

## Assignment One: Model Selection, Probability Theory and Distributions

Show that the variance of a sum is  $\text{var}[X + Y] = \text{var}[X] + \text{var}[Y] + 2\text{cov}[X, Y]$ .

Suppose  $\theta \sim \text{Beta}(\alpha, \beta)$ , derive the mean, mode and variance.

Since a positive definite matrix  $\Sigma$  can be defined as the quadratic form  $U^T \Lambda U$ , show that a necessary and sufficient condition for  $\Sigma$  to be positive definite is that all the eigenvalues  $\lambda_i$  of  $\Lambda$  are positive.

Derive the maximum likelihood solutions for the mean and the variance of a univariate Gaussian distribution by maximize the log likelihood function with respect to  $\mu$  and  $\Sigma$ .

Write a pseudo-code for using cross-validation to determine the best K value of K nearest neighbors classifier.