

**02 INFORMATION ABOUT PRINCIPAL INVESTIGATORS/PROJECT DIRECTORS(PI/PD) and  
co-PRINCIPAL INVESTIGATORS/co-PROJECT DIRECTORS**

Submit only ONE copy of this form for each PI/PD and co-PI/PD identified on the proposal. The form(s) should be attached to the original proposal as specified in GPG Section II.C.a. Submission of this information is voluntary and is not a precondition of award. This information will not be disclosed to external peer reviewers. **DO NOT INCLUDE THIS FORM WITH ANY OF THE OTHER COPIES OF YOUR PROPOSAL AS THIS MAY COMPROMISE THE CONFIDENTIALITY OF THE INFORMATION.**

**PI/PD Name:** Robert Beezer

**Gender:** ☐ Male ☐ Female

**Ethnicity:** (Choose one response) ☐ Hispanic or Latino ☐ Not Hispanic or Latino

**Race:**  
(Select one or more)

☐ American Indian or Alaska Native  
☐ Asian  
☐ Black or African American  
☐ Native Hawaiian or Other Pacific Islander  
☐ White

**Disability Status:**  
(Select one or more)

☐ Hearing Impairment  
☐ Visual Impairment  
☐ Mobility/Orthopedic Impairment  
☐ Other  
☐ None

**Citizenship:** (Choose one) ☐ U.S. Citizen ☐ Permanent Resident ☐ Other non-U.S. Citizen

**Check here if you do not wish to provide any or all of the above information (excluding PI/PD name):** ☒

**REQUIRED: Check here if you are currently serving (or have previously served) as a PI, co-PI or PD on any federally funded project** ☐

**Ethnicity Definition:**

**Hispanic or Latino.** A person of Mexican, Puerto Rican, Cuban, South or Central American, or other Spanish culture or origin, regardless of race.

**Race Definitions:**

**American Indian or Alaska Native.** A person having origins in any of the original peoples of North and South America (including Central America), and who maintains tribal affiliation or community attachment.

**Asian.** A person having origins in any of the original peoples of the Far East, Southeast Asia, or the Indian subcontinent including, for example, Cambodia, China, India, Japan, Korea, Malaysia, Pakistan, the Philippine Islands, Thailand, and Vietnam.

**Black or African American.** A person having origins in any of the black racial groups of Africa.

**Native Hawaiian or Other Pacific Islander.** A person having origins in any of the original peoples of Hawaii, Guam, Samoa, or other Pacific Islands.

**White.** A person having origins in any of the original peoples of Europe, the Middle East, or North Africa.

**WHY THIS INFORMATION IS BEING REQUESTED:**

The Federal Government has a continuing commitment to monitor the operation of its review and award processes to identify and address any inequities based on gender, race, ethnicity, or disability of its proposed PIs/PDs. To gather information needed for this important task, the proposer should submit a single copy of this form for each identified PI/PD with each proposal. Submission of the requested information is voluntary and will not affect the organization's eligibility for an award. However, information not submitted will seriously undermine the statistical validity, and therefore the usefulness, of information received from others. Any individual not wishing to submit some or all the information should check the box provided for this purpose. (The exceptions are the PI/PD name and the information about prior Federal support, the last question above.)

Collection of this information is authorized by the NSF Act of 1950, as amended, 42 U.S.C. 1861, et seq. Demographic data allows NSF to gauge whether our programs and other opportunities in science and technology are fairly reaching and benefiting everyone regardless of demographic category; to ensure that those in under-represented groups have the same knowledge of and access to programs and other research and educational opportunities; and to assess involvement of international investigators in work supported by NSF. The information may be disclosed to government contractors, experts, volunteers and researchers to complete assigned work; and to other government agencies in order to coordinate and assess programs. The information may be added to the Reviewer file and used to select potential candidates to serve as peer reviewers or advisory committee members. See Systems of Records, NSF-50, "Principal Investigator/Proposal File and Associated Records", 63 Federal Register 267 (January 5, 1998), and NSF-51, "Reviewer/Proposal File and Associated Records", 63 Federal Register 268 (January 5, 1998).

**02 INFORMATION ABOUT PRINCIPAL INVESTIGATORS/PROJECT DIRECTORS(PI/PD) and  
co-PRINCIPAL INVESTIGATORS/co-PROJECT DIRECTORS**

Submit only ONE copy of this form for each PI/PD and co-PI/PD identified on the proposal. The form(s) should be attached to the original proposal as specified in GPG Section II.C.a. Submission of this information is voluntary and is not a precondition of award. This information will not be disclosed to external peer reviewers. **DO NOT INCLUDE THIS FORM WITH ANY OF THE OTHER COPIES OF YOUR PROPOSAL AS THIS MAY COMPROMISE THE CONFIDENTIALITY OF THE INFORMATION.**

**PI/PD Name:** Thomas W Judson

**Gender:** ☐ Male ☐ Female

**Ethnicity:** (Choose one response) ☐ Hispanic or Latino ☐ Not Hispanic or Latino

**Race:**  
(Select one or more)

☐ American Indian or Alaska Native  
☐ Asian  
☐ Black or African American  
☐ Native Hawaiian or Other Pacific Islander  
☐ White

**Disability Status:**  
(Select one or more)

☐ Hearing Impairment  
☐ Visual Impairment  
☐ Mobility/Orthopedic Impairment  
☐ Other  
☐ None

**Citizenship:** (Choose one) ☐ U.S. Citizen ☐ Permanent Resident ☐ Other non-U.S. Citizen

**Check here if you do not wish to provide any or all of the above information (excluding PI/PD name):** ☒

**REQUIRED: Check here if you are currently serving (or have previously served) as a PI, co-PI or PD on any federally funded project** ☐

**Ethnicity Definition:**

**Hispanic or Latino.** A person of Mexican, Puerto Rican, Cuban, South or Central American, or other Spanish culture or origin, regardless of race.

**Race Definitions:**

**American Indian or Alaska Native.** A person having origins in any of the original peoples of North and South America (including Central America), and who maintains tribal affiliation or community attachment.

**Asian.** A person having origins in any of the original peoples of the Far East, Southeast Asia, or the Indian subcontinent including, for example, Cambodia, China, India, Japan, Korea, Malaysia, Pakistan, the Philippine Islands, Thailand, and Vietnam.

**Black or African American.** A person having origins in any of the black racial groups of Africa.

**Native Hawaiian or Other Pacific Islander.** A person having origins in any of the original peoples of Hawaii, Guam, Samoa, or other Pacific Islands.

**White.** A person having origins in any of the original peoples of Europe, the Middle East, or North Africa.

**WHY THIS INFORMATION IS BEING REQUESTED:**

The Federal Government has a continuing commitment to monitor the operation of its review and award processes to identify and address any inequities based on gender, race, ethnicity, or disability of its proposed PIs/PDs. To gather information needed for this important task, the proposer should submit a single copy of this form for each identified PI/PD with each proposal. Submission of the requested information is voluntary and will not affect the organization's eligibility for an award. However, information not submitted will seriously undermine the statistical validity, and therefore the usefulness, of information received from others. Any individual not wishing to submit some or all the information should check the box provided for this purpose. (The exceptions are the PI/PD name and the information about prior Federal support, the last question above.)

Collection of this information is authorized by the NSF Act of 1950, as amended, 42 U.S.C. 1861, et seq. Demographic data allows NSF to gauge whether our programs and other opportunities in science and technology are fairly reaching and benefiting everyone regardless of demographic category; to ensure that those in under-represented groups have the same knowledge of and access to programs and other research and educational opportunities; and to assess involvement of international investigators in work supported by NSF. The information may be disclosed to government contractors, experts, volunteers and researchers to complete assigned work; and to other government agencies in order to coordinate and assess programs. The information may be added to the Reviewer file and used to select potential candidates to serve as peer reviewers or advisory committee members. See Systems of Records, NSF-50, "Principal Investigator/Proposal File and Associated Records", 63 Federal Register 267 (January 5, 1998), and NSF-51, "Reviewer/Proposal File and Associated Records", 63 Federal Register 268 (January 5, 1998).

**02 INFORMATION ABOUT PRINCIPAL INVESTIGATORS/PROJECT DIRECTORS(PI/PD) and  
co-PRINCIPAL INVESTIGATORS/co-PROJECT DIRECTORS**

Submit only ONE copy of this form for each PI/PD and co-PI/PD identified on the proposal. The form(s) should be attached to the original proposal as specified in GPG Section II.C.a. Submission of this information is voluntary and is not a precondition of award. This information will not be disclosed to external peer reviewers. **DO NOT INCLUDE THIS FORM WITH ANY OF THE OTHER COPIES OF YOUR PROPOSAL AS THIS MAY COMPROMISE THE CONFIDENTIALITY OF THE INFORMATION.**

**PI/PD Name:** William A Stein

**Gender:** ☒ Male ☐ Female

**Ethnicity:** (Choose one response) ☐ Hispanic or Latino ☒ Not Hispanic or Latino

**Race:**  
(Select one or more)

☐ American Indian or Alaska Native  
☐ Asian  
☐ Black or African American  
☐ Native Hawaiian or Other Pacific Islander  
☒ White

**Disability Status:**  
(Select one or more)

☐ Hearing Impairment  
☐ Visual Impairment  
☐ Mobility/Orthopedic Impairment  
☐ Other  
☒ None

**Citizenship:** (Choose one) ☒ U.S. Citizen ☐ Permanent Resident ☐ Other non-U.S. Citizen

**Check here if you do not wish to provide any or all of the above information (excluding PI/PD name):** ☒

**REQUIRED: Check here if you are currently serving (or have previously served) as a PI, co-PI or PD on any federally funded project** ☒

**Ethnicity Definition:**

**Hispanic or Latino.** A person of Mexican, Puerto Rican, Cuban, South or Central American, or other Spanish culture or origin, regardless of race.

**Race Definitions:**

**American Indian or Alaska Native.** A person having origins in any of the original peoples of North and South America (including Central America), and who maintains tribal affiliation or community attachment.

**Asian.** A person having origins in any of the original peoples of the Far East, Southeast Asia, or the Indian subcontinent including, for example, Cambodia, China, India, Japan, Korea, Malaysia, Pakistan, the Philippine Islands, Thailand, and Vietnam.

**Black or African American.** A person having origins in any of the black racial groups of Africa.

**Native Hawaiian or Other Pacific Islander.** A person having origins in any of the original peoples of Hawaii, Guam, Samoa, or other Pacific Islands.

**White.** A person having origins in any of the original peoples of Europe, the Middle East, or North Africa.

**WHY THIS INFORMATION IS BEING REQUESTED:**

The Federal Government has a continuing commitment to monitor the operation of its review and award processes to identify and address any inequities based on gender, race, ethnicity, or disability of its proposed PIs/PDs. To gather information needed for this important task, the proposer should submit a single copy of this form for each identified PI/PD with each proposal. Submission of the requested information is voluntary and will not affect the organization's eligibility for an award. However, information not submitted will seriously undermine the statistical validity, and therefore the usefulness, of information received from others. Any individual not wishing to submit some or all the information should check the box provided for this purpose. (The exceptions are the PI/PD name and the information about prior Federal support, the last question above.)

Collection of this information is authorized by the NSF Act of 1950, as amended, 42 U.S.C. 1861, et seq. Demographic data allows NSF to gauge whether our programs and other opportunities in science and technology are fairly reaching and benefiting everyone regardless of demographic category; to ensure that those in under-represented groups have the same knowledge of and access to programs and other research and educational opportunities; and to assess involvement of international investigators in work supported by NSF. The information may be disclosed to government contractors, experts, volunteers and researchers to complete assigned work; and to other government agencies in order to coordinate and assess programs. The information may be added to the Reviewer file and used to select potential candidates to serve as peer reviewers or advisory committee members. See Systems of Records, NSF-50, "Principal Investigator/Proposal File and Associated Records", 63 Federal Register 267 (January 5, 1998), and NSF-51, "Reviewer/Proposal File and Associated Records", 63 Federal Register 268 (January 5, 1998).

**02 INFORMATION ABOUT PRINCIPAL INVESTIGATORS/PROJECT DIRECTORS(PI/PD) and  
co-PRINCIPAL INVESTIGATORS/co-PROJECT DIRECTORS**

Submit only ONE copy of this form for each PI/PD and co-PI/PD identified on the proposal. The form(s) should be attached to the original proposal as specified in GPG Section II.C.a. Submission of this information is voluntary and is not a precondition of award. This information will not be disclosed to external peer reviewers. **DO NOT INCLUDE THIS FORM WITH ANY OF THE OTHER COPIES OF YOUR PROPOSAL AS THIS MAY COMPROMISE THE CONFIDENTIALITY OF THE INFORMATION.**

**PI/PD Name:** Marja-Liisa Hassi

**Gender:** ☐ Male ☒ Female

**Ethnicity:** (Choose one response) ☐ Hispanic or Latino ☒ Not Hispanic or Latino

**Race:**  
(Select one or more)

☐ American Indian or Alaska Native  
☐ Asian  
☐ Black or African American  
☐ Native Hawaiian or Other Pacific Islander  
☒ White

**Disability Status:**  
(Select one or more)

☐ Hearing Impairment  
☐ Visual Impairment  
☐ Mobility/Orthopedic Impairment  
☐ Other  
☒ None

**Citizenship:** (Choose one) ☐ U.S. Citizen ☐ Permanent Resident ☒ Other non-U.S. Citizen

**Check here if you do not wish to provide any or all of the above information (excluding PI/PD name):** ☐

**REQUIRED: Check here if you are currently serving (or have previously served) as a PI, co-PI or PD on any federally funded project** ☐

**Ethnicity Definition:**

**Hispanic or Latino.** A person of Mexican, Puerto Rican, Cuban, South or Central American, or other Spanish culture or origin, regardless of race.

**Race Definitions:**

**American Indian or Alaska Native.** A person having origins in any of the original peoples of North and South America (including Central America), and who maintains tribal affiliation or community attachment.

**Asian.** A person having origins in any of the original peoples of the Far East, Southeast Asia, or the Indian subcontinent including, for example, Cambodia, China, India, Japan, Korea, Malaysia, Pakistan, the Philippine Islands, Thailand, and Vietnam.

**Black or African American.** A person having origins in any of the black racial groups of Africa.

**Native Hawaiian or Other Pacific Islander.** A person having origins in any of the original peoples of Hawaii, Guam, Samoa, or other Pacific Islands.

**White.** A person having origins in any of the original peoples of Europe, the Middle East, or North Africa.

**WHY THIS INFORMATION IS BEING REQUESTED:**

The Federal Government has a continuing commitment to monitor the operation of its review and award processes to identify and address any inequities based on gender, race, ethnicity, or disability of its proposed PIs/PDs. To gather information needed for this important task, the proposer should submit a single copy of this form for each identified PI/PD with each proposal. Submission of the requested information is voluntary and will not affect the organization's eligibility for an award. However, information not submitted will seriously undermine the statistical validity, and therefore the usefulness, of information received from others. Any individual not wishing to submit some or all the information should check the box provided for this purpose. (The exceptions are the PI/PD name and the information about prior Federal support, the last question above.)

Collection of this information is authorized by the NSF Act of 1950, as amended, 42 U.S.C. 1861, et seq. Demographic data allows NSF to gauge whether our programs and other opportunities in science and technology are fairly reaching and benefiting everyone regardless of demographic category; to ensure that those in under-represented groups have the same knowledge of and access to programs and other research and educational opportunities; and to assess involvement of international investigators in work supported by NSF. The information may be disclosed to government contractors, experts, volunteers and researchers to complete assigned work; and to other government agencies in order to coordinate and assess programs. The information may be added to the Reviewer file and used to select potential candidates to serve as peer reviewers or advisory committee members. See Systems of Records, NSF-50, "Principal Investigator/Proposal File and Associated Records", 63 Federal Register 267 (January 5, 1998), and NSF-51, "Reviewer/Proposal File and Associated Records", 63 Federal Register 268 (January 5, 1998).

**02 INFORMATION ABOUT PRINCIPAL INVESTIGATORS/PROJECT DIRECTORS(PI/PD) and  
co-PRINCIPAL INVESTIGATORS/co-PROJECT DIRECTORS**

Submit only ONE copy of this form for each PI/PD and co-PI/PD identified on the proposal. The form(s) should be attached to the original proposal as specified in GPG Section II.C.a. Submission of this information is voluntary and is not a precondition of award. This information will not be disclosed to external peer reviewers. **DO NOT INCLUDE THIS FORM WITH ANY OF THE OTHER COPIES OF YOUR PROPOSAL AS THIS MAY COMPROMISE THE CONFIDENTIALITY OF THE INFORMATION.**

**PI/PD Name:** Sandra L Laursen

**Gender:** ☐ Male ☒ Female

**Ethnicity:** (Choose one response) ☐ Hispanic or Latino ☒ Not Hispanic or Latino

**Race:**  
(Select one or more)

☐ American Indian or Alaska Native  
☐ Asian  
☐ Black or African American  
☐ Native Hawaiian or Other Pacific Islander  
☒ White

**Disability Status:**  
(Select one or more)

☐ Hearing Impairment  
☐ Visual Impairment  
☐ Mobility/Orthopedic Impairment  
☐ Other  
☒ None

**Citizenship:** (Choose one) ☒ U.S. Citizen ☐ Permanent Resident ☐ Other non-U.S. Citizen

**Check here if you do not wish to provide any or all of the above information (excluding PI/PD name):** ☐

**REQUIRED: Check here if you are currently serving (or have previously served) as a PI, co-PI or PD on any federally funded project** ☒

**Ethnicity Definition:**

**Hispanic or Latino.** A person of Mexican, Puerto Rican, Cuban, South or Central American, or other Spanish culture or origin, regardless of race.

**Race Definitions:**

**American Indian or Alaska Native.** A person having origins in any of the original peoples of North and South America (including Central America), and who maintains tribal affiliation or community attachment.

**Asian.** A person having origins in any of the original peoples of the Far East, Southeast Asia, or the Indian subcontinent including, for example, Cambodia, China, India, Japan, Korea, Malaysia, Pakistan, the Philippine Islands, Thailand, and Vietnam.

**Black or African American.** A person having origins in any of the black racial groups of Africa.

**Native Hawaiian or Other Pacific Islander.** A person having origins in any of the original peoples of Hawaii, Guam, Samoa, or other Pacific Islands.

**White.** A person having origins in any of the original peoples of Europe, the Middle East, or North Africa.

**WHY THIS INFORMATION IS BEING REQUESTED:**

The Federal Government has a continuing commitment to monitor the operation of its review and award processes to identify and address any inequities based on gender, race, ethnicity, or disability of its proposed PIs/PDs. To gather information needed for this important task, the proposer should submit a single copy of this form for each identified PI/PD with each proposal. Submission of the requested information is voluntary and will not affect the organization's eligibility for an award. However, information not submitted will seriously undermine the statistical validity, and therefore the usefulness, of information received from others. Any individual not wishing to submit some or all the information should check the box provided for this purpose. (The exceptions are the PI/PD name and the information about prior Federal support, the last question above.)

Collection of this information is authorized by the NSF Act of 1950, as amended, 42 U.S.C. 1861, et seq. Demographic data allows NSF to gauge whether our programs and other opportunities in science and technology are fairly reaching and benefiting everyone regardless of demographic category; to ensure that those in under-represented groups have the same knowledge of and access to programs and other research and educational opportunities; and to assess involvement of international investigators in work supported by NSF. The information may be disclosed to government contractors, experts, volunteers and researchers to complete assigned work; and to other government agencies in order to coordinate and assess programs. The information may be added to the Reviewer file and used to select potential candidates to serve as peer reviewers or advisory committee members. See Systems of Records, NSF-50, "Principal Investigator/Proposal File and Associated Records", 63 Federal Register 267 (January 5, 1998), and NSF-51, "Reviewer/Proposal File and Associated Records", 63 Federal Register 268 (January 5, 1998).

