

CP Template

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1 Custom Codes

```

freopen("input.in", "r", stdin);
freopen("output.out", "w", stdout);
ios_base::sync_with_stdio(0), cin.tie(0);
// pragma
#pragma GCC optimize("O3,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")// use
→ avx for older judges
#pragma GCC optimize("Ofast")
#pragma GCC optimize ("ffloat-store")
#pragma GCC target
→ ("sse,sse2,sse3,ssse3,sse4,abm,mmx")
// random number generator
mt19937_64 rng(std::chrono::steady_clock::now().time_since_
→ _epoch().count());
int num = rng() % limit;
int64_t rnd(int64_t l, int64_t r) { // can handle
→ negative range also
    if (l > r) swap(l, r);
    return l + (rng() % (r - l + 1));
}
// ignore white space
cin.ignore(); or cin >> ws;
// STL merge function: merge two vectors or sets
vector<int> a = {1, 2, 7}, b = {4, 2, 3};
sort(a.begin(), a.end());
sort(b.begin(), b.end());
vector<int> c(a.size() + b.size());
merge(a.begin(), a.end(), b.begin(), b.end(),
→ c.begin());

set<int> a = {3, 2, 1}, b = {4, 5, 1};
set<int> c;
merge(a.begin(), a.end(), b.begin(), b.end(),
→ inserter(c, c.begin()));
// tuple
tuple<int, int, int> tup = {1, 2, 3};
int first = get<0>(tup);
// custom compare function
struct item {
    int a, b;
};
bool cmp(item& a, item& b) {
    if(a.a != b.a) return a.a < b.a;
    return a.b > b.b;
}
bool custom(pair<int, int>& a, pair<int, int>& b) {
    if(a.first != b.first) return a.first > b.first;
    return a.second < b.second;
}
// custom compare in set
struct cmp{
    bool operator() (const pair<int, int>& a, const
→ pair<int, int>& b) const {
        if (a.first != b.first) return a.first > b.first;
        return a.second < b.second;
    }
};

```

```

set<pair<int, int>, cmp> a;
// greater functions
priority_queue<int, vector<int>, greater<int>>
set<int, greater<int>>
map<int, int, greater<int>>
// fill with elements
fill(v.begin(), v.end(), -1);
// fill for array
fill(&dp[0][0][0], &dp[0][0][0] + N * M * N, INF);
// string to number
stoi(num);
// number to string
to_string(num);
// Binary to decimal
int n = stoi(binary, 0, 2);
// decimal to binary
string binary = bitset<64>(n).to_string();
binary.erase(0, binary.find_first_not_of('0'));
// count digit
int d = log10(num) + 1;
// set ith bit
n |= (1 << i)
// unset ith bit
n & ~(1 << i)
// toggle or inverse ith bit
n ^= (1 << i)
__builtin_popcountll(x)
__builtin_clzll(x)
__builtin_ctzll(x)

```

2 Articulation Bridge

```

int t = 0;
vector<int> tin(N, -1), low(N);
vector<array<int, 2>> ab;
void dfs (int u, int p) {
    tin[u] = low[u] = t++;
    for (int v: adj[u]) {
        if (v != p) {
            if (tin[v] != -1) {
                low[u] = min(low[u], tin[v]);
            } else {
                dfs(v, u);
                if (tin[u] < low[v])
                    ab.push_back({u, v});
                low[u] = min(low[u], low[v]);
            }
        }
    }
}

```

3 Articulation Point

```

int t = 0;
vector<int> tin(N, -1), low(N), ap;
void dfs (int u, int p) {
    tin[u] = low[u] = t++;
    int is_ap = 0, child = 0;
    for (int v: adj[u]) {
        if (v != p) {

```

```

            if (tin[v] != -1) {
                low[u] = min(low[u], tin[v]);
            } else {
                child++;
                dfs(v, u);
                if (tin[u] <= low[v]) is_ap = 1;
                low[u] = min(low[u], low[v]);
            }
        }
    }
    if ((u != p or child > 1) and is_ap)
        ap.push_back(u);
}

```

4 Base Conversion

```

// 2 <= b <= 62
const string D = "0123456789ABCDEFHGIJKLMNOPQRSTUVWXYZ"
→ Zabcdefghijklmnopqrstuvwxyz";
string decimalToBase(ll n, int b) {
    if (n == 0) return "0";
    string result;
    bool neg = n < 0;
    if (neg) n = -n;
    while (n > 0) {
        result.push_back(D[n % b]);
        n /= b;
    }
    if (neg) result.push_back('-');
    reverse(result.begin(), result.end());
    return result;
}
ll baseToDecimal(const string &s, int b) {
    ll result = 0, start = 0, neg = 0;
    if (s[0] == '-') neg = start = 1;
    for (int i = start; i < (int)s.size(); i++) {
        char c = s[i];
        int val;
        if ('0' <= c && c <= '9') val = c - '0';
        else if ('A' <= c && c <= 'Z') val = c - 'A' + 10;
        else if ('a' <= c && c <= 'z') val = c - 'a' + 36;
        result = result * b + val;
    }
    return neg ? -result : result;
}

