

CP Template

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1 Custom Codes

```
freopen("input.in", "r", stdin);
freopen("output.out", "w", stdout);
ios_base::sync_with_stdio(0), cin.tie(0);
// pragma
#pragma GCC optimize("Ofast")
#pragma GCC target("avx,avx2,fma")
#pragma GCC optimize ("O3,unroll-loops")
#pragma GCC optimize ("-ffloat-store")
#pragma GCC target ("bmi,bmi2,lzcnt,popcnt")
#pragma GCC target
    ↪ ("sse,sse2,sse3,ssse3,sse4,abm,mmx")
// random number generator
mt19937_64
    ↪ rng(chrono::steady_clock::now().time_since_epoch().count());
int num = rng() % limit;
int64_t rnd(int64_t l, int64_t r) { // can handle
    ↪ negative range also
    if (l > r) swap(l, r);
    return l + (rng() % (r - l + 1));
}
// ignore white space
cin.ignore(); or cin >> ws;
// STL merge function: merge two vectors or sets
vector<int> a = {1, 2, 7}, b = {4, 2, 3};
sort(a.begin(), a.end());
sort(b.begin(), b.end());
vector<int> c(a.size() + b.size());
merge(a.begin(), a.end(), b.begin(), b.end(),
    ↪ c.begin());

set<int> a = {3, 2, 1}, b = {4, 5, 1};
set<int> c;
merge(a.begin(), a.end(), b.begin(), b.end(),
    ↪ inserter(c, c.begin()));
// tuple
tuple<int, int, int> tup = {1, 2, 3};
int first = get<0>(tup);
// custom compare function
struct item {
    int a, b;
};
bool cmp(item& a, item& b) {
    if(a.a != b.a) return a.a < b.a;
    return a.b > b.b;
}
bool custom(pair<int, int>& a, pair<int, int>& b) {
    if(a.first != b.first) return a.first > b.first;
    return a.second < b.second;
}
// custom compare in set
struct cmp{
    bool operator() (const pair<int, int>& a, const
        ↪ pair<int, int>& b) const {
        if (a.first != b.first) return a.first > b.first;
        return a.second < b.second;
    }
};
set<pair<int, int>, cmp> a;
```

```
// greater functions
priority_queue<int, vector<int>, greater<int>>
set<int, greater<int>>
map<int, int, greater<int>>
// fill with elements
fill(v.begin(), v.end(), -1);
// fill for array
fill(&dp[0][0][0], &dp[0][0][0] + N * M * N, INF);
// string to number
stoi(num);
// number to string
to_string(num);
// Binary to decimal
int n = stoi(binary, 0, 2);
// decimal to binary
string binary = bitset<64>(n).to_string();
binary.erase(0, binary.find_first_not_of('0'));
// count digit
int d = log10(num) + 1;
// set ith bit
n | (1 << i)
// unset ith bit
n & ~(1 << i)
// toggle or inverse ith bit
n ^ (1 << i)
__builtin_popcountll(x)
__builtin_clzll(x)
__builtin_ctzll(x)
```

2 Articulation Bridge

```
vector<int> adj[N];
int t = 0;
vector<int> tin(N, -1), low(N);
vector<array<int, 2>> ab;
void dfs (int u, int p) {
    tin[u] = low[u] = t++;
    for (int v: adj[u]) {
        if (v != p) {
            if (tin[v] != -1) {
                low[u] = min(low[u], tin[v]);
            } else {
                dfs(v, u);
                if (tin[u] < low[v]) {
                    ab.push_back({u, v});
                }
                low[u] = min(low[u], low[v]);
            }
        }
    }
}
```

3 Articulation Point

```
vector<int> adj[N];
int t = 0;
vector<int> tin(N, -1), low(N), ap;
void dfs (int u, int p) {
    tin[u] = low[u] = t++;
    int is_ap = 0, child = 0;
```

```
for (int v: adj[u]) {
    if (v != p) {
        if (tin[v] != -1) {
            low[u] = min(low[u], tin[v]);
        } else {
            child++;
            dfs(v, u);
            if (tin[u] <= low[v]) {
                is_ap = 1;
            }
            low[u] = min(low[u], low[v]);
        }
    }
}
if ((u != p or child > 1) and is_ap) {
    ap.push_back(u);
}
}
```

4 Bellman Ford

```
struct st {
    int a, b, cost;
} e[N];
const int INF = 2e9;
int32_t main() {
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < m; i++) cin >> e[i].a >> e[i].b
        ↪ >> e[i].cost;
    int s;
    cin >> s; //is there any negative cycle which is
    ↪ reachable from s?
    vector<int> d(n, INF); //for finding any cycle(not
    ↪ necessarily from s) set d[i] = 0 for all i
    d[s] = 0;
    vector<int> p(n, -1);
    int x;
    for (int i=0; i<n; ++i) {
        x = -1;
        for (int j=0; j<m; ++j) {
            if (d[e[j].a] < INF) {
                if (d[e[j].b] > d[e[j].a] + e[j].cost) {
                    d[e[j].b] = max(-INF, d[e[j].a] +
                        ↪ e[j].cost); //for overflow
                    p[e[j].b] = e[j].a;
                    x = e[j].b;
                }
            }
        }
    }
    if (x == -1) cout << "No negative cycle from "<<s;
    else {
        int y = x; //x can be on any cycle or reachable
        ↪ from some cycle
        for (int i=0; i<n; ++i) y = p[y];
        vector<int> path;
        for (int cur=y; ; cur=p[cur]) {
            path.push_back (cur);
            if (cur == y && path.size() > 1) break;
        }
    }
}
```

```

    }
    reverse (path.begin(), path.end());
    cout << "Negative cycle: ";
    for (int i=0; i<path.size(); ++i) cout << path[i]
    ↪ << ' ';
}
return 0;
}
// ## Bellman-ford (V * E)
vector<int> bellman_ford(int s){
    vector<int> dis(n, I);
    dis[s]=0;
    while(1){
        int any=0;
        for (auto& e: ed){
            if(dis[e.u]<I){
                if(dis[e.u]+e.cost < dis[e.v]){
                    dis[e.v] = dis[e.u]+e.cost;
                    any=1;
                }
            }
        }
        if(!any) break;
    }
    return dis;
}

```

5 Binary & Ternary Search

```

//Binary Search (integer)
int lo = 0, hi = n - 1;
while (lo <= hi) {
    int mid = (lo + hi) / 2;
    if (f(mid)) hi = mid - 1;
    else lo = mid + 1;
}
//Binary Search (double)
double lo = 0, hi = inf;
int itr = 50;
while (itr--){
    double mid = (lo + hi) / 2;
    if (f(mid)) hi = mid;
    else lo = mid;
}
//Ternary Search (integer, max)
int lo = 0, hi = n - 1;
while (lo < hi) {
    // int mid1 = lo + (hi - lo) / 3;
    // int mid2 = hi - (hi - lo) / 3;
    int mid = (lo + hi) / 2;
    if (f(mid) < f(mid + 1)) lo = mid + 1;
    else hi = mid;
}
//Ternary Search (double, max)
double lo = 0, hi = inf;
int itr = 50;
while (itr--){
    double mid1 = lo + (hi - lo) / 3;
    double mid2 = hi - (hi - lo) / 3;
    if (f(mid1) < f(mid2)) lo = mid1;

```

```

    else hi = mid2;
}

```

6 2D BIT Range Update & Range Query

```

const int N = 1009;
struct BIT2D {
    long long M[N][N][2], A[N][N][2];
    BIT2D() {
        memset(M, 0, sizeof M);
        memset(A, 0, sizeof A);
    }
    void upd2(long long t[N][N][2], int x, int y, long
    ↪ long mul, long long add) {
        for(int i = x; i < N; i += i & -i) {
            for(int j = y; j < N; j += j & -j) {
                t[i][j][0] += mul;
                t[i][j][1] += add;
            }
        }
    }
    void upd1(int x, int y1, int y2, long long mul, long
    ↪ long add) {
        upd2(M, x, y1, mul, -mul * (y1 - 1));
        upd2(M, x, y2, -mul, mul * y2);
        upd2(A, x, y1, add, -add * (y1 - 1));
        upd2(A, x, y2, -add, add * y2);
    }
    void upd(int x1, int y1, int x2, int y2, long long
    ↪ val) {
        upd1(x1, y1, y2, val, -val * (x1 - 1));
        upd1(x2, y1, y2, -val, val * x2);
    }
    long long query2(long long t[N][N][2], int x, int y)
    ↪ {
        long long mul = 0, add = 0;
        for(int i = y; i > 0; i -= i & -i) {
            mul += t[x][i][0];
            add += t[x][i][1];
        }
        return mul * y + add;
    }
    long long query1(int x, int y) {
        long long mul = 0, add = 0;
        for(int i = x; i > 0; i -= i & -i) {
            mul += query2(M, i, y);
            add += query2(A, i, y);
        }
        return mul * x + add;
    }
    long long query(int x1, int y1, int x2, int y2) {
        return query1(x2, y2) - query1(x1 - 1, y2) -
        ↪ query1(x2, y1 - 1) + query1(x1 - 1, y1 - 1);
    }
};

```

7 Centroid Decomposition

```

struct CentroidDecomposition {

```

```

    using T = vector<vector<int>>;
    int n;
    vector<int> sz, is_cen, cpar, cdep;
    CentroidDecomposition(T& adj, int root = 1) {
        n = (int)adj.size() + 1;
        sz.resize(n), is_cen.resize(n), cpar.resize(n),
        ↪ cdep.resize(n);
        Decompose(root, -1, 0, adj);
    }
    void Cal_sz(int u, int p, T& adj) {
        sz[u] = 1;
        for (auto& v : adj[u]) {
            if (v != p && !is_cen[v]) {
                Cal_sz(v, u, adj);
                sz[u] += sz[v];
            }
        }
    }
    int Get_cen(int u, int p, int csz, T& adj) {
        for (auto& v : adj[u]) {
            if (v != p && !is_cen[v] && (2 * sz[v] > csz)) {
                return Get_cen(v, u, csz, adj);
            }
        }
        return u;
    }
    void Decompose(int u, int p, int d, T& adj) {
        Cal_sz(u, p, adj);
        int c = Get_cen(u, p, sz[u], adj);
        is_cen[c] = 1, cpar[c] = p, cdep[c] = d;
        for (auto& v : adj[c]) {
            if (!is_cen[v]) {
                Decompose(v, c, d + 1, adj);
            }
        }
    }
};

```

8 Closest Index Where Each Element is Distinct

```

// 0 based, closest index where each element is
↪ distinct
array<vector<int>, 2>
↪ closestDistinctElementIndex(vector<int>& a) {
    int n = a.size(), mxIdx = -1;
    map<int, int> mp;
    vector<int> l(n);
    for (int i = 0; i < n; i++) {
        if (mp.count(a[i])) mxIdx = max(mxIdx, mp[a[i]]);
        mp[a[i]] = i, l[i] = i - mxIdx;
    }
    mp.clear(), mxIdx = n;
    vector<int> r(n);
    for (int i = n - 1; i >= 0; i--) {
        if (mp.count(a[i])) mxIdx = min(mxIdx, mp[a[i]]);
        mp[a[i]] = i, r[i] = mxIdx - i;
    }
    return {l, r};
}

```

9 Closest Min Max

```
// closest left, right index where current element is
// ↪ max or min
// closest max or min element from the current element
array<vector<int>, 2> closest_min_element(vector<int>
    ↪ &a) {
    int n = a.size();
    vector<int> l(n), r(n);
    stack<int> st;
    st.push(-1);
    for (int i = 0; i < n; i++) {
        while (st.top() != -1 && a[st.top()] > a[i])
            ↪ st.pop();
        l[i] = st.top() + 1; // closest index where
        ↪ current element is min
        // l[i] = st.top(); // closest min element index
        st.push(i);
    }
    while (!st.empty()) st.pop();
    st.push(n);
    for (int i = n - 1; i >= 0; i--) {
        while (st.top() != n && a[st.top()] >= a[i])
            ↪ st.pop();
        r[i] = st.top() - 1; // closest index where
        ↪ current element is min
        // r[i] = st.top(); // closest min element index
        st.push(i);
    }
    return {l, r};
}

array<vector<int>, 2> closest_max_element(vector<int>
    ↪ &a) {
    int n = a.size();
    vector<int> l(n), r(n);
    stack<int> st;
    st.push(-1);
    for (int i = 0; i < n; i++) {
        while (st.top() != -1 && a[st.top()] < a[i])
            ↪ st.pop();
        l[i] = st.top() + 1;
        // l[i] = st.top(); // closest max element index
        st.push(i);
    }
    while (!st.empty()) st.pop();
    st.push(n);
    for (int i = n - 1; i >= 0; i--) {
        while (st.top() != n && a[st.top()] <= a[i])
            ↪ st.pop();
        r[i] = st.top() - 1;
        // r[i] = st.top(); // closest max element index
        st.push(i);
    }
    return {l, r};
}
```