## List of Suggested Reviewers or Reviewers Not To Include (optional)

---

### **SUGGESTED REVIEWERS:**

Not Listed

### **REVIEWERS NOT TO INCLUDE:**

Not Listed

## List of Suggested Reviewers or Reviewers Not To Include (optional)

---

### **SUGGESTED REVIEWERS:**

Not Listed

### **REVIEWERS NOT TO INCLUDE:**

Not Listed

## List of Suggested Reviewers or Reviewers Not To Include (optional)

---

### **SUGGESTED REVIEWERS:**

Not Listed

### **REVIEWERS NOT TO INCLUDE:**

Not Listed



## List of Suggested Reviewers or Reviewers Not To Include (optional)

---

### **SUGGESTED REVIEWERS:**

Not Listed

### **REVIEWERS NOT TO INCLUDE:**

Not Listed

# COVER SHEET FOR PROPOSAL TO THE NATIONAL SCIENCE FOUNDATION

PROGRAM ANNOUNCEMENT/SOLICITATION NO./CLOSING DATE/if not in response to a program announcement/solicitation enter NSF 10-1					FOR NSF USE ONLY	
NSF 09-529 01/13/10					NSF PROPOSAL NUMBER	
FOR CONSIDERATION BY NSF ORGANIZATION UNIT(S) (Indicate the most specific unit known, i.e. program, division, etc.)						
DUE - CCLI-Phase 2 (Expansion)						
DATE RECEIVED	NUMBER OF COPIES	DIVISION ASSIGNED	FUND CODE	DUNS# (Data Universal Numbering System)	FILE LOCATION	
				004135930		
EMPLOYER IDENTIFICATION NUMBER (EIN) OR TAXPAYER IDENTIFICATION NUMBER (TIN)		SHOW PREVIOUS AWARD NO. IF THIS IS <input type="checkbox"/> A RENEWAL <input type="checkbox"/> AN ACCOMPLISHMENT-BASED RENEWAL		IS THIS PROPOSAL BEING SUBMITTED TO ANOTHER FEDERAL AGENCY? YES <input type="checkbox"/> NO <input checked="" type="checkbox"/> IF YES, LIST ACRONYM(S)		
943205114						
NAME OF ORGANIZATION TO WHICH AWARD SHOULD BE MADE American Institute of Mathematics			ADDRESS OF Awardee ORGANIZATION, INCLUDING 9 DIGIT ZIP CODE American Institute of Mathematics 360 Portage Avenue Palo Alto, CA. 943062244			
AWARDEE ORGANIZATION CODE (IF KNOWN) 5300011617						
NAME OF PERFORMING ORGANIZATION, IF DIFFERENT FROM ABOVE			ADDRESS OF PERFORMING ORGANIZATION, IF DIFFERENT, INCLUDING 9 DIGIT ZIP CODE			
PERFORMING ORGANIZATION CODE (IF KNOWN)						
IS AWARDEE ORGANIZATION (Check All That Apply) (See GPG II.C For Definitions)		<input type="checkbox"/> SMALL BUSINESS <input type="checkbox"/> FOR-PROFIT ORGANIZATION		<input type="checkbox"/> MINORITY BUSINESS <input type="checkbox"/> WOMAN-OWNED BUSINESS		<input type="checkbox"/> IF THIS IS A PRELIMINARY PROPOSAL THEN CHECK HERE
TITLE OF PROPOSED PROJECT UTMOST: Undergraduate Teaching in Mathematics with Open Software and Textbooks						
REQUESTED AMOUNT \$ 0	PROPOSED DURATION (1-60 MONTHS) 36 months		REQUESTED STARTING DATE 09/01/10		SHOW RELATED PRELIMINARY PROPOSAL NO. IF APPLICABLE	
CHECK APPROPRIATE BOX(ES) IF THIS PROPOSAL INCLUDES ANY OF THE ITEMS LISTED BELOW <input type="checkbox"/> BEGINNING INVESTIGATOR (GPG I.G.2) <input type="checkbox"/> DISCLOSURE OF LOBBYING ACTIVITIES (GPG II.C.1.e) <input type="checkbox"/> PROPRIETARY & PRIVILEGED INFORMATION (GPG I.D, II.C.1.d) <input type="checkbox"/> HISTORIC PLACES (GPG II.C.2.j) <input type="checkbox"/> EAGER* (GPG II.D.2) <input type="checkbox"/> RAPID** (GPG II.D.1) <input type="checkbox"/> VERTEBRATE ANIMALS (GPG II.D.6) IACUC App. Date _____ PHS Animal Welfare Assurance Number _____ <input type="checkbox"/> HUMAN SUBJECTS (GPG II.D.7) Human Subjects Assurance Number _____ Exemption Subsection _____ or IRB App. Date _____ <input type="checkbox"/> INTERNATIONAL COOPERATIVE ACTIVITIES: COUNTRY/COUNTRIES INVOLVED (GPG II.C.2.j) _____ <input type="checkbox"/> HIGH RESOLUTION GRAPHICS/OTHER GRAPHICS WHERE EXACT COLOR REPRESENTATION IS REQUIRED FOR PROPER INTERPRETATION (GPG I.G.1)						
PI/PD DEPARTMENT		PI/PD POSTAL ADDRESS 360 Portage Avenue				
PI/PD FAX NUMBER		Palo Alto, CA 943062244 United States				
NAMES (TYPED)	High Degree	Yr of Degree	Telephone Number	Electronic Mail Address		
PI/PD NAME Robert Beezer	DPhil	1984	650-845-2071	beezer@ups.edu		
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						

## CERTIFICATION PAGE

### Certification for Authorized Organizational Representative or Individual Applicant:

By signing and submitting this proposal, the Authorized Organizational Representative or Individual Applicant is: (1) certifying that statements made herein are true and complete to the best of his/her knowledge; and (2) agreeing to accept the obligation to comply with NSF award terms and conditions if an award is made as a result of this application. Further, the applicant is hereby providing certifications regarding debarment and suspension, drug-free workplace, lobbying activities (see below), responsible conduct of research, nondiscrimination, and flood hazard insurance (when applicable) as set forth in the NSF Proposal & Award Policies & Procedures Guide, Part I: the Grant Proposal Guide (GPG) (NSF 10-1). Willful provision of false information in this application and its supporting documents or in reports required under an ensuing award is a criminal offense (U. S. Code, Title 18, Section 1001).

### Conflict of Interest Certification

In addition, if the applicant institution employs more than fifty persons, by electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that the institution has implemented a written and enforced conflict of interest policy that is consistent with the provisions of the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.A; that to the best of his/her knowledge, all financial disclosures required by that conflict of interest policy have been made; and that all identified conflicts of interest will have been satisfactorily managed, reduced or eliminated prior to the institution's expenditure of any funds under the award, in accordance with the institution's conflict of interest policy. Conflicts which cannot be satisfactorily managed, reduced or eliminated must be disclosed to NSF.

### Drug Free Work Place Certification

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Drug Free Work Place Certification contained in Exhibit II-3 of the Grant Proposal Guide.

### Debarment and Suspension Certification

(If answer "yes", please provide explanation.)

Is the organization or its principals presently debarred, suspended, proposed for debarment, declared ineligible, or voluntarily excluded from covered transactions by any Federal department or agency?

Yes ☐

No ☒

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Debarment and Suspension Certification contained in Exhibit II-4 of the Grant Proposal Guide.

### Certification Regarding Lobbying

The following certification is required for an award of a Federal contract, grant, or cooperative agreement exceeding \$100,000 and for an award of a Federal loan or a commitment providing for the United States to insure or guarantee a loan exceeding \$150,000.

### Certification for Contracts, Grants, Loans and Cooperative Agreements

The undersigned certifies, to the best of his or her knowledge and belief, that:

- (1) No federal appropriated funds have been paid or will be paid, by or on behalf of the undersigned, to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with the awarding of any federal contract, the making of any Federal grant, the making of any Federal loan, the entering into of any cooperative agreement, and the extension, continuation, renewal, amendment, or modification of any Federal contract, grant, loan, or cooperative agreement.
- (2) If any funds other than Federal appropriated funds have been paid or will be paid to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with this Federal contract, grant, loan, or cooperative agreement, the undersigned shall complete and submit Standard Form-LLL, "Disclosure of Lobbying Activities," in accordance with its instructions.
- (3) The undersigned shall require that the language of this certification be included in the award documents for all subawards at all tiers including subcontracts, subgrants, and contracts under grants, loans, and cooperative agreements and that all subrecipients shall certify and disclose accordingly.

This certification is a material representation of fact upon which reliance was placed when this transaction was made or entered into. Submission of this certification is a prerequisite for making or entering into this transaction imposed by section 1352, Title 31, U.S. Code. Any person who fails to file the required certification shall be subject to a civil penalty of not less than \$10,000 and not more than \$100,000 for each such failure.

### Certification Regarding Nondiscrimination

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative is providing the Certification Regarding Nondiscrimination contained in Exhibit II-6 of the Grant Proposal Guide.

### Certification Regarding Flood Hazard Insurance

Two sections of the National Flood Insurance Act of 1968 (42 USC §4012a and §4106) bar Federal agencies from giving financial assistance for acquisition or construction purposes in any area identified by the Federal Emergency Management Agency (FEMA) as having special flood hazards unless the:

- (1) community in which that area is located participates in the national flood insurance program; and
- (2) building (and any related equipment) is covered by adequate flood insurance.

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant located in FEMA-designated special flood hazard areas is certifying that adequate flood insurance has been or will be obtained in the following situations:

- (1) for NSF grants for the construction of a building or facility, regardless of the dollar amount of the grant; and
- (2) for other NSF Grants when more than \$25,000 has been budgeted in the proposal for repair, alteration or improvement (construction) of a building or facility.

### Certification Regarding Responsible Conduct of Research (RCR)

(This certification is not applicable to proposals for conferences, symposia, and workshops.)

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that, in accordance with the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.B., the institution has a plan in place to provide appropriate training and oversight in the responsible and ethical conduct of research to undergraduates, graduate students and postdoctoral researchers who will be supported by NSF to conduct research.

The undersigned shall require that the language of this certification be included in any award documents for all subawards at all tiers.

AUTHORIZED ORGANIZATIONAL REPRESENTATIVE		SIGNATURE		DATE	
NAME					
TELEPHONE NUMBER	ELECTRONIC MAIL ADDRESS			FAX NUMBER	

\* EAGER - Early-concept Grants for Exploratory Research

\*\* RAPID - Grants for Rapid Response Research

## COVER SHEET FOR PROPOSAL TO THE NATIONAL SCIENCE FOUNDATION

PROGRAM ANNOUNCEMENT/SOLICITATION NO./CLOSING DATE(if not in response to a program announcement/solicitation enter NSF 10-1					FOR NSF USE ONLY	
NSF 09-529 01/13/10					NSF PROPOSAL NUMBER	
FOR CONSIDERATION BY NSF ORGANIZATION UNIT(S) (Indicate the most specific unit known, i.e. program, division, etc.)						
DUE - CCLI-Phase 2 (Expansion)						
DATE RECEIVED	NUMBER OF COPIES	DIVISION ASSIGNED	FUND CODE	DUNS# (Data Universal Numbering System)	FILE LOCATION	
				073894727		
EMPLOYER IDENTIFICATION NUMBER (EIN) OR TAXPAYER IDENTIFICATION NUMBER (TIN)		SHOW PREVIOUS AWARD NO. IF THIS IS <input type="checkbox"/> A RENEWAL <input type="checkbox"/> AN ACCOMPLISHMENT-BASED RENEWAL		IS THIS PROPOSAL BEING SUBMITTED TO ANOTHER FEDERAL AGENCY? YES <input type="checkbox"/> NO <input checked="" type="checkbox"/> IF YES, LIST ACRONYM(S)		
756002514						
NAME OF ORGANIZATION TO WHICH AWARD SHOULD BE MADE Stephen F. Austin State University			ADDRESS OF Awardee ORGANIZATION, INCLUDING 9 DIGIT ZIP CODE Stephen F. Austin State University Box 6078 Nacogdoches, TX. 759626078			
AWARDEE ORGANIZATION CODE (IF KNOWN) 0036244000						
NAME OF PERFORMING ORGANIZATION, IF DIFFERENT FROM ABOVE			ADDRESS OF PERFORMING ORGANIZATION, IF DIFFERENT, INCLUDING 9 DIGIT ZIP CODE			
PERFORMING ORGANIZATION CODE (IF KNOWN)						
IS Awardee ORGANIZATION (Check All That Apply) (See GPG II.C For Definitions)		<input type="checkbox"/> SMALL BUSINESS <input type="checkbox"/> FOR-PROFIT ORGANIZATION		<input type="checkbox"/> MINORITY BUSINESS <input type="checkbox"/> WOMAN-OWNED BUSINESS		<input type="checkbox"/> IF THIS IS A PRELIMINARY PROPOSAL THEN CHECK HERE
TITLE OF PROPOSED PROJECT Collaborative Research: UTMOST: Undergraduate Teaching in Mathematics with Open Software and Textbooks						
REQUESTED AMOUNT \$ 45,986	PROPOSED DURATION (1-60 MONTHS) 36 months		REQUESTED STARTING DATE 09/01/10		SHOW RELATED PRELIMINARY PROPOSAL NO. IF APPLICABLE	
CHECK APPROPRIATE BOX(ES) IF THIS PROPOSAL INCLUDES ANY OF THE ITEMS LISTED BELOW <input type="checkbox"/> BEGINNING INVESTIGATOR (GPG I.G.2) <input type="checkbox"/> DISCLOSURE OF LOBBYING ACTIVITIES (GPG II.C.1.e) <input type="checkbox"/> PROPRIETARY & PRIVILEGED INFORMATION (GPG I.D. II.C.1.d) <input type="checkbox"/> HISTORIC PLACES (GPG II.C.2.j) <input type="checkbox"/> EAGER* (GPG II.D.2) <input type="checkbox"/> RAPID** (GPG II.D.1) <input type="checkbox"/> VERTEBRATE ANIMALS (GPG II.D.6) IACUC App. Date _____ PHS Animal Welfare Assurance Number _____						
PI/PD DEPARTMENT Mathematics and Statistics			PI/PD POSTAL ADDRESS Box 6078 nacogdoches, TX 759626078 United States			
PI/PD FAX NUMBER 936-468-1669						
NAMES (TYPED)	High Degree	Yr of Degree	Telephone Number	Electronic Mail Address		
PI/PD NAME Thomas W Judson	PhD	1984	936-468-2201	judsontw@sfasu.edu		
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						

## CERTIFICATION PAGE

### Certification for Authorized Organizational Representative or Individual Applicant:

By signing and submitting this proposal, the Authorized Organizational Representative or Individual Applicant is: (1) certifying that statements made herein are true and complete to the best of his/her knowledge; and (2) agreeing to accept the obligation to comply with NSF award terms and conditions if an award is made as a result of this application. Further, the applicant is hereby providing certifications regarding debarment and suspension, drug-free workplace, lobbying activities (see below), responsible conduct of research, nondiscrimination, and flood hazard insurance (when applicable) as set forth in the NSF Proposal & Award Policies & Procedures Guide, Part I: the Grant Proposal Guide (GPG) (NSF 10-1). Willful provision of false information in this application and its supporting documents or in reports required under an ensuing award is a criminal offense (U. S. Code, Title 18, Section 1001).

### Conflict of Interest Certification

In addition, if the applicant institution employs more than fifty persons, by electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that the institution has implemented a written and enforced conflict of interest policy that is consistent with the provisions of the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.A; that to the best of his/her knowledge, all financial disclosures required by that conflict of interest policy have been made; and that all identified conflicts of interest will have been satisfactorily managed, reduced or eliminated prior to the institution's expenditure of any funds under the award, in accordance with the institution's conflict of interest policy. Conflicts which cannot be satisfactorily managed, reduced or eliminated must be disclosed to NSF.

### Drug Free Work Place Certification

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Drug Free Work Place Certification contained in Exhibit II-3 of the Grant Proposal Guide.

### Debarment and Suspension Certification

(If answer "yes", please provide explanation.)

Is the organization or its principals presently debarred, suspended, proposed for debarment, declared ineligible, or voluntarily excluded from covered transactions by any Federal department or agency?

Yes ☐

No ☒

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Debarment and Suspension Certification contained in Exhibit II-4 of the Grant Proposal Guide.

### Certification Regarding Lobbying

The following certification is required for an award of a Federal contract, grant, or cooperative agreement exceeding \$100,000 and for an award of a Federal loan or a commitment providing for the United States to insure or guarantee a loan exceeding \$150,000.

### Certification for Contracts, Grants, Loans and Cooperative Agreements

The undersigned certifies, to the best of his or her knowledge and belief, that:

- (1) No federal appropriated funds have been paid or will be paid, by or on behalf of the undersigned, to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with the awarding of any federal contract, the making of any Federal grant, the making of any Federal loan, the entering into of any cooperative agreement, and the extension, continuation, renewal, amendment, or modification of any Federal contract, grant, loan, or cooperative agreement.
- (2) If any funds other than Federal appropriated funds have been paid or will be paid to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with this Federal contract, grant, loan, or cooperative agreement, the undersigned shall complete and submit Standard Form-LLL, "Disclosure of Lobbying Activities," in accordance with its instructions.
- (3) The undersigned shall require that the language of this certification be included in the award documents for all subawards at all tiers including subcontracts, subgrants, and contracts under grants, loans, and cooperative agreements and that all subrecipients shall certify and disclose accordingly.

This certification is a material representation of fact upon which reliance was placed when this transaction was made or entered into. Submission of this certification is a prerequisite for making or entering into this transaction imposed by section 1352, Title 31, U.S. Code. Any person who fails to file the required certification shall be subject to a civil penalty of not less than \$10,000 and not more than \$100,000 for each such failure.

### Certification Regarding Nondiscrimination

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative is providing the Certification Regarding Nondiscrimination contained in Exhibit II-6 of the Grant Proposal Guide.

### Certification Regarding Flood Hazard Insurance

Two sections of the National Flood Insurance Act of 1968 (42 USC §4012a and §4106) bar Federal agencies from giving financial assistance for acquisition or construction purposes in any area identified by the Federal Emergency Management Agency (FEMA) as having special flood hazards unless the:

- (1) community in which that area is located participates in the national flood insurance program; and
- (2) building (and any related equipment) is covered by adequate flood insurance.

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant located in FEMA-designated special flood hazard areas is certifying that adequate flood insurance has been or will be obtained in the following situations:

- (1) for NSF grants for the construction of a building or facility, regardless of the dollar amount of the grant; and
- (2) for other NSF Grants when more than \$25,000 has been budgeted in the proposal for repair, alteration or improvement (construction) of a building or facility.

### Certification Regarding Responsible Conduct of Research (RCR)

(This certification is not applicable to proposals for conferences, symposia, and workshops.)

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that, in accordance with the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.B., the institution has a plan in place to provide appropriate training and oversight in the responsible and ethical conduct of research to undergraduates, graduate students and postdoctoral researchers who will be supported by NSF to conduct research.

The undersigned shall require that the language of this certification be included in any award documents for all subawards at all tiers.

AUTHORIZED ORGANIZATIONAL REPRESENTATIVE		SIGNATURE		DATE	
NAME					
TELEPHONE NUMBER	ELECTRONIC MAIL ADDRESS			FAX NUMBER	

\* EAGER - Early-concept Grants for Exploratory Research

\*\* RAPID - Grants for Rapid Response Research

## COVER SHEET FOR PROPOSAL TO THE NATIONAL SCIENCE FOUNDATION

PROGRAM ANNOUNCEMENT/SOLICITATION NO./CLOSING DATE/if not in response to a program announcement/solicitation enter NSF 10-1					<b>FOR NSF USE ONLY</b>	
<b>NSF 09-529</b> <span style="float: right;"><b>01/13/10</b></span>					<b>NSF PROPOSAL NUMBER</b>	
FOR CONSIDERATION BY NSF ORGANIZATION UNIT(S) (Indicate the most specific unit known, i.e. program, division, etc.)						
<b>DUE - CCLI-Phase 2: Expansion</b>						
<b>DATE RECEIVED</b>	<b>NUMBER OF COPIES</b>	<b>DIVISION ASSIGNED</b>	<b>FUND CODE</b>	<b>DUNS#</b> (Data Universal Numbering System)	<b>FILE LOCATION</b>	
				<b>605799469</b>		
EMPLOYER IDENTIFICATION NUMBER (EIN) OR TAXPAYER IDENTIFICATION NUMBER (TIN)		SHOW PREVIOUS AWARD NO. IF THIS IS <input type="checkbox"/> A RENEWAL <input type="checkbox"/> AN ACCOMPLISHMENT-BASED RENEWAL		IS THIS PROPOSAL BEING SUBMITTED TO ANOTHER FEDERAL AGENCY? YES <input type="checkbox"/> NO <input checked="" type="checkbox"/> IF YES, LIST ACRONYM(S)		
<b>916001537</b>						
NAME OF ORGANIZATION TO WHICH AWARD SHOULD BE MADE			ADDRESS OF Awardee ORGANIZATION, INCLUDING 9 DIGIT ZIP CODE			
<b>University of Washington</b>			<b>4333 Brooklyn Ave NE</b>			
AWARDEE ORGANIZATION CODE (IF KNOWN)			<b>SEATTLE, WA 98195-9472</b>			
<b>0037986000</b>						
NAME OF PERFORMING ORGANIZATION, IF DIFFERENT FROM ABOVE			ADDRESS OF PERFORMING ORGANIZATION, IF DIFFERENT, INCLUDING 9 DIGIT ZIP CODE			
PERFORMING ORGANIZATION CODE (IF KNOWN)						
IS Awardee ORGANIZATION (Check All That Apply) (See GPG II.C For Definitions)			<input type="checkbox"/> SMALL BUSINESS <input type="checkbox"/> FOR-PROFIT ORGANIZATION		<input type="checkbox"/> MINORITY BUSINESS <input type="checkbox"/> WOMAN-OWNED BUSINESS <input type="checkbox"/> IF THIS IS A PRELIMINARY PROPOSAL THEN CHECK HERE	
TITLE OF PROPOSED PROJECT <b>Collaborative Research: UTMOST Undergraduate Teaching in Mathematics with Open Software and Textbooks</b>						
REQUESTED AMOUNT \$ <b>84,156</b>		PROPOSED DURATION (1-60 MONTHS) <b>36</b> months		REQUESTED STARTING DATE <b>09/01/10</b>		SHOW RELATED PRELIMINARY PROPOSAL NO. IF APPLICABLE
CHECK APPROPRIATE BOX(ES) IF THIS PROPOSAL INCLUDES ANY OF THE ITEMS LISTED BELOW						
<input type="checkbox"/> BEGINNING INVESTIGATOR (GPG I.G.2) <input type="checkbox"/> HUMAN SUBJECTS (GPG II.D.7) Human Subjects Assurance Number _____ Exemption Subsection _____ or IRB App. Date _____						
<input type="checkbox"/> DISCLOSURE OF LOBBYING ACTIVITIES (GPG II.C.1.e) <input type="checkbox"/> INTERNATIONAL COOPERATIVE ACTIVITIES: COUNTRY/COUNTRIES INVOLVED (GPG II.C.2.j)						
<input type="checkbox"/> PROPRIETARY & PRIVILEGED INFORMATION (GPG I.D, II.C.1.d) <input type="checkbox"/> HIGH RESOLUTION GRAPHICS/OTHER GRAPHICS WHERE EXACT COLOR REPRESENTATION IS REQUIRED FOR PROPER INTERPRETATION (GPG I.G.1)						
<input type="checkbox"/> HISTORIC PLACES (GPG II.C.2.j)						
<input type="checkbox"/> EAGER* (GPG II.D.2) <input type="checkbox"/> RAPID** (GPG II.D.1)						
<input type="checkbox"/> VERTEBRATE ANIMALS (GPG II.D.6) IACUC App. Date _____ PHS Animal Welfare Assurance Number _____						
PI/PD DEPARTMENT <b>Mathematics</b>			PI/PD POSTAL ADDRESS <b>C138 Padelford</b>			
PI/PD FAX NUMBER <b>206-543-0397</b>			<b>Box 354350</b>			
			<b>Seattle, WA 981954350</b>			
			<b>United States</b>			
NAMES (TYPED)	High Degree	Yr of Degree	Telephone Number	Electronic Mail Address		
PI/PD NAME <b>William A Stein</b>	<b>PhD</b>	<b>2000</b>	<b>206-543-1916</b>	<b>wstein@math.washington.edu</b>		
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						

## CERTIFICATION PAGE

### Certification for Authorized Organizational Representative or Individual Applicant:

By signing and submitting this proposal, the Authorized Organizational Representative or Individual Applicant is: (1) certifying that statements made herein are true and complete to the best of his/her knowledge; and (2) agreeing to accept the obligation to comply with NSF award terms and conditions if an award is made as a result of this application. Further, the applicant is hereby providing certifications regarding debarment and suspension, drug-free workplace, lobbying activities (see below), responsible conduct of research, nondiscrimination, and flood hazard insurance (when applicable) as set forth in the NSF Proposal & Award Policies & Procedures Guide, Part I: the Grant Proposal Guide (GPG) (NSF 10-1). Willful provision of false information in this application and its supporting documents or in reports required under an ensuing award is a criminal offense (U. S. Code, Title 18, Section 1001).

