

Claim

$$\#(i \rightarrow j: j \text{ is a root}) \leq O(m)$$