10 Compress Array

```
void CompressArray(vector<int>& a) {
```

```
    auto b = a;
    sort(b.begin(), b.end());
    b.erase(unique(b.begin(), b.end()), b.end());
    for (auto& ai : a) {
        ai = lower_bound(b.begin(), b.end(), ai) -
            ↪ b.begin();
    }
}
```

11 Convex Hull

```
const double PI = acos((double)-1.0);
using ll = long long;
struct PT {
    ll x, y;
    bool operator < (const PT &p) const {
        return x == p.x ? y < p.y : x < p.x;
    }
};
ll area(PT a, PT b, PT c) {
    return (b.x - a.x) * (c.y - a.y) - (b.y - a.y) *
        ↪ (c.x - a.x);
}

vector<PT> ConvexHull(vector<PT> p) {
    int n = p.size(), m = 0;
    if (n < 3) return p;
    vector<PT> hull(n + n);
    sort(p.begin(), p.end());
    for (int i = 0; i < n; ++i) {
        while (m > 1 and area(hull[m - 2], hull[m - 1],
            ↪ p[i]) <= 0) --m;
        hull[m++] = p[i];
    }
    for (int i = n - 2, j = m + 1; i >= 0; --i) {
        while (m >= j and area(hull[m - 2], hull[m - 1],
            ↪ p[i]) <= 0) --m;
        hull[m++] = p[i];
    }
    hull.resize(m - 1);
    return hull;
}
```

12 DFS with LCA

```
struct DFS {
    int n, k, t = 0;
    vector<int> tin, tout, depth, height, subtree_size,
        ↪ heavy;
    vector<bool> is_leaf;
    vector<vector<int>> parent;
    DFS() {}
    DFS(vector<vector<int>>& adj, int root = 1) {
        n = (int)adj.size() + 1;
        k = __lg(n) + 1;
        tin.resize(n), tout.resize(n), depth.resize(n),
            ↪ height.resize(n), subtree_size.resize(n),
            ↪ heavy.assign(n, -1), is_leaf.assign(n, 1);
        parent = vector<vector<int>>(n, vector<int>(k));
        dfs(root, root, adj);
    }
};
```

```

    }
    void dfs(int u, int p, vector<vector<int>>& adj) {
        tin[u] = ++t;
        subtree_size[u] = 1;
        parent[u][0] = p;
        for (int i = 1; i < k; i++) {
            if (parent[u][i - 1] != -1) parent[u][i] =
                ↪ parent[parent[u][i - 1]][i - 1];
            else parent[u][i] = -1;
        }
        for (auto& v : adj[u]) {
            if (v != p) {
                depth[v] = depth[u] + 1;
                is_leaf[u] = 0;
                dfs(v, u, adj);
                height[u] = max(height[u], height[v] + 1);
                subtree_size[u] += subtree_size[v];
                if (heavy[u] == -1 || subtree_size[heavy[u]] <
                    ↪ subtree_size[v]) {
                    heavy[u] = v;
                }
            }
        }
        tout[u] = ++t;
    }

    bool is_ancestor(int u, int v) {
        return tin[u] <= tin[v] && tout[v] <= tout[u];
    }

    int kth_parent(int u, int kth) {
        for (int i = k - 1; i >= 0; i--) {
            if (kth & (1 << i)) {
                u = parent[u][i];
                if (u == -1) return u;
            }
        }
        return u;
    }

    int lca(int u, int v) {
        if (is_ancestor(u, v)) return u;
        for (int i = k - 1; i >= 0; i--) {
            if (!is_ancestor(parent[u][i], v)) {
                u = parent[u][i];
            }
        }
        return parent[u][0];
    }

    int dis(int u, int v) {
        return depth[u] + depth[v] - 2 * depth[lca(u, v)];
    }
};
```

13 Dijkstra

```
using ll = long long;
const ll INF = 1.1e17;
vector<ll> Dijkstra(vector<vector<array<ll, 2>>>& adj,
    ↪ int source = 1) {
    int n = (int)adj.size();
    vector<ll> dis(n, INF);
    vector<bool> vis(n);
    dis[source] = 0;
```

```

priority_queue<array<ll, 2>, vector<array<ll, 2>>,
    greater<array<ll, 2>>> pq;
pq.push({0, source});
while (!pq.empty()) {
    auto [d, u] = pq.top();
    pq.pop();
    if (vis[u]) continue;
    vis[u] = 1;
    for (auto& [v, c] : adj[u]) {
        if (dis[v] > d + c) {
            dis[v] = d + c;
            pq.push({dis[v], v});
        }
    }
    return dis;
}

```

14 Digit DP

```

#2 countWithExactDigitCount // f(0, 0, 1, 0)
int dp[11][11][2][2];
int targetDigit, targetCnt;
int f(int i, int digitCnt, int tight, int started) {
    if (i == n) {
        return targetCnt == digitCnt;
    }
    auto& ret = dp[i][digitCnt][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newDigitCnt = digitCnt;
        if (newStarted) newDigitCnt += (d == targetDigit);
        ret += f(i + 1, newDigitCnt, newTight,
            newStarted);
    }
    return ret;
}

#6 countNumbersWithOnly1234 // f(0, 1, 0)
int dp[11][2][2];
int f(int i, int tight, int started) {
    if (i == n) {
        return started;
    }
    auto& ret = dp[i][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        if (d > 4) continue;
        if (!newStarted && d == 0) ret += f(i + 1,
            newTight, newStarted);
        else if (d >= 1 && d <= 4) ret += f(i + 1,
            newTight, newStarted);
    }
}

```

```

    return ret;
}

#8 countDistinctDigitNumbers // f(0, 0, 1, 0)
int dp[11][1025][2][2];
int f(int i, int mask, int tight, int started) {
    if (i == n) return started;
    auto& ret = dp[i][mask][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) {
            if (mask & (1 << d)) continue;
            newMask |= (1 << d);
        }
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}

#9 countWithAnyRepeatedDigits -> n -
    f(countDistinctDigitNumbers)
#10 countNumbersWithKDistinctDigits // f(0, 0, 1, 0)
int k, dp[11][1025][2][2];
int f(int i, int mask, int tight, int started) {
    if (i == n) return started &&
        (__builtin_popcount(mask) == k);
    auto& ret = dp[i][mask][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}

#11 count Numbers Divisible By k and Contains No Digit
    m // f(0, 0, 1, 0)
int dp[11][100][2][2];
int k, m;
int f(int i, int rem, int tight, int started) {
    if (i == n) return started && (rem == 0);
    auto& ret = dp[i][rem][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        if (d == m) continue;
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newRem = (rem * 10 + d) % k;
        ret += f(i + 1, newRem, newTight, newStarted);
    }
    return ret;
}

```

```

}
--> find sum of integers and count at same time
#12 sum and count of all numbers x that has at most k
    distinct digits // f(0, 0, 1, 0)
const int mod = 998244353;
int64_t n, k, Pow10[20];
array<int64_t, 2> dp[20][1025][2][2]; // dp[0] -> cnt,
    dp[1] -> sum;
string s;
array<int64_t, 2> f(int i, int mask, int tight, int
    started) {
    if (i == n) {
        return {started && (__builtin_popcount(mask) <=
            k), 0};
    }
    auto& ret = dp[i][mask][tight][started];
    if (~ret[0]) return ret;
    ret = {0, 0};
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        auto [currCnt, currSum] = f(i + 1, newMask,
            newTight, newStarted);
        auto& [cnt, sum] = ret;
        cnt = (cnt + currCnt) % mod;
        sum = (sum + (currCnt * d % mod) * Pow10[n - i -
            1] % mod) % mod;
        sum = (sum + currSum) % mod;
    }
    return ret;
}

int64_t Cnt(int64_t num) {
    if (num <= 0) return 0;
    memset(dp, -1, sizeof dp);
    s = to_string(num);
    n = s.size();
    Pow10[0] = 1;
    for (int i = 1; i < 20; i++) {
        Pow10[i] = (Pow10[i - 1] * 10) % mod;
    }
    return f(0, 0, 1, 0)[1];
}

--> find digit sum upto n, this is optimized version,
    use memset just once
string s;
int64_t dp[20][2][2];
int64_t cnt[20][2][2];
pair<int64_t, int64_t> f(int i, int tight, int
    started) {
    if (i < 0) return {0, started ? 1 : 0}; // {sum,
        count of valid numbers}
    if (~dp[i][tight][started] && !tight) return
        {dp[i][tight][started], cnt[i][tight][started]};
    int64_t totalSum = 0, totalCount = 0;
}

```



```

int limit = tight ? (s[i] - '0') : 9;
for (int d = 0; d <= limit; d++) {
    int newTight = tight && (d == limit);
    int newStarted = started || (d > 0);
    auto [nextSum, nextCount] = f(i - 1, newTight,
    ↪ newStarted);
    if (newStarted) {
        totalSum += d * nextCount + nextSum;
        totalCount += nextCount;
    } else {
        totalSum += nextSum;
        totalCount += nextCount;
    }
}
dp[i][tight][started] = totalSum;
cnt[i][tight][started] = totalCount;
return {totalSum, totalCount};
}
int64_t sumOfAllDigits(int64_t num) {
    if (num < 0) return 0;
    s = to_string(num);
    reverse(s.begin(), s.end());
    return f(s.size() - 1, 1, 0).first;
}
memset(dp, -1, sizeof dp);
memset(cnt, -1, sizeof cnt);

// Optimized versions -->
## with only 1 memset, reverse the number then
↪ calculate from (n - 1) ->
## so when some state is already calculated and tight
↪ == 0, then return 'ret', or else again calculate
↪ the state
#13 count of 3 = 6 = 9, and count of 3 > 0
const int mod = 1e9 + 7, N = 17;
string s;
int dp[51][N][N][N][2]; // f(s.size() - 1, 0, 0, 0, 1)
int f(int i, int three, int six, int nine, int tight)
↪ {
    if (three > 16 || six > 16 || nine > 16) return 0;
    if (i < 0) {
        return (three > 0) && (three == six) && (six ==
        ↪ nine);
    }
    auto& ret = dp[i][three][six][nine][tight];
    if (ret != -1 && !tight) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        ret = (ret + f(i - 1, three + (d == 3), six + (d
        ↪ == 6), nine + (d == 9), newTight)) % mod;
    }
    return ret;
}
// optimized, without tight state
// when the state is not tight then return 'ret' also
↪ memoize the dp;
int dp[51][N][N][N][N];

```

```

int f(int i, int three, int six, int nine, int tight)
↪ {
    if (three > 16 || six > 16 || nine > 16) return 0;
    if (i < 0) {
        return (three > 0) && (three == six) && (six ==
        ↪ nine);
    }
    auto ret = dp[i][three][six][nine];
    if (ret != -1 && !tight) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        ret = (ret + f(i - 1, three + (d == 3), six + (d
        ↪ == 6), nine + (d == 9), newTight)) % mod;
    }
    if (!tight) dp[i][three][six][nine] = ret;
    return ret;
}
int Cnt(string a) {
    reverse(a.begin(), a.end());
    s = a;
    return f(s.size() - 1, 0, 0, 0, 1);
}
int check(string& s) {
    // problem condition
}
void solve() {
    string a, b;
    cin >> a >> b;
    cout << Cnt(b) - Cnt(a) + check(a); // check if only
    ↪ string a can satisfy the condition
}

// calculate between l and r in one function
int dp[51][2][2][18][18][18];
string l, r;
int f(int i, int tightLower, int tightUpper, int c3,
↪ int c6, int c9) {
    if (c3 >= 17 || c6 >= 17 || c9 >= 17) return 0;
    if (i < 0) {
        return c3 && c3 == c6 && c6 == c9;
    }
    int& ret =
    ↪ dp[i][tightLower][tightUpper][c3][c6][c9];
    if (~ret && !tightLower && !tightUpper) return ret;
    int lo = tightLower ? l[i] - '0' : 0;
    int hi = tightUpper ? r[i] - '0' : 9;
    ret = 0;
    for (int d = lo; d <= hi; d++) {
        int newTightLower = tightLower && (d == lo);
        int newTightUpper = tightUpper && (d == hi);
        ret = (ret + f(i - 1, newTightLower,
        ↪ newTightUpper, c3 + (d == 3), c6 + (d == 6),
        ↪ c9 + (d == 9))) % mod;
    }
    return ret;
}