### Conflict of Interest Certification

In addition, if the applicant institution employs more than fifty persons, by electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that the institution has implemented a written and enforced conflict of interest policy that is consistent with the provisions of the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.A; that to the best of his/her knowledge, all financial disclosures required by that conflict of interest policy have been made; and that all identified conflicts of interest will have been satisfactorily managed, reduced or eliminated prior to the institution's expenditure of any funds under the award, in accordance with the institution's conflict of interest policy. Conflicts which cannot be satisfactorily managed, reduced or eliminated must be disclosed to NSF.

### Drug Free Work Place Certification

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Drug Free Work Place Certification contained in Exhibit II-3 of the Grant Proposal Guide.

### Debarment and Suspension Certification

(If answer "yes", please provide explanation.)

Is the organization or its principals presently debarred, suspended, proposed for debarment, declared ineligible, or voluntarily excluded from covered transactions by any Federal department or agency?

Yes ☐

No ☒

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Debarment and Suspension Certification contained in Exhibit II-4 of the Grant Proposal Guide.

### Certification Regarding Lobbying

The following certification is required for an award of a Federal contract, grant, or cooperative agreement exceeding \$100,000 and for an award of a Federal loan or a commitment providing for the United States to insure or guarantee a loan exceeding \$150,000.

### Certification for Contracts, Grants, Loans and Cooperative Agreements

The undersigned certifies, to the best of his or her knowledge and belief, that:

- (1) No federal appropriated funds have been paid or will be paid, by or on behalf of the undersigned, to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with the awarding of any federal contract, the making of any Federal grant, the making of any Federal loan, the entering into of any cooperative agreement, and the extension, continuation, renewal, amendment, or modification of any Federal contract, grant, loan, or cooperative agreement.
- (2) If any funds other than Federal appropriated funds have been paid or will be paid to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with this Federal contract, grant, loan, or cooperative agreement, the undersigned shall complete and submit Standard Form-LLL, "Disclosure of Lobbying Activities," in accordance with its instructions.
- (3) The undersigned shall require that the language of this certification be included in the award documents for all subawards at all tiers including subcontracts, subgrants, and contracts under grants, loans, and cooperative agreements and that all subrecipients shall certify and disclose accordingly.

This certification is a material representation of fact upon which reliance was placed when this transaction was made or entered into. Submission of this certification is a prerequisite for making or entering into this transaction imposed by section 1352, Title 31, U.S. Code. Any person who fails to file the required certification shall be subject to a civil penalty of not less than \$10,000 and not more than \$100,000 for each such failure.

### Certification Regarding Nondiscrimination

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative is providing the Certification Regarding Nondiscrimination contained in Exhibit II-6 of the Grant Proposal Guide.

### Certification Regarding Flood Hazard Insurance

Two sections of the National Flood Insurance Act of 1968 (42 USC §4012a and §4106) bar Federal agencies from giving financial assistance for acquisition or construction purposes in any area identified by the Federal Emergency Management Agency (FEMA) as having special flood hazards unless the:

- (1) community in which that area is located participates in the national flood insurance program; and
- (2) building (and any related equipment) is covered by adequate flood insurance.

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant located in FEMA-designated special flood hazard areas is certifying that adequate flood insurance has been or will be obtained in the following situations:

- (1) for NSF grants for the construction of a building or facility, regardless of the dollar amount of the grant; and
- (2) for other NSF Grants when more than \$25,000 has been budgeted in the proposal for repair, alteration or improvement (construction) of a building or facility.

### Certification Regarding Responsible Conduct of Research (RCR)

(This certification is not applicable to proposals for conferences, symposia, and workshops.)

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that, in accordance with the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.B., the institution has a plan in place to provide appropriate training and oversight in the responsible and ethical conduct of research to undergraduates, graduate students and postdoctoral researchers who will be supported by NSF to conduct research.

The undersigned shall require that the language of this certification be included in any award documents for all subawards at all tiers.

AUTHORIZED ORGANIZATIONAL REPRESENTATIVE		SIGNATURE		DATE	
NAME					
TELEPHONE NUMBER	ELECTRONIC MAIL ADDRESS			FAX NUMBER	

\* EAGER - Early-concept Grants for Exploratory Research

\*\* RAPID - Grants for Rapid Response Research

# COVER SHEET FOR PROPOSAL TO THE NATIONAL SCIENCE FOUNDATION

PROGRAM ANNOUNCEMENT/SOLICITATION NO./CLOSING DATE/if not in response to a program announcement/solicitation enter NSF 10-1					<b>FOR NSF USE ONLY</b>	
<b>NSF 09-529</b> <span style="float: right;"><b>01/13/10</b></span>					<b>NSF PROPOSAL NUMBER</b>	
FOR CONSIDERATION BY NSF ORGANIZATION UNIT(S) (Indicate the most specific unit known, i.e. program, division, etc.)						
<b>DUE - CCLI-Phase 2: Expansion</b>						
<b>DATE RECEIVED</b>	<b>NUMBER OF COPIES</b>	<b>DIVISION ASSIGNED</b>	<b>FUND CODE</b>	<b>DUNS#</b> (Data Universal Numbering System)	<b>FILE LOCATION</b>	
				<b>007431505</b>		
EMPLOYER IDENTIFICATION NUMBER (EIN) OR TAXPAYER IDENTIFICATION NUMBER (TIN)		SHOW PREVIOUS AWARD NO. IF THIS IS <input type="checkbox"/> A RENEWAL <input type="checkbox"/> AN ACCOMPLISHMENT-BASED RENEWAL		IS THIS PROPOSAL BEING SUBMITTED TO ANOTHER FEDERAL AGENCY? YES <input type="checkbox"/> NO <input checked="" type="checkbox"/> IF YES, LIST ACRONYM(S)		
<b>846000555</b>						
NAME OF ORGANIZATION TO WHICH AWARD SHOULD BE MADE			ADDRESS OF Awardee ORGANIZATION, INCLUDING 9 DIGIT ZIP CODE			
<b>University of Colorado at Boulder</b>			<b>3100 Marine Street, Room 481</b>			
AWARDEE ORGANIZATION CODE (IF KNOWN)			<b>572 UCB</b>			
<b>0013706000</b>			<b>Boulder, CO 80309-0572</b>			
NAME OF PERFORMING ORGANIZATION, IF DIFFERENT FROM ABOVE			ADDRESS OF PERFORMING ORGANIZATION, IF DIFFERENT, INCLUDING 9 DIGIT ZIP CODE			
PERFORMING ORGANIZATION CODE (IF KNOWN)						
IS Awardee ORGANIZATION (Check All That Apply) (See GPG II.C For Definitions) <input type="checkbox"/> SMALL BUSINESS <input type="checkbox"/> MINORITY BUSINESS <input type="checkbox"/> IF THIS IS A PRELIMINARY PROPOSAL THEN CHECK HERE <input type="checkbox"/> FOR-PROFIT ORGANIZATION <input type="checkbox"/> WOMAN-OWNED BUSINESS						
TITLE OF PROPOSED PROJECT <b>Collaborative Research: UTMOST: Undergraduate Teaching in Mathematics with Open Software and Textbooks</b>						
REQUESTED AMOUNT \$ <b>0</b>		PROPOSED DURATION (1-60 MONTHS) <b>36</b> months		REQUESTED STARTING DATE <b>09/01/10</b>		SHOW RELATED PRELIMINARY PROPOSAL NO. IF APPLICABLE
CHECK APPROPRIATE BOX(ES) IF THIS PROPOSAL INCLUDES ANY OF THE ITEMS LISTED BELOW <input checked="" type="checkbox"/> BEGINNING INVESTIGATOR (GPG I.G.2) <input checked="" type="checkbox"/> HUMAN SUBJECTS (GPG II.D.7) Human Subjects Assurance Number _____ Exemption Subsection _____ or IRB App. Date <b>Pending</b> <input type="checkbox"/> DISCLOSURE OF LOBBYING ACTIVITIES (GPG II.C.1.e) <input type="checkbox"/> PROPRIETARY & PRIVILEGED INFORMATION (GPG I.D, II.C.1.d) <input type="checkbox"/> HISTORIC PLACES (GPG II.C.2.j) <input type="checkbox"/> EAGER* (GPG II.D.2) <input type="checkbox"/> RAPID** (GPG II.D.1) <input type="checkbox"/> VERTEBRATE ANIMALS (GPG II.D.6) IACUC App. Date _____ PHS Animal Welfare Assurance Number _____ <input type="checkbox"/> INTERNATIONAL COOPERATIVE ACTIVITIES: COUNTRY/COUNTRIES INVOLVED (GPG II.C.2.j) <input type="checkbox"/> HIGH RESOLUTION GRAPHICS/OTHER GRAPHICS WHERE EXACT COLOR REPRESENTATION IS REQUIRED FOR PROPER INTERPRETATION (GPG I.G.1)						
PI/PD DEPARTMENT <b>Ethnography &amp; Evaluation Research/CARTSS</b>			PI/PD POSTAL ADDRESS <b>572 UCB</b>			
PI/PD FAX NUMBER <b>303-492-2154</b>			<b>Boulder, CO 803090580</b>			
			<b>United States</b>			
NAMES (TYPED)	High Degree	Yr of Degree	Telephone Number	Electronic Mail Address		
PI/PD NAME <b>Marja-Liisa Hassi</b>	<b>PhD</b>	<b>2001</b>	<b>303-735-6168</b>	<b>marja-liisa.hassi@colorado.edu</b>		
CO-PI/PD <b>Sandra L Laursen</b>	<b>PhD</b>	<b>1990</b>	<b>303-735-2942</b>	<b>sandra.laursen@colorado.edu</b>		
CO-PI/PD						
CO-PI/PD						
CO-PI/PD						



## CERTIFICATION PAGE

### Certification for Authorized Organizational Representative or Individual Applicant:

By signing and submitting this proposal, the Authorized Organizational Representative or Individual Applicant is: (1) certifying that statements made herein are true and complete to the best of his/her knowledge; and (2) agreeing to accept the obligation to comply with NSF award terms and conditions if an award is made as a result of this application. Further, the applicant is hereby providing certifications regarding debarment and suspension, drug-free workplace, lobbying activities (see below), responsible conduct of research, nondiscrimination, and flood hazard insurance (when applicable) as set forth in the NSF Proposal & Award Policies & Procedures Guide, Part I: the Grant Proposal Guide (GPG) (NSF 10-1). Willful provision of false information in this application and its supporting documents or in reports required under an ensuing award is a criminal offense (U. S. Code, Title 18, Section 1001).

### Conflict of Interest Certification

In addition, if the applicant institution employs more than fifty persons, by electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that the institution has implemented a written and enforced conflict of interest policy that is consistent with the provisions of the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.A; that to the best of his/her knowledge, all financial disclosures required by that conflict of interest policy have been made; and that all identified conflicts of interest will have been satisfactorily managed, reduced or eliminated prior to the institution's expenditure of any funds under the award, in accordance with the institution's conflict of interest policy. Conflicts which cannot be satisfactorily managed, reduced or eliminated must be disclosed to NSF.

### Drug Free Work Place Certification

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Drug Free Work Place Certification contained in Exhibit II-3 of the Grant Proposal Guide.

### Debarment and Suspension Certification

(If answer "yes", please provide explanation.)

Is the organization or its principals presently debarred, suspended, proposed for debarment, declared ineligible, or voluntarily excluded from covered transactions by any Federal department or agency?

Yes ☐

No ☒

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant is providing the Debarment and Suspension Certification contained in Exhibit II-4 of the Grant Proposal Guide.

### Certification Regarding Lobbying

The following certification is required for an award of a Federal contract, grant, or cooperative agreement exceeding \$100,000 and for an award of a Federal loan or a commitment providing for the United States to insure or guarantee a loan exceeding \$150,000.

### Certification for Contracts, Grants, Loans and Cooperative Agreements

The undersigned certifies, to the best of his or her knowledge and belief, that:

- (1) No federal appropriated funds have been paid or will be paid, by or on behalf of the undersigned, to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with the awarding of any federal contract, the making of any Federal grant, the making of any Federal loan, the entering into of any cooperative agreement, and the extension, continuation, renewal, amendment, or modification of any Federal contract, grant, loan, or cooperative agreement.
- (2) If any funds other than Federal appropriated funds have been paid or will be paid to any person for influencing or attempting to influence an officer or employee of any agency, a Member of Congress, an officer or employee of Congress, or an employee of a Member of Congress in connection with this Federal contract, grant, loan, or cooperative agreement, the undersigned shall complete and submit Standard Form-LLL, "Disclosure of Lobbying Activities," in accordance with its instructions.
- (3) The undersigned shall require that the language of this certification be included in the award documents for all subawards at all tiers including subcontracts, subgrants, and contracts under grants, loans, and cooperative agreements and that all subrecipients shall certify and disclose accordingly.

This certification is a material representation of fact upon which reliance was placed when this transaction was made or entered into. Submission of this certification is a prerequisite for making or entering into this transaction imposed by section 1352, Title 31, U.S. Code. Any person who fails to file the required certification shall be subject to a civil penalty of not less than \$10,000 and not more than \$100,000 for each such failure.

### Certification Regarding Nondiscrimination

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative is providing the Certification Regarding Nondiscrimination contained in Exhibit II-6 of the Grant Proposal Guide.

### Certification Regarding Flood Hazard Insurance

Two sections of the National Flood Insurance Act of 1968 (42 USC §4012a and §4106) bar Federal agencies from giving financial assistance for acquisition or construction purposes in any area identified by the Federal Emergency Management Agency (FEMA) as having special flood hazards unless the:

- (1) community in which that area is located participates in the national flood insurance program; and
- (2) building (and any related equipment) is covered by adequate flood insurance.

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative or Individual Applicant located in FEMA-designated special flood hazard areas is certifying that adequate flood insurance has been or will be obtained in the following situations:

- (1) for NSF grants for the construction of a building or facility, regardless of the dollar amount of the grant; and
- (2) for other NSF Grants when more than \$25,000 has been budgeted in the proposal for repair, alteration or improvement (construction) of a building or facility.

### Certification Regarding Responsible Conduct of Research (RCR)

(This certification is not applicable to proposals for conferences, symposia, and workshops.)

By electronically signing the NSF Proposal Cover Sheet, the Authorized Organizational Representative of the applicant institution is certifying that, in accordance with the NSF Proposal & Award Policies & Procedures Guide, Part II, Award & Administration Guide (AAG) Chapter IV.B., the institution has a plan in place to provide appropriate training and oversight in the responsible and ethical conduct of research to undergraduates, graduate students and postdoctoral researchers who will be supported by NSF to conduct research.

The undersigned shall require that the language of this certification be included in any award documents for all subawards at all tiers.

AUTHORIZED ORGANIZATIONAL REPRESENTATIVE		SIGNATURE		DATE	
NAME					
TELEPHONE NUMBER	ELECTRONIC MAIL ADDRESS			FAX NUMBER	

\* EAGER - Early-concept Grants for Exploratory Research

\*\* RAPID - Grants for Rapid Response Research

## NSF FORM 1295: PROJECT DATA FORM

**NATIONAL SCIENCE FOUNDATION**  
**Division of Undergraduate Education**

**NSF FORM 1295: PROJECT DATA FORM**

The instructions and codes to be used in completing this form are provided in Appendix II.

1. **Program-track** to which the Proposal is submitted: CCLI-Phase 2: Expansion
2. Name of **Principal Investigator/Project Director** (as shown on the Cover Sheet):  
Hassi, Marja-Liisa
3. Name of submitting **Institution** (as shown on Cover Sheet):  
University of Colorado at Boulder
4. **Other Institutions** involved in the project's operation:  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_

**Project Data:**

- A. Major Discipline Code: 21
- B. Academic Focus Level of Project: BO
- C. Highest Degree Code: D
- D. Category Code: --
- E. Business/Industry Participation Code: NA
- F. Audience Code: F \_\_\_\_\_
- G. Institution Code: PUBL
- H. Strategic Area Code: \_\_\_\_\_
- I. Project Features: C I \_\_\_\_\_

Estimated number in each of the following categories to be directly affected by the activities of the project during its operation:

- J. Undergraduate Students: 1000
- K. Pre-college Students: \_\_\_\_\_
- L. College Faculty: 10
- M. Pre-college Teachers: \_\_\_\_\_
- N. Graduate Students: 0

## UTMOST Project Summary

This project will demonstrate the use of Sage, which is comprehensive free open source mathematics software for mathematics, coupled with existing free open textbooks, as a tool for faculty and institutions to more easily bring the power of mathematical software to their students. Authors of open source software and open textbooks provide licenses that permit free copying and modifications of their work, allowing others to modify or extend them to suit their needs or make improvements. Primarily UTMOST will convert existing open textbooks into web-based electronic texts that integrate traditional mathematical exposition with Sage code and hands-on demonstrations. Ten different undergraduate institutions will help test and refine these materials using a comprehensive, professional evaluation procedure. The main goal driving this project is to create technical and pedagogical tools and methods that greatly simplify the deployment and use of powerful software to increase learning and experimentation in undergraduate mathematics.

### INTELLECTUAL MERIT

Research has shown that powerful software for mathematics can increase a student's understanding. But despite decades of experience with these programs, they have not had a broad transformative effect on undergraduate mathematics education. Cost, license restrictions and weak textbook support are significant obstacles to the adoption of mathematics software in a course. This project will use free comprehensive software, which by design only requires a student to have a connected web browser. By converting open textbooks to electronic worksheets integrated with software, UTMOST will give students the full power of the software, available in their textbook for interactive demonstrations and experimentation. The goal is to make it easier for institutions, faculty and students to benefit from mathematics software in their courses.

UTMOST will select ten institutions as test sites. They will represent a wide variety of institutional profiles and will include schools serving underrepresented and disadvantaged student populations. In the first year, UTMOST will convert three open textbooks to Sage worksheets, enhanced with Sage code and interactive demonstrations. As part of these conversions, UTMOST will create a system others can use to author similar materials. Five test sites will use these materials in their courses in the second year. Work will continue in the second year to convert other open textbooks. For the third year, five more test sites will join the project, so materials will be in use at all ten institutions. During the second and third years, the project will refine the materials, and their use, based on workshops with faculty from the test sites, and a formative evaluation.

Members of the project team have extensive, wide-ranging and overlapping experience in undergraduate teaching, software development, textbook authoring, classroom teaching with mathematics software, assessing mathematics education and conducting original research in mathematics, and come from a variety of different institutions. The project will professionally assess the adoption and use of these materials, including their effect in the classroom. The result will be a refined process that other authors and instructors can employ to create and use similar materials.

### BROADER IMPACTS

Free open source software and open textbooks decrease the cost of mathematics education for students and institutions. This is a critical consideration for institutions such as community colleges and those serving disadvantaged groups of students. Through the project's selection of ten test sites, these institutions and students will participate in refining the project's materials and their use. This project will determine effective ways to deliver these materials and tools to institutions and students, while creating a procedure that will allow others to simply and efficiently produce similar materials. With vibrant websites and communities already in place, and through workshops and short courses, UTMOST will disseminate widely the procedures for using and creating these materials, making it easier for institutions, faculty and students to benefit from mathematics software in their courses.

## TABLE OF CONTENTS

For font size and page formatting specifications, see GPG section II.B.2.

	Total No. of Pages	Page No.* (Optional)*
Cover Sheet for Proposal to the National Science Foundation		
Project Summary (not to exceed 1 page)	1	
Table of Contents	1	
Project Description (Including Results from Prior NSF Support) (not to exceed 15 pages) <b>(Exceed only if allowed by a specific program announcement/solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	21	
References Cited		
Biographical Sketches (Not to exceed 2 pages each)	4	
Budget (Plus up to 3 pages of budget justification)	0	
Current and Pending Support	1	
Facilities, Equipment and Other Resources	0	
Special Information/Supplementary Documentation	0	
Appendix (List below. ) <b>(Include only if allowed by a specific program announcement/ solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>		
Appendix Items:		

\*Proposers may select any numbering mechanism for the proposal. The entire proposal however, must be paginated. Complete both columns only if the proposal is numbered consecutively.

## TABLE OF CONTENTS

For font size and page formatting specifications, see GPG section II.B.2.

	Total No. of Pages	Page No.* (Optional)*
Cover Sheet for Proposal to the National Science Foundation		
Project Summary (not to exceed 1 page)	_____	_____
Table of Contents	1	_____
Project Description (Including Results from Prior NSF Support) (not to exceed 15 pages) <b>(Exceed only if allowed by a specific program announcement/solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	0	_____
References Cited	_____	_____
Biographical Sketches (Not to exceed 2 pages each)	2	_____
Budget (Plus up to 3 pages of budget justification)	5	_____
Current and Pending Support	1	_____
Facilities, Equipment and Other Resources	1	_____
Special Information/Supplementary Documentation	0	_____
Appendix (List below. ) <b>(Include only if allowed by a specific program announcement/ solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	_____	_____
Appendix Items:		

\*Proposers may select any numbering mechanism for the proposal. The entire proposal however, must be paginated. Complete both columns only if the proposal is numbered consecutively.

## TABLE OF CONTENTS

For font size and page formatting specifications, see GPG section II.B.2.

	Total No. of Pages	Page No.* (Optional)*
Cover Sheet for Proposal to the National Science Foundation		
Project Summary (not to exceed 1 page)	_____	_____
Table of Contents	1	_____
Project Description (Including Results from Prior NSF Support) (not to exceed 15 pages) <b>(Exceed only if allowed by a specific program announcement/solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	0	_____
References Cited	_____	_____
Biographical Sketches (Not to exceed 2 pages each)	2	_____
Budget (Plus up to 3 pages of budget justification)	4	_____
Current and Pending Support	1	_____
Facilities, Equipment and Other Resources	2	_____
Special Information/Supplementary Documentation	0	_____
Appendix (List below. ) <b>(Include only if allowed by a specific program announcement/ solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	_____	_____
Appendix Items:		

\*Proposers may select any numbering mechanism for the proposal. The entire proposal however, must be paginated. Complete both columns only if the proposal is numbered consecutively.