```

5 Bellman Ford

```

struct st {
    int a, b, cost;
} e[N];
const int INF = 2e9;
int32_t main() {
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < m; i++) cin >> e[i].a >> e[i].b
→ >> e[i].cost;
    int s;
    cin >> s; //is there any negative cycle which is
→ reachable from s?
}

```

```

vector<int> d (n, INF); //for finding any cycle(not
→ necessarily from s) set d[i] = 0 for all i
d[s] = 0;
vector<int> p (n, -1);
int x;
for (int i=0; i<n; ++i) {
    x = -1;
    for (int j=0; j<m; ++j) {
        if (d[e[j].a] < INF) {
            if (d[e[j].b] > d[e[j].a] + e[j].cost) {
                d[e[j].b] = max (-INF, d[e[j].a] +
→ e[j].cost); //for overflow
                p[e[j].b] = e[j].a;
                x = e[j].b;
            }
        }
    }
    if (x == -1) cout << "No negative cycle from " << s;
    else {
        int y = x; //x can be on any cycle or reachable
→ from some cycle
        for (int i=0; i<n; ++i) y = p[y];
        vector<int> path;
        for (int cur=y; ; cur=p[cur]) {
            path.push_back (cur);
            if (cur == y && path.size() > 1) break;
        }
        reverse (path.begin(), path.end());
        cout << "Negative cycle: ";
        for (int i=0; i<path.size(); ++i) cout << path[i]
→ << ' ';
    }
    return 0;
}

// ## Bellman-ford (V * E)
vector<int> bellman_ford(int s){
    vector<int> dis(n, I);
    dis[s]=0;
    while(1){
        int any=0;
        for (auto& e: ed){
            if(dis[e.u]<I){
                if(dis[e.u]+e.cost < dis[e.v]){
                    dis[e.v] = dis[e.u]+e.cost;
                    any=1;
                }
            }
        }
        if(!any) break;
    }
    return dis;
}

```

6 Binary And Ternary Search

```

//Binary Search (integer)
int lo = 0, hi = n - 1;
while (lo <= hi) {
    int mid = (lo + hi) / 2;
    if (f(mid)) hi = mid - 1;
    else lo = mid + 1;
}

```

```

}
// -> another version
while (lo < hi) {
    int mid = (lo + hi) / 2;
    if (f(mid)) hi = mid;
    else lo = mid + 1;
}
//Binary Search (double)
double lo = 0, hi = inf;
int itr = 50;
while (itr--) {
    double mid = (lo + hi) / 2;
    if (f(mid)) hi = mid;
    else lo = mid;
}
//Ternary Search (integer, max)
int lo = 0, hi = n - 1;
while (lo < hi) {
    // int mid1 = lo + (hi - lo) / 3;
    // int mid2 = hi - (hi - lo) / 3;
    int mid = (lo + hi) / 2;
    if (f(mid) < f(mid + 1)) lo = mid + 1;
    else hi = mid;
}
//Ternary Search (double, max)
double lo = 0, hi = inf;
int itr = 50;
while (itr--) {
    double mid1 = lo + (hi - lo) / 3;
    double mid2 = hi - (hi - lo) / 3;
    if (f(mid1) < f(mid2)) lo = mid1;
    else hi = mid2;
}

```

7 Bit 2d Range Update Range Query

```

const int N = 1009;
struct BIT2D {
    ll M[N][N][2], A[N][N][2];
    BIT2D() {
        memset(M, 0, sizeof M);
        memset(A, 0, sizeof A);
    }
    void upd2(ll t[N][N][2], int x, int y, ll mul, ll
→ add) {
        for(int i = x; i < N; i += i & -i) {
            for(int j = y; j < N; j += j & -j)
                t[i][j][0] += mul, t[i][j][1] += add;
        }
    }
    void upd1(int x, int y1, int y2, ll mul, ll add) {
        upd2(M, x, y1, mul, -mul * (y1 - 1));
        upd2(M, x, y2, -mul, mul * y2);
        upd2(A, x, y1, add, -add * (y1 - 1));
        upd2(A, x, y2, -add, add * y2);
    }
    void upd(int x1, int y1, int x2, int y2, ll val) {
        upd1(x1, y1, y2, val, -val * (x1 - 1));
        upd1(x2, y1, y2, -val, val * x2);
    }
}