```

```

// optimized, without (tightLower, tightUpper) state
int f(int i, int tightLower, int tightUpper, int c3,
↪ int c6, int c9) {
    if (c3 >= 17 || c6 >= 17 || c9 >= 17) return 0;
    if (i < 0) {
        return c3 && c3 == c6 && c6 == c9;
    }
    int ret = dp[i][c3][c6][c9];
    if (~ret && !tightLower && !tightUpper) return ret;
    int lo = tightLower ? l[i] - '0' : 0;
    int hi = tightUpper ? r[i] - '0' : 9;
    ret = 0;
    for (int d = lo; d <= hi; d++) {
        int newTightLower = tightLower && (d == lo);
        int newTightUpper = tightUpper && (d == hi);
        ret = (ret + f(i - 1, newTightLower,
        ↪ newTightUpper, c3 + (d == 3), c6 + (d == 6),
        ↪ c9 + (d == 9))) % mod;
    }
    if (!tightLower && !tightUpper) dp[i][c3][c6][c9] =
    ↪ ret;
    return ret;
}
void solve() {
    cin >> l >> r;
    int n = r.size();
    while (l.size() < n) l = "0" + l;
    reverse(l.begin(), l.end());
    reverse(r.begin(), r.end());
    cout << f(n - 1, 1, 1, 0, 0, 0) << '\n';
}

```

15 Distinct Subsequence

```

const int mod = 1e9 + 7;
int distinctSubseq(string &a) {
    vector<int> last(26); // for array, use map
    int res = 1;
    for(auto& ai : a) {
        int curr = (2LL * res - last[ai - 'a']) % mod;
        if (curr < 0) curr += mod;
        last[ai - 'a'] = res;
        res = curr;
    }
    return (res - 1 + mod) % mod; // without empty set
}

```

16 DSU Kruskal's Algorithm MST

```

struct DSU {
    vector<int> parent, sz;
    DSU(int n) {
        parent.resize(n + 1), sz.resize(n + 1, 1);
        iota(parent.begin(), parent.end(), 0);
    }
    int Find(int u) {
        if (u == parent[u]) return u;
        return parent[u] = Find(parent[u]);
    }
}

```

```

bool Is_connected(int u, int v) {
    return Find(u) == Find(v);
}
void Merge(int u, int v) {
    u = Find(u), v = Find(v);
    if (u != v) {
        if (sz[u] < sz[v]) swap(u, v);
        parent[v] = u;
        sz[u] += sz[v];
    }
}
};

```

17 Exclusion DP

```

vector<int> f(n), g(n);
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) {
        f[i] += cnt[j];
    }
    f[i] = nC2(f[i]);
}
for (int i = N - 1; i > 0; i--) {
    g[i] = f[i];
    for (int j = i * 2; j < N; j += i) {
        g[i] -= g[j];
    }
}
// g[i] = how many pairs have gcd i

```

18 Fenwick Tree 2D

```

struct FenWick2D {
    int n, m;
    vector<vector<long long>> ft;
    FenWick2D() {}
    FenWick2D(int _n, int _m) {
        n = _n, m = _m;
        ft.assign(n + 1, vector<long long> (m + 1));
    }
    void Add(int x, int y, long long val) {
        for (int i = x; i <= n; i += i & -i) {
            for (int j = y; j <= m; j += j & -j) {
                ft[i][j] += val;
            }
        }
    }
    long long Csum(int x, int y) {
        long long res = 0;
        for (int i = x; i > 0; i -= i & -i) {
            for (int j = y; j > 0; j -= j & -j) {
                res += ft[i][j];
            }
        }
        return res;
    }
    long long Rsum(int x1, int y1, int x2, int y2) {
        return Csum(x2, y2) - Csum(x1 - 1, y2) - Csum(x2,
            ↪ y1 - 1) + Csum(x1 - 1, y1 - 1);
    }
}

```

```
};
```

19 Fenwick Tree BIT

```

struct FenWickTree {
    int n;
    vector<long long> ft;
    FenWickTree() {}
    FenWickTree(int n) { Initial(n); }
    FenWickTree(vector<int>& a) {
        Initial((int)a.size());
        Build(a);
    }
    void Initial(int _n) {
        n = _n;
        ft.assign(n + 1, 0);
    }
    void Build(vector<int>& a) {
        for (int i = 0; i < (int)a.size(); i++) {
            Add(i, i, a[i]); #change
        }
    }
    void Add(int idx, long long val) {
        for (int i = idx; i <= n; i += i & -i) {
            ft[i] += val;
        }
    }
    void Add(int l, int r, long long val) {
        Add(l, val);
        Add(r + 1, -val);
    }
    long long Csum(int idx) {
        long long res = 0;
        for (int i = idx; i > 0; i -= i & -i) {
            res += ft[i];
        }
        return res;
    }
    long long Rsum(int l, int r) {
        return Csum(r) - Csum(l - 1);
    }
};

```

20 FFT

```

struct cplx {
    long double a, b;
    cplx(long double a = 0, long double b = 0) : a(a),
        ↪ b(b) {}
    const cplx operator + (const cplx &c) const { return
        ↪ cplx(a + c.a, b + c.b); }
    const cplx operator - (const cplx &c) const { return
        ↪ cplx(a - c.a, b - c.b); }
    const cplx operator * (const cplx &c) const { return
        ↪ cplx(a * c.a - b * c.b, a * c.b + b * c.a); }
    const cplx operator / (const long double &d) const {
        ↪ return cplx(a / d, b / d); }
};
const long double PI = acos(-1);

```

```

vector<int> rev;
void Preprocess(int sz) {
    if ((int)rev.size() == sz) return;
    rev.resize(sz);
    rev[0] = 0;
    int lg_n = __builtin_ctz(sz);
    for (int i = 1; i < sz; ++i) {
        rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (lg_n -
            ↪ 1));
    }
}
void fft(vector<cplx> &a, bool inv = 0) {
    int n = a.size();
    for (int i = 1; i < n - 1; ++i) {
        if (i < rev[i]) swap(a[i], a[rev[i]]);
    }
    for (int len = 2; len <= n; len <= 1) {
        long double t = 2 * PI / len * (inv ? -1 : 1);
        cplx wlen = {cos(t), sin(t)};
        for (int st = 0; st < n; st += len) {
            cplx w(1);
            for (int i = 0; i < len / 2; ++i) {
                cplx ev = a[st + i], od = a[st + i + len / 2]
                    ↪ * w;
                a[st + i] = ev + od;
                a[st + i + len / 2] = ev - od;
                w = w * wlen;
            }
        }
    }
    if (inv) {
        for (cplx& z : a) z = z / n;
    }
}
vector<long long> multiply(vector<int> &a, vector<int>
    ↪ &b) {
    int n = a.size(), m = b.size(), sz = 1;
    while (sz < n + m - 1) sz <= 1;
    vector<cplx> x(sz), y(sz), z(sz);
    for (int i = 0; i < sz; i++) {
        x[i] = i < n ? cplx(a[i], 0) : cplx(0, 0);
        y[i] = i < m ? cplx(b[i], 0) : cplx(0, 0);
    }
    Preprocess(sz);
    fft(x), fft(y);
    for (int i = 0; i < sz; i++) z[i] = x[i] * y[i];
    fft(z, 1);
    vector<long long> c(n + m - 1);
    for (int i = 0; i < n + m - 1; i++) c[i] =
        ↪ round(z[i].a);
    return c;
}
auto c = multiply(a, b);

```

21 Floyd Warshall

```

void FloydWarshall(vector<vector<long long>>& adj) {
    int n = (int)adj.size();
}

```

```

for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            adj[i][j] = min(adj[i][j], adj[i][k] +
                ↪ adj[k][j]);
            adj[i][i] = 0;
        }
    }
}

```

22 Geometry

```

const double PI = acos((double)-1.0);
using ld = long double;
using ll = long long;
struct point { ld x, y; };
void manhattanToChebyshev(int& x, int& y) {
    int X = x + y, Y = x - y;
    x = X, y = Y;
}
void chebyshevToManhattan(int& x, int& y) {
    int X = (x + y) / 2, Y = (x - y) / 2;
    x = X, y = Y;
}
ll manhattanDistance(point& p1, point& p2) {
    return abs(p1.x - p2.x) + abs(p1.y - p2.y);
}
ll chebyshevDistance(point& p1, point& p2) {
    return max(abs(p1.x - p2.x), abs(p1.y - p2.y));
}
// determines the relative position (cross product) of
↪ a point (p3)
// with respect to the line passing through (p1) and
↪ (p2)
// if (d > 0): point (p3) is to the left of the line
// if (d < 0): point (p3) is to the right of the line
// if (d == 0): point (p3) lies exactly on the line.
ll determinant(point p1, point p2, point p3) {
    ll d = (p2.x - p1.x) * (p3.y - p1.y) - (p2.y - p1.y)
        ↪ * (p3.x - p1.x);
    return d;
}
bool arePointsOnSameSide(point p1, point p2, point p3,
    ↪ point p4) {
    ll d1 = determinant(p1, p2, p3);
    ll d2 = determinant(p1, p2, p4);
    return (d1 * d2) > 0;
}
bool doLinesIntersect(point p1, point p2, point p3,
    ↪ point p4) {
    ll d1 = determinant(p3, p4, p1);
    ll d2 = determinant(p3, p4, p2);
    ll d3 = determinant(p1, p2, p3);
    ll d4 = determinant(p1, p2, p4);
    return (d1 * d2 < 0) && (d3 * d4 < 0);
}
// distance of two points
ld distance(point& p1, point& p2) {

```

```

    return sqrt((p2.x - p1.x) * (p2.x - p1.x) + (p2.y -
        ↪ p1.y) * (p2.y - p1.y));
}
// a point inside cricle
// x1, y1 = point of circle, r = radius of circle
// x2, y2 = target point
bool isInside(int x1, int y1, int x2, int y2, int r) {
    return ((x2 - x1) * (x2 - x1)) + ((y2 - y1) * (y2 -
        ↪ y1)) <= r * r;
}
ld toDegrees(ld radians) {
    return radians * (180.0 / PI);
}
// circle with radius r
struct Circle {
    ld r;
    Circle(ld _r) { r = _r; }
    ld Diameter() { return 2 * r; }
    ld Circumference() { return 2 * PI * r; }
    ld Area() { return PI * r * r; }
    // if theta in radians, make it to degrees
    // all the calculations are in degree
    ld Sector_Area(ld theta) { return (theta / 360.0) *
        ↪ Area(); }
    ld Arc_Length(ld theta) { return (theta / 360.0) *
        ↪ Circumference(); }
    ld Chord_Length(ld theta) { return 2 * r *
        ↪ sin((theta * PI) / 360.0); }
    ld Segment_Area(ld theta) { return
        ↪ Sector_Area(theta) - (0.5 * r * r * sin((theta *
        ↪ PI) / 180.0)); }
    ld Circumscribed_Square_Area() { return 4 * r * r; }
    ld Inscribed_Square_Area() { return 2 * r * r; }
    ld Sphere_Surface_Area() { return 4 * PI * r * r; }
    ld Sphere_Volume() { return (4.0 / 3.0) * PI * r * r
        ↪ * r; }
    ld Cylinder_Surface_Area(ld h) { return 2 * PI * r *
        ↪ (r + h); }
    ld Cylinder_Volume(ld h) { return PI * r * r * h; }
    ld Cone_Surface_Area(ld l) { return PI * r * (r +
        ↪ l); }
    ld Cone_Volume(ld h) { return (1.0 / 3.0) * PI * r *
        ↪ r * h; }
    ld Annulus_Area(ld R) { return PI * (r * r - R * R);
        ↪ }
};
// triangle with three sides: a, b, c
struct Triangle {
    ld a, b, c, s;
    Triangle(point x, point y, point z) {
        a = distance(x, y);
        b = distance(y, z);
        c = distance(z, x);
        s = (a + b + c) / 2;
    }
    Triangle(ld _a, ld _b, ld _c) {
        a = _a, b = _b, c = _c;
        s = (a + b + c) / 2;
    }