## TABLE OF CONTENTS

For font size and page formatting specifications, see GPG section II.B.2.

	Total No. of Pages	Page No.* (Optional)*
Cover Sheet for Proposal to the National Science Foundation		
Project Summary (not to exceed 1 page)	_____	_____
Table of Contents	1	_____
Project Description (Including Results from Prior NSF Support) (not to exceed 15 pages) <b>(Exceed only if allowed by a specific program announcement/solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	0	_____
References Cited	_____	_____
Biographical Sketches (Not to exceed 2 pages each)	1	_____
Budget (Plus up to 3 pages of budget justification)	4	_____
Current and Pending Support	1	_____
Facilities, Equipment and Other Resources	2	_____
Special Information/Supplementary Documentation	0	_____
Appendix (List below. ) <b>(Include only if allowed by a specific program announcement/ solicitation or if approved in advance by the appropriate NSF Assistant Director or designee)</b>	_____	_____
Appendix Items:		

\*Proposers may select any numbering mechanism for the proposal. The entire proposal however, must be paginated. Complete both columns only if the proposal is numbered consecutively.



## 1. UTMOST PROJECT SUMMARY

### UNDERGRADUATE TEACHING IN MATHEMATICS WITH OPEN SOFTWARE AND TEXTBOOKS

Software for mathematical explorations, including computer algebra systems (CAS), have held great promise for education since their first appearance in the 1960s (Reduce, Macsyma (47; 59)) and the introduction of Maple and Mathematica in the 1980s (45; 79). Currently, CAS are widely found in the undergraduate classroom and a considerable amount of mathematics education research has focused on the use of CAS in learning undergraduate mathematics. Studies have documented the improvement in students' understanding (30; 31; 40; 52). For example, the use of technology allows students to avoid tedious or unreasonable computations, avoid long tables of integrals or Laplace transforms, visualize complicated 2d plots and 3d mathematical objects, and easily deal with unweildy matrices in linear algebra. There is strong agreement that most calculus students should learn the basic techniques of integration; however, CAS replaces the lengthy tables of integrals that were commonplace two decades ago. In addition, technology has allowed a qualitative approach to teaching differential equations. Most differential equations cannot be solved explicitly, but numerical and graphical software has enabled teachers to incorporate a qualitative approach in the courses that they teach (6). The ability to make large computations, quickly and without errors, with graphical output, can greatly aid a students' understanding of difficult ideas in mathematics and provides them with an incredible capacity for experimentation and conjecture.

Computer algebra systems are now common in the undergraduate classroom, yet we rarely see a seamless integration with the curriculum. To accommodate competing commercial systems that divide the market, textbooks typically offer supplements for several different CAS, or they are "technology-enhanced" with generic sidebars; otherwise the textbook can only be marketed to the subset of the audience that licenses a particular computer algebra system. Licensing restrictions for campus use, the expense of personal copies, and underpowered hardware often mean that students can only work with commercial software in campus labs. Some institutions are unable to afford the cost of building such labs for their students.

There have been efforts at seamless integration of technology and curriculum. An example of such an experiment is the Calculus & Mathematica project, which generated much excitement in the early 1990s and had demonstrable success in helping diverse students learn more effectively. However, today its use seems limited to the two institutions where it originated (50; 76). Likewise, the use of interactive Java applets to support teaching mathematics (such as (2; 9; 32)) does not seem to have been widely adopted. The undergraduate curriculum has not seen the broad transformative effect of these powerful tools for increasing the learning and understanding of mathematics. What is needed to increase the uptake of software for mathematical exploration across the spectrum of undergraduate education so we will see the benefits that isolated, successful pilot programs have predicted?

**1.1. An open approach.** Sage (4; 68) is free open source software designed to be an alternative to Magma, Maple, Mathematica and Matlab. Coinciding with the development of Sage, there is a general movement to freely-available open textbooks that includes many quality texts in mathematics ((11; 51), Section 5.1.3). Our proposition is that freely-available open software, open textbooks, and other open curricular material can allow teachers everywhere to transform the undergraduate mathematics curriculum by tightly and seamlessly integrating mathematics software with more traditional curricular materials. We will test this hypothesis by integrating Sage into existing open textbooks and other curricular materials, placing the full computational power of Sage *directly into* a student's text, usable at all times and from anywhere simply via a web browser. For the institution and the instructor, the cost and time-consuming licensing inconveniences of commercial software are removed by open software, freely accessible with no license restrictions. Sage can also be used remotely from a standard web browser, eliminating the expenses and inconveniences of a dedicated local computer lab. Furthermore, the essential nature of open software means that

curricular decisions and needs can drive the development of the software, with the classroom teacher actively advising, or actually doing, the software development. Likewise, open curricular materials can be adapted to course needs and teacher preferences, and can be distributed with the software freely in an integrated package. Leveraging these inherent advantages of an open approach to software and curricular materials, the promise of mathematical software in education can be fully realized by faculty and students. Our work will create and disseminate a model for this integration, addressing both the pedagogical and technical aspects, so that other faculty authors can realize the advantages in their own curricular materials and courses.

More specifically, UTMOST will build and test a model for easily integrating open mathematics software and open educational materials into the mathematics curriculum and classroom as follows.

- We plan to create a system that makes it easy for authors to convert open textbooks and other curricular materials to Sage worksheets interspersing runnable interactive demonstrations and exercises and live Sage code with publication-quality typeset mathematics.
- We plan to convert existing mature open textbooks to this format and create new curricular materials targeting this format, as demonstrations and tests of both the technical and pedagogical aspects of this new approach.
- We plan to partner with ten diverse institutions to test these materials in a wide variety of courses, while providing support for their use and assistance for the creation of new materials.
- We plan to evaluate the effectiveness of our model for making it easy to adopt open mathematics software and textbooks and making it easy to create integrated open curricular materials, and we plan to measure the resulting impact on teaching practices and the learning of mathematics with the expert assistance of professional evaluators.

In addition to workshops and other presentations, materials created or enhanced by UTMOST will be widely distributed with open licenses as much as possible. The materials will be available through the global Sage website ([sagemath.org](http://sagemath.org), (68)). As appropriate, they will also be available in Sage itself or through a new open textbook website created at the American Institute of Mathematics (1) as part of this grant.

## 2. TRENDS IN SCIENTIFIC COMMUNICATION

The cost of academic research journals, especially in science, combined with dissemination restrictions imposed by copyright law and new dissemination possibilities afforded by technology, are collectively referred to by librarians as the “serials crisis” (8). Faculty have come a long way in their efforts to return scientific publication to a free exchange of ideas. Electronic journals and public repositories now publish articles with licenses that explicitly allow for sharing new results easily via the Internet without distribution fees. Government initiatives, such as the Public Access Policy of the National Institutes of Health (49) and the Policy Forum on Public Access of the White House Office of Science and Technology (78), are working to accelerate this trend.

Following on the sea change in research publication, the next wave is open textbooks. Faculty are all too familiar with the problems that plague commercial textbook publication, such as high prices, edition churn, and orphaned works. Open licenses are now being used to assert control of these critical resources for education, with faculty in mathematics, computer science and business as the leaders (20; 72). Government is poised to accelerate this open textbook trend at all levels, with Senator Durbin proposing legislation directing the Department of Education to award grants for the creation of open textbooks by faculty (17), Washington State’s initiative to provide open textbooks for the eighty highest-enrollment courses in their community college system (77), and California’s initiative to create free digital textbooks for its high schools (64).

With the emergence of viable and comprehensive open source software for mathematics, there is now a spectacular opportunity for mathematics teachers to use, extend, and create this important

software for mathematics education and shape it to reach its full potential in the service of educating students. UTMOST will create an easy path for all faculty to make the initial transition to open software, open textbooks, and open curricular materials in their courses. This path will make it easy for diverse schools and faculty to employ mathematical software to transform the classroom into an interactive laboratory which takes the study of mathematics to a new level.

**2.1. Imagine this!** A student is learning about row-reducing matrices in a beginning linear algebra course. The electronic version of their textbook is an online Sage worksheet they can view from anywhere. Mathematical equations, with publication-quality typesetting, describe the procedure. An interactive demonstration, embedded in the worksheet where an example normally would be, allows the student to step through row-reducing a matrix that was generated on-the-fly. When ready to guide the procedure themselves, the student may choose the row operation to apply at each step of the reduction. The correct notation for each operation is displayed and the operation itself is highlighted with color-coded entries in the displayed matrix. Another example shows the student how to use a built-in Sage command to row-reduce a matrix. With a single click, the student creates an empty code cell under the example to experiment with the command.<sup>i</sup>

i

In class, the instructor does one simple example on the board. Then the instructor opens a Sage worksheet, displaying the same demonstration that is in every student's electronic textbook. Students guide the choice of row operations at each step for several example matrices of increasing complexity. At the end of class, the instructor clicks a button to publish the work from that day's class session to the class Sage server. After class, students view the worksheet as they review their notes. They can also, with a click, copy the worksheet into their notes, as well as annotate or change it.

The book's exercises include an interactive problem generator that creates matrices of student-specified sizes and complexity for the student to row-reduce. There is a "Solution" button which generates a step-by-step solution. An advanced exercise guides a student through investigating numerical issues that arise in row reduction. By changing one parameter within a command, the matrices track numeric error bounds via interval arithmetic, and the student discovers that numerical errors can be a significant problem for some matrices.

A group exercise asks students to collaboratively write and test a short function to implement row-reduction using row operations. The student clicks a button to open a new Sage worksheet and types in a few lines using Sage matrices and commands. The student evaluates the code with a single click. Satisfied with their work, the student clicks another button, publishing the worksheet to the rest of the group for testing. Later that evening, the student checks the worksheet and sees that other students have tested the function, found an error and repaired it.

The next week, the instructor logs into the online Sage server with a web browser and looks over all of the published worksheets for the group projects. The instructor annotates each worksheet online, using an embedded word processor that supports mathematical typesetting (75; 12).

The instructor writes a quiz covering row-reduction techniques. Inside of the  $\text{\LaTeX}$  file for the quiz, the instructor includes a Sage command to create a simple matrix in reduced-row echelon form, which will be the *answer* to a quiz problem. The instructor then uses Sage commands inside his  $\text{\LaTeX}$  file to do several simple row operations using integers to transform the answer matrix to the matrix the students will row-reduce. The embedded Sage commands are executed automatically when the quiz is formatted with  $\text{\LaTeX}$ , and the resulting question matrix is automatically incorporated in the printed quiz, while the answer matrix and a detailed solution are automatically incorporated in the answer key.

<sup>i</sup>TODO for Jason on screenshot: Make sure the color is dark enough to look good on black and white. Highlight the rows by surrounding the row with a box. Color the  $R_2$  and  $R_3$  above the arrow to emphasize which row is which.

Section RREF Reduced Row-Echelon Form - Mozilla Firefox

File Edit View History Bookmarks Tools Help

http://linear.ups.edu/jsmath/latest/fcla-jsmath-latest118.html#x19-340C

To write the set of solution vectors in set notation, we have

$$S = \left\{ \begin{bmatrix} 3-x_3 \\ 2+x_3 \\ x_3 \end{bmatrix} \mid x_3 \in \mathbb{C} \right\}$$

We'll learn more in the next section about systems with infinitely many solutions and how to express their solution sets. Right now, you might look back at [Example 1S](#). ☒

Generate new matrix

Operation:

Row A:  Row B:  Multiple:

$$\begin{pmatrix} 1 & 2 & -1 & -3 \\ 0 & -1 & 2 & 1 \\ 0 & 4 & -8 & -4 \end{pmatrix} \xrightarrow{4R_2+R_3 \rightarrow R_3} \begin{pmatrix} 1 & 2 & -1 & -3 \\ 0 & -1 & 2 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

**Theorem RREFU**  
**Reduced Row-Echelon Form is Unique**  
 Suppose that  $A$  is an  $m \times n$  matrix and that  $B$  and  $C$  are  $m \times n$  matrices that are row-equivalent to  $A$  and in reduced row-echelon form. Then  $B = C$ . ☐

**Proof** We need to begin with no assumptions about any relationships between  $B$  and  $C$ , other than they are both in reduced row-echelon form, and they are both row-equivalent to  $A$ .

If  $B$  and  $C$  are both row-equivalent to  $A$ , then they are row-equivalent to each other. Repeated row operations on a matrix combine the rows with each other using operations that are linear, and are identical in each column. A key observation for this proof is that each individual row of  $B$  is linearly related to the rows of  $C$ . This relationship is different for each row of  $B$ , but once we fix a row, the relationship is the same across columns. More precisely, there are scalars  $\delta_{ik}$ ,  $1 \leq i, k \leq m$  such that for any  $1 \leq i \leq m$ ,  $1 \leq j \leq n$ ,

$$[B]_{ij} = \sum_{k=1}^m \delta_{ik} [C]_{kj}$$

You should read this as saying that an entry of row  $i$  of  $B$  (in column  $j$ ) is a linear function of the entries of all the rows of  $C$  that are also in column  $j$ , and the scalars ( $\delta_{ik}$ ) depend on which row of  $B$  we are considering (the  $i$  subscript on  $\delta_{ik}$ ), but are the same for every column (no dependence on  $j$  in  $\delta_{ik}$ ). This idea may be complicated now, but will feel more familiar once we discuss "linear combinations" ([Definition LCCV](#)) and jsMath

Find:  Previous Next Highlight all Match case

Done

Prototype of a Sage-enhanced mathematics open textbook

### 3. WHY SAGE?

Sage is a natural choice for software to realize the benefits of an open approach to the undergraduate mathematics curriculum. Sage is a comprehensive program with an open development process, a modular design philosophy, an easy-to-use interface utilizing standard web browsers, an industry-standard programming language, and tight integration with  $\text{\LaTeX}$ . These are consequences of

a steadfast commitment to open design principles and concrete examples of the benefits of this approach. With an open license, the ability to run on a remote server, and a platform-independent interface, Sage removes substantial financial and logistical barriers to classroom use of mathematics software. In this section, we describe the many features of Sage that make it a good choice for integrating mathematics software with open textbooks and other curricular materials.

ii

ii

**3.1. A comprehensive program.** Sage is becoming a comprehensive program for mathematics. Its modular design allows symbolic, exact, and numerical approaches to mathematics to coexist equally. Mathematical objects, such as functions, differential equations, rings, fields, modules, and vector spaces are “objects” that look and behave as their abstract mathematical definitions intend. Sage has been designed from the outset to incorporate many different computational strategies, and so does not rely solely on a single computational strategy, such as pattern-matching, which favors symbolic computation, or floating-point numbers, which favors numerical work.

Institutional, departmental, and course-by-course decisions about the use of a CAS require a commitment to a particular vendor’s vision for the curriculum. With a modular design that allows for packages specializing in different approaches, Sage can seamlessly support many approaches to computationally exploring mathematical problems. Additions and extensions to Sage, driven by real curricular needs, can be easily and quickly incorporated. As individuals and institutions extend the software, the entire mathematics community benefits from a comprehensive program that students and faculty can employ in courses ranging from pre-calculus and introductory statistics through advanced courses like abstract algebra and number theory, as well as in graduate courses and professional careers.

**3.2. Curriculum and open development.** The closed development process for commercial software creates a high barrier for teachers and students to alter or extend the software to meet their curricular needs. For example, while external extensions, such as libraries or packages, can extend proprietary systems, these must be purchased, distributed, and installed by every end-user. However, an open development process allows students and faculty to shape the core technology in a timely fashion to support the transformation of teaching and learning of mathematics on a broad scale. Software developed openly and collaboratively, such as Sage, allows the teaching and learning of mathematics to drive the technology, rather than the technology driving the teaching and learning. Two concrete examples of this important principle are given in Section 4.

**3.3. Building the car, not reinventing the wheel.** The genius of Sage is the way it unifies over one hundred mature, best-of-breed, open source packages. These packages range from focused libraries that excel at specific types of computations (e.g., Fast Library for Number Theory for the world’s fastest implementation of integer polynomial arithmetic (21), the Integer Matrix Library for the fastest implementation of solutions to linear systems over the rationals (33), or M4RI for the fastest implementation of exact computations with binary matrices (43)) to complete applications or general libraries for broad areas of mathematics (e.g., R for statistics, GAP for group theory, and SciPy for numeric scientific computations (23; 58; 65)). Sage ties these packages into a single open source system with a consistent interface, making it easy for a teacher or student to smoothly explore vast areas of mathematics seamlessly, using the best tools under the hood for each computation.

---

<sup>ii</sup>Jason says: I reordered the following sections, because it seemed like the comprehensive section naturally goes with the building the car section, which is naturally followed by the glue language section (Python). However, this pushes the notebook section and the open development section towards the bottom, which seems to downplay their importance. I’m not sure what the right order here should be.

Rob says: I moved curriculum up (important for the grant) and Python down (programming is way down the list for the grant).

As a student moves from course to course, the Sage notebook interface and commands remain consistent, even if the particular computations relevant to a new course may be performed by an entirely different package under the hood.

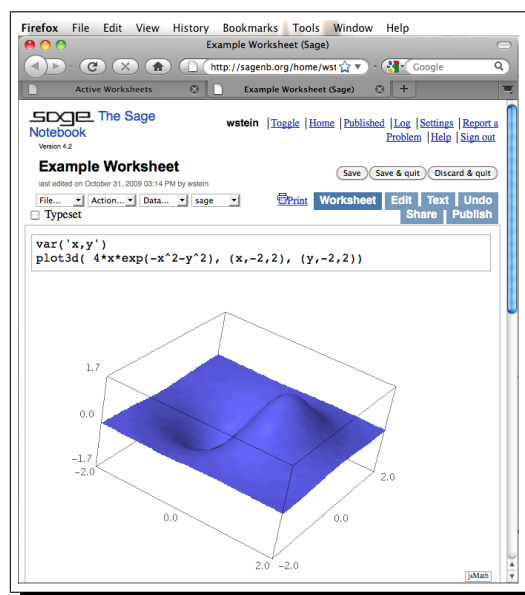
**3.4. Sage anytime, anywhere.** Sage's notebook interface allows a student to communicate with a Sage server through a standard web browser—interactively running commands, viewing textual and graphic output, and annotating their computations with an online word processor that supports mathematical typesetting. The notebook interface removes many of the logistical barriers to using software in the study of mathematics. A student can employ the full power of Sage using a remote Sage server with only a web browser and a minimal network connection on a desktop computer, a small laptop or netbook, or even a cell phone (62)! This flexibility means that instead of an institution providing an expensive lab of machines with commercial software that can only be used on the dedicated computers, most any computer located anywhere can harness the full power of Sage.

<sup>iii</sup> The Sage notebook interface relies heavily on industry-standard Javascript and acts as a web application similar to Google Docs, GMail, or wiki software. Students have designed and implemented much of the current notebook. For example, Tim Dumol, a high school student in the Philippines, has been a very active developer in Fall 2009.

Every copy of Sage includes the Sage server software. To establish a local server, colleges can download and use the ready-made Sage virtual computer image on a computer that supports their needs. There are also publicly-available servers that can be used to support students and classes. The flagship public Sage server is [sagenb.org](http://sagenb.org), a \$100,000 rack of servers located at the University of Washington that was fully funded by an NSF SCREMS grant (DMS-0821725), and is currently home to over 21,000 accounts. Because it is publicly accessible, students from the poorest universities all over the world are running computations on the same version of Sage, on the same hardware cluster, with leading researchers in computational number theory. Constructed in January 2009, this powerful server should be a viable resource for many years to come. Publicly-accessible notebook servers continue to appear throughout the world (most recently in Hungary (61)), and many more run behind campus firewalls for dedicated use (63).

For occasions when there is no network access, Sage can be installed directly on a computer and used as a private server with exactly the same online notebook interface as the remote Sage servers use.

The flexibility of freely-available online access is a key consequence of the open nature of Sage and its importance cannot be overemphasized in education. As student populations become increasingly mobile, having technology that can be used freely from anywhere, especially from underpowered mobile devices, supports natural trends in student life.



The Sage notebook interface running in Mac OS X on Firefox

<sup>iii</sup> Jason says: figure todo: make the window wider, so the buttons aren't squished, and maybe show it on Windows, so people know we can access it from Windows (to take care of complaints people may have heard about Sage not running on Windows).

Rob says: I stole this from William. Go ahead and make a new one on Windows.

**3.5. Communicating mathematics.**  $\text{\LaTeX}$ , with its add-on package  $\text{\LaTeX}$ , is another open source success story, and is the typesetting language of choice for mathematicians and other technical disciplines. Every mathematical object in Sage can be typeset in  $\text{\LaTeX}$  automatically. The Sage notebook uses jsMath (12) to typeset mathematics beautifully in a Sage worksheet (within a standard web browser). Furthermore, the Sage notebook interface allows a user to insert new text, including typeset mathematics. This is another example of how open standards and open software combine to make powerful tools, which is especially relevant for our plan to convert  $\text{\LaTeX}$  documents into Sage worksheets.

In addition to using  $\text{\LaTeX}$  in the notebook interface, Sage can be used from within any  $\text{\LaTeX}$  file to perform computations and create figures. Dan Drake, a Visiting Professor at Korea Advanced Institute of Science and Technology, authored a Sage $\text{\TeX}$  (16), a  $\text{\LaTeX}$  package which allows Sage code in the file to easily be run as part of the process of formatting a  $\text{\LaTeX}$  document. Output (as typeset mathematics or images) is then automatically embedded in the resulting document.

**3.6. A standard programming language.** The many components of Sage are held together with a significant library of new code, written in the industry-standard programming language Python (55). Through the power of Python, new open source packages written in a variety of programming languages are added easily to Sage, bringing users new functionality, or improving existing functionality<sup>iv</sup>. More and more packages are appearing for mathematics and science written in Python, often with open licenses (57; 65).

iv

Students may use Sage through point-and-click interactive demonstrations written by others, or they may execute a sequence of single-line commands in the notebook. However, for more involved computations, they can use Python, since it also serves as the user language in Sage. This is in contrast to other comprehensive programs for mathematics that have chosen to create and develop their own programming languages, which are of no use outside of the CAS itself. A user with knowledge of Python is ready to be incredibly productive in Sage immediately, while a student using Sage that is new to programming receives a basic familiarity and education in Python—a skill that is readily transferable to mathematical and non-mathematical applications in a wide variety of fields, including art, business, science, engineering, and many other disciplines (56).

