# **Big O Notation**

Using not-boring math to measure code's efficiency

## The idea behind big O notation

**Big O notation is the language we use for articulating how long an algorithm takes to run**. It's how we compare the efficiency of different approaches to a problem.

With big O notation we express the runtime in terms of–brace yourself–how quickly it grows relative to the input, as the input gets arbitrarily large.

Let's break that down:

- 1. **how quickly the runtime grows**—Some external factors affect the time it takes for a function to run: the speed of the processor, what else the computer is running, etc. So it's hard to make strong statements about the *exact runtime* of an algorithm. Instead we use big O notation to express *how quickly its runtime grows*.
- 2. **relative to the input**–Since we're not looking at an exact number, we need something to phrase our runtime growth in terms of. We use the size of the input. So we can say things like the runtime grows "on the order of the size of the input" (O(n)) or "on the order of the square of the size of the input"  $(O(n^2))$ .
- 3. **as the input gets arbitrarily large**—Our algorithm may have steps that seem expensive when n is small but are eclipsed eventually by other steps as n gets huge. For big O analysis, we care most about the stuff that grows fastest as the input grows, because everything else is quickly eclipsed as n gets very large. If you know what an asymptote is, you might see why "big O analysis" is sometimes called "asymptotic analysis."

Big O notation is like math except it's an **awesome**, **not-boring kind of math** where you get to wave your hands through the details and just focus on what's *basically* happening.

If this seems abstract so far, that's because it is. Let's look at some examples.

## Some examples

```
public void printFirstItem(int[] arrayOfItems) {
    System.out.println(arrayOfItems[0]);
}
```

This function runs in O(1) time (or "constant time") relative to its input. The input array could be 1 item or 1,000 items, but this function would still just require one "step."

```
public void printAllItems(int[] arrayOfItems) {
    for (int item : arrayOfItems) {
        System.out.println(item);
    }
}
```

This function runs in O(n) time (or "linear time"), where n is the number of items in the array. If the array has 10 items, we have to print 10 times. If it has 1,000 items, we have to print 1,000 times.

```
public void printAllPossibleOrderedPairs(int[] arrayOfItems) {
    for (int firstItem : arrayOfItems) {
        for (int secondItem : arrayOfItems) {
            int[] orderedPair = new int[]{firstItem, secondItem};
            System.out.println(Arrays.toString(orderedPair));
        }
    }
}
```

Here we're nesting two loops. If our array has n items, our outer loop runs n times and our inner loop runs n times for each iteration of the outer loop, giving us  $n^2$  total prints. Thus **this function** runs in  $O(n^2)$  time (or "quadratic time"). If the array has 10 items, we have to print 100 times. If it has 1,000 items, we have to print 1,000,000 times.

## N could be the actual input, or the size of the input

Both of these functions have O(n) runtime, even though one takes an integer as its input and the other takes an array:

```
public void sayHiNTimes(int n) {
    for (int x = 0; x < n; x++) {
        System.out.println("hi");
    }
}

public void printAllItemsInArray(int[] theArray) {
    for (int item : theArray) {
        System.out.println(item);
    }
}</pre>
```

So sometimes n is an actual number that's an input to our function, and other times n is the number of items in an input array (or an input map, or an input object, etc.).

# **Drop the constants**

This is why big O notation *rules*. When you're calculating the big O complexity of something, you just throw out the constants. So like:

```
public void printAllItemsTwice(int[] theArray) {
    for (int item : theArray) {
        System.out.println(item);
    }

    // once more, with feeling
    for (int item : theArray) {
        System.out.println(item);
    }
}
```

This is O(2n), which we just call O(n).

```
public void printFirstItemThenFirstHalfThenSayHi100Times(int[] theArray) {
    System.out.println(theArray[0]);

    int middleIndex = theArray.length / 2;
    int index = 0;

    while (index < middleIndex) {
        System.out.println(theArray[index]);
        index++;
    }

    for (int x = 0; x < 100; x++) {
        System.out.println("hi");
    }
}</pre>
```

This is O(1 + n/2 + 100), which we just call O(n).

Why can we get away with this? Remember, for big O notation we're looking at what happens **as** n **gets arbitrarily large**. As n gets really big, adding 100 or dividing by 2 has a decreasingly significant effect.