```

```

}
ld Area() { return sqrt(s * (s - a) * (s - b) * (s -
    ↪ c)); }
ld Perimeter() { return a + b + c; }
ld Angle_A_Radians() { return acos((b * b + c * c -
    ↪ a * a) / (2 * b * c)); }
ld Angle_B_Radians() { return acos((a * a + c * c -
    ↪ b * b) / (2 * a * c)); }
ld Angle_C_Radians() { return acos((a * a + b * b -
    ↪ c * c) / (2 * a * b)); }
ld Angle_A_Degrees() { return
    ↪ toDegrees(Angle_A_Radians()); }
ld Angle_B_Degrees() { return
    ↪ toDegrees(Angle_B_Radians()); }
ld Angle_C_Degrees() { return
    ↪ toDegrees(Angle_C_Radians()); }
ld Inradius() { return sqrt((s - a) * (s - b) * (s -
    ↪ c) / s); }
ld Circumradius() { return (a * b * c) / (4 *
    ↪ Area()); }
ld Exradius_A() { return sqrt((s - a) * (s - b) * (s
    ↪ - c) / (s - a)); }
ld Exradius_B() { return sqrt((s - a) * (s - b) * (s
    ↪ - c) / (s - b)); }
ld Exradius_C() { return sqrt((s - a) * (s - b) * (s
    ↪ - c) / (s - c)); }
ld Altitude_A() { return 2 * Area() / a; }
ld Altitude_B() { return 2 * Area() / b; }
ld Altitude_C() { return 2 * Area() / c; }
ld Median_A() { return sqrt((2 * b * b + 2 * c * c -
    ↪ a * a) / 4); }
ld Median_B() { return sqrt((2 * a * a + 2 * c * c -
    ↪ b * b) / 4); }
ld Median_C() { return sqrt((2 * a * a + 2 * b * b -
    ↪ c * c) / 4); }
};
// n sided polygon (n-gon) with side length a
struct Polygon {
    int n;
    ld a;
    Polygon(int _n, ld _a) { n = _n, a = _a; }
    ld Perimeter() { return n * a; }
    ld Exterior_Angle_Degrees() { return 360.0 / n; }
    ld Exterior_Angle_Radians() { return (2 * PI) / n; }
    ld Interior_Angle_Degrees() { return (n - 2) * 180.0
        ↪ / n; }
    ld Interior_Angle_Radians() { return PI - (2 * PI /
        ↪ n); }
    ld Circumradius() { return a / (2 * sin(PI / n)); }
    ld Inradius() { return a / (2 * tan(PI / n)); }
    ld Area() { return (n * a * a) / (4 * tan(PI / n));
        ↪ }
    ld Central_Angle_Degrees() { return 360.0 / n; }
    ld Central_Angle_Radians() { return (2 * PI) / n; }
    ll Diagonals_count() { return n * (n - 3) / 2; }
    ld Diagonal_length() { return a / sin(PI / n); }
    ld Height() {

```



```

    if (n & 1) return 2 * Inradius();
    else return Inradius() + Circumradius();
}
ld Width() {
    if (n & 1) {
        return 2 * Circumradius() * sin((n - 1) * PI /
            ↪ (2 * n));
    } else {
        if ((n / 2) & 1) return 2 * Circumradius();
        else return 2 * Inradius();
    }
}
};

```

23 Hash Map

```

#include <ext/pb_ds/assoc_container.hpp>
struct splitmix64_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            ↪ std::chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
template <typename K, typename V, typename Hash =
    ↪ splitmix64_hash>
using hash_map = __gnu_pbds::gp_hash_table<K, V,
    ↪ Hash>;
template <typename K, typename Hash = splitmix64_hash>
using hash_set = hash_map<K, __gnu_pbds::null_type,
    ↪ Hash>;

```

24 Hashing with Update

```

const int MAX = int(1e6) + 9;
vector<long long> MOD = {1909999999, 1999990999};
vector<array<long long, 2>> pw(MAX), ipw(MAX);
array<long long, 2> bs = {137, 277};
int BinExp(long long a, long long b, int mod) {
    a %= mod;
    int res = 1;
    while (b) {
        if (b & 1) res = (res * a) % mod;
        a = (a * a) % mod;
        b >>= 1;
    }
    return res;
}
void Preprocess() {
    pw[0][0] = pw[0][1] = 1;
    for (int i = 1; i < MAX; i++) {
        pw[i][0] = (pw[i - 1][0] * bs[0]) % MOD[0];
        pw[i][1] = (pw[i - 1][1] * bs[1]) % MOD[1];
    }
}

```

```

ipw[0][0] = ipw[0][1] = 1;
long long ip1 = BinExp(bs[0], MOD[0] - 2, MOD[0]);
long long ip2 = BinExp(bs[1], MOD[1] - 2, MOD[1]);
for (int i = 1; i < MAX; i++) {
    ipw[i][0] = (ipw[i - 1][0] * ip1) % MOD[0];
    ipw[i][1] = (ipw[i - 1][1] * ip2) % MOD[1];
}
}
struct Hashing {
    int n;
    vector<array<long long, 2>> hs;
    Hashing(string& s) {
        if (pw[2][0] == 0) Preprocess();
        n = s.size();
        hs.resize(n + 1);
        for (int i = 0; i < n; i++) {
            hs[i + 1][0] = (hs[i][0] + (pw[i][0] * s[i]) %
                ↪ MOD[0]) % MOD[0];
            hs[i + 1][1] = (hs[i][1] + (pw[i][1] * s[i]) %
                ↪ MOD[1]) % MOD[1];
        }
    }
    array<long long, 2> get_hash(int l, int r) { // 0
        ↪ based query
        l++, r++; // 1 based hashing
        long long res1 = ((hs[r][0] - hs[l - 1][0]) +
            ↪ MOD[0]) % MOD[0];
        long long res2 = ((hs[r][1] - hs[l - 1][1]) +
            ↪ MOD[1]) % MOD[1];
        res1 = (res1 * ipw[l - 1][0]) % MOD[0];
        res2 = (res2 * ipw[l - 1][1]) % MOD[1];
        //return res1 << 31 | res2;
        return {res1, res2};
    }
};
auto Hash_Merge(array<long long, 2> left, array<long
    ↪ long, 2> right, int left_sz) {
    for (int i = 0; i < 2; i++) {
        (right[i] += pw[left_sz][i]) %= MOD[i];
        (left[i] += right[i]) %= MOD[i];
    }
    return left;
};
// # with update, find palindrome O(nlogn)
const int N = 1e6 + 9;
int power(long long n, long long k, const int mod) {
    int ans = 1 % mod;
    n %= mod;
    if (n < 0) n += mod;
    while (k) {
        if (k & 1) ans = (long long) ans * n % mod;
        n = (long long) n * n % mod;
        k >>= 1;
    }
    return ans;
}
using T = array<int, 2>;
const T MOD = {127657753, 987654319};
const T p = {137, 277};

```

```

T operator + (T a, int x) {return {(a[0] + x) %
    ↪ MOD[0], (a[1] + x) % MOD[1]};}
T operator - (T a, int x) {return {(a[0] - x + MOD[0])
    ↪ % MOD[0], (a[1] - x + MOD[1]) % MOD[1]};}
T operator * (T a, int x) {return {(int)((long long)
    ↪ a[0] * x % MOD[0]), (int)((long long) a[1] * x %
    ↪ MOD[1])};}
T operator + (T a, T x) {return {(a[0] + x[0]) %
    ↪ MOD[0], (a[1] + x[1]) % MOD[1]};}
T operator - (T a, T x) {return {(a[0] - x[0] +
    ↪ MOD[0]) % MOD[0], (a[1] - x[1] + MOD[1]) %
    ↪ MOD[1]};}
T operator * (T a, T x) {return {(int)((long long)
    ↪ a[0] * x[0] % MOD[0]), (int)((long long) a[1] *
    ↪ x[1] % MOD[1])};}
ostream& operator << (ostream& os, T hash) {return os
    ↪ << "(" << hash[0] << ", " << hash[1] << ")";}
T pw[N], ipw[N];
void prec() {
    pw[0] = {1, 1};
    for (int i = 1; i < N; i++) {
        pw[i] = pw[i - 1] * p;
    }
    ipw[0] = {1, 1};
    T ip = {power(p[0], MOD[0] - 2, MOD[0]), power(p[1],
        ↪ MOD[1] - 2, MOD[1])};
    for (int i = 1; i < N; i++) {
        ipw[i] = ipw[i - 1] * ip;
    }
}
struct Hashing {
    int n;
    string s; // 1 - indexed
    vector<array<T, 2>> t; // (normal, rev) hash
    array<T, 2> merge(array<T, 2> l, array<T, 2> r) {
        l[0] = l[0] + r[0];
        l[1] = l[1] + r[1];
        return l;
    }
    void build(int node, int b, int e) {
        if (b == e) {
            t[node][0] = pw[b] * s[b];
            t[node][1] = pw[n - b + 1] * s[b];
            return;
        }
        int mid = (b + e) >> 1, l = node << 1, r = l | 1;
        build(l, b, mid);
        build(r, mid + 1, e);
        t[node] = merge(t[l], t[r]);
    }
    void upd(int node, int b, int e, int i, char x) {
        if (b > i || e < i) return;
        if (b == e && b == i) {
            t[node][0] = pw[b] * x;
            t[node][1] = pw[n - b + 1] * x;
            return;
        }
        int mid = (b + e) >> 1, l = node << 1, r = l | 1;
    }
}

```

```

    upd(l, b, mid, i, x);
    upd(r, mid + 1, e, i, x);
    t[node] = merge(t[l], t[r]);
}
array<T, 2> query(int node, int b, int e, int i, int
    ↪ j) {
    if (b > j || e < i) return {T{0, 0}}, T{0, 0}};
    if (b >= i && e <= j) return t[node];
    int mid = (b + e) >> 1, l = node << 1, r = l | 1;
    return merge(query(l, b, mid, i, j), query(r, mid
    ↪ + 1, e, i, j));
}
Hashing() {}
Hashing(string _s) {
    n = _s.size();
    s = ". " + _s;
    t.resize(4 * n + 1);
    build(1, 1, n);
}
void upd(int i, char c) {
    upd(1, 1, n, i, c);
    s[i] = c;
}
T get_hash(int l, int r) { // 1 - indexed
    return query(1, 1, n, l, r)[0] * ipw[l - 1];
}
T rev_hash(int l, int r) { // 1 - indexed
    return query(1, 1, n, l, r)[1] * ipw[n - r];
}
T get_hash() return get_hash(1, n);
bool is_palindrome(int l, int r) return get_hash(l,
    ↪ r) == rev_hash(l, r);
};

```

25 HLD

```

struct HeavyLightDecomposition {
    int t = 0;
    vector<int> tin, depth, subtree_size, parent, heavy,
    ↪ head, euler;
    SegmentTreeIterative<int> sg;
    HeavyLightDecomposition(int root,
    ↪ vector<vector<int>>& adj, vector<int>& values) {
        int n = (int)adj.size() + 1;
        tin.resize(n), depth.resize(n),
        ↪ subtree_size.resize(n), parent.resize(n),
        ↪ heavy.assign(n, -1), head.resize(n),
        ↪ euler.resize(n);
        Dfs(root, root, adj);
        Decompose(root, root, adj, values);
        sg = SegmentTreeIterative<int> (euler);
    }
    void Dfs(int u, int p, vector<vector<int>>& adj) {
        subtree_size[u] = 1;
        parent[u] = p;
        for (auto& v : adj[u]) {
            if (v != p) {
                depth[v] = depth[u] + 1;
                Dfs(v, u, adj);
            }
        }
        subtree_size[u] += subtree_size[v];
        if (heavy[u] == -1 || subtree_size[heavy[u]] <
            ↪ subtree_size[v]) {
            heavy[u] = v;
        }
    }
}
void Decompose(int u, int h, vector<vector<int>>&
    ↪ adj, vector<int>& values) {
    tin[u] = ++t;
    euler[t] = values[u];
    head[u] = h;
    if (heavy[u] != -1) {
        Decompose(heavy[u], h, adj, values);
    }
    for (auto& v : adj[u]) {
        if (v != parent[u] && v != heavy[u]) {
            Decompose(v, v, adj, values);
        }
    }
}
void Update(int u, int val) {
    sg.Update(tin[u], val);
}
int neutral = 0; #change
int Merge(int a, int b) {
    return max(a, b); #change
}
int PathQuery(int a, int b) {
    int res = neutral;
    for (; head[a] != head[b]; b = parent[head[b]]) {
        if (depth[head[a]] > depth[head[b]]) {
            swap(a, b);
        }
        res = Merge(res, sg.Query(tin[head[b]],
            ↪ tin[b]));
    }
    if (depth[a] > depth[b]) {
        swap(a, b);
    }
    res = Merge(res, sg.Query(tin[a], tin[b]));
    return res;
}
};
HeavyLightDecomposition hld(1, adj, a);
// add segment tree

```

26 Hopcroft Karp

```

// O(√V * E)
// works for only directed graph, or on two graphs
// 1 to n is left graph, n + 1 to n + m is right graph
// make directed edges for two graph
// match pairs -> if (i < match[i]) (i <-> match[i])
const int N = 2e5 + 9, INF = 1.1e9;
vector<int> adj[N];
int n, m, match[N], dist[N];
bool bfs() {
    queue<int> q;

```

```

    for (int i = 1; i <= n; ++i) {
        if (!match[i]) dist[i] = 0, q.emplace(i);
        else dist[i] = INF;
    }
    dist[0] = INF;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        if (!u) continue;
        for (int v : adj[u]) {
            if (dist[match[v]] == INF) {
                dist[match[v]] = dist[u] + 1,
                q.emplace(match[v]);
            }
        }
        return dist[0] != INF;
    }
}
bool dfs(int u) {
    if (!u) return 1;
    for (int v : adj[u]) {
        if (dist[match[v]] == dist[u] + 1 and
            ↪ dfs(match[v])) {
            match[u] = v, match[v] = u;
            return 1;
        }
    }
    dist[u] = INF;
    return 0;
}
int max_matching() {
    int ret = 0;
    while (bfs()) {
        for (int i = 1; i <= n; ++i) {
            ret += !match[i] and dfs(i);
        }
    }
    return ret;
}

