

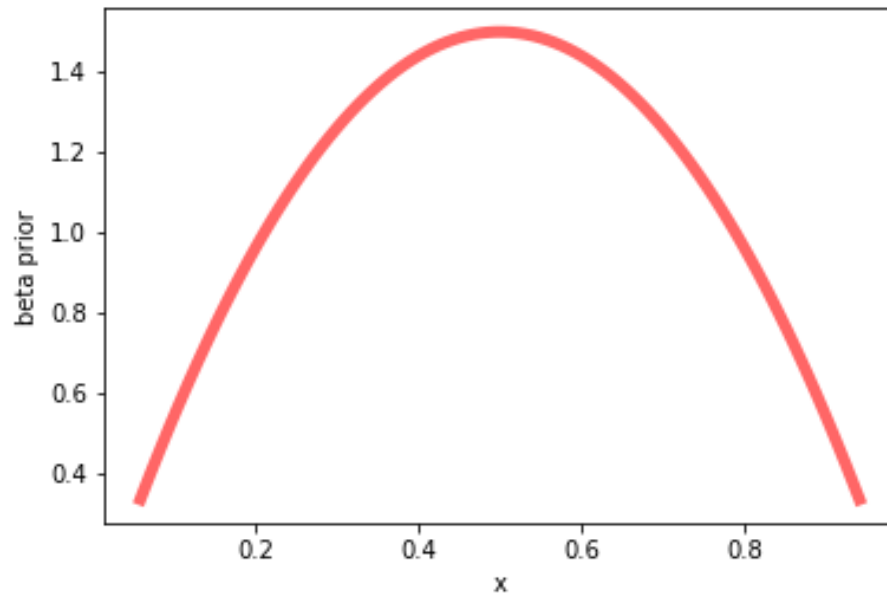
CISC 863 Quiz -1

Submitted by: Sagar Kukreja

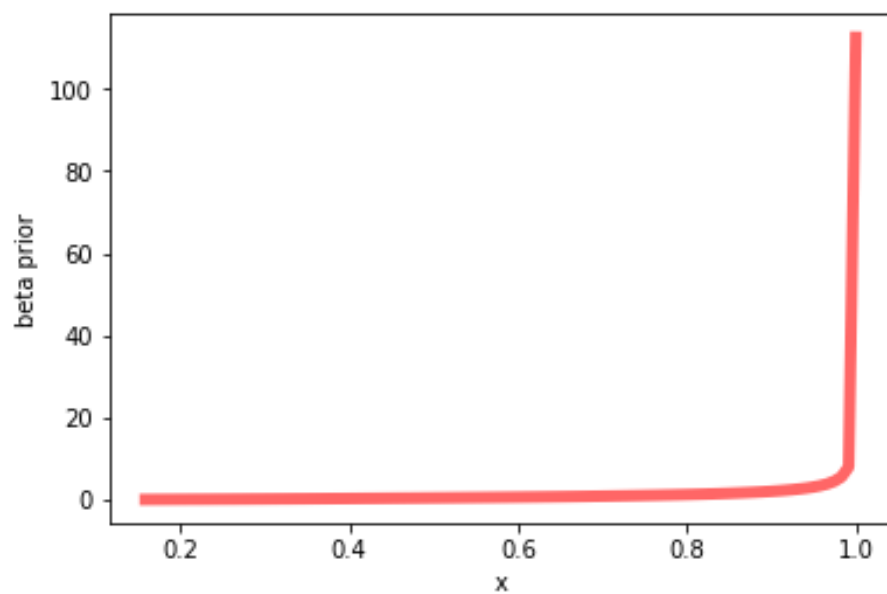
1) Beta Prior Distribution

Initially we assume coin to be fair and hence we take a and b to be same and hence, we get a peak at 0.5