```

```

ll query2(ll t[N][N][2], int x, int y) {
    ll mul = 0, add = 0;
    for(int i = y; i > 0; i -= i & -i)
        mul += t[x][i][0], add += t[x][i][1];
    return mul * y + add;
}
ll query1(int x, int y) {
    ll mul = 0, add = 0;
    for(int i = x; i > 0; i -= i & -i)
        mul += query2(M, i, y), add += query2(A, i, y);
    return mul * x + add;
}
ll query(int x1, int y1, int x2, int y2) {
    return query1(x2, y2) - query1(x1 - 1, y2) -
→ query1(x2, y1 - 1) + query1(x1 - 1, y1 - 1);
}
};


```

8 Centroid Decomposition

```

struct CentroidDecomposition {
    using T = vector<vector<int>>;
    int n;
    vector<int> sz, is_cen, cpar, cdep;
    CentroidDecomposition(T& adj, int root = 1) {
        n = (int)adj.size() + 1;
        sz.resize(n), is_cen.resize(n), cpar.resize(n),
→ cdep.resize(n);
        Decompose(root, -1, 0, adj);
    }
    void Cal_sz(int u, int p, T& adj) {
        sz[u] = 1;
        for (auto& v : adj[u]) {
            if (v != p && !is_cen[v]) {
                Cal_sz(v, u, adj);
                sz[u] += sz[v];
            }
        }
    }
    int Get_cen(int u, int p, int csz, T& adj) {
        for (auto& v : adj[u])
            if (v != p && !is_cen[v] && (2 * sz[v] > csz))
                return Get_cen(v, u, csz, adj);
        return u;
    }
    void Decompose(int u, int p, int d, T& adj) {
        Cal_sz(u, p, adj);
        int c = Get_cen(u, p, sz[u], adj);
        is_cen[c] = 1, cpar[c] = p, cdep[c] = d;
        for (auto& v : adj[c])
            if (!is_cen[v])
                Decompose(v, c, d + 1, adj);
    }
};

```

9 Chessboard And Queens

```
string board[8];
```

```

bool col[8], diag1[15], diag2[15];
ll ans = 0;
void dfs(int r) {
    if (r == 8) { ans++; return; }
    for (int c = 0; c < 8; c++) {
        if (board[r][c] == '*') continue;
        if (col[c] || diag1[r + c] || diag2[r - c + 7])
            continue;
        col[c] = diag1[r + c] = diag2[r - c + 7] = true;
        dfs(r + 1);
        col[c] = diag1[r + c] = diag2[r - c + 7] = false;
    }
}
int main() {
    for (int i = 0; i < 8; i++) cin >> board[i];
    dfs(0);
    cout << ans << '\n';
}

```

10 Closest Min Max

```

// closest left, right index where current element is
// max or min
// closest max or min element from the current element
array<vector<int>, 2> closest_min_element(vector<int>
    &a) {
    int n = a.size();
    vector<int> l(n), r(n);
    stack<int> st; st.push(-1);
    for (int i = 0; i < n; i++) {
        while (st.top() != -1 && a[st.top()] > a[i])
            st.pop();
        l[i] = st.top() + 1; // closest index where
        // current element is min
        // l[i] = st.top(); // closest min element index
        st.push(i);
    } while (!st.empty()) st.pop();
    st.push(n);
    for (int i = n - 1; i >= 0; i--) {
        while (st.top() != n && a[st.top()] >= a[i])
            st.pop();
        r[i] = st.top() - 1; // closest index where
        // current element is min
        // r[i] = st.top(); // closest min element index
        st.push(i);
    } return {l, r};
}

array<vector<int>, 2> closest_max_element(vector<int>
    &a) {
    int n = a.size();
    vector<int> l(n), r(n);
    stack<int> st; st.push(-1);
    for (int i = 0; i < n; i++) {
        while (st.top() != -1 && a[st.top()] < a[i])
            st.pop();
        l[i] = st.top() + 1;
        // l[i] = st.top(); // closest max element index
        st.push(i);
    } while (!st.empty()) st.pop();
}

```

```

st.push(n);
for (int i = n - 1; i >= 0; i--) {
    while (st.top() != n && a[st.top()] <= a[i])
        st.pop();
    r[i] = st.top() - 1;
    // r[i] = st.top(); // closest max element index
    st.push(i);
} return {l, r};
}

