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1. Show that for any positive integer n , an injective (one-to-one) function $f : \{1, 2, \dots, n\} \rightarrow \{1, 2, \dots, n\}$ must be a bijection.
2. Find a bijection between \mathbb{N} and the set of all integers congruent to 1 mod n , for a fixed n .
3. Are these sets countably infinite/uncountably infinite/finite? If finite, what is the order of the set? Reminder: A bit string is a sequence of digits where each digit corresponds to either a 1 (on) or a 0 (off).
 - (a) Finite bit strings of length n .
 - (b) All finite bit strings of length 1 to n .
 - (c) All finite bit strings
 - (d) All infinite bit strings
 - (e) All finite or infinite bit strings.
 - (f) Suppose that we try to show that infinite bit strings are countable by induction. We show that for any positive integer n , a bit string of length n is countable. Why does this not work for infinite strings?
4. Is the power set $\mathcal{P}(S)$, where S is countably infinite, finite, countably infinite, or uncountably infinite? Provide a proof for your answer. Reminder: the power set of a set is the set of all possible subsets of that set. Ex: $S = \{A, B\}$, $\mathcal{P}(S) = \{\{\}, \{A\}, \{B\}, \{A, B\}\}$