#### 4. TWO EXAMPLES OF TEACHERS DRIVING OPEN DEVELOPMENT

In this section, we provide two concrete examples of how teachers and classroom needs drive the development of Sage to directly create better and more comprehensive tools for use in the teaching and learning of mathematics.

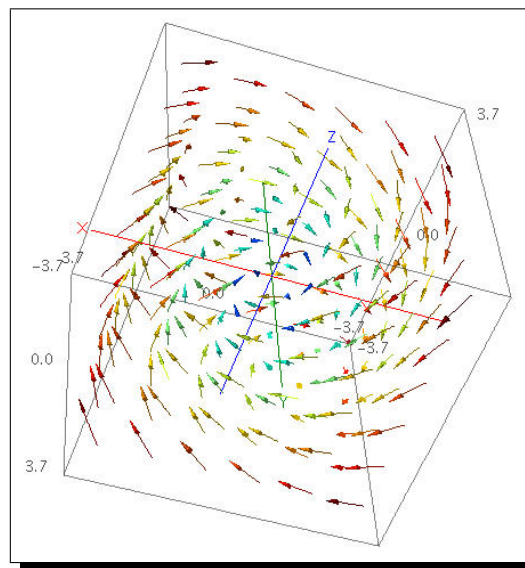
**4.1. 3D vector fields.** Jason Grout, then a postdoctoral associate at Iowa State University, was asked one day by a meteorology student if Sage had a 3D vector field plotting function. Grout quickly wrote a simple one. Open development communities encourage sharing even experimental code, so he posted his code online in Sage’s publicly-accessible online database of enhancements and bugs. Robert Bradshaw, a graduate student at University of Washington who had written much of the 3D graphing code in Sage, suggested a small change that greatly increased the efficiency of the function. Several months later, another person authored a very similar function which had slightly improved options and published their code on the public Sage notebook server. In Fall 2008, Grout needed the 3D vector field plotting function for his multivariable calculus class. He made a few suggested changes to the function and posted it for his class to use. If he had been using a commercial CAS, this is where the story likely would have ended.

<sup>iv</sup>Jason says: Also, interfaces are easily written to non-open software. Also mention that these programs don’t have to be written in python, as I can see some people assuming that they do have to be.

Rob says: I think this is too detailed for our purposes here.

In the next few months, improvements were made to the internals of Sage 3D graphics (many by William Cauchois, a University of Washington freshman supported for a summer by an NSF VIGRE grant). Some of these improvements were directly the result of wanting to make the 3D vector field plotting function easier to write. Jason then taught multivariable calculus again. He incorporated the best ideas from the various sources and posted a documented, efficient version of the function, this time asking the community for a formal review (a prerequisite for his code to be added to the core Sage library). Marshall Hampton, an Assistant Professor at University of Minnesota, Duluth, who has been active in the Sage project, reviewed the function immediately, with the comment “Very nice, positive review. This is great timing since I am about to teach vector fields in a week or two.” The function was incorporated into the next release of Sage, two weeks later, ready for immediate use by the entire Sage user community.

Now not only do the original students benefit from the invested effort, but the collaborative effort of at least five teachers and students has directly led to a function that will serve all who use Sage.



$\vec{f}(x, y, z) = y\vec{i} + z\vec{j} + x\vec{k}$  plotted with Sage's `plot_vector_field3d` command

**4.2. Dicyclic groups.** When Rob Beezer teaches introductory group theory, as he did in Fall 2009 with Tom Judson's open source text, he explores classifying all the finite groups of order less than 16 as a way of exhibiting the power of the theorems developed through the term. Each of these groups is easily constructed and realized in Sage as a permutation group, except for one of the three non-abelian groups of order 12.

In Fall 2009, Beezer decided to add this group to the collection of constructions in Sage. First, on a Friday evening, he polled the Sage development email list about the best way to realize this group. John Palmieri, an Associate Professor at the University of Washington, who is an expert in algebraic topology, responded 90 minutes later with information about the dicyclic groups, a sequence of groups of order  $4m$ , including the group of order 12 in question, the quaternion group of order 8, and the generalized quaternions of order  $2^n$ . David Joyner, a Professor at the US Naval Academy who was the second Sage developer after Stein, and who implemented much of Sage's support for group theory, joined the conversation an hour later. Jaap Spies weighed in from Holland with a source for more information. With this help, Beezer was able to easily create an efficient permutation representation of these groups in the next few days, and posted code and documentation, including comprehensive information and references about the group's construction and properties, to Sage's enhancement database. Joyner positively reviewed the code and documentation several days later. Two weeks later, this new code and documentation was incorporated in a preliminary Sage release. Within a month, Mike Hansen, a volunteer working from Thailand, oversaw the release of the next version of Sage, which included this code.

In this example, the net result is new capabilities for Sage, relevant to the undergraduate curriculum, with associated mathematical explanations in the Sage documentation. Beezer's course was improved by this exercise, and the benefits are now available to all through Sage. The dicyclic groups are now a worthwhile future addition to Judson's text, completing a virtuous cycle.

These two examples illustrate many strengths of the open development process used by Sage, where teachers and curriculum drive the technology. Teachers, students, and individuals bring



their talents as educators, mathematicians, and programmers together to make Sage an astonishing product of open development.

## 5. IMPLEMENTATION

Our goal is to have a broad, positive influence on the teaching and learning of mathematics. By using open curricular materials, integrated with powerful and comprehensive open software, we will realize a transformative effect. UTMOST will revolve around three coordinated efforts: (1) creating Sage-enhanced curricular materials, (2) working with, and providing classroom support for, teachers using these new materials in the classroom, and (3) providing the Sage infrastructure to support these materials. More specifically, UTMOST can be divided into five main activities.

- (1) We plan to create a system to convert open mathematics textbooks to Sage worksheets that can incorporate live Sage code, as well as interactive demonstrations and exercises powered by Sage. Our work to make these textbooks Sage-enhanced will provide a model for other authors to create Sage-enhanced textbooks. The first courses we will address are linear algebra, abstract algebra, and number theory.
- (2) We plan to further implement our model for authoring Sage-enhanced curricular materials by creating modules for standard undergraduate courses, especially courses not covered by the textbooks we are converting. These materials will include subject-specific guides to introduce faculty and students to Sage in the context of a particular topic. These materials will be created by members of the UTMOST team and by faculty at our ten test sites. Topics under consideration include single variable calculus, multivariable calculus, differential equations, and complex variables.
- (3) We plan to improve the Sage library and its surrounding infrastructure (e.g., server design, notebook usability, and collaboration tools) where the improvements have a direct and obvious benefit for undergraduate education.
- (4) We plan to identify and work closely with teachers at ten different institutions to test, refine, improve, and extend the work described above. We will select a broad range of institutions, including some with diverse student profiles. Dedicated Sage community workshops (“Sage Days”) will provide opportunities for the UTMOST team and representatives from the test sites to all collaborate on the project’s activities. These ten sites will provide extensive opportunities for our evaluation team to measure the success of our efforts and the impact on teaching and learning.
- (5) We plan to disseminate our materials and the results of UTMOST through Sage Days workshops, MAA PREP workshops, and MAA minicourses (national and regional). We will use these opportunities to train faculty outside of the ten test sites in the use of these materials for their courses, and in the process for creating their own new materials. Our materials will all carry open licenses and be available through the global Sage website. As appropriate, they will also be available in Sage itself or through a new open textbook website created at the American Institute of Mathematics as part of this grant.

**5.1. Sage-enhanced open textbooks.** Our principal activity is the design and creation of Sage-enhanced textbooks.

**5.1.1. Infrastructure for textbooks.** UTMOST proposes creating and fully testing a system for integrating Sage and textbooks. Pilot projects have already demonstrated the feasibility of this process for short documents, and technical improvements have been identified to make integrating Sage and book-length documents easy for authors. The primary tool is the existing `tex4ht` translator (NSF IIS-0312487) (73) which can convert  $\text{\LaTeX}$  into the jsMath format adopted by the Sage notebook for rendering publication-quality mathematics. The end result will be a folder of Sage worksheets, each a mixture of text, typeset mathematics, Sage input cells and Sage interactive demonstrations

and exercises. Because L<sup>A</sup>T<sub>E</sub>X is the accepted standard for authoring mathematics, we expect this process to be applicable to a broad range of current and future mathematics textbooks.

5.1.2. *Targeted textbooks.* Listed below are our initial candidates for conversion to Sage-enhanced textbooks that bring the full power of mathematics software to the student *directly within their book*. In addition to converting existing content to Sage worksheets, we plan to add to the texts: interactive demonstrations and exercises, live Sage code, and guidance on the Sage library itself. There is significant care and thought required to integrate these uses of mathematical software properly. Our work will provide a tested model other authors can consult when authoring new textbooks. We expect to have the three texts below available for use in the Fall 2011 term at our test sites. Each of these is authored by a project member, and so provides an excellent testbed for the enhancement process, since project members will then be able to directly refine the conversion process.

- Beezer's *A First Course in Linear Algebra* (3). This is a mature textbook designed from the start to be open source, and thus has a highly modular design. The first version of this book was released in December 2006, and has been used as the primary text in courses at 13 different universities. The author has taught from various versions of the book ten times. It will be an excellent choice as a full-scale test of the technical conversion process, the integration of Sage code, and classroom use.
- Judson's *Abstract Algebra: Theory and Applications* (34). This book was originally published by PWS-Kent in the early 1990s, but the author has received the copyright back and released it under an open source license. Beezer has taught from this text the past two years and created supplementary material utilizing Sage and contributed code to the Sage library to support the book. First released as open source in Spring 2009, eight universities adopted the book for the Fall 2009 term. As a year-long course, this is a larger project to tackle next, and will be a collaborative project between two team members.
- Stein's *Elementary Number Theory* (67). This text already has an extensive collection of Sage examples. Additionally, the author has taught from the book four times. It is currently being published by Springer-Verlag, but Stein has the rights to make it freely available starting May 2010, so will be able create a Sage-enhanced version for free distribution. While it will not carry a true open license that allows modifications by others, it will be a good test of the technical aspects of the conversion process and will be made freely available.

5.1.3. *Open mathematics textbooks.* The catalog of open mathematics textbooks is growing rapidly, and will likely have many more entries by Summer 2012 when we will select more textbooks for conversion. There is a wide range of books available now that could be converted to cover parts of the standard undergraduate curriculum, including math for liberal arts (42), trigonometry (13), college algebra (69), single and multivariable calculus (14; 15; 24; 26; 46; 71), linear algebra (3; 29), differential equations (39), numerical analysis (53), number theory (48; 67), cryptography (35), logic (5; 44), probability (25), combinatorics (7), real analysis (18; 19; 38), and abstract algebra (34). Almost without exception, these textbooks are licensed with a GNU Free Documentation License (GFDL) or a Creative Commons License (CC) that allows anyone to distribute modified versions, typically only requiring attribution of the original author's work and the use of the same license. Authors come from a wide range of institutions, representing community colleges (15; 42; 69), liberal arts colleges (3; 7; 26) and research institutions (38; 67; 71).

5.2. **Sage-enhanced curricular materials.** In addition to enhancing selected open textbooks, we will also enhance and develop smaller-scale curricular materials for other undergraduate courses.

5.2.1. *Subject-specific guides.* For selected courses where we do not provide a Sage-enhanced textbook, or no suitable open book currently exists, we will create subject-specific tutorials. These short guides will explain how to use Sage to investigate questions in a standard course, following a typical order

for such a course. Existing examples of these smaller-scale materials include multivariate calculus worksheets by Jason Grout and Ben Woodruff<sup>v</sup>, John Perry's course notes for a Mathematical Computing course (54), and Stein and Mazur's Riemann Hypothesis book (48), which targets a curious undergraduate.

v

Stipends will be provided to faculty outside the project team, ideally from our test sites, to author such materials. These will be designed from the start for conversion to Sage worksheets, providing a test of our system for this conversion.<sup>vi</sup>

vi

5.2.2. *Interactive demonstrations and exercises.* Sage has a powerful, but extremely simple-to-use framework for creating web-based interactive demonstrations. Input boxes, sliders, selectors, and other controls are simple to create. Output can use HTML, tables, typeset mathematics, and 2D or 3D graphics. Computations have the full Sage library at their disposal. The example in the screenshot in Appendix ?? is an example of such an interactive demonstration. Stein created the first implementation and continues to improve it with significant contributions from Grout and many other Sage developers. Current work by Mitesh Patel<sup>vii</sup>, supported by an NSF FRG grant (DMS-0757627), will allow embedding these interactive demonstrations into standard web pages, usable without having to log into a Sage server.

vii

For select courses we will create comprehensive collections of demonstrations for inclusion in our Sage-enhanced textbooks and into Sage itself. We will also create an easily-searchable repository of high quality, reviewed Sage interacts, which will be included in every copy of Sage.

5.3. **Sage into the classroom.** The heart of UTMOST is putting Sage-enhanced materials in the hands of teachers and students to assist them in teaching and learning mathematics. We will work with selected faculty at ten partner institutions by providing support for using Sage in their classrooms, offering technical support for Sage, assisting with the Sage-enhanced materials that we have created, and helping them write their own Sage-enhanced materials. Our teacher-authors and their students will receive access to Sage on a server dedicated to the UTMOST project, with dedicated technical support provided through this project.<sup>viii</sup>

viii

We will recruit two groups of teacher-authors for UTMOST, with the first group beginning in Summer 2011 for a two-year commitment and the second group beginning Summer 2012 for a one-year commitment, for a total of ten test sites. Teacher-authors will receive a stipend for their participation in UTMOST and support to attend a workshop on using Sage in the classroom. In order to forge a strong relationship with the teacher-authors and provide the best possible support, each teacher-author will be paired with a member of the UTMOST team who will serve as a contact and adviser. This adviser will also make visits to the test site to provide support and gather evaluation data. We will expect the following from these participants.

- Teacher-authors will commit to using Sage in their classrooms during their time with UTMOST. More specifically, they will be expected to use Sage-enhanced materials extensively in at least one semester-long course during the academic year.
- Teacher-authors will write and test comprehensive Sage-enhanced curricular materials for the class that they are teaching.

<sup>v</sup>Jason: publish these as a set of worksheets

<sup>vi</sup>Jason says: Have we included this in the budget? Mention later in test-sites.

Rob says: I don't think this is explicitly in the budget. There is money for "other personnel" but I think that is programming.

<sup>vii</sup>Jason says: a student? If so, say so

Rob says: no, just a guy

<sup>viii</sup>Jason says: In the budget?

Rob says: yes, \$2K in year 2, \$2K in year 3

- Teacher-authors will collect evaluation data from their students, and organize focus groups to gather feedback on the design and use of Sage-enhanced curricular materials. Focus groups will be led by the project member who is advising the teacher-author.
- Teacher-authors will offer training to others at their institution on how to use Sage and how to use Sage-enhanced materials in the classroom. Such training could be offered as departmental workshops or seminars.
- Teacher-authors from the first group will be selected to mentor the new teacher-authors in the second group.
- Teacher-authors will submit a report each year on their teaching experiences with Sage and new curricular materials.

5.3.1. *Recruitment plan.* Selection of the teacher-authors for UTMOST will be based on the following points.

- A narrative statement by the applicant regarding rationale for applying, the course or courses in which they plan to use UTMOST materials, and their familiarity with Sage.
- Limited or no familiarity with Sage, since we aim to make it easy for all faculty to integrate mathematics software into their courses, not just those who already have this experience.
- A letter of support from the department chair, indicating the flexibility to schedule faculty for the appropriate courses, a commitment to using Sage and new curricular materials in their department, and an awareness of evaluation activities.
- Consideration will be given to achieving a diverse mix of institutions and student populations, along with geographic proximity to a member of the UTMOST team.

5.4. **Sage infrastructure.** While the heart of Sage is its library of commands, the notebook interface and server configurations are key elements of a successful experience for students and faculty using Sage in their courses. A portion of our work will be to improve Sage itself, in those areas where the improvements *directly support* educational applications of Sage. Discussions and initial queries in the Sage-Edu email list indicate that faculty around the world are excited about setting up Sage servers for their students' use (63). We see three main areas for work on Sage.

5.4.1. *The Sage library.* Experience has shown us that teaching with Sage invariably suggests new capabilities or exposes needed commands. Our work enhancing textbooks, and our teacher-authors at test sites, will certainly suggest extensions and corrections to the Sage library. We will continue to refine and enhance Sage at an accelerated pace with support from this grant. All changes will undergo the existing code review process, and will then become permanent contributions to Sage, maintained and further extended by the worldwide Sage community. We have already identified specific improvements for linear algebra, abstract algebra, calculus, differential equations, number theory, and combinatorics, as well as broader areas like 2D and 3D graphics. Targeted fixes and improvements will greatly improve the educational experience for students. In many cases, undergraduate students can, and already have, contributed code and other suggestions; we plan to employ several students in these efforts.

5.4.2. *Notebook development.* The Sage notebook interface is a powerful tool for experimentation and collaboration. Stein worked fulltime during Fall 2009, supported by the University of Washington, on improving the robustness and scalability of the notebook. In Fall 2009, we have typically seen two thousand new accounts created on [sagenb.org](http://sagenb.org) every month. The notebook interface is the face of Sage for students and can be improved in many ways<sup>ix</sup>

ix

---

<sup>ix</sup>William can you expand here?: "like collaboration and....

5.4.3. *Sage servers the easy way.* Sage servers allow a user with just a standard web browser to use Sage over the network. Initiating and maintaining a server should be as simple as possible, making it easy for faculty and system administrators everywhere to get their students started with Sage.

<sup>x</sup>We will create a Virtual Box Sage notebook server appliance with a graphical interface, two virtual machines that provide a rock-solid secure Sage notebook server setup. Users will be able to very easily install this appliance on Windows, Linux, OS X, and Solaris (x86) servers. The management interface will provide clear and easy documentation about setting up this server, creating new notebook servers for specific classes or instructors, starting and stopping notebook servers, monitoring resource usage, adding users and authentication frameworks (such as LDAP), and upgrading Sage with minimal user downtime.

For users at our ten test sites, we will create a new mailing list for server administration issues, and in addition to the help we provide ourselves, we will hire a knowledgeable employee to answer support questions on a daily basis.

Several specific goals for notebook and server development include the following.

- We plan to improve the notebook so that it will robustly handle up to 250 simultaneous users viewing worksheets and doing typical computations for an undergraduate course when running on a single high-end server, as demonstrated by a robust automated test suite.
- We plan to implement management tools so administrators can manage the notebook load and better balance resources.
- We plan to create easy-to-use tools for educators to get automatic feedback about how their students use Sage.

In summary, we propose to provide high-quality enterprise-level software infrastructure and support to educators.

## 6. EVALUATION

<sup>xi</sup> Formative and summative evaluation will be conducted at different phases of the project to address questions about the effectiveness of the project in creating and implementing the UTMOST model and materials for undergraduate mathematics teaching and learning. Drs. Judson and Hassi<sup>xii</sup> will coordinate internal evaluation data-gathering, and will serve as the liaisons to evaluators from Ethnography & Evaluation Research at the University of Colorado at Boulder. The evaluation questions include:

- (1) What aspects of the Sage-based tools and materials are beneficial to instructors, what challenges do they face, and what kinds of support do they need in using these tools?
- (2) How do instructors use and apply the Sage-integrated curriculum materials, and how do these benefit (or fail to benefit) their teaching of mathematics?
- (3) How do the tools and materials impact instructors' content knowledge, pedagogical content knowledge, classroom instructional practice, and their students' learning?

Information will be gathered on both the processes and outcomes of the project at different stages, and results will be organized as case studies of participating instructors and their students. Formative components will focus on monitoring the quality of project activities, enabling the project to make mid-course corrections and plan for future development. Summative components will focus on the impact of the project on instructors' instruction and student learning at the test

<sup>x</sup>Explain something about virtual images and how easy they are to use

<sup>xi</sup>Check changes in this section. For example, lots of mentions of the "Sage tool and material" has been changed to "model and Sage-enhanced materials". Do the evaluators know we are evaluating a model, as well as specific curricular materials?

<sup>xii</sup>added Hassi here

sites. Instructors and classrooms will be sampled, taking into account instructor interest and local institutional cooperation. In addition to offering feedback on<sup>xiii</sup>

xiii

**6.1. Study design.** The study design includes pre- and post-surveys, follow-up surveys included in yearly self-reports, and interviews of the<sup>xiv</sup> participating instructors. In addition, students will answer an online post-survey focusing on their experiences and gains in learning mathematics, including their classroom use of the Sage tool and materials. The design is informed by previous evaluation studies on professional development, education, and workshops in STEM fields (10; 22; 41; 66; 74) and on student outcomes of active instructional methods in undergraduate mathematics (27; 28).

xiv

**6.1.1. Pre-survey.** While registering for the summer workshops, participants will complete a short pre-survey to gather demographic and contact data, and information about their classes, institution, current teaching practices, and pedagogical needs. This information will also help the project leaders to plan workshops and later support.

**6.1.2. Post-survey and feedback.** Participants will complete a survey on the summer workshops so that project leaders can make adjustments for future workshops and implementation support. The survey will ask about participants plans for using the model and Sage-enhanced materials, to help guide later components of the study. They will also be asked to sign a consent form to participate in a follow-up interview. Evaluators will observe the summer workshop and conduct a focus group with current and past participants.

**6.1.3. Follow-up survey and reports.** After using the model and Sage-enhanced materials for one year, the participants will file a report on their implementation, including some follow-up survey questions. They will report their use of the model and materials in their own classrooms and their future plans. Additional data on implementation will be gathered by the project team during site visits; they will conduct student focus groups using a protocol co-developed with the evaluators and share site visit notes that will be used as data sources<sup>xv</sup>.

xv

**6.1.4. Student learning assessment.** Student learning will be evaluated after the first year of implementation with a post-survey based on the NSF-supported SALG instrument (DUE-0920801) (70), in which students report about their experiences of and learning gains from their mathematics course. This will provide information on student outcomes as well as formative feedback for the instructors using the model and Sage-enhanced materials in their classroom. A mathematics-specific version (SALG-M) has already been validated and used in a large evaluation study, and is sensitive to differences by student group and classroom practice (27; 37).

**6.1.5. Follow-up interviews.** Based on instructor and student responses on other measures, about half<sup>xvi</sup> of the instructors will be interviewed to study factors that affect their success in implementing Sage-enhanced materials in their class. The interviews will explore classroom use of the model and Sage-enhanced materials, impacts on their instructional practices, and instructors' perception of students' response.

xvi

<sup>xiii</sup>never got the end of this sentence

<sup>xiv</sup>removed number

<sup>xv</sup>data sources for what?

