

Week 6: Counting

1. I have a 6-sided die. I roll it 5 times.

ABCDE 5!

(a) How many sequences of 5 numbers?

$$6^5$$

— — — — — 6 choices per spot

12113 51543
11213, 55143, 65423, ...

(b) How many sequences like 66666? 1

like $x_1 x_2 x_3 x_4 x_5$, $x_i \in \{5, 6\}$? 2^5

— — — — —

55565 ✓ 66656 ✓ 46654 X

(c) How many contain at least one 3?

$$6^5 - 5^5 = 4651$$

31333 ✓ 66653 ✓ 12456 X

$$5 \cdot 6^4 = 5 \cdot 1296 = 6480$$

$$\begin{array}{r} \text{— — — — —} \\ 3 \\ \hline 33333 \end{array}$$