```

27 Hungarian Min Assignment

```

// returns the max sum and permutation
// for minimum, convert each value to negative.
template<typename T>
pair<T, vector<int>> hungarian(const vector<vector<T>
    ↪ > &a) {
    if (a.empty()) return {0, {}};
    int n = a.size() + 1, m = a[0].size() + 1;
    vector<int> p(m), ans(n - 1);
    vector<T> u(n), v(m);
    for (int i = 1; i < n; i++) {
        p[0] = i;
        int now = 0;
        vector<int> pre(m, -1), vis(m + 1);
        vector<T> dis(m, numeric_limits<T>::max());
        do {
            vis[now] = true;
            int t = p[now], nxt;

```

```

T d = numeric_limits<T>::max();
for (int j = 1; j < m; j++)
    if (!vis[j]) {
        T cur = -a[t - 1][j - 1] - u[t] - v[j];
        if (cur < dis[j]) dis[j] = cur, pre[j] =
            now;
        if (dis[j] < d) d = dis[j], nxt = j;
    }
for (int j = 0; j < m; j++) {
    if (vis[j]) u[p[j]] += d, v[j] -= d;
    else dis[j] -= d;
}
now = nxt;
} while (p[now]);
while (now) {
    int t = pre[now];
    p[now] = p[t], now = t;
}
}
for (int i = 1; i < m; i++)
    if (p[i]) ans[p[i] - 1] = i - 1;
return {v[0], ans};
}

```

28 KMP

```

// length of longest proper prefix of P[0...i] that is
// also a suffix of P[0...i]
// Pattern: a b a b a c a
// Index:   0 1 2 3 4 5 6
// LPS[]:   0 0 1 2 3 0 1
vector<int> get_pi(string& s) {
    int n = s.size();
    vector<int> pi(n);
    for (int i = 1, j = 0; i < n; i++) {
        if (s[i] == s[j]) pi[i] = ++j;
        else if (j == 0) pi[i] = 0;
        else j = pi[j - 1], i--;
    }
    return pi;
}
// count the number of p occurs in s
string s, p;
s = p + "#" + s;
vector<int> pi = get_pi(s);
int ans = 0;
for (auto& i : pi) ans += (i == p.size());
}

```

29 LIS With Vector Pair

```

vector<int> lis(vector<int> a) {
    int n = a.size();
    if (n == 0) return {};
    vector<pair<int, int>> sorted;
    vector<int> prev(n);
    for (int i = 0; i < n; ++i) {
        auto it = lower_bound(sorted.begin(),
            sorted.end(), make_pair(a[i], 0));
        if (it == sorted.end()) {
            sorted.emplace_back();

```

```

        it = sorted.end() - 1;
    }
    *it = {a[i], i};
    prev[i] = it == sorted.begin() ? 0 :
        (it - 1) -> second;
}
int l = sorted.size();
int cur = sorted.back().second;
vector<int> ret(l);
while (l--) {
    ret[l] = cur;
    cur = prev[cur];
}
return ret;
}

```

30 Longest Path in DAG

```

vector<int> adj[N];
int dp[N], vis[N], n;
int dfs (int u) {
    vis[u] = dp[u] = 1;
    for (int v : adj[u]) {
        if (!vis[v]) dfs(v);
        dp[u] = max(dp[u], dp[v] + 1);
    }
    return dp[u];
}
int longestpath() {
    int ans = 0;
    for (int i = 1; i <= n; i++)
        if (!vis[i]) ans = max(ans, dfs(i));
    return ans;
}

```

31 Manacher

```

struct Manacher { // 0 based
    int n;
    vector<int> p;
    Manacher(string& s) {
        n = s.size();
        p.resize(2 * n);
        build(s);
    }
    void build(string& s) {
        for (int i = 0, j = 0, k; i < n * 2; i += k, j =
            max(j - k, 0)) {
            while (i >= j && i + j + 1 < n * 2 && s[(i - j)
                / 2] == s[(i + j + 1) / 2]) ++j;
            p[i] = j;
            for (k = 1; i >= k && j >= k && p[i - k] != j -
                k; ++k) {
                p[i + k] = min(p[i - k], j - k);
            }
        }
    }
    bool is_palindrome(int l, int r) {
        int len = (r - l + 1), idx = -1;
        if ((len & 1) && idx = (1 + len / 2) * 2;

```

```

        else idx = (1 + len / 2 - 1) * 2 + 1;
        return p[idx] >= len;
    }
    int odd_length_of_center_i(int i) {return p[i * 2];
        }
    int even_length_of_center_i(int i) {return p[i * 2
        + 1];
    };
};

```

32 Merge Sort Tree

```

// add ordered multiset
struct MergeSortTree {
    int size = 1;
    vector<ordered_multiset<int>> st; #change
    MergeSortTree() {}
    MergeSortTree(int n) { Initial(n); }
    MergeSortTree(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(1, 1, size, a);
    }
    void Initial(int _n) {
        size = _n;
        int tree_size = 1;
        while (tree_size < _n) tree_size *= 2;
        st.resize(tree_size * 2);
    }
    void Build(int u, int s, int e, vector<int>& a) {
        if (s == e) { #change
            st[u].insert(a[s]);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        Build(v, s, m, a);
        Build(w, m + 1, e, a);
        for (int i = s; i <= e; i++) st[u].insert(a[i]);
    }
    void Update(int u, int s, int e, int k, int prev,
        int curr) {
        if (s == e) { #change
            st[u].erase(st[u].find_by_order(st[u].order_of_key(
                prev)));
            st[u].insert(curr);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        if (k <= m) Update(v, s, m, k, prev, curr);
        else Update(w, m + 1, e, k, prev, curr);
        #change
        st[u].erase(st[u].find_by_order(st[u].order_of_key(
            prev)));
        st[u].insert(curr);
    }
    void Update(int k, int prev, int curr) {
        Update(1, 1, size, k, prev, curr);
    }
    int Query(int u, int s, int e, int l, int r, int
        val) {

```

```

    if (e < l || r < s) { #change
        return 0;
    }
    if (l <= s && e <= r) { #change
        return st[u].order_of_key(val);
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    int lsum = Query(v, s, m, l, r, val);
    int rsum = Query(w, m + 1, e, l, r, val);
    return lsum + rsum; #change
}
int Query(int l, int r, int val) {
    return Query(1, 1, size, l, r, val);
}
};

```

33 MEX with TRIE

```

const int N = 2e5 * 22 + 9;
int nxt[N][2], cnt[N], intCnt[N], node = 2;
void insert(int x) {
    int u = 1;
    for(int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        if(!nxt[u][bit]) nxt[u][bit] = node++;
        u = nxt[u][bit];
        cnt[u]++;
    }
    intCnt[u]++;
}
int find(int x) {
    int u = 1;
    for(int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        if(!nxt[u][bit]) return 0;
        u = nxt[u][bit];
    }
    return intCnt[u];
}
void erase(int x) {
    if (find(x) == 0) return;
    int u = 1;
    for(int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        int v = nxt[u][bit];
        cnt[v]--;
        u = v;
    }
    intCnt[u]--;
}
int mex() {
    int u = 1, ret = 0;
    for(int i = 20; i >= 0; i--) {
        if(u == 0 || !nxt[u][0]) return ret;
        if(cnt[nxt[u][0]] >= (1 << i)) {
            u = nxt[u][1];
            ret |= (1 << i);
        } else {
            u = nxt[u][0];
        }
    }
}

```

```

    }
    return ret;
}

```

34 Minimum Expression

```

// lexicographically smallest rotation
int minimumExpression(string s) {
    s = s + s;
    int i = 0, j = 1, k = 0, len = s.size();
    while(i + k < len && j + k < len) {
        if(s[i + k] == s[j + k]) k++;
        else if(s[i + k] < s[j + k]) { j = max(j + k + 1,
            i + 1); k = 0; }
        else { i = max(i + k + 1, j + 1); k = 0; }
    } return min(i, j);
}

```

35 Number Theory

```

const int N = 1e6 + 9;
vector<int> lpf(N), gp(N);
vector<array<int, 2>> factors[N];
// sieve for finding lowest prime and highest prime
    upto N
for(int i = 2; i < N; i++) {
    if(lpf[i] == 0) {
        for(int j = i; j < N; j += i) {
            gp[j] = i;
            if(!lpf[j]) lpf[j] = i;
        }
    }
}
// find all factors upto N
for(int i = 2; i < N; i++) {
    int num = i;
    while(num > 1) {
        int p = lpf[num], cnt = 0;
        while(num > 1 && num % p == 0) {
            cnt++;
            num /= p;
        }
        factors[i].push_back({p, cnt});
    }
}
int num = 10;
int total_divisors = 1;
long long sum_of_divisors = 1;
for(auto& [p, c] : factors[num]) {
    total_divisors *= (c + 1);
    sum_of_divisors *= (pow(p, c + 1) - 1) / (p - 1);
}
// (a ^ b) % p (Binary Exponentiation)
int BinExp(long long a, long long b, int mod) {
    a %= mod;
    int res = 1;
    while(b) {
        if(b & 1) res = (res * a) % mod;
        a = (a * a) % mod;
        b >>= 1;
    }
}

```

```

    }
    return res;
}
// (a * b) % p (Binary Multiplication)
int BinMul(long long a, long long b, int mod) {
    a %= mod;
    int res = 0;
    while(b) {
        if(b & 1) res = (res + a) % mod;
        a = (a + a) % mod;
        b >>= 1;
    }
    return res;
}
// (a ^ -1) % mod (inverse of a number)
BinExp(a, mod - 2);
// (a / b) % mod
BinMul(a, BinExp(b, mod - 2, mod), mod);
// (a ^ (b ^ c)) % mod
BinExp(a, BinExp(b, c, mod - 1), mod);

// Permutations and Combinations
struct Combinatorics {
    vector<long long> fact, inv, ifact;
    Combinatorics(int n) {
        fact.assign(n + 1, 1), inv.assign(n + 1, 1),
        ifact.assign(n + 1, 1);
        inv[0] = 0;
        for(int i = 2; i <= n; i++) fact[i] = (fact[i - 1] * i) % mod;
        for(int i = 2; i <= n; i++) inv[i] = mod - (mod / i) * inv[mod % i] % mod;
        for(int i = 2; i <= n; i++) ifact[i] = (ifact[i - 1] * inv[i]) % mod;
    }
    int nPr(int n, int r) { // Permutations
        if(n < r) return 0;
        return (fact[n] * ifact[n - r]) % mod;
    }
    int nCr(int n, int r) { // Combinations
        return (nPr(n, r) * ifact[r]) % mod;
    }
    int nCRR(int n, int r) { // Combinations with repetition
        return (nPr(n + r - 1, r) * ifact[r]) % mod;
    }
} comb(N);

// phi of single integer
int n = 10;
long long num = n;
long long phi_of_n = n;
for(long long i = 2; i * i <= num; i++) {
    if(num % i == 0) {
        while(num % i == 0) num /= i;
        phi_of_n -= phi_of_n / i;
    }
}
}

```

```

if (num > 1) phi_of_n -= phi_of_n / num;

// phi upto N
vector<int> phi(N);
// initial 0 to N
iota(phi.begin(), phi.end(), 0);
for (int i = 2; i < N; i++) {
    if (phi[i] == i) {
        for (int j = i; j < N; j += i) {
            phi[j] -= phi[j] / i;
        }
    }
}

// gcd sum ->  $\sum \text{gcd}(i, n)$  for  $1 \leq i \leq n$ ; ( $n \leq 1e9$ )
//  $\text{gcd}(1, n) + \text{gcd}(2, n) + \dots + \text{gcd}(n, n)$ 
long long sum = 0;
for (int i = 1; 1LL * i * i <= n; i++) {
    if (n % i == 0) {
        sum += i * phi(n / i);
        if (n / i != i) sum += (n / i) * phi(n / (n / i));
    }
}

// all pair gcd sum from 1 to N ( $N \leq 4e6$ )
//  $\sum_{i=1}^n \sum_{j=1}^{n-i} [\text{gcd}(i, j)]$ 
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) sum[j] += i * phi[j / i];
}

for (int i = 1; i < N; i++) sum[i] += sum[i - 1] - i;

// lcm sum ->  $\sum \text{lcm}(i, n)$  for  $1 \leq i \leq n$ ; ( $n \leq 1e6$ )
//  $\text{lcm}(1, n) + \text{lcm}(2, n) + \dots + \text{lcm}(n, n)$ 
phi[1] = 2; // phi[1] should be 2 for this algorithm
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) lcm_sum[j] += 1LL * j
        * phi[i] * i / 2;
}

// all pair lcm sum from 1 to N ( $N \leq 1e6$ )
//  $\sum_{i=1}^n \sum_{j=1}^{n-i} [\text{lcm}(i, j)]$ 
phi[1] = 2; // phi[1] should be 2 for this algorithm
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) lcm_sum[j] += (long
        * long) j * (1LL * i * phi[i] / 2);
}

for (int i = 1; i < N; i++) lcm_sum[i] += lcm_sum[i - 1] - i;

