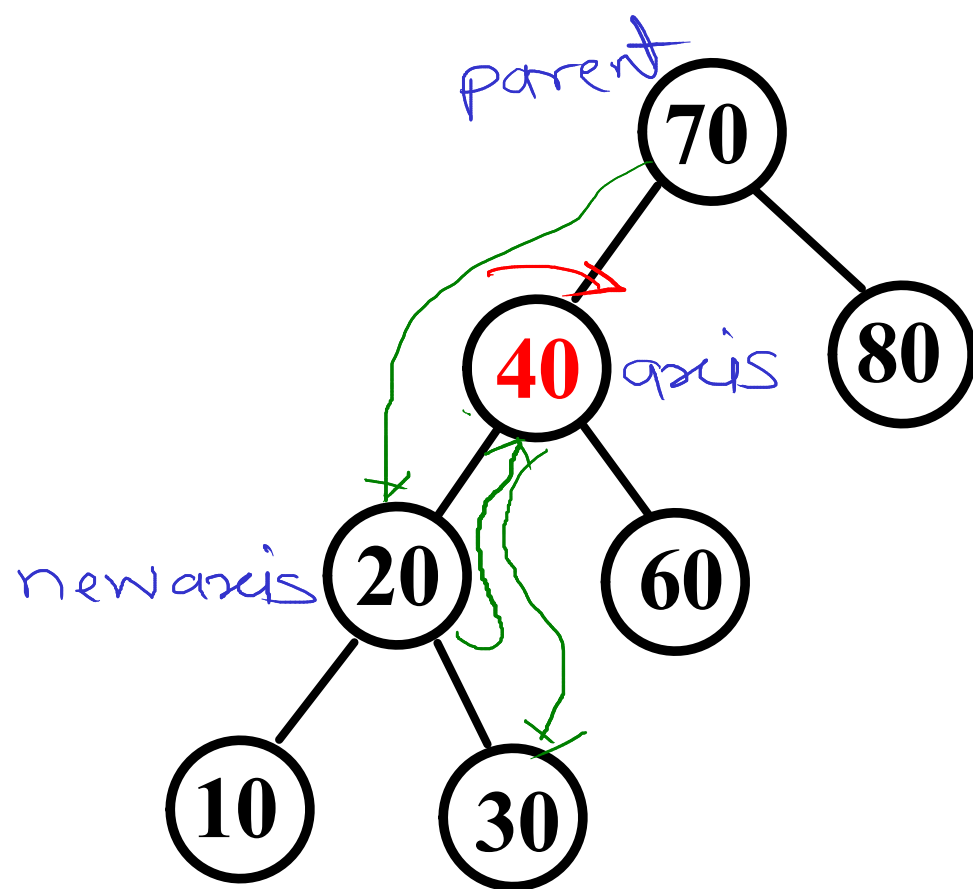


Right Rotation

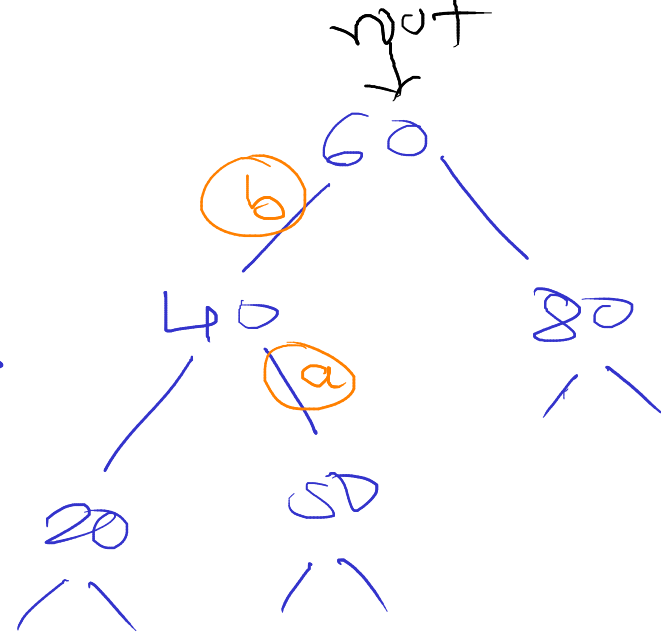
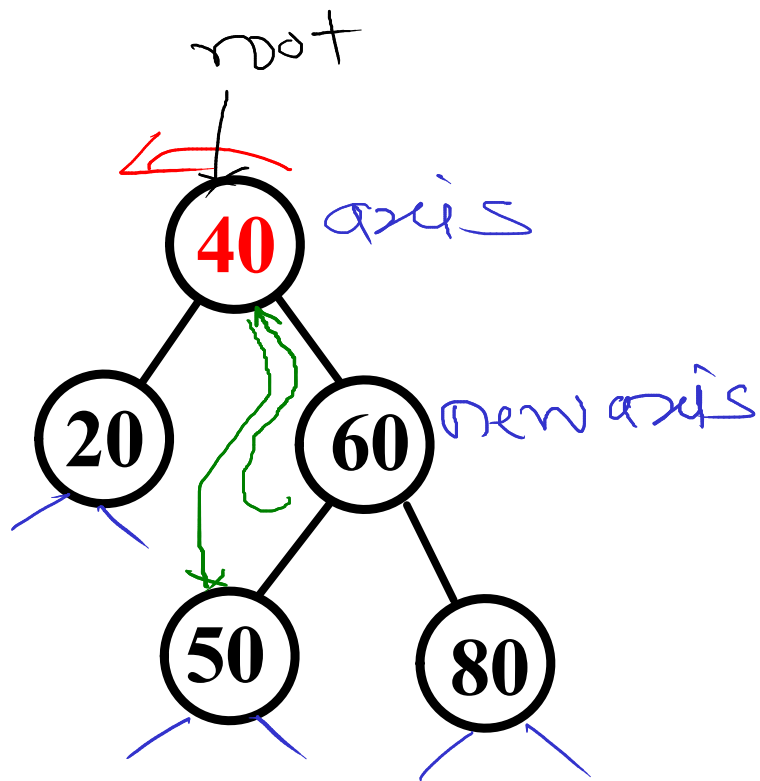


```

newaxis = axis.left;
a axis.left = newaxis.right;
b newaxis.right = axis;
if (axis == root)
    root = newaxis;
else if (axis == parent.left)
    parent.left = newaxis;
else if (axis == parent.right)
    parent.right = newaxis;
  