<sup>xvi</sup>still only half? Or are we now interviewing all 10 instructors?

**6.2. Management and dissemination.** The evaluation will be led by Dr. Marja-Liisa Hassi from Ethnography & Evaluation Research (E&ER) at the University of Colorado at Boulder. E&ER has extensive experience evaluating large mathematics and science education projects (NSF DUE-0920126, DUE-0723600, DUE-0450088).

Drs. Judson and Hassi will collaborate with the project director, members of the project, and partner institutions to conduct the evaluation study. Dr. Judson and the project PIs will conduct site visits to partner institutions to observe and document the use of Sage-enhanced materials. Dr. Judson will have primary responsibility for extracting information from the site visits and workshop data to feed back to developers to improve the technology and classroom resources. Surveys and interview protocols will be prepared and conducted by Drs. Hassi and Judson. They will analyze all data and will prepare an annual report to document the evaluation activities and results. This will provide formative evaluation feedback to the project PIs and participating instructors to inform design decisions and mid-course corrections. A final report will gather results after the implementation of the tools and material by the second group of instructors in 2013. These findings will be shared also with the broader mathematics education community through a presentation and a coauthored article about the impacts of using CAS-integrated materials in teaching and learning undergraduate mathematics.

## 7. DISSEMINATION

UTMOST is principally about dissemination—the focus issue is how we can enable the widespread implementation of approaches which have already been proven to work. In addition to working with our test sites, we will broadly disseminate the results of UTMOST through a variety of forums, several of which are already in place.

**7.1. Sage website.** The Sage website, [sagemath.org](http://sagemath.org) (68), is an established venue for sharing materials related to Sage. This central location receives 90,000 visitors a month, with 42% of the visitors from the Americas (North, Central, and South) and 45% of the visitors from Europe. What we learn and create will be made available on the Sage website with open licenses. Further, some of our work will be incorporated into Sage itself, which already has an effective distribution system, designed to make Sage extremely easy to download and run on a personal machine or a server. Complete, integrated documentation ships with every copy of Sage (such as the 4,641 page reference manual), and it is possible that much of our material, *including complete textbooks*, could ship as a core component of Sage itself. A library of high-quality interactive demonstrations will also be included in Sage, where they will be able to be browsed topically or searched. These included demonstrations will benefit from Sage’s automated test-suite that users routinely run on a wide variety of hardware.

**7.2. Sage Days workshops.** Sage Days, which are a series of conferences and workshops devoted to the development of Sage, are an ideal venue for dissemination. To date there have been nineteen Sage Days conferences, with nine more planned. These workshops now include sessions dedicated to using Sage in the undergraduate classroom, with the first such session taking place in December 2009 at the Clay Mathematics Institute on the final day of a week-long workshop on Sage and number theory. It attracted roughly thirty college faculty (and a few high school faculty) from around the Northeast, all eager to learn more about the use of Sage in educational settings.

A Sage Days devoted to training others to use our model and materials, and receiving and incorporating feedback and new ideas, will be entirely consistent to the way Sage Days have been used to drive Sage development. We plan to have a Sage Days event in Summer 2012, involving the UTMOST team and all ten test sites, as an opportunity to discuss the project at the midpoint of our experiences in the classroom. Another Sage Days event at the American Institute of Mathematics in Summer 2013 will be an opportunity to more generally review the experiences of the project

and plan for the future of integrating open software and open textbooks in the undergraduate mathematics curriculum.

**7.3. National workshops.** We will apply to offer special sessions and workshops on the use of Sage in the classroom at the national Joint Mathematics Meetings and MathFest conferences, where we will be able to share the results of UTMOST with the undergraduate teaching community. We will also publish articles about the impact of using our materials on the teaching and learning of undergraduate mathematics. Drs. Beezer and Grout are part of a team delivering a workshop in Summer 2010 on how to use Sage in the classroom as part of the NSF-funded Mathematical Association of America Professional Enhancement Program (MAA PREP). We will apply to lead future PREP workshops that will incorporate the results of UTMOST. Notably, Stein has recently been invited to propose an American Mathematical Society Short Course on Sage for the 2011 Joint Meetings.

**7.4. AIM open textbook initiative.** <sup>xvii</sup>The American Institute of Mathematics is a respected NSF-funded institute that has supported both leading research mathematicians and mathematics education at all levels. As the sponsoring organization for UTMOST, AIM will conduct a pilot project to test the feasibility of sponsoring and supporting a series of open mathematics textbooks. A hindrance to the adoption of open textbooks is the lack of an acknowledged authority to vouch for the content. Usually this is a role played by a publisher, so a recognized organization within the mathematics community with a trusted reputation, such as AIM, will be another component to broadly disseminating our materials. This has the potential to positively impact open textbooks, in mathematics and more generally.

xvii

## 8. FUTURE DIRECTIONS

The limited scope of this proposal suggests several broader new directions. In particular, the project team was intrigued by the possibilities for using Sage to generate and check homework through integration with a system like WebWork, but decided such an initiative was too ambitious and disjoint to be included in this proposal. <sup>xviii</sup>

xviii

- Create new open textbooks with Sage enhancements designed in from the start.
- Create Sage-enhanced open textbooks for every standard course in the undergraduate mathematics curriculum.
- Integrate Sage with an open source homework delivery system such as WebWork.
- Integrate collaboration features of the Sage notebook with a course management system such as Moodle.
- More????

## 9. QUALIFICATIONS AND PREPARATION

The UTMOST team consists of five senior personnel plus an experienced evaluator of STEM education initiatives. The five senior personnel together have many years of experience teaching undergraduates at a wide range of institutions, four are active Sage developers (including its founder), three are authors of open textbooks, all have significant mathematics research experience, and one specializes in mathematics education research. As Sage developers, they are in a position to quickly and accurately shape changes in Sage based on the experience of working with faculty at other institutions that are new to Sage. Each is familiar with, and has extensive experience using, open source software and tools in their teaching and other professional activities. Besides

<sup>xvii</sup>Jason says: It feels like this AIM website is an afterthought. It feels like it should be fleshed out more clearly; what exactly will the criteria for endorsement be, how will it be done, what is the time frame, etc.

Rob says: I don't have much more than this, I think the idea is to explore all this?

<sup>xviii</sup>Delete this, or clean it up.



the applicability of this experience to the project's central theme, they are also extremely adept at working collaboratively while still being separated geographically. Working together, they have the wide range of complementary experience and skills that will make UTMOST a success.

### 9.1. Personnel.

**Dr. William A. Stein**, Associate Professor of Mathematics at the University of Washington, is a leader in both computational and theoretical number theory, and the author of two published number theory books. He started the Sage project in 2005, and has passionately led its development ever since, including co-organizing over 25 workshops during the last 4 years and directing dozens of Sage development projects by students at Harvard, UC San Diego, and U of Washington. Dr. Stein will implement improvements to Sage, direct work by students, contribute curricular materials he has authored, supervise test sites, and co-organize workshops.

**Dr. Kiran S. Kedlaya**, Associate Professor of Mathematics at Massachusetts Institute of Technology and University of California, San Diego, is a leading researcher in arithmetic algebraic geometry. He has received an NSF CAREER grant, a PECASE award, and a Sloan Fellowship, and was selected to speak at the 2010 International Congress of Mathematicians. Dr. Kedlaya brings extensive experience in undergraduate and graduate education at all levels, from calculus to mentoring Ph.D. students. He is also deeply involved with mathematics competitions and other programs for exceptional students, such as the USA Math Olympiad, the Putnam competition, and the Art of Problem Solving Foundation. In addition, Dr. Kedlaya brings extensive knowledge of the Sage system, having been an active user and developer since 2005. Dr. Kedlaya will review improvements for Sage related to the project, supervise test sites, and provide additional overall guidance.

**Dr. Jason Grout**, Assistant Professor of Mathematics at Drake University, is an undergraduate teacher, an active researcher in combinatorial matrix theory and graph theory, and a Sage developer. Dr. Grout has contributed extensively to the Sage code base over the last three years in the linear algebra, graph theory, plotting, and notebook interface components of Sage. Dr. Grout has used Sage in research and in teaching a number of undergraduate courses. He has also given numerous presentations and tutorials on Sage, and in Summer 2010 will be co-directing an MAA PREP workshop with Dr. Beezer and Dr. Karl-Dieter Crisman to help participants develop new curricular materials in Sage. Dr. Grout will implement improvements to Sage, direct work by students, supervise test sites, help organize workshops, and contribute curricular materials.

**Dr. Robert Beezer**, Professor of Mathematics at the University of Puget Sound, is a undergraduate teacher with 31 years of experience, an active researcher in algebraic graph theory, one of the first open textbook authors, and a Sage developer. He began writing his open source linear algebra textbook in 2004 and has assisted Dr. Judson with the recent release of his very successful open source abstract algebra text. He began using Sage in 2007 and began contributing code in early 2009. He will lead the technical process of converting textbooks from  $\text{\LaTeX}$  to Sage worksheets, producing a simple system for other authors to use. The pedagogical implications of this new capability will be explored as he incorporates Sage into existing textbooks on topics he teaches frequently, such as linear algebra, abstract algebra, combinatorics, calculus and cryptography. He will continue to contribute code to Sage where the new functionality enables a more complete experience for undergraduate students, and will suggest, review and test the project's improvements to interactive demonstrations and the notebook interface.

**Dr. Thomas Judson**, Associate Professor of Mathematics at Stephen F. Austin State University, is an active researcher in both mathematics and mathematics education, with 32 years of teaching experience. He is the author of an open source undergraduate abstract algebra textbook, and will work with Dr. Beezer to produce Sage-enhanced materials for abstract algebra. Dr. Judson has worked extensively with undergraduate mathematics teachers and has mentored graduate students in

the teaching of mathematics. In addition to his teaching and research accomplishments, Dr. Judson brings added experience in working with diverse groups both in the US and abroad. He will work with Dr. Hassi to guide research and evaluation efforts for UTMOST. With experience in working with undergraduate faculty and graduate student mentoring, Dr. Judson will also provide insight and assistance in the implementation of Sage-enhanced materials in the undergraduate classroom. Project efforts connected to research in mathematics education will be under the direction of Dr. Judson.

**Dr. Marja-Liisa Hassi**, Ethnography & Evaluation Research, University of Colorado at Boulder, has a Master's Degree in Mathematics and a Ph.D. in Education. She has expertise in both theory and methodology of mathematics education research, as well as teaching experience in education, mathematics education, and research methods for undergraduate and graduate students. Her recent publications address theory and measurement of affect in undergraduate and adult mathematics learners and comparative student outcomes of inquiry-based and traditional undergraduate mathematics courses. She will be assisted by Dr. Sandra Laursen, co-director of E&ER and an experienced evaluator of STEM education initiatives in higher education.

## 9.2. Grant experience and support.

- As a sponsoring organization, the American Institute of Mathematics has a ten-year history of successfully administering, supporting and executing 38 NSF grants in mathematics, including a recent CCLI Phase 1 award.
- Stein has successfully administered many grants supporting Sage development from varied organizations such as NSF, UC San Diego, U of Washington, Google, Sun, Microsoft, and the US Department of Defense. National Science Foundation grants include awards from the SCREMS program for the [sagenb.org](http://sagenb.org) computing cluster (DMS-0821725), the FRG program (sponsored by the American Institute for Mathematics, DMS-0757627) and the COMPMATH program to fund two postdoctoral positions (DMS-0713225).
- Judson works with middle and high school mathematics teachers from high-needs school districts to help them become teacher-leaders in their schools and districts, and preparing them to deliver pedagogical content and mathematical content to their colleagues. He also collaborates with the PIs on these NSF grants to help direct the mathematics education research component. (Texas Leadership Initiative: Mathematics Instruction Transformed, "Texas LIMIT," DUE-0934878; Texas Middle and Secondary Mathematics Project—Supplemental Funds, DUE-0227128)
- Beezer has been awarded a competitive year-long sabbatical leave from the University of Puget Sound for the 2010-11 academic year. This will allow him to begin converting textbooks, increasing the possible textbooks available for test sites to use beginning in the Fall 2011 term.
- Some of Grout's recent work on Sage been partially supported by an NSF postdoctoral appointment in Summer 2008.<sup>xix</sup>
- Beezer and Grout will co-direct (with Karl-Dieter Crisman) an MAA PREP workshop on Sage in Summer 2009, as part of a program funded by the NSF (DUE-0817071).
- Dr. Hassi is an expert in the research and evaluation of mathematics education and is currently working with a large evaluation study focused on inquiry-based learning and teaching of undergraduate mathematics at four large research universities (28; 36). She is also currently working with an evaluation study of NSF DUE-funded workshops on inquiry-based learning for instructors<sup>xx</sup>.

xix

xx

<sup>xix</sup>Jason: find award number

<sup>xx</sup>citation? Award number?

## REFERENCES

- [1] American Institute of Mathematics, <http://www.aimath.org/>
- [2] Thomas Banchoff, *Interactive Geometry and Multivariable Calculus on the Internet*, in Ki-hyong Ko, Deane Arganbright (Eds.), *Enhancing university mathematics: Proceedings of the first KAIST international symposium on teaching*, Conference Board of the Mathematical Sciences, *Issues in Mathematics Education*, **14** (2007) 17–31
- [3] Robert A. Beezer, *A First Course in Linear Algebra*, <http://linear.pugetsound.edu>
- [4] Robert A. Beezer, *Sage (Version 3.4)*, *SIAM Review*, **51** (2009) no. 4, 785–807
- [5] Stefan Bilaniuk, *A Problem Course in Mathematical Logic*, <http://euclid.trentu.ca/math/sb/pcml/welcome.html>
- [6] Paul Blanchard, Robert L. Devaney, Glen R. Hall, *The Boston University Ordinary Differential Equations Project*, <http://math.bu.edu/odes/>
- [7] Kenneth Bogart, *Combinatorics Through Guided Discovery*, NSF DUE-0087466, <http://www.math.dartmouth.edu/news-resources/electronic/kpbogart/>
- [8] Joseph J. Branin, Mary Case, *Reforming Scholarly Publishing in the Sciences: A Librarian Perspective*, *Notices of the American Mathematical Society*, **45** (1998) no. 4, 475–486, <http://www.ams.org/notices/199804/branin.pdf>
- [9] Brown University, *Interactive Internet-Based Teaching and Learning in Mathematics*, NSF DUE-0428280
- [10] K. A. Burke, T. J. Greenbowe, J. Gelder, *The Multi-Initiative Dissemination Project Workshops: Who attends and how effective are they?*, *Journal of Chemical Education*, **81** 2004 no. 6, 897–902
- [11] George Cain, *Online Mathematics Textbooks*, <http://people.math.gatech.edu/~cain/textbooks/onlinebooks.html>
- [12] Davide P. Cervone, *jsMath: A Method of Including Mathematics in Web Pages*, <http://www.math.union.edu/~dpvc/jsMath/>
- [13] Michael Corral, *Trigonometry*, <http://www.mecmath.net/trig/>
- [14] Michael Corral, *Vector Calculus*, <http://www.mecmath.net/>
- [15] Benjamin Crowell, *Crowell's Calculus*, <http://www.lightandmatter.com/calc/>
- [16] Dan Drake, *SageTeX*, <http://tug.ctan.org/pkg/sagetex>
- [17] Senator Dick Durbin, News Release, October 6, 2009, <http://durbin.senate.gov/showRelease.cfm?releaseId=318797>
- [18] John M. Erdman, *A Companion to Real Analysis*, <http://www.mth.pdx.edu/~erdman/CTRA/CRAlicensepage.html>
- [19] John M. Erdman, *A Problem Text in Advanced Calculus*, <http://www.mth.pdx.edu/~erdman/PTAC/PTAClicensepage.html>
- [20] Flat World Knowledge, <http://www.flatworldknowledge.com/>
- [21] Fast Library for Number Theory, <http://www.flintlib.org/>
- [22] L. Gafney, P. Varma-Nelson, *Peer-led team learning: Evaluation, dissemination and institutionalization of a college-level initiative*, *Innovations in Science Education and Technology*, **16** (2008) New York: Springer
- [23] GAP—Groups, Algorithms, Programming—a System for Computational Discrete Algebra, <http://www.gap-system.org/>
- [24] William Granville, David Joyner, *Differential Calculus and Sage*, <http://sage.math.washington.edu/home/wdj/teaching/calc1-sage/>
- [25] Charles M. Grinstead, J. Laurie Snell, *Introduction to Probability*, [http://www.dartmouth.edu/~chance/teaching\\_aids/books\\_articles/probability\\_book/book.html](http://www.dartmouth.edu/~chance/teaching_aids/books_articles/probability_book/book.html)
- [26] David Guichard, *Whitman Calculus*, <http://sites.google.com/site/whitmanmathematics/>

- [27] M.-L. Hassi, *Empowering undergraduate students through mathematical thinking and learning*, Safford-Ramus, K. (ed.), A Declaration of Numeracy: Empowering Adults through Mathematics Education, Proceedings of the 15th International Conference of Adults Learning Mathematics (ALM) (2009) 53–69. Lancaster, PA: DEStech Publications
- [28] M.-L. Hassi, S. Laursen, *Studying undergraduate mathematics: Exploring students' beliefs, experiences and gains*, in S.L. Swars, D.W. Stinson, S. Lemons-Smith (Eds.), Proceedings of the 31st Annual Meeting of the North American Chapter of the International Group for the Psychology of Mathematics Education (PME-NA), (2009) 113–121. Atlanta, GA: Georgia State University.
- [29] Jim Hefferon, *Linear Algebra*, <http://joshua.smcvt.edu/linearalgebra/>
- [30] M. Kathleen Heid, *The technological revolution and the reform of school mathematics*, American Journal of Education, **106** (1997) no. 1, 5–61
- [31] M. Kathleen Heid, Michael T. Edwards, *Computer algebra systems: revolution or retrofit for today's mathematics classrooms?*, Theory into Practice, **40** (2001) no. 2, 128–136
- [32] Hobart and William Smith Colleges, Java Components for Mathematics, NSF DUE-9950473, <http://math.hws.edu/javamath/>
- [33] Integer Matrix Library, <http://www.cs.uwaterloo.ca/~astorjoh/iml.html>
- [34] Thomas W. Judson, *Abstract Algebra: Theory and Applications*, <http://abstract.pugetsound.edu>
- [35] David Kohel, *Cryptography*, <http://echidna.maths.usyd.edu.au/kohel/tch/Crypto/crypto.pdf>
- [36] S. L. Laursen, M.-L. Hassi, *Inquiring about inquiry: Progress on research and evaluation studies of Inquiry-Based Learning in undergraduate mathematics at four campuses*, Presented at the Joint Mathematics Meetings, January 5–8, 2009, Washington, DC.
- [37] S. Laursen, M.-L. Hassi, R. Crane, *First findings from evaluation studies of the IBL Mathematics Projects*, presented to the Legacy of R. L. Moore Conference, Austin, TX, July 16–18, 2009
- [38] Jiří Lebl, *Basic Analysis: Introduction to Real Analysis*, <http://www.jirka.org/ra/>
- [39] Jiří Lebl, *Notes on Diffy Qs: Differential Equations for Engineers*, <http://www.jirka.org/diffyqs/>
- [40] David Leigh-Lancaster, et al., *The 2007 Common Technology Free Examination for Victorian Certificate of Education (VCE) Mathematical Methods and Mathematical Methods Computer Algebra System (CAS)*, in M. Goos, R. Brown, K. Makar (Eds.), Proceedings of the 31st Annual Conference of the Mathematics Education Research Group of Australasia, 2008.
- [41] S. E. Lewis, J. E. Lewis, *Effectiveness of a workshop to encourage action: Evaluation from a post-workshop survey*, Journal of Chemical Education, **83**(2006) no. 2, 299–304, <http://www.wcer.wisc.edu/publications/LEADcenter/nt-wkshop.pdf>
- [42] David Lippman, *Math in Society*, <http://www.pierce.ctc.edu/dlippman/mathinsociety/>
- [43] M4RI, *Linear Algebra over  $GF(2)$* , <http://m4ri.sagemath.org/performance.html>
- [44] P.D. Magnus, *forall X: An Introduction to Formal Logic*, <http://www.fecundity.com/logic/>
- [45] Maplesoft, *Maple*, <http://www.maplesoft.com/Products/Maple/>
- [46] David B. Massey, *Worldwide Differential Calculus*, <http://www.centerofmath.org/textbooks/diffcalc.html>
- [47] Maxima Wiki, *The Macsyma Saga*, [http://maxima-project.org/wiki/index.php?title=The\\_Macsyma\\_Saga](http://maxima-project.org/wiki/index.php?title=The_Macsyma_Saga)
- [48] Barry Mazur, William Stein, *What is Riemann's Hypothesis?*, (NSF DMS-0653968) <http://wstein.org/rh/>
- [49] National Institutes of Health, *Public Access Policy*, <http://publicaccess.nih.gov/>
- [50] The Ohio State University, *Calculus & Mathematica*, <http://socrates.math.ohio-state.edu/>
- [51] Open Knowledge Foundation, *Open Text Book*, <http://www.opentextbook.org/category/maths/>