```

36 Ordered Set

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <class T> using ordered_set = tree<T,
    null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T> using ordered_multiset = tree<T,
    null_type, less_equal<T>, rb_tree_tag,
    tree_order_statistics_node_update>;

```

```

template <class T, class R> using ordered_map =
    tree<T, R, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
// Sorting Descending (or Equal)
template <class T> using ordered_set = tree<T,
    null_type, greater<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T> using ordered_multiset = tree<T,
    null_type, greater_equal<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T, class R> using ordered_map =
    tree<T, R, greater<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
// Functions
st.order_of_key(k); // count of elements smaller than
    k. -  $O(\log n)$ 
st.find_by_order(k); // Returns the iterator for the
    kth element (0 based index). -  $O(\log n)$ 
st.size() - st.order_of_key(k + 1); // count of
    elements greater than k. -  $O(\log n)$ 
st.order_of_key(r + 1) - st.order_of_key(l); // count
    of elements between l to r
st.erase(st.find_by_order(st.order_of_key(k))); //
    erase in multiset

```

37 SCC

```

// clear everything first, 1 based
// reverse scc for topological order
const int N = 5e5 + 10;
vector<int> adj[N], trans[N], scc[N];
int col[N], vis[N], idx = 0, n, m;
stack<int> st;
void dfs(int u) {
    vis[u] = 1;
    for (int v : adj[u]) if (!vis[v]) dfs(v);
    st.push(u);
}
void dfs2(int u) {
    col[u] = idx;
    scc[idx].push_back(u);
    for (int v : trans[u]) if (!col[v]) dfs2(v);
}
void findSCC() {
    for (int i = 1; i <= n; i++)
        if (!vis[i]) dfs(i);
    for (int u = 1; u <= n; u++)
        for (int v : adj[u])
            trans[v].push_back(u);
    while (!st.empty()) {
        int u = st.top(); st.pop();
        if (col[u]) continue;
        idx++; dfs2(u);
    }
}
// take input and call findSCC();

```

38 Segment Tree Iterative Point Update Range Query

```

template <class T> struct SegmentTreeIterative {
    int n = 1;
    vector<T> st;
    SegmentTreeIterative() {}
    SegmentTreeIterative(int n) { Initial(n); }
    SegmentTreeIterative(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(a);
    }
    void Initial(int _n) {
        n = _n;
        int tree_size = 1;
        while (tree_size <= n) tree_size *= 2;
        st.resize(tree_size * 2);
    }
    T neutral = INT_MAX; #change
    T Merge(T& a, T& b) { #change
        return min(a, b);
    }
    void Build(vector<int>& a) {
        for (int i = 1; i <= n; ++i) {
            st[n + i] = a[i];
        }
        for (int u = n - 1; u > 0; --u) {
            st[u] = Merge(st[u << 1], st[u << 1 | 1]);
        }
    }
    void Update(int idx, T val) {
        st[idx + n] = val;
        for (idx /= 2; idx; idx /= 2) {
            st[idx] = Merge(st[idx << 1], st[idx << 1 | 1]);
        }
    }
    T Query(int l, int r) {
        T res = neutral;
        for (l += n, r += n + 1; l < r; l >>= 1, r >>= 1)
            {
                if (l & 1) res = Merge(res, st[l++]);
                if (r & 1) res = Merge(res, st[--r]);
            }
        return res;
    }
};

```

39 Segment Tree Lazy

```

const long long INF = 1.1e17;
struct node { #change
    long long sum, lazy_add;
    node() {
        sum = 0;
        lazy_add = INF;
    }
};
struct SegmentTreeLazy {
    int size = 1;
    vector<node> st;
};

```



```

SegmentTreeLazy() {}
SegmentTreeLazy(int n) { Initial(n); }
SegmentTreeLazy(vector<int>& a) {
    Initial((int)a.size() - 1);
    Build(1, 0, size, a);
}
void Initial(int _n) {
    size = _n;
    int tree_size = 1;
    while (tree_size <= size) tree_size *= 2;
    st.resize(tree_size * 2);
}
node Make_node(long long val) { #change
    node res;
    res.sum = val;
    res.lazy_add = INF;
    return res;
}
node Merge(node& l, node& r) { #change
    node res;
    res.sum = l.sum + r.sum;
    return res;
}
void Push(int u, int l, int r) { #change
    if (st[u].lazy_add == INF) return;
    if (l != r) {
        int v = 2 * u, w = 2 * u + 1;
        if (st[v].lazy_add != INF) st[v].lazy_add +=
            ↪ st[u].lazy_add;
        else st[v].lazy_add = st[u].lazy_add;
        if (st[w].lazy_add != INF) st[w].lazy_add +=
            ↪ st[u].lazy_add;
        else st[w].lazy_add = st[u].lazy_add;
    }
    st[u].sum += (r - l + 1) * st[u].lazy_add;
    st[u].lazy_add = INF;
}
void Build(int u, int s, int e, vector<int>& a) {
    if (s == e) {
        st[u] = Make_node(a[s]);
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    Build(v, s, m, a);
    Build(w, m + 1, e, a);
    st[u] = Merge(st[v], st[w]);
}
void Update(int u, int s, int e, int l, int r, long
    ↪ long val) {
    Push(u, s, e);
    if (e < l || r < s) return;
    if (l <= s && e <= r) { #change
        if (st[u].lazy_add != INF) st[u].lazy_add +=
            ↪ val;
        else st[u].lazy_add = val;
        Push(u, s, e);
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    Update(v, s, m, l, r, val);

```

```

    Update(w, m + 1, e, l, r, val);
    st[u] = Merge(st[v], st[w]);
}
void Update(int l, int r, long long val) {
    Update(1, 0, size, l, r, val);
}
node Query(int u, int s, int e, int l, int r) {
    Push(u, s, e);
    if (e < l || r < s) { #change
        return node();
    }
    if (l <= s && e <= r) return st[u];
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    node lsum = Query(v, s, m, l, r);
    node rsum = Query(w, m + 1, e, l, r);
    return Merge(lsum, rsum);
}
node Query(int l, int r) {
    return Query(1, 0, size, l, r);
}
int Idx_query(int u, int s, int e, int l, int r) {
    Push(u, s, e);
    if (e < l || r < s) return -1;
    if (s == e) return st[u].mn == 0 ? s : -1;
    int v = u << 1, w = v | 1, m = (s + e) >> 1;
    int lq = Idx_query(v, s, m, l, r);
    if (lq == -1) {
        return Idx_query(w, m + 1, e, l, r);
    }
    return lq;
}
int Idx_query(int l, int r) {
    return Idx_query(1, 0, size, l, r);
}
};

```

40 Segment Tree

```

struct node { #change
    long long sum, pref, suff, ans;
    node() {
        sum = pref = suff = ans = 0;
    }
};
struct SegmentTree {
    int size = 1;
    vector<node> st;
    SegmentTree() {}
    SegmentTree(int n) { Initial(n); }
    SegmentTree(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(1, 0, size, a);
    }
    void Initial(int _n) {
        size = _n;
        int tree_size = 1;
        while (tree_size <= size) tree_size *= 2;
        st.resize(tree_size * 2);
    }
    node Make_node(int val) { #change

```

```

        node res;
        res.sum = val;
        res.pref = res.suff = res.ans = max(0, val);
        return res;
    }
    node Merge(node& l, node& r) { #change
        node res;
        res.sum = l.sum + r.sum;
        res.pref = max(l.pref, l.sum + r.pref);
        res.suff = max(r.suff, r.sum + l.suff);
        res.ans = max(max(l.ans, r.ans), l.suff + r.pref);
        return res;
    }
    void Build(int u, int s, int e, vector<int>& a) {
        if (s == e) {
            st[u] = Make_node(a[s]);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        Build(v, s, m, a);
        Build(w, m + 1, e, a);
        st[u] = Merge(st[v], st[w]);
    }
    void Update(int u, int s, int e, int k, long long
        ↪ val) {
        if (s == e) { #change
            st[u] = Make_node(val);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        if (k <= m) Update(v, s, m, k, val);
        else Update(w, m + 1, e, k, val);
        st[u] = Merge(st[v], st[w]);
    }
    void Update(int k, long long val) {
        Update(1, 0, size, k, val);
    }
    node Query(int u, int s, int e, int l, int r) {
        if (e < l || r < s) { #change
            return node();
        }
        if (l <= s && e <= r) return st[u];
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        node lsum = Query(v, s, m, l, r);
        node rsum = Query(w, m + 1, e, l, r);
        return Merge(lsum, rsum);
    }
    node Query(int l, int r) {
        return Query(1, 0, size, l, r);
    }
};

```

41 SOS DP

```

const int mod = 1e9 + 7;
const int B = 20, N = (1 << B) + 9;
int f[N], g[N], pairF[N], pairG[N], subseqF[N],
    ↪ subseqG[N], Pow2[N];

```

```

void sub(int& a, int& b) { // a = a - b
    a -= b;
    if (a < 0) a += mod;
}
int nC2(int n) {
    return (n * 1LL * (n - 1) / 2) % mod;
}
void forward1() { // sum over subset
    for (int bit = 0; bit < B; bit++) {
        for (int i = 0; i < N; i++) {
            if (i & (1 << bit)) {
                f[i] += f[i ^ (1 << bit)];
            }
        }
    }
}
void backward1() { // exclude subset sum
    for (int bit = 0; bit < B; bit++) {
        for (int i = N - 1; i >= 0; i--) {
            if (i & (1 << bit)) {
                // f[i] -= f[i ^ (1 << bit)];
                sub(pairF[i], pairF[i ^ (1 << bit)]);
                sub(subseqF[i], subseqF[i ^ (1 << bit)]);
            }
        }
    }
}
void forward2() { // sum over superset
    for (int bit = 0; bit < B; bit++) {
        for (int i = N - 1; i >= 0; i--) {
            if (i & (1 << bit)) {
                g[i ^ (1 << bit)] += g[i];
            }
        }
    }
}
void backward2() { // exclude superset sum
    for (int bit = 0; bit < B; bit++) {
        for (int i = 0; i < N; i++) {
            if (i & (1 << bit)) {
                // g[i ^ (1 << bit)] -= g[i];
                sub(pairG[i ^ (1 << bit)], pairG[i]);
                sub(subseqG[i ^ (1 << bit)], subseqG[i]);
            }
        }
    }
}
void sosDP(vector<int>& a) {
    Pow2[0] = 1;
    for (int i = 1; i < N; i++) {
        Pow2[i] = (Pow2[i - 1] * 2) % mod;
    }
    for (auto& ai : a) {
        f[ai]++;
        g[ai]++;
    }
    forward1();
    forward2();
    for (int i = 0; i < N; i++) {
        // all pair (i < j)
    }
}

```

```

pairF[i] = nC2(f[i]);
pairG[i] = nC2(g[i]);
// subsequence
subseqF[i] = Pow2[f[i]] - 1;
subseqG[i] = Pow2[g[i]] - 1;
}
backward1();
backward2();
}
int subMaskOf(int x) { // x | y = x
    return f[x];
}
int superMaskOf(int x) { // x & y = x
    return g[x];
}
int countPairsWithAnd(int x) { // y & z = x (i < j)
    return pairG[x];
}
int countPairsWithOr(int x) { // y | z = x (i < j)
    return pairF[x];
}
int countSubseqWithAnd(int x) {
    return subseqG[x];
}
int countSubseqWithOr(int x) {
    return subseqF[x];
}
}
sosDP(a); // clear everything

```

42 Sparse Table RMQ

```

const int N = (int)2e5 + 9;
int lg[N];
void Preprocess() {
    for (int i = 2; i < N; ++i) {
        lg[i] = lg[i / 2] + 1;
    }
}
template <class T> struct RMQ {
    int n = 1, LOG = 1;
    vector<vector<T>> st;
    vector<vector<T>> st;
    T Merge(T& a, T& b) {
        return min(a, b); #change
    }
    RMQ() {}
    RMQ(vector<T>& a) {
        if (lg[2] == 0) Preprocess();
        n = (int)a.size(), LOG = __lg(n) + 1;
        st.assign(n, vector<T>(LOG));
        for (int j = 0; j < LOG; j++) {
            for (int i = 0; i + (1 << j) - 1 < n; i++) {
                if (j == 0) st[i][j] = a[i];
                else st[i][j] = Merge(st[i][j - 1], st[i + (1 << (j - 1))][j - 1]);
            }
        }
    }
    T Query(int l, int r) {
        // if (l > r) return 0;
        int k = lg[r - l + 1];
    }
}

```

```

        return Merge(st[l][k], st[r - (1 << k) + 1][k]);
    }
};

```

43 Stress Testing