## **Drop the less significant terms**

For example:

```
public void printAllNumbersThenAllPairSums(int[] arrayOfNumbers) {

    System.out.println("these are the numbers:");
    for (int number : arrayOfNumbers) {
        System.out.println(number);
    }

    System.out.println("and these are their sums:");
    for (int firstNumber : arrayOfNumbers) {
        for (int secondNumber : arrayOfNumbers) {
            System.out.println(firstNumber + secondNumber);
        }
    }
}
```

Here our runtime is  $O(n + n^2)$ , which we just call  $O(n^2)$ . Even if it was  $O(n^2/2 + 100n)$ , it would still be  $O(n^2)$ .

Similarly:

- $O(n^3 + 50n^2 + 10000)$  is  $O(n^3)$
- O((n+30)\*(n+5)) is  $O(n^2)$

Again, we can get away with this because the less significant terms quickly become, well, less significant as n gets big.

## We're usually talking about the "worst case"

Often this "worst case" stipulation is implied. But sometimes you can impress your interviewer by saying it explicitly.

Sometimes the worst case runtime is significantly worse than the best case runtime:

```
public boolean contains(int[] haystack, int needle) {

    // does the haystack contain the needle?
    for (int i = 0; i < haystack.length; i++) {
        if (haystack[i] == needle) return true;
    }

    return false;
}</pre>
```

Here we might have 100 items in our haystack, but the first item might be the needle, in which case we would return in just 1 iteration of our loop.

In general we'd say this is O(n) runtime and the "worst case" part would be implied. But to be more specific we could say this is worst case O(n) and best case O(1) runtime. For some algorithms we can also make rigorous statements about the "average case" runtime.

## **Space complexity: the final frontier**

Sometimes we want to optimize for using less memory instead of (or in addition to) using less time. Talking about memory cost (or "space complexity") is very similar to talking about time cost. We simply look at the total size (relative to the size of the input) of any new variables we're allocating.

This function takes O(1) space (we aren't allocating any new variables):

```
public void sayHiNTimes(int n) {
    for (int x = 0; x < n; x++) {
        System.out.println("hi");
    }
}</pre>
```

This function takes O(n) space (the size of hiArray scales with the size of the input):

```
public String[] arrayOfHiNTimes(int n) {
    String[] hiArray = new String[n];
    for (int i = 0; i < n; i++) {
        hiArray[i] = "hi";
    }
    return hiArray;
}</pre>
```

Usually when we talk about space complexity, we're talking about *additional space*, so we don't include space taken up by the inputs. For example, this function takes constant space even though the input has n items:

```
public int getLargestItem(int[] arrayOfItems) {
   int largest = 0;
   for (int item : arrayOfItems) {
      if (item > largest) {
         largest = item;
      }
   }
   return largest;
}
```

**Sometimes there's a tradeoff between saving time and saving space**, so you have to decide which one you're optimizing for.

## Big O analysis is awesome except when it's not

You should make a habit of thinking about the time and space complexity of algorithms *as you design them*. Before long this'll become second nature, allowing you to see optimizations and potential performance issues right away.

Asymptotic analysis is a powerful tool, but wield it wisely.

Big O ignores constants, but **sometimes the constants matter**. If we have a script that takes 5 hours to run, an optimization that divides the runtime by 5 might not affect big O, but it still saves you 4 hours of waiting.

**Beware of premature optimization**. Sometimes optimizing time or space negatively impacts readability or coding time. For a young startup it might be more important to write code that's easy to ship quickly or easy to understand later, even if this means it's less time and space efficient than it could be.

But that doesn't mean startups don't care about big O analysis. A great engineer (startup or otherwise) knows how to strike the right *balance* between runtime, space, implementation time, maintainability, and readability.

You should develop the *skill* to see time and space optimizations, as well as the *wisdom* to judge if those optimizations are worthwhile.

### What's next?

If you're ready to start applying these concepts to some problems, check out our mock coding interview questions (/next).

They mimic a real interview by offering hints when you're stuck or you're missing an optimization.

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#### **By Parker Phinney**

Parker founded Interview Cake (/) to help more people like Alice land the jobs they deserve (/about). He runs coding interview workshops at several coding boot camps and personally tutors engineers with various backgrounds. Catch him wearing a ridiculous Superman onesie around The Mission District of San Francisco.

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