Proof (Continued)

- there are at most $\frac{n}{2^k}$ nodes with rank in $\{k+1, \ldots, 2^k\}$
- each of them contributes at most 2^k
- the contribution of all the nodes with rank from this interval is at most $O(n)$