- [52] Jeanette R. Palmiter, *Effects of computer algebra systems on concept and skill acquisition in calculus*. Journal for Research in Mathematics Education, **22** (1991) no. 2, 151–156
- [53] Steven Pav, *Numerical Analysis*, <http://scicomp.ucsd.edu/~spav/pub/numas.pdf>
- [54] John Perry, *Mathematical Computing*, MAT 305, University of Mississippi, <http://www.math.usm.edu/perry/mat305fa09/index.html>
- [55] Python Website, *Python*, <http://www.python.org/>.
- [56] Python Website, *Python Success Stories*, <http://www.python.org/about/success/>
- [57] Python Wiki, *Numeric and Scientific Packages*, <http://wiki.python.org/moin/NumericAndScientific>
- [58] The R Project for Statistical Computing, <http://www.r-project.org/>
- [59] REDUCE, A portable general-purpose computer algebra system. <http://reduce-algebra.sourceforge.net/>
- [60] Sage Notebook Server, <http://sagenb.org>
- [61] Sage Server (public), Hungary, <http://sage.math.u-szeged.hu/>
- [62] Sage Server, cell phone interface, Sungkyunkwan University, Korea, [http://math1.skku.ac.kr/wap\\_html](http://math1.skku.ac.kr/wap_html)
- [63] Sage Wiki, *Sage Notebook Servers*, <http://wiki.sagemath.org/sagenb>
- [64] Governor Arnold Schwarzenegger, Press Release, Free Digital Textbook Initiative, <http://gov.ca.gov/press-release/12225/>
- [65] SciPy, Scientific Tools for Python, <http://www.scipy.org/>
- [66] G. R. Sell, *A review of research-based literature pertinent to an evaluation of workshop programs and related professional development activities for undergraduate faculty in the sciences, mathematics and engineering*, report commissioned by SRI International as part of an evaluation for the Undergraduate Faculty Enhancement (UFE) program for the National Science Foundation, (1998) (Available from the author)
- [67] William Stein, *Elementary Number Theory: Primes, Congruences, and Secrets*, Undergraduate Texts in Mathematics, 2009, Springer-Verlag, <http://modular.math.washington.edu/ent/>
- [68] William Stein et al., *Sage, Version 4.2*, <http://www.sagemath.org>
- [69] Carl Stitz, Jeff Zeager, *Free College Algebra Book*, [http://www.stitz-zeager.com/College\\_Algebra\\_Book/Free\\_College\\_Algebra\\_Book\\_Download.html](http://www.stitz-zeager.com/College_Algebra_Book/Free_College_Algebra_Book_Download.html)
- [70] Student Assessment of their Learning Gains (SALG), [www.salgsite.org](http://www.salgsite.org)
- [71] Gilbert Strang, *Calculus*, <http://ocw.mit.edu/ans7870/resources/Strang/strangtext.htm>
- [72] The Student PIRGs, *Open Textbook Catalog*, <http://www.studentpirgs.org/open-textbooks/catalog>
- [73] T<sub>E</sub>X4ht: L<sup>A</sup>T<sub>E</sub>X and T<sub>E</sub>X for Hypertext, <http://www.cse.ohio-state.edu/~gurari/TeX4ht/>
- [74] H. Thiry, S. L. Laursen, A.-B. Hunter, *Professional development needs and outcomes for education-engaged scientists: A research-based framework and its application*, Journal of Geoscience Education, **56** (2008) no. 3, 235–246.
- [75] TinyMCE Javascript Editor, <http://tinymce.moxiecode.com/>
- [76] University of Illinois at Urbana-Champaign, *Calculus & Mathematica*, <http://www-cm.math.uiuc.edu>
- [77] Washington State Board for Community and Technical Colleges, Washington State Student Completion Initiative, [http://www.sbctc.ctc.edu/college/e\\_studentcompletioninitiative.aspx](http://www.sbctc.ctc.edu/college/e_studentcompletioninitiative.aspx)
- [78] White House Office of Science and Technology Policy, *Public Consultation on Public Access Policy*, <http://www.whitehouse.gov/blog/2009/12/09/ostp-launch-public-forum-how-best-make-federally>
- [79] Wolfram Research, *Mathematica*, <http://www.wolfram.com/products/mathematica/index.html>

# Biographical Sketch

## Robert A. Beezer

- Email: [beezer@ups.edu](mailto:beezer@ups.edu)
- Web: <http://buzzard.ups.edu>
- Phone: 253-879-3564

## Professional Preparation

University of Santa Clara	Mathematics, Computer Science, B.S. 1978
University of Illinois at Urbana-Champaign	Statistics, M.S. 1982
University of Illinois at Urbana-Champaign	Mathematics, Ph.D. 1984

## Appointments

- Professor of Mathematics, University of Puget Sound, 1996–present.
- University Professor, University of Puget Sound, Fall 2001–Spring 2006.
- Chair, Mathematics and Computer Science Department, Univ. of Puget Sound, 1999–2002.
- Research Visitor, University of Western Australia, Fall 1997.
- Associate Professor of Mathematics, University of Puget Sound, 1990–1996.
- Visiting Lecturer, University of the West Indies, Trinidad, Spring 1991.
- Assistant Professor of Mathematics, University of Puget Sound, 1984–1990.

## Most Relevant Publications

- *The Truly Free Textbook*, EDUCAUSE Review Magazine, **44**, no. 1 (2009) 22–24.
- *A First Course in Linear Algebra*, 806 pp., GFDL licensed textbook, <http://linear.ups.edu>.
- *Sage (Version 3.4)*, Featured Review, SIAM Review, **51**, no. 4 (2009).
- *Sylow subgraphs of self-complementary vertex transitive graphs*, Expositiones Mathematicae, **24**, no. 2 (2006) 185–194.
- *Counting configurations in designs*, Journal of Combinatorial Theory, Series A **96** (2001), no. 2, 341–357.

## Other Publications

- *Using minimum degree to bound average distance*, with B. Smith and J. Riegsecker, Discrete Mathematics, **226** (2001) 365–371.
- *Closing in on the internal rate of return*, The UMAP Journal, **17**, no. 2 (1996).  
Reprinted in *Tools for Teaching 1996*, 47–78. COMAP, Inc.. Lexington, Mass. 1997.
- *The matching polynomial of a regular graph*, with E.J. Farrell, Discrete Mathematics, **137** (1995) 7–18.
- *Trees with very few eigenvalues*, Journal of Graph Theory, **14**, no. 4 (1990) 509–517.
- *Trivalent orbit polynomial graphs*, Linear Algebra and Its Applications, **73** (1986) 133–146.

## Synergistic Activities

- **Sage** Contribute and review code for Sage in the areas of linear algebra, group theory, graph theory and  $\text{\LaTeX}$  integration. Sage is a comprehensive open source program for mathematics.
- **Open Textbooks** Author of an open textbook for linear algebra. Production Editor for Judson's open source abstract algebra book. Advocate for wider acceptance of open educational resources, through writings and presentations, both in mathematics and more widely.

## Collaborators and Other Affiliations

- **Collaborators and Coauthors** T. Judson (Stephen F. Austin State U.), Sage Developers (various).
- **Ph.D. Advisor** Paul Weichsel, University of Illinois at Urbana-Champaign.
- **Graduate Students Supervised** None.

# Biographical Sketch (Kiran S. Kedlaya)

## a. Professional Preparation

Undergraduate: Harvard University, Mathematics/Physics *summa cum laude*, A.B., 1996.

Graduate: Princeton University, Mathematics, M.A., 1997.

Graduate: MIT, Mathematics, Ph.D., 2000.

Postdoctoral: Clay Mathematics Institute, Mathematics, summer 2000.

Postdoctoral: MSRI, Mathematics, fall 2000.

Postdoctoral: University of California, Berkeley, Mathematics, 2000–2003.

Postdoctoral: Institute for Advanced Study, Mathematics, fall 2003.

## b. Appointments

University of California, San Diego, Associate Professor, 2009–present.

Institute for Advanced Study, member, 2009–2010.

MIT, Assistant Professor, 2003–2007; Associate Professor without tenure, 2007–2009; Associate Professor with tenure, 2009–present; Cecil and Ida Green Career Development Professor, 2008–2011.

Université de Rennes, Professeur invité, May–June 2002, June 2003.

## c. Publications

*Publications/projects related to current research:*

- Sage project, <http://www.sagemath.org/>.
- *The William Lowell Putnam Mathematical Competition 1985–2000: Problems, Solutions and Commentary* (with Bjorn Poonen and Ravi Vakil), Mathematical Association of America, Washington, 2002.
- Search techniques for root-unitary polynomials, in K.E.Lauter and K.A. Ribet (eds.), *Computational Arithmetic Geometry*, Contemporary Math. 463, Amer. Math. Soc., 2008, 71–82 (uses Sage).
- Hyperelliptic curves,  $L$ -polynomials, and random matrices (with Andrew Sutherland), in *Arithmetic, Geometry, Cryptography, and Coding Theory (AGC<sup>2</sup>T 2007)*, Contemporary Math. 487, Amer. Math. Soc., 2009.
- Bounding Picard numbers of surfaces using  $p$ -adic cohomology (with Timothy G. Abbott and David Roe), to appear in *Arithmetic, Geometry and Coding Theory (AGCT 2005)*, Sminaires et Congrès 21, Societ Mathmatique de France, 2010, 125–159 (uses Magma).

*Other significant publications:*

- Fast modular composition in any characteristic (with Christopher Umans), in *49th Annual IEEE Symposium on Foundations of Computer Science 2008 (FOCS '08)*, 2008, 146–155.
- Slope filtrations for relative Frobenius, *Astrisque* **319** (2008), 259–301.



- Semistable reduction for overconvergent F-isocrystals, III: local semistable reduction at monomial valuations, *Compositio Mathematica* **145** (2009), 143–172.
- Some new directions in  $p$ -adic Hodge theory, *Journal de Theorie des Nombres de Bordeaux* **21** (2009), 285–300.
- Good formal structures for flat meromorphic connections, I: Surfaces, *Duke Math. Journal*, to appear (probably 2010).

#### d. Synergistic Activities

- The PI has pursued explicit methods in algebraic geometry, demonstrating that some techniques thought only to have theoretical value are in fact relevant to applications involving algebraic geometry (e.g., cryptography). Some of these techniques have now been implemented in the *Magma* and *Sage* computer algebra systems.
- The PI has participated extensively in the development of activities for students of exceptional mathematical abilities, including competitions such as the USA Math Olympiad, the International Math Olympiad, the USA Math Talent Search, and the Putnam competition; summer programs such as the Math Olympiad Summer Program and the Canada/USA Mathcamp; the Art of Problem Solving Foundation; and the web site [cogito.org](http://cogito.org).
- The PI has given a number of expository talks, to high school students, undergraduates, and high school teachers, on a wide variety of topics in algebra, combinatorics, and number theory.
- The PI has engaged undergraduates in ongoing research (largely through MIT's Undergraduate Research Opportunities Program), in an attempt to bridge the gap between the undergraduate curriculum and the research frontiers in number theory.
- The PI has developed a number of pedagogical materials; some, such as the book with Poonen and Vakil, use mathematical problem solving as a device for bringing students towards the frontiers of current research.

#### e. Collaborators and Other Affiliations

Collaborators: T. Abbott (KSplice), M. Baker (Georgia Tech), J. Balakrishnan (MIT), R. Bradshaw (Washington), B. Conrad (Stanford), S. Dasgupta (California–Santa Cruz), D. Gulotta (Princeton), R. Liu (McGill), J. Propp (Massachusetts–Lowell), D. Roe (Harvard), D. Savitt (Arizona), X. Shao (MIT), A. Sutherland (MIT), J. Teitelbaum (Connecticut), D. Thakur (Arizona), C. Umans (Caltech), L. Xiao (Chicago), S. Yekhanin (IAS).

Advisors: A.J. de Jong (graduate, MIT/Columbia), Ken Ribet (postdoctoral, Berkeley).

Advisees: J. Balakrishnan (doctoral, MIT), C. Davis (doctoral, MIT), R. Liu (doctoral, MIT), J. Suh (postdoctoral, MIT), F. Tan (doctoral, MIT), L. Xiao (doctoral, MIT). Total of 5 doctoral advisees, 1 postdoctoral advisee.

**Thomas W. Judson, Project Faculty****Professional Preparation**

- **Ph.D.** – University of Oregon, Mathematics, 1984.
- **M.A.** – University of Oregon, Mathematics, 1979.
- **B.S.** – University of Illinois, Mathematics, 1975.

**Appointments**

- 2008 – Present Associate Professor, Department of Mathematics and Statistics, SFASU
- 2002 – 2008 Preceptor, Department of Mathematics, Harvard University
- 2001 – 2002 Visiting Assistant Professor, Department of Mathematics and Computer Science, University of Puget Sound
- 1993 – 2001 Associate Professor, Department of Mathematics, University of Portland
- 1984 – 1993 Assistant Professor, Department of Mathematics, University of Portland
- 1978 – 1984 Graduate Teaching Fellow, Department of Mathematics, University of Oregon
- 1987 – 1988 Graduate Teaching Assistant, Department of Mathematics, Univ. California, Irvine

**Publications**

- Judson, T. with Alvine, A., Schein, M. Yoshida, T. What Graduate Students (and the Rest of Us) Can Learn from Japanese Lesson Study. *College Teaching*, 55(2007), 109-113.
- Judson, T. with Nishimori, T. Concepts and skills in high school calculus: An examination of a special case in Japan and the U.S. *Journal of Research in Mathematics Education*, 36(2005), 24-43.
- Judson, T. Complete Filtered Lie Algebras over a Vector Space of Dimension Two. *Journal of Lie Theory*, 12(2002), 423-447.
- Judson, T. Amerika ni okeru suugaku kyouiku ni tuite no ronsou (in Japanese), *Journal of Higher Education and Lifelong Learning*, 9(2001), 10-15.
- Judson, T. Japan: A Different Model of Mathematics Education, *1996 Proceedings of the Symposium on the Future of Mathematics Education at Research Universities*, The Mathematical Sciences Research Institute, Cambridge University Press, Cambridge, 1999.
- Judson, T. Calculus Education in the United States, *Proceedings of ICME-EARCOME~1*, 1998.
- Judson, T. Teaching a laboratory based linear algebra course, *1995 Proceedings of the Asian Technology Conference in Mathematics*.
- Judson, T. Experiences from the ATLAST Project: Implementing a laboratory based linear algebra course, *1993 Proceedings of the International Conference on Technology in Collegiate Mathematics*.
- Judson, T. *Abstract Algebra: Theory and Applications*, PWS Publishing Company, Boston, 1994.
- Judson, T. Complete Filtered Lie Algebras and their Spencer Cohomology, *Journal of Algebra*, 25(1989), 66-109.

**Synergistic Activities**

- Texas Leadership Initiative: Mathematics Instruction Transformed (Texas LIMIT). NSF Award #0934878. Conducting teacher development workshops and educational research (2009 to present).
- Texas Middle and Secondary Mathematics Project - Supplemental Funds. NSF Award #0227128. Conducting teacher development workshops and educational research (2008 to present).
- Graduate teaching fellow training programs at Harvard University and Stephen F. Austin State University. Worked with a small group of faculty in each department to create and oversee

teacher training programs for graduate students who are teaching in the undergraduate curriculum (2001 to present).

- Undergraduate Faculty Program at the IAS/Park City Mathematics Institute (2001).
- National Science Foundation ATLAST Workshop at Michigan State University, East Lansing, MI (1993).

**Collaborators and Other Affiliations**

Dr. Matthew Leingang, NYU  
Dr. Toshiyuki Nishimori, Hokkaido University  
Dr. Teruyoshi Yoshida, Harvard University  
Dr. Michael Schein, Bar-Ilan University  
Dr. Amanda Alvine, Harvard University  
Dr. Andrew Engelward, Harvard University  
Dr. Bret Benesh, College of Saint Benedict, Saint John's University

# Biographical Sketch

## William Stein

- Email: [wstein@gmail.com](mailto:wstein@gmail.com)
- Web: <http://wstein.org>
- Phone: 206-419-0925

## Professional Preparation

Northern Arizona University  
University of California at **Berkeley**  
**Harvard University**

Mathematics, B.S. 1994  
Mathematics, Ph.D. 2000  
Postdoc, 2000–2005

## Appointments

- Associate Professor of Mathematics (with tenure), University of Washington, September 2006–present.
- Associate Professor of Mathematics (with tenure), UC San Diego, July 2005–June 2006.
- Benjamin Peirce Assistant Professor of Mathematics, Harvard University, July 2001–May 2005.
- NSF Postdoctoral Research Fellowship under Barry Mazur at Harvard University, August 2000–May 2004.
- Clay Mathematics Institute Liftoff Fellow, Summer 2000.

## Most Relevant Publications

- *Average Ranks of Elliptic Curves: Tension Between Data and Conjecture*, with B. Bektemirov, B. Mazur, W. Stein, and M. Watkins, *Bulletins of the AMS* **44** (2007), no. 2, 233–254.
- *Modular forms, a computational approach* (xvi+268 pp.) Graduate Studies in Mathematics (AMS) 79 2007, with an appendix by Paul Gunnells.
- *Verification of the Birch and Swinnerton-Dyer Conjecture for Specific Elliptic Curves*, with G. Grigorov, A. Jorza, S. Patrikis, and C. Patrascu (26 pages), 2005, to appear in *Mathematics of Computation*.
- *Computation of  $p$ -Adic Heights and Log Convergence*, with B. Mazur and J. Tate (36 pages), *Documenta Mathematica*, 2006, Extra Vol., 577–614.
- *Visible Evidence for the Birch and Swinnerton-Dyer Conjecture for Rank 0 Modular Abelian Varieties* (31 pages), with A. Agashe, *Mathematics of Computation* **74** (2005), no. 249, 455–484.

## Other Publications

- *The Manin Constant*, with A. Agashe and K. Ribet, Pure Appl. Math., (2006), no. 2., 617–636.
- *Studying the Birch and Swinnerton-Dyer Conjecture for Modular Abelian Varieties Using Magma* (22 pages), a chapter in the Springer–Verlag book “Computational Experiments in Algebra and Geometry”.
- *Shafarevich-Tate Groups of Nonsquare Order*, Progress in Math., **224** (2004), 277–289, Birkhauser.
- *Constructing Elements in Shafarevich-Tate Groups of Modular Motives*, (19 pages) with N. Dummigan and M. Watkins, “Number theory and algebraic geometry—to Peter Swinnerton-Dyer on his 75th birthday”, Ed. by M. Reid and A. Skorobogatov.
- $J_1(p)$  has connected fibers, with B. Conrad and B. Edixhoven, Documenta Math., **8** (2003), 331–408.

## Synergistic Activities

- **Research Tools:** Principal author of Sage, which is a major new piece of software. Author of the modular forms, modular symbols and modular abelian varieties parts of the Magma computer algebra system (425 pages (26000 lines) of code plus documentation). These are tools used by mathematicians who do computations with modular forms.
- **Databases:** Created and maintain the Modular Forms Database. This contains continually expanding data about elliptic curves and modular forms: <http://wstein.org/Tables/>.
- **Outside Service:** IDA/CCR consultant. Also, Defense Science Study Group member 2002–2003: DSSG is a DARPA funded program administered by the Institute for Defense Analysis; paper on GPS vulnerabilities.
- **Outreach:** SIMUW 2007; SIMUW 2006; Canada/USA MathCamp mentor (2002); Several Math Circles talks in Boston.

## Collaborators and Other Affiliations

- **Coauthors:** A. Agashe (Florida State U.), K. Buzzard (Imperial College, London), R. Coleman (UC Berkeley), B. Conrad (Univ. of Michigan), N. Dummigan (Sheffield, UK), S. Edixhoven (Leiden, Netherlands), F. Leprévost (Univ. Joseph Fourier, Technische Univ. Berlin), E. V. Flynn (Liverpool, UK), D. Kohel (Univ. of Sydney), B. Mazur (Harvard), L. Merel (Paris 6), K. Ribet (UC Berkeley), E. F. Schaefer (Santa Clara Univ.), M. Stoll (Inter. Univ. Bremen, Germany), J. Tate, H. A. Verrill (Louisiana State), M. Watkins (Bristol.), J. L. Wetherell (CCR, San Diego)
- **Graduate and Postdoctoral Advisors:**
  - **Ph.D. advisor:** Hendrik Lenstra, University of Leiden, Netherlands.
  - **NSF Postdoctoral advisor:** Barry Mazur, Harvard University.
- **Thesis Students:** 2 Ph.D. students: Robert Bradshaw’s Ph.D. thesis at Univ. of Washington and Ifti Burhanuddin’s at Univ. of Southern California. Advised eight undergraduate senior theses at Harvard.