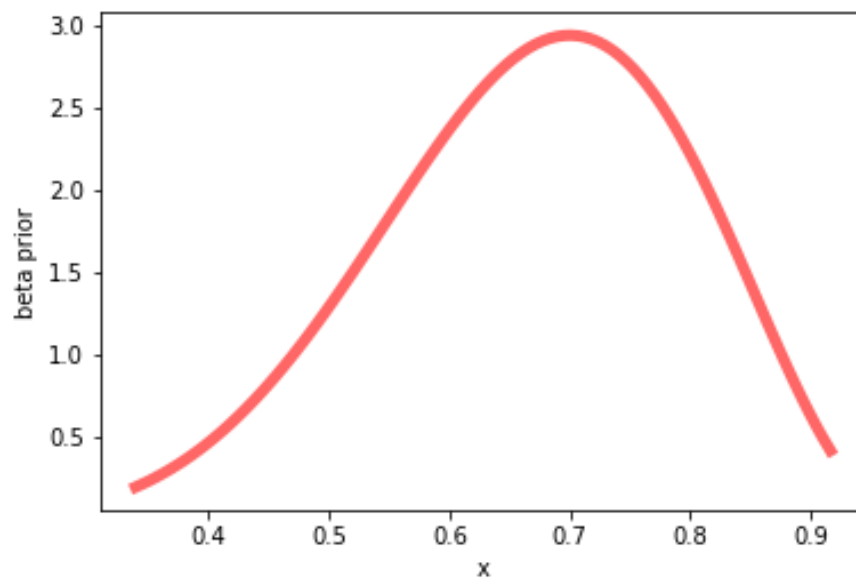
Beta(2,2)



Beta (2, 0.5)

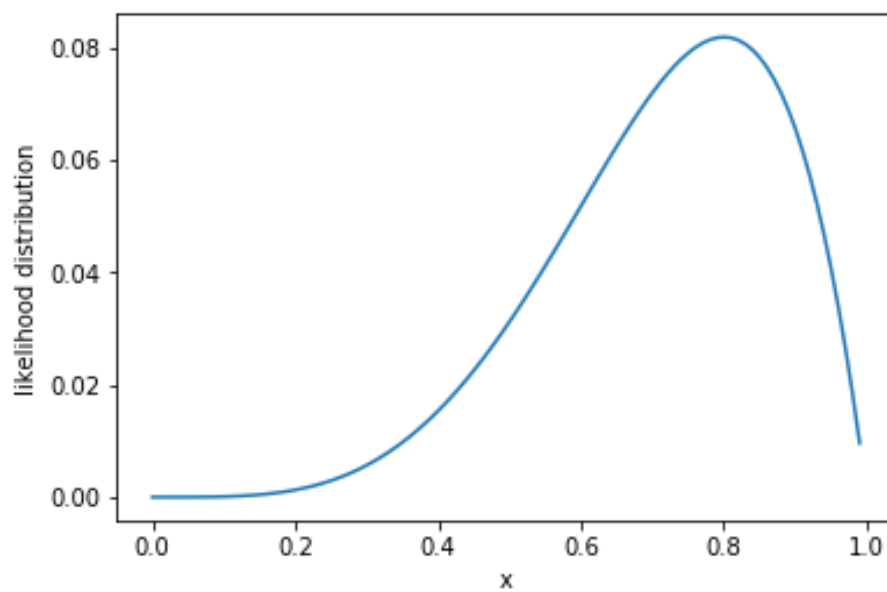


Beta(8,4)