```

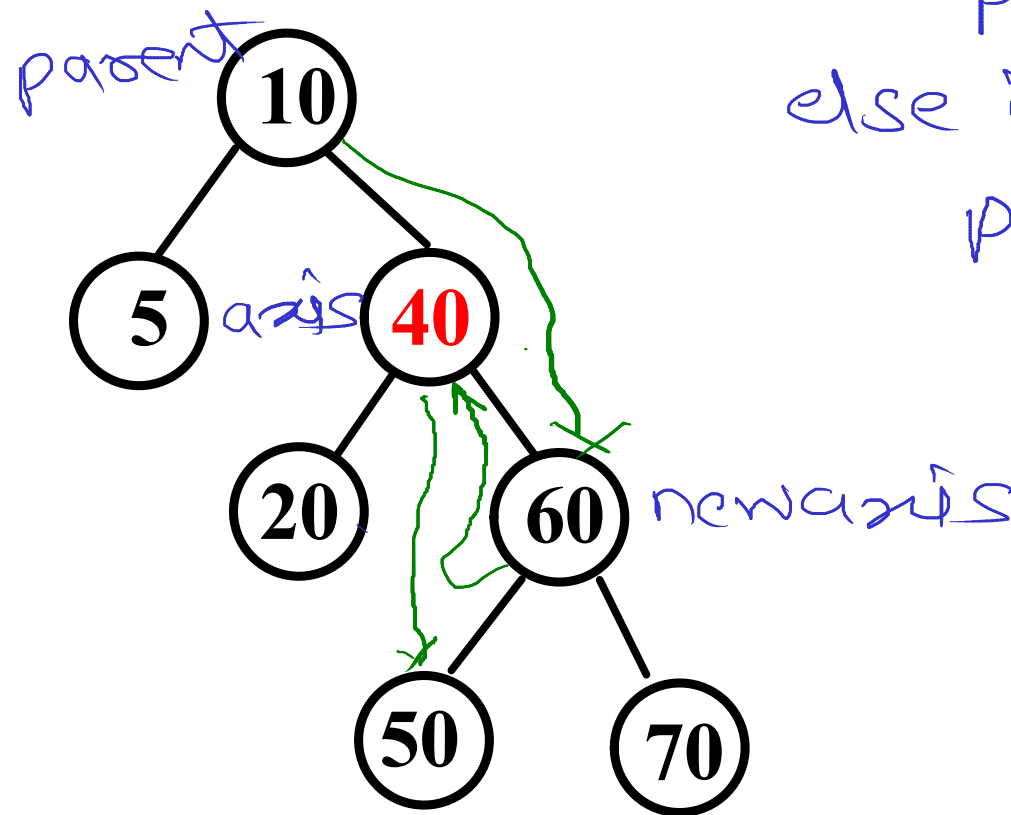
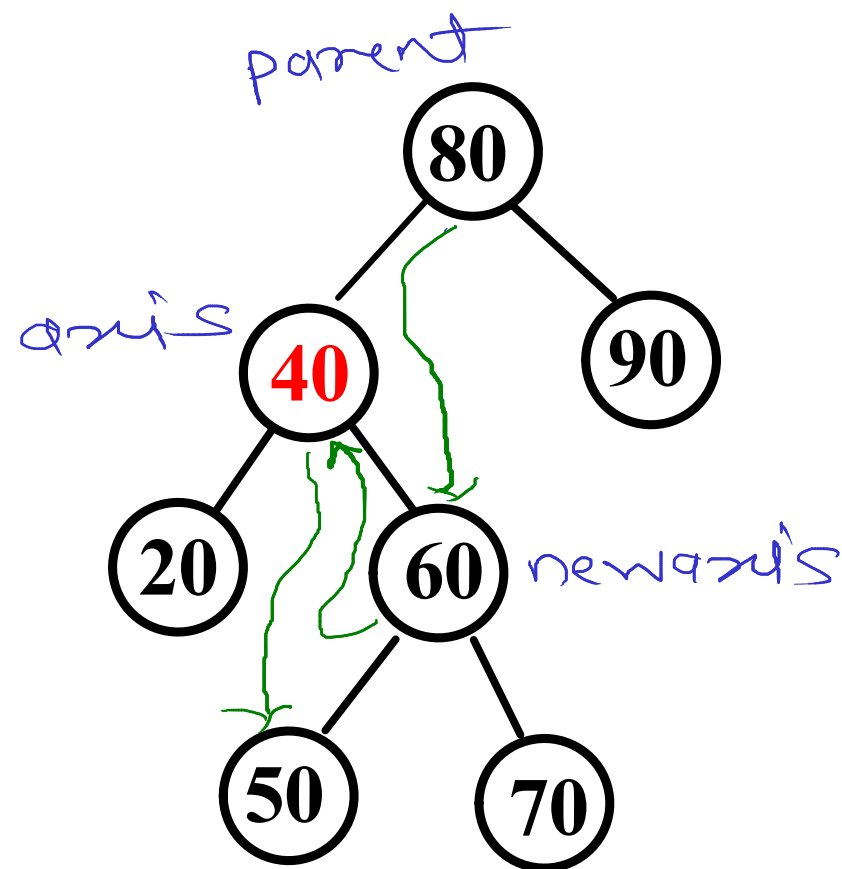


Left Rotation



```

newaxis = axis.right
a axis.right = newaxis.left
b newaxis.left = axis
if (axis == root)
    root = newaxis;
else if (axis == parent.left)
    parent.left = newaxis;
else if (axis == parent.right)
    parent.right = newaxis;
    
```



AVL Tree

- Self balancing binary Search Tree
- on every insertion and deletion of node, tree is balanced
- All operation on AVL tree are performed in $O(\log n)$ time
- Balance factor of all nodes is either -1, 0 or +1

Keys : 40, 20, 10, 25, 30, 22, 50

