

Proof

- assume $\text{rank}[i] \in \{k+1, \dots, 2^k\}$
- the number of nodes with rank lying in this interval is at most

$$\frac{n}{2^{k+1}} + \frac{n}{2^{k+2}} + \dots \leq \frac{n}{2^k}$$