# BIOGRAPHICAL SKETCH

---

No Bio Data Provided

# SUMMARY PROPOSAL BUDGET

YEAR 1

ORGANIZATION <b>Stephen F. Austin State University</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>Thomas W Judson</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PI, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>Thomas W Judson - Co-PI</b>				0.00	0.00	1.25	\$ <b>8,583</b>
2.							
3.							
4.							
5.							
6. ( 0 ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	0
7. ( 1 ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	1.25	<b>8,583</b>
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( 0 ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	0
2. ( 0 ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	0
3. ( 0 ) GRADUATE STUDENTS							0
4. ( 0 ) UNDERGRADUATE STUDENTS							0
5. ( 0 ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							0
6. ( 0 ) OTHER							0
TOTAL SALARIES AND WAGES (A + B)							<b>8,583</b>
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							<b>1,859</b>
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							<b>10,442</b>
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							0
E. TRAVEL 1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							0
2. FOREIGN							0
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS \$ _____				0			
2. TRAVEL _____				0			
3. SUBSISTENCE _____				0			
4. OTHER _____				0			
TOTAL NUMBER OF PARTICIPANTS ( 0 ) TOTAL PARTICIPANT COSTS							0
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							0
2. PUBLICATION COSTS/DOCUMENTATION/DISEMINATION							0
3. CONSULTANT SERVICES							0
4. COMPUTER SERVICES							0
5. SUBAWARDS							0
6. OTHER							0
TOTAL OTHER DIRECT COSTS							0
H. TOTAL DIRECT COSTS (A THROUGH G)							<b>10,442</b>
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE) <b>Salaries/wages (Rate: 50.0000, Base: 8583)</b>							
TOTAL INDIRECT COSTS (F&A)							<b>4,292</b>
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							<b>14,734</b>
K. RESIDUAL FUNDS							0
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ <b>14,734</b> \$
M. COST SHARING PROPOSED LEVEL \$ 0				AGREED LEVEL IF DIFFERENT \$			
PI/PI NAME <b>Thomas W Judson</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

1 \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

# SUMMARY PROPOSAL BUDGET

YEAR **2**

ORGANIZATION <b>Stephen F. Austin State University</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>Thomas W Judson</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PI, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>Thomas W Judson - Co-PI</b>				0.00	0.00	2.00	\$ <b>14,420</b>
2.							
3.							
4.							
5.							
6. ( <b>0</b> ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	<b>0</b>
7. ( <b>1</b> ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	2.00	<b>14,420</b>
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( <b>0</b> ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	<b>0</b>
2. ( <b>0</b> ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	<b>0</b>
3. ( <b>0</b> ) GRADUATE STUDENTS							<b>0</b>
4. ( <b>0</b> ) UNDERGRADUATE STUDENTS							<b>0</b>
5. ( <b>0</b> ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							<b>0</b>
6. ( <b>0</b> ) OTHER							<b>0</b>
TOTAL SALARIES AND WAGES (A + B)							<b>14,420</b>
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							<b>3,124</b>
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							<b>17,544</b>
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							<b>0</b>
E. TRAVEL 1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							<b>0</b>
2. FOREIGN							<b>0</b>
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS \$ <b>0</b>							
2. TRAVEL <b>0</b>							
3. SUBSISTENCE <b>0</b>							
4. OTHER <b>0</b>							
TOTAL NUMBER OF PARTICIPANTS ( <b>0</b> ) TOTAL PARTICIPANT COSTS							<b>0</b>
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							<b>0</b>
2. PUBLICATION COSTS/DOCUMENTATION/DISEMINATION							<b>0</b>
3. CONSULTANT SERVICES							<b>0</b>
4. COMPUTER SERVICES							<b>0</b>
5. SUBAWARDS							<b>0</b>
6. OTHER							<b>0</b>
TOTAL OTHER DIRECT COSTS							<b>0</b>
H. TOTAL DIRECT COSTS (A THROUGH G)							<b>17,544</b>
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE) <b>Salaries/wages (Rate: 50.0000, Base: 14420)</b>							
TOTAL INDIRECT COSTS (F&A)							<b>7,210</b>
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							<b>24,754</b>
K. RESIDUAL FUNDS							<b>0</b>
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ <b>24,754</b> \$
M. COST SHARING PROPOSED LEVEL \$ <b>0</b>				AGREED LEVEL IF DIFFERENT \$			
PI/PI NAME <b>Thomas W Judson</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

2 \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET



# SUMMARY PROPOSAL BUDGET

YEAR 3

ORGANIZATION <b>Stephen F. Austin State University</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>Thomas W Judson</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PI, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>Thomas W Judson - Co-PI</b>				0.00	0.00	0.50	\$ <b>3,785</b>
2.							
3.							
4.							
5.							
6. ( 0 ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	<b>0</b>
7. ( 1 ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	0.50	<b>3,785</b>
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( 0 ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	<b>0</b>
2. ( 0 ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	<b>0</b>
3. ( 0 ) GRADUATE STUDENTS							<b>0</b>
4. ( 0 ) UNDERGRADUATE STUDENTS							<b>0</b>
5. ( 0 ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							<b>0</b>
6. ( 0 ) OTHER							<b>0</b>
TOTAL SALARIES AND WAGES (A + B)							<b>3,785</b>
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							<b>820</b>
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							<b>4,605</b>
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							<b>0</b>
E. TRAVEL 1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							<b>0</b>
2. FOREIGN							<b>0</b>
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS \$ <b>0</b>							
2. TRAVEL <b>0</b>							
3. SUBSISTENCE <b>0</b>							
4. OTHER <b>0</b>							
TOTAL NUMBER OF PARTICIPANTS ( 0 ) TOTAL PARTICIPANT COSTS							<b>0</b>
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							<b>0</b>
2. PUBLICATION COSTS/DOCUMENTATION/DISEMINATION							<b>0</b>
3. CONSULTANT SERVICES							<b>0</b>
4. COMPUTER SERVICES							<b>0</b>
5. SUBAWARDS							<b>0</b>
6. OTHER							<b>0</b>
TOTAL OTHER DIRECT COSTS							<b>0</b>
H. TOTAL DIRECT COSTS (A THROUGH G)							<b>4,605</b>
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE)							
<b>Salaries/wages (Rate: 50.0000, Base: 3785)</b>							
TOTAL INDIRECT COSTS (F&A)							<b>1,893</b>
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							<b>6,498</b>
K. RESIDUAL FUNDS							<b>0</b>
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ <b>6,498</b> \$
M. COST SHARING PROPOSED LEVEL \$ <b>0</b>				AGREED LEVEL IF DIFFERENT \$			
PI/PI NAME <b>Thomas W Judson</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

3 \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

# SUMMARY PROPOSAL BUDGET

Cumulative

ORGANIZATION <b>Stephen F. Austin State University</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>Thomas W Judson</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PI, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>Thomas W Judson - Co-PI</b>				0.00	0.00	3.75	\$ 26,788
2.							
3.							
4.							
5.							
6. ( ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	0
7. ( 1 ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	3.75	26,788
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( 0 ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	0
2. ( 0 ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	0
3. ( 0 ) GRADUATE STUDENTS							0
4. ( 0 ) UNDERGRADUATE STUDENTS							0
5. ( 0 ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							0
6. ( 0 ) OTHER							0
TOTAL SALARIES AND WAGES (A + B)							26,788
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							5,803
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							32,591
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							0
E. TRAVEL 1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							0
2. FOREIGN							0
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS \$ 0							
2. TRAVEL 0							
3. SUBSISTENCE 0							
4. OTHER 0							
TOTAL NUMBER OF PARTICIPANTS ( 0 ) TOTAL PARTICIPANT COSTS							0
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							0
2. PUBLICATION COSTS/DOCUMENTATION/DISEMINATION							0
3. CONSULTANT SERVICES							0
4. COMPUTER SERVICES							0
5. SUBAWARDS							0
6. OTHER							0
TOTAL OTHER DIRECT COSTS							0
H. TOTAL DIRECT COSTS (A THROUGH G)							32,591
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE)							
TOTAL INDIRECT COSTS (F&A)							13,395
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							45,986
K. RESIDUAL FUNDS							0
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ 45,986
M. COST SHARING PROPOSED LEVEL \$ 0				AGREED LEVEL IF DIFFERENT \$			
PI/PI NAME <b>Thomas W Judson</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

C \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

**Stephen F. Austin State University  
Budget Justification**

**Personnel**

In accordance with university estimates, cost-of-living raises have been calculated at 5% annually.

*Co-Principal Investigator.* As Co-PI, Dr. Thomas Judson will be responsible for the following:

- Year 1 (2010-2011). Work with Dr. Robert Beezer to create integrated curricular materials for linear algebra and abstract algebra. Work with the other members of the project to select test sites and assist in training faculty at these test sites. Assist Drs. Marja-Liisa Hassi and Sandra Laursen with the evaluation of the project.
- Year 2 (2011-2012). Work with Dr. Robert Beezer to create integrated curricular materials for linear algebra and abstract algebra. Work with the other members of the project to select test sites and assist in training faculty at these test sites. Assist Drs. Marja-Liisa Hassi and Sandra Laursen with the evaluation of the project.
- Year 3 (2012-2013). Work with the other members of the project to train faculty at the test sites. Assist Drs. Marja-Liisa Hassi and Sandra Laursen with the evaluation of the project.

Funds are requested during the summer months only, although Dr. Judson will be involved in the project during the academic year as well. Specifically, summer salary is requested at \$8,583 for 1.25 months in Year 1; \$14,420 for 2 months in Year 2; and \$3,785 for .5 months in Year 3. (The requested amounts for this project have been calculated to ensure that Dr. Judson's NSF-funded salary across all projects will not exceed a total of 2 months per year.)

**Fringe Benefits**

The university's fringe benefits for full-time faculty include FICA/Medicare, retirement matching, worker's compensation, and unemployment compensation calculated at 16.05% of salary plus health insurance. Dr. Judson's fringe benefits are requested in proportion to his requested summer salary, with \$1,859 in Year 1; \$3,124 in Year 2; and \$820 in Year 3.

**Indirect Costs**

Stephen F. Austin State University's DHHS-negotiated indirect cost rate is 50% salaries and wages (excluding fringe benefits). Accordingly, \$4,292 is requested in Year 1; \$7,210 is requested in Year 2; and \$1,893 is requested in Year 3.

**TOTAL ANNUAL REQUEST**

Year 1 = \$14,734

Year 2 = \$24,754

Year 3 = \$6,498

## YEAR 2

2 \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

# SUMMARY PROPOSAL BUDGET

YEAR 3

ORGANIZATION <b>University of Washington</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>William A Stein</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PI, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>William A Stein - none</b>				0.00	0.00	2.00	\$ 22,251
2.							
3.							
4.							
5.							
6. ( 0 ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	0
7. ( 1 ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	2.00	22,251
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( 0 ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	0
2. ( 0 ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	0
3. ( 0 ) GRADUATE STUDENTS							0
4. ( 0 ) UNDERGRADUATE STUDENTS							0
5. ( 0 ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							0
6. ( 0 ) OTHER							0
TOTAL SALARIES AND WAGES (A + B)							22,251
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							5,251
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							27,502
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							0
E. TRAVEL 1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							0
2. FOREIGN							0
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS \$ 0							
2. TRAVEL 0							
3. SUBSISTENCE 0							
4. OTHER 0							
TOTAL NUMBER OF PARTICIPANTS ( 0 ) TOTAL PARTICIPANT COSTS							0
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							0
2. PUBLICATION COSTS/DOCUMENTATION/DISEMINATION							0
3. CONSULTANT SERVICES							0
4. COMPUTER SERVICES							0
5. SUBAWARDS							0
6. OTHER							0
TOTAL OTHER DIRECT COSTS							0
H. TOTAL DIRECT COSTS (A THROUGH G)							27,502
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE) <b>A., C. (Rate: 56.0000, Base: 27502)</b>							
TOTAL INDIRECT COSTS (F&A)							15,401
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							42,903
K. RESIDUAL FUNDS							0
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ 42,903
M. COST SHARING PROPOSED LEVEL \$ 0				AGREED LEVEL IF DIFFERENT \$			
PI/PD NAME <b>William A Stein</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

3 \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

# SUMMARY PROPOSAL BUDGET

Cumulative

ORGANIZATION <b>University of Washington</b>				FOR NSF USE ONLY			
PRINCIPAL INVESTIGATOR / PROJECT DIRECTOR <b>William A Stein</b>				PROPOSAL NO.	DURATION (months)		
				AWARD NO.	Proposed	Granted	
A. SENIOR PERSONNEL: PI/PD, Co-PI's, Faculty and Other Senior Associates (List each separately with title, A.7. show number in brackets)				NSF Funded Person-months		Funds Requested By proposer	Funds granted by NSF (if different)
				CAL	ACAD	SUMR	
1. <b>William A Stein - none</b>				0.00	0.00	4.00	\$ <b>43,646</b>
2.							
3.							
4.							
5.							
6. ( ) OTHERS (LIST INDIVIDUALLY ON BUDGET JUSTIFICATION PAGE)				0.00	0.00	0.00	<b>0</b>
7. ( <b>1</b> ) TOTAL SENIOR PERSONNEL (1 - 6)				0.00	0.00	4.00	<b>43,646</b>
B. OTHER PERSONNEL (SHOW NUMBERS IN BRACKETS)							
1. ( <b>0</b> ) POST DOCTORAL SCHOLARS				0.00	0.00	0.00	<b>0</b>
2. ( <b>0</b> ) OTHER PROFESSIONALS (TECHNICIAN, PROGRAMMER, ETC.)				0.00	0.00	0.00	<b>0</b>
3. ( <b>0</b> ) GRADUATE STUDENTS							<b>0</b>
4. ( <b>0</b> ) UNDERGRADUATE STUDENTS							<b>0</b>
5. ( <b>0</b> ) SECRETARIAL - CLERICAL (IF CHARGED DIRECTLY)							<b>0</b>
6. ( <b>0</b> ) OTHER							<b>0</b>
TOTAL SALARIES AND WAGES (A + B)							<b>43,646</b>
C. FRINGE BENEFITS (IF CHARGED AS DIRECT COSTS)							<b>10,300</b>
TOTAL SALARIES, WAGES AND FRINGE BENEFITS (A + B + C)							<b>53,946</b>
D. EQUIPMENT (LIST ITEM AND DOLLAR AMOUNT FOR EACH ITEM EXCEEDING \$5,000.)							
TOTAL EQUIPMENT							<b>0</b>
E. TRAVEL            1. DOMESTIC (INCL. CANADA, MEXICO AND U.S. POSSESSIONS)							<b>0</b>
2. FOREIGN							<b>0</b>
F. PARTICIPANT SUPPORT COSTS							
1. STIPENDS        \$ _____ <b>0</b>							
2. TRAVEL                _____ <b>0</b>							
3. SUBSISTENCE        _____ <b>0</b>							
4. OTHER                _____ <b>0</b>							
TOTAL NUMBER OF PARTICIPANTS    ( <b>0</b> )                      TOTAL PARTICIPANT COSTS							<b>0</b>
G. OTHER DIRECT COSTS							
1. MATERIALS AND SUPPLIES							<b>0</b>
2. PUBLICATION COSTS/DOCUMENTATION/DISSEMINATION							<b>0</b>
3. CONSULTANT SERVICES							<b>0</b>
4. COMPUTER SERVICES							<b>0</b>
5. SUBAWARDS							<b>0</b>
6. OTHER							<b>0</b>
TOTAL OTHER DIRECT COSTS							<b>0</b>
H. TOTAL DIRECT COSTS (A THROUGH G)							<b>53,946</b>
I. INDIRECT COSTS (F&A)(SPECIFY RATE AND BASE)							
TOTAL INDIRECT COSTS (F&A)							<b>30,210</b>
J. TOTAL DIRECT AND INDIRECT COSTS (H + I)							<b>84,156</b>
K. RESIDUAL FUNDS							<b>0</b>
L. AMOUNT OF THIS REQUEST (J) OR (J MINUS K)							\$ <b>84,156</b> \$
M. COST SHARING PROPOSED LEVEL \$ <b>0</b>				AGREED LEVEL IF DIFFERENT \$			
PI/PD NAME <b>William A Stein</b>				FOR NSF USE ONLY			
ORG. REP. NAME*				INDIRECT COST RATE VERIFICATION			
				Date Checked	Date Of Rate Sheet	Initials - ORG	

C \*ELECTRONIC SIGNATURES REQUIRED FOR REVISED BUDGET

## **Budget Justification**

### **A. Salary**

PI is requesting salary for two months each summer starting in year 2 with a 4% increase in year 3 to participate in this collaborative research with AIMath.org. PI is not requesting support in year 1.

### **C. Benefits**

Benefits are calculated in PI salary at 23.6% according to a negotiated rate established by the university every two years or biennium.

### **I. Indirect Cost**

The Indirect Cost Rate for on-campus research of 56% is the negotiated by the university with the cognizant institution, DHHS, in the agreement of October 13, 2009 .

(See GPG Section II.C.2.h for guidance on information to include on this form.)

Investigator: Kiran Kedlaya

Support: ☒ Current ☐ Pending ☐ Submission Planned in Near Future ☐ \*Transfer of Support

Project/Proposal Title: Cohomological methods in algebraic geometry and number theory

Total Award Amount: \$ 400,000 Total Award Period Covered: 07/01/06 - 06/30/11

Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 2.00

Total Award Amount: \$ Total Award Period Covered:

Person-Months Per Year Committed to the Project.      Cal:              Acad:              Sumr:

Total Award Amount: \$ Total Award Period Covered:

Person-Months Per Year Committed to the Project.      Cal:              Acad:              Sumr:

Total Award Amount: \$ Total Award Period Covered:

Person-Months Per Year Committed to the Project.      Cal:              Acad:              Sumr:

Total Award Amount: \$ Total Award Period Covered:

Person-Months Per Year Committed to the Project.	Cal:	Acad:	Summ:
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			
17			
18			
19			
20			
21			
22			
23			
24			
25			
26			
27			
28			
29			
30			
31			
32			
33			
34			
35			
36			
37			
38			
39			
40			
41			
42			
43			
44			
45			
46			
47			
48			
49			
50			
51			
52			
53			
54			
55			
56			
57			
58			
59			
60			
61			
62			
63			
64			
65			
66			
67			
68			
69			
70			
71			
72			
73			
74			
75			
76			
77			
78			
79			
80			
81			
82			
83			
84			
85			
86			
87			
88			
89			
90			
91			
92			
93			
94			
95			
96			
97			
98			
99			
100			

USE ADDITIONAL SHEETS AS NECESSARY



## Current and Pending Support

(See GPG Section II.C.2.h for guidance on information to include on this form.)

The following information should be provided for each investigator and other senior personnel. Failure to provide this information may delay consideration of this proposal.			
Investigator: Thomas Judson	Other agencies (including NSF) to which this proposal has been/will be submitted.		
Support: <input type="checkbox"/> Current <input checked="" type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    UTMOST: Undergraduate Teaching in Mathematics with Open Software and Textbooks			
Source of Support:    National Science Foundation Total Award Amount: \$    45,986 Total Award Period Covered:    09/01/10 - 08/31/13 Location of Project:    Stephen F. Austin State University Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 1.25			
Support: <input checked="" type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    Texas Leadership Initiative: Mathematics Instruction Transformed (Texas LIMIT)			
Source of Support:    National Science Foundation Total Award Amount: \$    1,494,187 Total Award Period Covered:    06/01/09 - 05/31/15 Location of Project:    Stephen F. Austin State University Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 1.35    Sumr: 0.50			
Support: <input checked="" type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    Texas Middle and Secondary Mathematics Project - Supplemental Funds			
Source of Support:    National Science Foundation Total Award Amount: \$    581,821 Total Award Period Covered:    09/11/08 - 09/30/12 Location of Project:    Stephen F. Austin State University Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 1.13    Sumr: 0.75			
Support: <input type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:			
Source of Support: Total Award Amount: \$                      Total Award Period Covered: Location of Project: Person-Months Per Year Committed to the Project.    Cal:                      Acad:                      Sumr:			
Support: <input type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:			
Source of Support: Total Award Amount: \$                      Total Award Period Covered: Location of Project: Person-Months Per Year Committed to the Project.    Cal:                      Acad:                      Summ:			

\*If this project has previously been funded by another agency, please list and furnish information for immediately preceding funding period.

## Current and Pending Support

(See GPG Section II.C.2.h for guidance on information to include on this form.)

The following information should be provided for each investigator and other senior personnel. Failure to provide this information may delay consideration of this proposal.	
Investigator: William Stein	Other agencies (including NSF) to which this proposal has been/will be submitted.

Support: <input checked="" type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    SAGE Software for Algebra and Geometry Experimentation
Source of Support:    NSF Total Award Amount: \$    144,543 Total Award Period Covered:    07/15/07 - 06/30/10 Location of Project:    University of Washington Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 0.00

Support: <input checked="" type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    Explicit Approaches to the Birch and Swinnerton-Dyer Conjecture
Source of Support:    NSF Total Award Amount: \$    129,994 Total Award Period Covered:    09/01/07 - 08/31/10 Location of Project:    University of Washington Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 2.00

Support: <input checked="" type="checkbox"/> Current <input type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    SCREMS: The Computational Frontiers of Number Theory, Representation Theory and Mathematical Physics
Source of Support:    NSF Total Award Amount: \$    106,869 Total Award Period Covered:    09/01/08 - 08/31/11 Location of Project:    University of Washington Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 0.00

Support: <input type="checkbox"/> Current <input checked="" type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    SAGE: Unifying Mathematical Software for Scientists, Engineers and Mathematicians
Source of Support:    NSF Total Award Amount: \$    239,358 Total Award Period Covered:    07/01/10 - 06/30/13 Location of Project:    University of Washington Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Sumr: 0.50

Support: <input type="checkbox"/> Current <input checked="" type="checkbox"/> Pending <input type="checkbox"/> Submission Planned in Near Future <input type="checkbox"/> *Transfer of Support Project/Proposal Title:    UTMOST: Undergraduate Teaching in Mathematics with Open Software and Textbooks
Source of Support:    NSF via AIMath.org (collaborative research) Total Award Amount: \$    84,155 Total Award Period Covered:    09/01/10 - 08/31/13 Location of Project:    University of Washington Person-Months Per Year Committed to the Project.    Cal:0.00    Acad: 0.00    Summ: 2.00

\*If this project has previously been funded by another agency, please list and furnish information for immediately preceding funding period.

## FACILITIES, EQUIPMENT & OTHER RESOURCES

---

**FACILITIES:** Identify the facilities to be used at each performance site listed and, as appropriate, indicate their capacities, pertinent capabilities, relative proximity, and extent of availability to the project. Use "Other" to describe the facilities at any other performance sites listed and at sites for field studies. USE additional pages as necessary.

**Laboratory:** Laboratory space will be in the teaching lab and research labs in the Department of Mathematics and Statistics within the SFA College of Science and Mathematics. The Department has dedicated laboratory classrooms for computer-based instruction.

**Clinical:** NA

**Animal:** NA

**Computer:** The Department of Mathematics and Statistics currently operates two computer laboratories for classroom use and maintains up-to-date statistics, computer algebra, and dynamic geometry software on computers in these labs.

**Office:** The proposed PI at SFA has his own offices and desktop computer which will be used during the project period.

**Other:** NA

---

**MAJOR EQUIPMENT:** List the most important items available for this project and, as appropriate identifying the location and pertinent capabilities of each.

NA

---

**OTHER RESOURCES:** Provide any information describing the other resources available for the project. Identify support services such as consultant, secretarial, machine shop, and electronics shop, and the extent to which they will be available for the project. Include an explanation of any consortium/contractual arrangements with other organizations.

NA

---

## FACILITIES, EQUIPMENT & OTHER RESOURCES

---

**FACILITIES:** Identify the facilities to be used at each performance site listed and, as appropriate, indicate their capacities, pertinent capabilities, relative proximity, and extent of availability to the project. Use "Other" to describe the facilities at any other performance sites listed and at sites for field studies. USE additional pages as necessary.

**Laboratory:**

**Clinical:**

**Animal:**

**Computer:** Mathematics Department facilities at the University of Washington for research/administrative computing: Windows 2003 R2 SP2 File/Print Server - 1.5TB disk storage, 4 Xeon Processors at 2GHz, 4GB RAM RHEL 3 Web Server - 36GB disk storage, 2 Pentium III Processors at 800MHz, 2GB RAM RHEL 3

**Office:** PI has a private office, Padelford C423.

**Other:**

---

**MAJOR EQUIPMENT:** List the most important items available for this project and, as appropriate identifying the location and pertinent capabilities of each.

---

**OTHER RESOURCES:** Provide any information describing the other resources available for the project. Identify support services such as consultant, secretarial, machine shop, and electronics shop, and the extent to which they will be available for the project. Include an explanation of any consortium/contractual arrangements with other organizations.

Library Facilities are available both within the department an on the main campus.

---

## FACILITIES, EQUIPMENT & OTHER RESOURCES

---

Continuation Page:

### COMPUTER FACILITIES (continued):

Email Server - 36GB disk storage, 2 Pentium III Processors at 800MHz, 2GB  
RAM RHEL 3 Compute Servers (2) - 36GB disk storage, 2 Pentium III  
Processors at 800MHz, 2GB RAM.