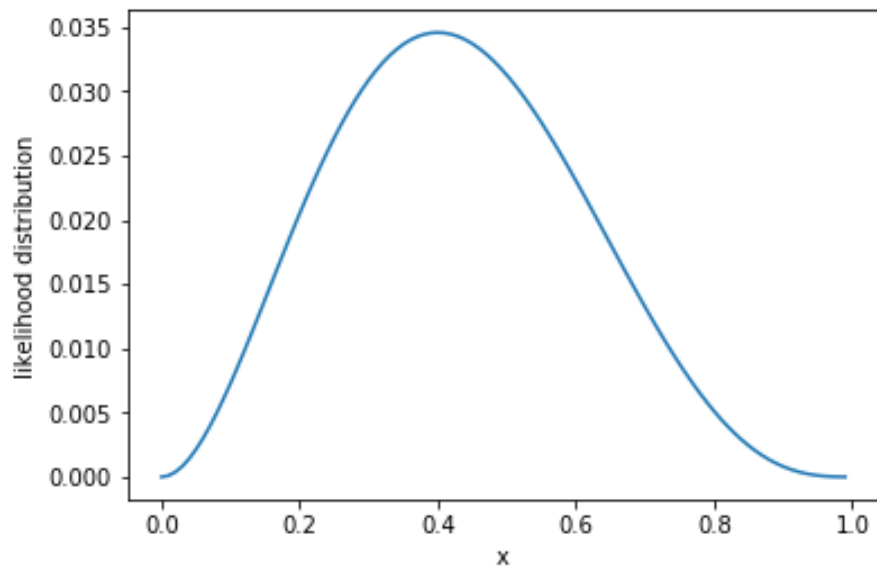


2) Bernoulli Likelihood
 $\text{Ber}(\text{'HHTHH'} \mid \theta)$

But when we calculate the distribution from $N=5$ trials, we observe that the coin is biased and hence the peak favors occurrence of head.



Ber('HHTTT'| θ)

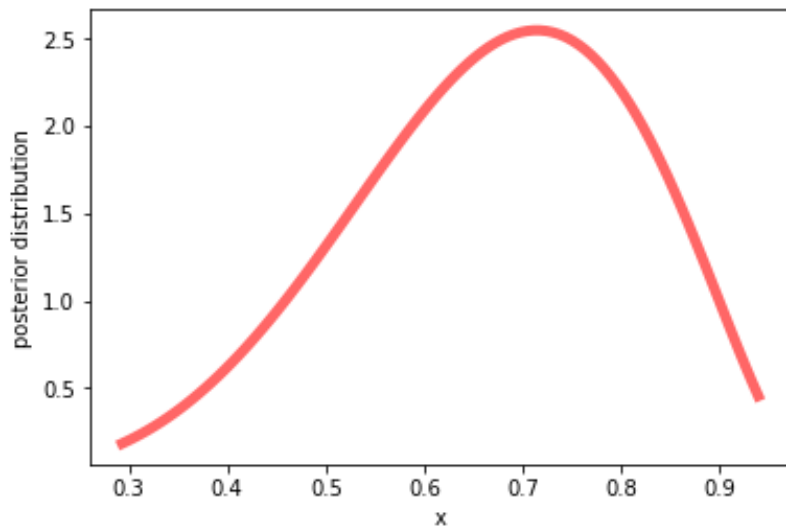


3) Posterior for beta prior is posterior only , hence,

For posterior, we sum up $NH + FH$ and $NT + FT$, which now gives the peak at around 0.7.

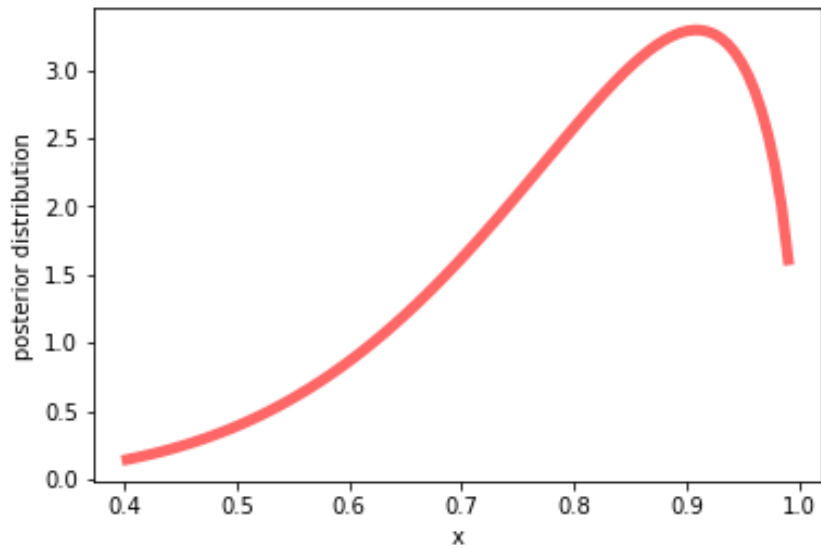
$FH = 2, NH = 4$

$FT = 2, NT = 1$



$FH = 2, NH = 4$

$FT = 0.5, NT = 1$



FH = 8, NH = 4

FT = 4, NH = 1

