1 RSA Practice

Consider the following RSA schemes and solve for asked variables.

- (a) Assume for an RSA scheme we pick 2 primes p = 5 and q = 11 with encryption key e = 9, what is the decryption key d? Calculate the exact value.
- (b) If the receiver gets 4, what was the original message?
- (c) Encode your answer from part (b) to check its correctness.

2 RSA Practice

Bob would like to receive encrypted messages from Alice via RSA.

- (a) Bob chooses p = 7 and q = 11. His public key is (N, e). What is N?
- (b) What number is *e* relatively prime to?
- (c) *e* need not be prime itself, but what is the smallest prime number *e* can be? Use this value for *e* in all subsequent computations.
- (d) What is gcd(e, (p-1)(q-1))?
- (e) What is the decryption exponent d?

- (f) Now imagine that Alice wants to send Bob the message 30. She applies her encryption function *E* to 30. What is her encrypted message?
- (g) Bob receives the encrypted message, and applies his decryption function D to it. What is D applied to the received message?

3 RSA Lite

Woody misunderstood how to use RSA. So he selected prime P = 101 and encryption exponent e = 67, and encrypted his message m to get $35 = m^e \mod P$. Unfortunately he forgot his original message m and only stored the encrypted value 35. But Carla thinks she can figure out how to recover m from $35 = m^e \mod P$, with knowledge only of P and e. Is she right? Can you help her figure out the message m? Show all your work.

4 RSA with Three Primes

Show how you can modify the RSA encryption method to work with three primes instead of two primes (i.e. N = pqr where p,q,r are all prime), and prove the scheme you come up with works in the sense that $D(E(x)) \equiv x \pmod{N}$.

CS 70, Fall 2020, DIS 04B