```
1 from collections import defaultdict
 2 import numpy as np
 3 from statistics import mean
 4 from scipy.sparse import dok_matrix, csr_matrix, triu, tril
 5 from random import randint
 6
 7 from tqdm.notebook import tqdm
 8
9 """
10 utils.py
11
12 Written by Sagar Kumar, April 2023
13
14 This is a Python script with useful functions which I have written and which are utilized
    throughout the scripts which
15 have been written for Problem 3, Homework 2 in NETS6116.
16
17 Some come from HW1.
18 """
19
20
21 def count_faster(I):
22
      dic = \{\}
23
24
      for i in I:
25
26
        if i in dic.keys():
27
          dic[i] += 1
28
29
        else:
30
          dic[i] = 1
31
32
      return [(key, dic[key]) for key in dic.keys()]
33
34
35
36 def distributionBin(x: 'input data',
37
              B: 'number of bins'
38
              ):
39
40
41
      :param x: (list) list of real-valued integers interpreted as the input data sampled from a
   presumed heavy-tail distribution
42
      :param B: (positive int) number of log-scaled bins to create a histogram from x
43
44
      distributionBin: Tuple, int -> Tuple, Tuple[Float]
45
46
      distributionBin takes a list of input data :x: assumed to be sampled from some heavy-tailed
    distribution and bins in :B: log
```

```
47
      sized bins in such a way that the output function *integrates* to 1. The output is a list of bin-
    midpoints X and the binned
48
      estimated distribution values Y.
49
50
51
      xmin = min(x)
52
      xmax = max(x)
53
54
      # creating the B+1 bin edges
55
      bin_edges = np.logspace(max(1,np.log10(xmin)), np.log10(xmax), num=B+1)
56
57
      # using numpy's histogram function get distributions
58
      density, _ = np.histogram(x, bins=bin_edges, density=True)
59
60
      # obtaining bin midpoints for cleaner absciss
61
      log be = np.log10(bin edges)
62
      xout = 10**((log_be[1:] + log_be[:-1])/2)
63
64
      return xout, density
65
66
67 def functionBin(x: 'preimage',
68
            y: 'function output for some function y \mid y_i = y(x)',
69
             B: 'number of bins'
70
            ):
71
72
73
      :param x: (list) list of real-valued numbers interpreted as the preimage of the function y(x)
74
      :param y: (list) list of real-valued numbers interpreted as the values of function y applied to each
    input value in x
75
      :param B: (positive int) number of log-scaled bins to create a histogram
76
77
      functionBin: Tuple, Tuple, int -> Tuple, Tuple
78
79
      functionBin takes an ordered list of sampled input values :x: and their corresponding outputs
    under some function :y: (
      i.e. y(x)) and bins the input values into :B: log sized bins, averaging the output values within
80
    each bin. The output is
81
      the bin-midpoints X and the binned outputs.
82
      111111
83
84
85
      xmin = min(x)
86
      xmax = max(x)
87
88
      # creating the B+1 bin edges
89
      bin edges = np.logspace(max(1,np.log10(xmin)), np.log10(xmax), num=B+1)
90
91
      # obtaining bin midpoints for cleaner absciss
```

```
92
        log be = np.log10(bin edges)
 93
        bm = 10**((log_be[1:] + log_be[:-1])/2)
 94
 95
       # creating (input, output) pairs and sorting by input value
 96
       fpairs = list(zip(x,y))
 97
       fpairs.sort(key=lambda x: x[0])
 98
 99
       # creating (label, boundary) pairs using midpoint and right boundary for each bin
100
       mid_redge_pairs = list(zip(bm, bin_edges[1:]))
101
102
        # dictionary of values where key corresponds to the bin and values are those which fit in the
     bin
103
        bin out list = defaultdict(list)
104
105
       idx = 0
106
       for mid, redge in tqdm(mid redge pairs, desc='Binning Function'):
107
          while (fpairs[idx][0] < redge) & (idx < len(fpairs)-1):
108
            bin_out_list[mid].append(fpairs[idx])
109
            idx += 1
110
111
       # adding the last value
112
       bin out list[list(bin out list.keys())[-1]].append(fpairs[-1])
113
114
       xout = list(bin out list.keys())
115
116
       # y value is the average of each bin
117
       yout = [mean([i[1] for i in b]) for b in bin_out_list.values()]
118
119
       return xout, yout
120
121
122 def simpleSF(n: 'graph size' = 10**4,
123
            s: 'number of samples' = 10,
124
            sparse: 'choice of numpy vs. scipy sparse matrix' = False
125
            ):
126
        111111
127
128
       :param n: (positive int) total number of nodes in the desired graph after completing its
     percolation
129
       :param s: (positive int) total number of graphs created
130
        :param sparse: (boolean) False maps output to dense numpy ndarrays, True maps them to
     scipy sparse csr_matrix
131
132
       simpleSF: Int, Int, Bool -> Tuple[np.ndarray OR scipy.sparse.csr_matrix]
133
134
       simpleSF takes a value for the size of the graph :n: and the number of samples :s: and
     percolates :s: scale-free graphs of
135
       size :n: by randomly selecting an edge E := (i,j) and attaching new incoming nodes to both i and
     i. The output is a list of
```

```
136
       :s: (:n: x :n:) matrices which act as the adjacency matrix of each sample graph. Choosing scipy
     sparse matrix allows for
137
       larger graph sizes.
138
139
140
       outlist = list()
141
       pbar = tqdm(range(s), desc=f"Generating Samples")
142
143
       for i in pbar:
144
145
          # edgelist
146
          edgelist = \{(0,1)\}
147
148
          # selecting a random edge and making the incident nodes the fruits of an incoming cherry to
     create a triangle
149
          # process repeats until t == n
150
         t = 2
151
         while t < n:
152
            m = randint(0, len(edgelist)-1)
153
            i,j = list(edgelist)[m]
154
            edgelist = edgelist | \{(i, t), (j, t)\} |
155
            t += 1
156
157
         # mapping corresponding matrix values for all pairs in edgelist from 0 -> 1
158
         if sparse:
159
            A = dok matrix((n, n), dtype=int)
160
            for e in edgelist:
161
              A[e] = 1
162
163
            # currently only have upper triangle, so making the matrix symmetric about the main
     diagonal
164
            # triu and tril authomatically change it from dok_matrix to csr_matrix
165
            A = triu(A) + tril(A.T)
166
167
         else:
168
            A = np.zeros((n,n))
169
            for e in edgelist:
170
              A[e] = 1
171
172
            # currently only have upper triangle, so making the matrix symmetric about the main
     diagonal
173
            A = np.triu(A) + np.tril(A.T)
174
175
          outlist.append(A)
176
177
       return outlist
178
```