Proof

- assume rank[i] $\in \{k+1,\ldots,2^k\}$
- the number of nodes with rank lying in this interval is at most

$$\frac{n}{2^{k+1}} + \frac{n}{2^{k+2}} + \dots \leq \frac{n}{2^k}$$

after a call to Find(i), the node i is adopted by a new parent of strictly larger rank