```

// rename file -> testing.sh
set -e
g++ -std=c++17 gen.cpp -o gen
g++ -std=c++17 main.cpp -o main
g++ -std=c++17 brute.cpp -o brute
for((i = 1; ; ++i)); do
    echo $i
    ./gen $i > in
    ./main < in > out
    ./brute < in > out2
    diff -w out out2 || break
done

```

44 String Stream

```

string s;
getline(cin, s);
stringstream custom_in(s);
string word;
int count_word = 0;
while (custom_in >> word) {
    count_word++;
}

```

45 Sublime Build

```

// check the gcc version and replace
// name the file -> cp.sublime-build
// ubuntu
{
    "cmd" : ["g++ -std=c++14 $file_name -o
    ↪ $file_base_name && timeout 4s
    ↪ ./ $file_base_name<input.txt>output.txt"],
    "selector" : "source.c",
    "shell" : true,
    "working_dir" : "$file_path"
}
// windows
{
    "cmd": ["g++.exe", "-std=c++14", "${file}", "-o",
    ↪ "${file_base_name}.exe", "&&" ,
    ↪ "${file_base_name}.exe<input.txt>output.txt"],
    "selector": "source.cpp",
    "shell": true,
    "working_dir": "$file_path"
}
// mac
{
    "cmd" : ["g++-14 $file_name -o $file_base_name &&
    ↪ gtimeout 4s
    ↪ ./ $file_base_name<input.txt>output.txt"],
    "selector" : "source.c",
}

```

```

    "shell": true,
    "working_dir" : "$file_path"
}

```

46 Suffix Array

```

/*
for integer, just change string to vector<int> and
↳ minimum value of vector must be >= 1
for integer, lim will be the maximum value of the
↳ array
LCP of suffix (sa[i], sa[i + 1]) = lcp[i + 1]
O(nlogn)
*/
array<vector<int>, 2> get_sa(string& s, int lim = 128)
↳ {
    int n = s.size() + 1, k = 0, a, b;
    vector<int> x(begin(s), end(s) + 1), y(n), sa(n),
    ↳ lcp(n), ws(max(n, lim)), rank(n);
    x.back() = 0;
    iota(begin(sa), end(sa), 0);
    for (int j = 0, p = 0; p < n; j = max(1, j * 2), lim
    ↳ = p) {
        p = j, iota(begin(y), end(y), n - j);
        for (int i = 0; i < n; ++i) if (sa[i] >= j) y[p++]
        ↳ = sa[i] - j;
        fill(begin(ws), end(ws), 0);
        for (int i = 0; i < n; ++i) ws[x[i]]++;
        for (int i = 1; i < lim; ++i) ws[i] += ws[i - 1];
        for (int i = n; i--;) sa[--ws[x[y[i]]]] = y[i];
        swap(x, y), p = 1, x[sa[0]] = 0;
        for (int i = 1; i < n; ++i) a = sa[i - 1], b =
        ↳ sa[i],
        x[b] = (y[a] == y[b] && y[a + j] == y[b + j]) ?
        ↳ p - 1 : p++;
    }
    for (int i = 1; i < n; ++i) rank[sa[i]] = i;
    for (int i = 0, j; i < n - 1; lcp[rank[i++]] = k)
        for (k && k--, j = sa[rank[i] - 1]; s[i + k] ==
        ↳ s[j + k]; k++);
    sa.erase(sa.begin()), lcp.erase(lcp.begin());
    return {sa, lcp};
}

/*
O(|S| + |alphabet|) Suffix Array
LIM := max{s[i]} + 2
LCP of suffix (sa[i], sa[i + 1]) = lcp[i]
*/
void inducedSort(const vector<int>& vec, int
↳ val_range, vector<int>& SA, const vector<int>& sl,
↳ const vector<int>& lms_idx) {
    vector<int> l(val_range, 0), r(val_range, 0);
    for (int c : vec) {
        ++r[c]; if (c + 1 < val_range) ++l[c + 1];
    }
    partial_sum(l.begin(), l.end(), l.begin());
    partial_sum(r.begin(), r.end(), r.begin());
    fill(SA.begin(), SA.end(), -1);

```

```

    for (int i = lms_idx.size() - 1; i >= 0; --i)
        ↳ SA[--r[vec[lms_idx[i]]]] = lms_idx[i];
    for (int i : SA) if (i > 0 and sl[i - 1]) SA[l[vec[i]
    ↳ - 1]++] = i - 1;
    fill(r.begin(), r.end(), 0);
    for (int c : vec) ++r[c];
    partial_sum(r.begin(), r.end(), r.begin());
    for (int k = SA.size() - 1, i = SA[k]; k; --k, i =
    ↳ SA[k]) {
        if (i and !sl[i - 1]) SA[--r[vec[i - 1]]] = i - 1;
    }
}
vector<int> suffixArray(const vector<int>& vec, int
↳ val_range) {
    const int n = vec.size();
    vector<int> sl(n), SA(n), lms_idx;
    for (int i = n - 2; i >= 0; --i) {
        sl[i] = vec[i] > vec[i + 1] or (vec[i] == vec[i +
        ↳ 1] and sl[i + 1]);
        if (sl[i] and !sl[i + 1]) lms_idx.emplace_back(i +
        ↳ 1);
    }
    reverse(lms_idx.begin(), lms_idx.end());
    inducedSort(vec, val_range, SA, sl, lms_idx);
    vector<int> new_lms_idx(lms_idx.size(),
    ↳ lms_vec(lms_idx.size()));
    for (int i = 0, k = 0; i < n; ++i) {
        if (SA[i] > 0 and !sl[SA[i]] and sl[SA[i] - 1])
        ↳ new_lms_idx[k++] = SA[i];
    }
    int cur = 0; SA[n - 1] = 0;
    for (int k = 1; k < new_lms_idx.size(); ++k) {
        int i = new_lms_idx[k - 1], j = new_lms_idx[k];
        if (vec[i] ^ vec[j]) {
            SA[j] = ++cur; continue;
        }
        bool flag = 0;
        for (int a = i + 1, b = j + 1; ; ++a, ++b) {
            if (vec[a] ^ vec[b]) {
                flag = 1; break;
            }
            if ((!sl[a] and sl[a - 1]) or (!sl[b] and sl[b -
            ↳ 1])) {
                flag = 1; break;
            }
            if ((!sl[a] and sl[a - 1] and !sl[b] and
            ↳ sl[b - 1])) break;
        }
        SA[j] = flag ? ++cur : cur;
    }
    for (int i = 0; i < lms_idx.size(); ++i) lms_vec[i]
    ↳ = SA[lms_idx[i]];
    if (cur + 1 < lms_idx.size()) {
        auto lms_SA = suffixArray(lms_vec, cur + 1);
        for (int i = 0; i < lms_idx.size(); ++i)
            ↳ new_lms_idx[i] = lms_idx[lms_SA[i]];
    }
    inducedSort(vec, val_range, SA, sl, new_lms_idx);
    ↳ return SA;

```

```

}
vector<int> getSuffixArray(const string& s, const int
↳ LIM = 128) { // change limit for integer array,
↳ (integer > 0)
    vector<int> vec(s.size() + 1);
    copy(begin(s), end(s), begin(vec)); vec.back() =
    ↳ '!';
    auto ret = suffixArray(vec, LIM);
    ret.erase(ret.begin()); return ret;
}
// build RMQ on it to get LCP of any two suffix
vector<int> getLCParray(const string& s, const
↳ vector<int>& SA) {
    int n = s.size(), k = 0;
    vector<int> lcp(n), rank(n);
    for (int i = 0; i < n; ++i) rank[SA[i]] = i;
    for (int i = 0; i < n; ++i, k ? --k : 0) {
        if (rank[i] == n - 1) {
            k = 0; continue;
        }
        int j = SA[rank[i] + 1];
        while (i + k < n and j + k < n and s[i + k] == s[j
        ↳ + k]) ++k;
        lcp[rank[i]] = k;
    }
    lcp[n - 1] = 0; return lcp;
}
int lower_bound(string& s, string& t, vector<int>& sa)
↳ {
    int n = s.size(), m = t.size(), lo = 0, hi = n - 1;
    while (lo <= hi) {
        int mid = (lo + hi) / 2;
        if (s.substr(sa[mid], m) < t) lo = mid + 1;
        else hi = mid - 1;
    }
    return lo;
}
int upper_bound(string& s, string& t, vector<int>& sa)
↳ {
    int n = s.size(), m = t.size(), lo = 0, hi = n - 1;
    while (lo <= hi) {
        int mid = (lo + hi) / 2;
        if (s.substr(sa[mid], m) <= t) lo = mid + 1;
        else hi = mid - 1;
    }
    return lo;
}
int find_occurrence(string& s, string& t, vector<int>& sa)
↳ {
    return upper_bound(s, t, sa) - lower_bound(s, t,
    ↳ sa);
}
const int N = 1e6 + 9;
int64_t distPref[N];
void kthSubstringDistinctPreprocess(vector<int>& sa,
↳ vector<int>& lcp) {
    int last = 0, n = sa.size();
    for (int i = 0; i < n; ++i) {

```

```

    distPref[i] = n - sa[i] - last;
    if (i) distPref[i] += distPref[i - 1];
    last = lcp[i];
}
array<int, 2> kthSubstringDistinctPos(string& s,
    ↪ int64_t k, vector<int>& sa, vector<int>& lcp) {
    int n = s.size(); k--;
    int i = upper_bound(distPref, distPref + n, k) -
    ↪ distPref;
    int len = k - (i == 0 ? 0 : distPref[i - 1]) + (i ==
    ↪ 0 ? 0 : lcp[i - 1]) + 1;
    return {i, len};
}
string kthSubstringDistinct(string& s, int64_t k,
    ↪ vector<int>& sa, vector<int>& lcp) {
    auto [i, len] = kthSubstringDistinctPos(s, k, sa,
    ↪ lcp);
    return s.substr(sa[i], len);
}
int64_t pref[N];
void kthSubstringPreprocess(vector<int>& sa) {
    int n = sa.size();
    for (int i = 0; i < n; i++) {
        pref[i] = n - sa[i];
        if (i) pref[i] += pref[i - 1];
    }
}
string kthSubstring(string& s, int64_t k, vector<int>&
    ↪ sa, vector<int>& lcp) {
    int n = s.size();
    int64_t lo = 1, hi = distPref[n - 1];
    while (lo <= hi) {
        int64_t mid = (lo + hi) >> 1;
        auto [i, len] = kthSubstringDistinctPos(s, mid,
        ↪ sa, lcp);
        int64_t totCnt = (i == 0 ? 0 : pref[i - 1]) + len;
        int mn = len;
        for (int j = i; j < n; j++) {
            mn = min(mn, lcp[j]);
            if (mn == 0) break;
            totCnt += mn;
        }
        if (totCnt < k) lo = mid + 1;
        else hi = mid - 1;
    }
    return kthSubstringDistinct(s, lo, sa, lcp);
}
int main() {
    string s;
    auto sa = getSuffixArray(s);
    auto lcp = getLCParrray(s, sa);
    kthSubstringDistinctPreprocess(sa, lcp);
    kthSubstringPreprocess(sa);
}

```

47 Topological Sort

```
bool topological_sort(vector<vector<int>>& adj) {
```

```

    int n = adj.size();
    vector<int> in_degree(n + 1);
    for (int u = 1; u <= n; u++) {
        for (auto& v : adj[u]) in_degree[v]++;
    }
    // without sorting the order
    queue<int> q;
    // sort with lexicographically
    // priority_queue<int, vector<int>, greater<int>> q;
    for (int u = 1; u <= n; u++) {
        if (in_degree[u] == 0) {
            q.push(u);
        }
    }
    if (q.empty()) return 0;
    vector<int> order;
    while (!q.empty()) {
        # change the queue operation
        int u = q.front();
        q.pop();
        for (auto& v : adj[u]) {
            in_degree[v]--;
            if (in_degree[v] == 0) {
                q.push(v);
            }
        }
        order.push_back(u);
    }
    return (int)order.size() == n;
}

```

48 Trie

```

// iterative
const int N = 1e6 + 9, A = 26;
int nxt[N][A], pref_cnt[N], word_cnt[N], node = 2;
void insert(string& s) {
    int u = 1;
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) nxt[u][idx] = node++;
        u = nxt[u][idx];
        pref_cnt[u]++;
    }
    word_cnt[u]++;
}
int countPref(string& s) {
    int u = 1;
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) return 0;
        u = nxt[u][idx];
    }
    return pref_cnt[u];
}
int find(string& s) {
    int u = 1;
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) return 0;

```

```

        u = nxt[u][idx];
    }
    return word_cnt[u];
}
void erase(string& s) {
    if (find(s) == 0) return;
    int u = 1;
    for (auto& c : s) {
        int idx = c - 'a';
        int v = nxt[u][idx];
        pref_cnt[v][idx]--;
        u = v;
    }
    word_cnt[u]--;
}
// trie integer iterative (max xor, min xor)
const int N = 2e5 * 31 + 9, A = 2;
int nxt[N][A], pref_cnt[N], int_cnt[N], node = 2;
void insert(int num) {
    int u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (!nxt[u][idx]) nxt[u][idx] = node++;
        u = nxt[u][idx];
        pref_cnt[u]++;
    }
    int_cnt[u]++;
}
int find(int num) {
    int u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (!nxt[u][idx]) return 0;
        u = nxt[u][idx];
    }
    return int_cnt[u];
}
void erase(int num) {
    if (find(num) == 0) return;
    int u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        int v = nxt[u][idx];
        pref_cnt[v]--;
        u = v;
    }
    int_cnt[u]--;
}
int maxXor(int num) {
    int res = 0, u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        int flip = idx ^ 1;
        if (nxt[u][flip] && pref_cnt[nxt[u][flip]]) {
            res += (1 << bit);
            u = nxt[u][flip];
        } else {
            u = nxt[u][idx];

```

```

    }
}
return res;
}
int minXor(int num) {
    int res = 0, u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (nxt[u][idx] && pref_cnt[nxt[u][idx]]) {
            u = nxt[u][idx];
        } else {
            res += (1 << bit);
            u = nxt[u][idx ^ 1];
        }
    }
    return res;
}
}

```

49 XOR Basis

```

using ll = long long;
const int D = 60;
struct XorBasis {
    // number of subsequences of xor-sum X, for ith
    ↪ prefix -> 2 ^ (i - sz);
    ll basis[D] = {};
    int sz = 0, n = 0;
    void insert(ll x) {
        for (int i = D - 1; i >= 0; i--) {
            if (!(x >> i) & 1) continue;
            if (!basis[i]) {
                basis[i] = x;
                sz++;
                break;
            }
            x ^= basis[i];
        } n++;
    }
    bool canRepresent(ll x) {
        for (int i = D - 1; i >= 0; i--) {
            if ((x >> i) & 1) x ^= basis[i];
        }
        return x == 0;
    }
    ll maxXor(ll x = 0) {
        for (int i = D - 1; i >= 0; i--) {
            if ((x ^ basis[i]) > x) x ^= basis[i];
        }
        return x;
    }
    ll minXor() { // except xor 0
        for (int i = 0; i < D; i++) {
            if (basis[i]) return basis[i];
        }
        return 0;
    }
    ll maxXorWith(ll x) {
        return maxXor(x);
    }
    ll minXorWith(ll x) {

```

```

        for (int i = D - 1; i >= 0; i--) {
            if ((x ^ basis[i]) < x) x ^= basis[i];
        }
        return x;
    }
    ll countDistinctXors() {
        return 1LL << sz;
    }
    ll kthXor(ll k) { // returns k + 1 th xor, 1st xor
    ↪ is 0
        ll res = 0;
        ll tot = countDistinctXors();
        if (tot < k) return -1;
        for (int i = D - 1; i >= 0; i--) {
            if (basis[i]) {
                ll low = tot / 2;
                if ((low < k && (res & 1 << i) == 0) ||
                    (low >= k && (res & 1 << i) > 0)) res ^=
                    ↪ basis[i];
                if (low < k) k -= low;
                tot /= 2;
            }
        }
        return res;
    }
    ll kthLargestXor(ll k) {
        return kthXor(countDistinctXors() - 1 - k);
    }
    ll kthXorAllCombinations(ll k) {
        if (n - sz > 60) return kthXor(1);
        ll totComb = 1LL << n;
        ll disComb = countDistinctXors();
        ll dupPerDis = totComb / disComb;
        ll disIdx = (k - 1) / dupPerDis + 1;
        return kthXor(disIdx);
    }
    ll kthLargestXorAllCombinations(ll k) {
        if (n - sz > 60) return
            ↪ kthXor(countDistinctXors());
        ll totComb = 1LL << n;
        ll disComb = countDistinctXors();
        ll dupPerDis = totComb / disComb;
        ll disIdx = (k - 1) / dupPerDis + 1;
        ll desIdx = disComb - disIdx + 1;
        return kthXor(desIdx);
    }
    ll countSubsetsLessThan(ll x) {
        ll lo = 0, hi = countDistinctXors();
        while (lo <= hi) {
            ll mid = (lo + hi) / 2;
            if (kthXor(mid) < x) lo = mid + 1;
            else hi = mid - 1;
        }
        return hi;
    }
    ll countSubsetsWithXor(ll x) {
        if (!canRepresent(x)) return 0;
        return 1LL << (n - sz); // if n > 60 use mod
    }
};

```

50 Z Function

```

// 0 based, longest substring lenght starting at
↪ position i that is also a prefix
// String: a b c a b c b b
// Index:  0 1 2 3 4 5 6 7
// Z[]:    - 0 0 3 0 0 0 0
vector<int> get_z(string& s) {
    int n = s.size(), l = 0, r = 0;
    vector<int> z(n);
    z[0] = n;
    for (int i = 1; i < n; i++) {
        if (i < r) z[i] = min(r - i, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            ↪ z[i]++;
        if (i + z[i] > r) l = i, r = i + z[i];
    }
    return z;
}

```

51 Mathematical Formulas & Notes

1. PI up to 31: 3.1415926535897932384626433832795
2. PI value in CPP: $2 * \text{acos}(0), 2 * \text{asin}(1), M_PI$
3. Formula for angle C using the Law of Cosines

$$C = \cos^{-1} \left(\frac{a^2 + b^2 - c^2}{2ab} \right)$$
4. Sum remainder: $n \bmod 1 + n \bmod 2 + n \bmod 3 + \dots + n \bmod m : n * m$ -sum of divisors from 1 to n
5. A number is divisible by 60 if and only if it is divisible by 3 and 20
6. All numbers greater than 1099 can be written as a sum of 11 and 111
7. Legendre's formula: $\nu_p(n!) = \sum_{i=1}^L \left\lfloor \frac{n}{p^i} \right\rfloor$, where $L = \lfloor \log_p n \rfloor$
8. ${}^nC_r = \binom{n}{r} = \frac{n!}{r!(n-r)!}$, ${}^nP_r = \frac{n!}{(n-r)!}$
9. $(a - b) \% M = (a \% M - b \% M + M) \% M$
10. $(a/b) \% M = (a \% M * b^{-1} \% M) \% M$
11. $(a^b) \% M = ((a \% M)^b) \% M$

12. **Euler's Totient Function (ETF):** Count of numbers less than n that are co-prime to n is,
 $\phi(n) = n * \prod_{p|n} (1 - \frac{1}{p})$
 Here, p = distinct prime factors of n
13. **Congruence:** $a \equiv b \pmod{M}$
 if $a \% M = b \% M$ and $M \mid (a - b)$
14. **Euler's Theorem:** $a^{\phi(M)} \equiv 1 \pmod{M}$,
 where a and M are co-prime
15. **Fermat's Little Theorem:** $a^{M-1} \equiv 1 \pmod{M}$,
 where M is prime
16. $a^b \equiv a^{b \bmod \phi(M)} \pmod{M}$ or it can be written that,
 $a^b \bmod M = a^{b \bmod \phi(M)} \bmod M$ or,
 $a^b \bmod M = a^{b \bmod M-1} \bmod M$
17. **x steps forward or backward in a circular number range:**
 $newPos = l + ((pos - l + x) \% N) + N) \% N$
 Where $N = l - r + 1$ (total numbers in range)
18. **Stars & Bars:** $x_1 + x_2 + \dots + x_k = n$ with $x_i \geq 0$ has $\binom{n+k-1}{n}$ solutions and with $x_i > 0$ has $\binom{n-1}{k-1}$ solutions.
19. Number of subsequences of length k from an array of size n such that x appears at least once in the subsequence, where that x appears c times in the array:
 $nC_k - n^{k-1}C_k$
20. **Hockey-stick Identity:** $n > r, \sum_{i=r}^n \binom{i}{r} = \binom{n+1}{r+1}$
21. $a^k - b^k = (a - b) \cdot (a^{k-1}b^0 + a^{k-2}b^1 + \dots + a^0b^{k-1})$
22. $ab \bmod ac = a(b \bmod c)$
23. $|a - b| + |b - c| + |c - a| = 2(\max(a, b, c) - \min(a, b, c))$
24. if $a \cdot b \leq c$ then $a \leq \left\lfloor \frac{c}{b} \right\rfloor$ Same for $<, \leq, >, \geq$
25. For positive integer n & arbitrary real numbers m, x ,
 $\left\lfloor \frac{\lfloor x/m \rfloor}{n} \right\rfloor = \left\lfloor \frac{x}{mn} \right\rfloor$ and $\left\lceil \frac{\lceil x/m \rceil}{n} \right\rceil = \left\lceil \frac{x}{mn} \right\rceil$

Simple Formulas

1. $(a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3$
2. $a^3 \pm b^3 = (a + b)(a^2 \mp ab + b^2)$
3. $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
4. $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
5. $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
6. $\sin A \pm \sin B = 2 \sin\left(\frac{A \pm B}{2}\right) \cos\left(\frac{A \mp B}{2}\right)$
7. $\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
8. $\cos A - \cos B = 2 \sin\left(\frac{A+B}{2}\right) \sin\left(\frac{B-A}{2}\right)$
9. $\sin A \sin B = -\frac{1}{2}[\cos(A+B) - \cos(A-B)]$
10. $\cos A \cos B = \frac{1}{2}[\cos(A+B) + \cos(A-B)]$
11. $\sin A \cos B = \frac{1}{2}[\sin(A+B) + \sin(A-B)]$
12. $\sin 2\theta = 2 \sin \theta \cos \theta = \frac{2 \tan \theta}{1 + \tan^2 \theta}$
13. $\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1$
 $= 1 - 2 \sin^2 \theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$
14. $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$
15. $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$
16. $\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$
17. $\tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$
18. $1 + \cos 2\theta = 2 \cos^2 \theta$
19. $1 - \cos 2\theta = 2 \sin^2 \theta$
20. $1 \pm \sin 2\theta = (\cos \theta \pm \sin \theta)^2$
21. $\sin^{-1} x = \cos^{-1} \sqrt{1 - x^2}$
22. $2 \sin^{-1} x = \sin^{-1}(2x\sqrt{1 - x^2})$
23. $2 \cos^{-1} x = \cos^{-1}(2x^2 - 1)$
24. $2 \tan^{-1} x = \tan^{-1}\left(\frac{2x}{1 - x^2}\right)$
25. $2 \tan^{-1} x = \sin^{-1}\left(\frac{2x}{1 + x^2}\right)$
26. $2 \tan^{-1} x = \cos^{-1}\left(\frac{1 - x^2}{1 + x^2}\right)$
27. $3 \sin^{-1} x = \sin^{-1}(3x - 4x^3)$
28. $3 \cos^{-1} x = \cos^{-1}(4x^3 - 3x)$
29. $3 \tan^{-1} x = \tan^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right)$
30. $\sin^{-1} x \pm \sin^{-1} y = \sin^{-1} \left[x\sqrt{1 - y^2} \pm y\sqrt{1 - x^2} \right]$
31. $\cos^{-1} x \pm \cos^{-1} y = \cos^{-1} \left[xy \mp \sqrt{1 - x^2} \sqrt{1 - y^2} \right]$
32. $\tan^{-1} x \pm \tan^{-1} y = \tan^{-1} \left(\frac{x \pm y}{1 \mp xy} \right)$
33. $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \tan^{-1} \left(\frac{x + y + z - xyz}{1 - xy - yz - zx} \right)$

Short Formulas

1. $\sin(-\theta) = -\sin \theta$
2. $\cos(-\theta) = \cos \theta$
3. $\tan(-\theta) = -\tan \theta$
4. $\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$
5. $\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$
6. $\tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta$
7. $\cot\left(\frac{\pi}{2} - \theta\right) = \tan \theta$
8. $\csc\left(\frac{\pi}{2} - \theta\right) = \sec \theta$
9. $\sec\left(\frac{\pi}{2} - \theta\right) = \csc \theta$
10. $\sin\left(\frac{\pi}{2} + \theta\right) = \cos \theta$
11. $\cos\left(\frac{\pi}{2} + \theta\right) = -\sin \theta$
12. $\tan\left(\frac{\pi}{4} + \theta\right) = \frac{1 + \tan \theta}{1 - \tan \theta}$
13. $\tan\left(\frac{\pi}{4} - \theta\right) = \frac{1 - \tan \theta}{1 + \tan \theta}$
14. $\sin(\pi + \theta) = -\sin \theta$
15. $\cos(\pi + \theta) = -\cos \theta$
16. $\sin(\pi - \theta) = \sin \theta$
17. $\cos(\pi - \theta) = -\cos \theta$
18. $\log_a a = 1$
19. $a^{\log_a b} = b$
20. $\log_b a = \frac{\log a}{\log b}$
21. $\log a^m = m \log a$