```

11 Combinatorics

```

// (a ^ b) % p (Binary Exponentiation)
int BinExp(ll a, ll b, int mod) {
    a %= mod; int res = 1;
    while (b) {
        if (b & 1) res = (res * a) % mod;
        a = (a * a) % mod;
        b >>= 1;
    } return res;
}
// (a * b) % p (Binary Multiplication)
int BinMul(ll a, ll b, int mod) {
    a %= mod; int res = 0;
    while (b) {
        if (b & 1) res = (res + a) % mod;
        a = (a + a) % mod;
        b >>= 1;
    } return res;
}
// (a ^ -1) % mod (inverse of a number)
int modInv(ll a) {
    return BinExp(a, mod - 2);
}
// (a / b) % mod
BinMul(a, modInv(b), mod);
// (a ^ (b ^ c)) % mod
BinExp(a, BinExp(b, c, mod - 1), mod);
// a^(b^(c^d)) % mod
ll e1 = BinExp(c, d, mod - 1);
ll e2 = BinExp(b, e1, mod - 1);
ll ans = BinExp(a, e2, mod);

// Permutations and Combinations
vector<ll> fact, inv, ifact;
void CombinatoricsPrecalculate() {
    fact.assign(N + 1, 1), inv.assign(N + 1, 1),
    ifact.assign(N + 1, 1);
    inv[0] = 0;
    for (int i = 2; i < N; i++) fact[i] = (fact[i - 1]
        * i) % mod;
    for (int i = 2; i < N; i++) inv[i] = mod - (mod /
        i) * inv[mod % i] % mod;
    for (int i = 2; i < N; i++) ifact[i] = (ifact[i - 1]
        * inv[i]) % mod;
}
// Permutations: Arrangements of r elements from n
// distinct elements
int nPr(int n, int r) {

```

```

if (n < r) return 0;
return (fact[n] * ifact[n - r]) % mod;
}
// Combinations: Selections of r elements from n
// distinct elements
int nCr(int n, int r) {
    if (n < r) return 0;
    return (nPr(n, r) * ifact[r]) % mod;
}
// Combinations with Repetition: Choosing r items from
// n types (multisets)
int nCr_rep(int n, int r) {
    return nCr(n + r - 1, r);
}
// Number of ways to distribute n identical items into
// k bins (bins can be empty)
ll stars_and_bars(int n, int k) {
    return nCr(n + k - 1, k - 1);
}
// Number of ways to distribute n identical items into
// k bins (each bin >= 1)
ll stars_and_bars_positive(int n, int k) {
    if (n < k) return 0;
    return nCr(n - 1, k - 1);
}
/*
- Balanced parentheses: number of valid expressions
with n pairs, e.g., n=3 → 5 ways
- Binary trees: number of distinct binary trees with n
nodes
- Dyck paths: paths from (0,0) to (n,n) never crossing
above diagonal
- Polygon triangulations: number of ways to split a
convex polygon with n+2 sides into triangles
- Stack-sorting / pattern avoiding permutations:
number of permutations avoiding certain patterns
*/
int catalan(int n) {
    if (n < 0) return 0;
    return nCr(2 * n, n) * inv[n + 1] % mod;
}
ll perm_with_restrictions(int n, int r, int fixed) {
    // Example: nPr with some positions fixed
    if (r < fixed) return 0;
    return nPr(n - fixed, r - fixed);
}
// multinomial(v) = number of ways to arrange sum(v)
// items into groups of sizes v[0], v[1], ..., v[k-1]
ll multinomial(const vector<int>& v) {
    int sum = 0;
    for (int x : v) sum += x;
    ll res = fact[sum];
    for (int x : v) res = res * ifact[x] % mod;
    return res;
}
vector<int> groups = {2, 2, 1}; // AABBC
cout << multinomial(groups) << "\n"; // Output: 30
// der[i] = number of permutations of i elements with
// no element in its original position

```

```

11 der[N];
void precomputeDerangements() {
    der[0] = 1, der[1] = 0;
    for(int i = 2; i < N; i++)
        der[i] = ((i - 1) * (der[i - 1] + der[i - 2]) %
                    mod) % mod;
}
// Returns nCr % p for large n, r and small p (p <=
// 10^5)
11 lucas(ll n, ll r, int p) {
    if (r == 0) return 1;
    return (lucas(n / p, r / p, p) * nCr(n % p, r % p)) %
        p; // Note: nCr here must use p as MOD
}
// Stirling numbers of the second kind: S(n,k) =
// number of ways to partition n elements into k
// non-empty subsets
11 stirling2(int n, int k) { // O(klogn)
    ll ans = 0;
    for(int i = 0; i <= k; i++) {
        ll term = (ll)nCr(k, i) * BinExp(k - i, n, mod) %
                    mod;
        if(i % 2) term = mod - term;
        ans = (ans + term) % mod;
    }
    ans = ans * ifact[k] % mod;
    return ans;
}
// Burnside's lemma for necklace counting: number of
// distinct necklaces with n beads and k colors
11 burnside_necklace(ll n, ll k) {
    ll sum = 0;
    for (ll r = 0; r < n; r++) {
        sum += BinExp(k, __gcd(n, r), mod);
        sum %= mod;
    }
    return sum * BinExp(n, mod - 2, mod) % mod;
}
// Pascal's Triangle -> 0 based
// 0)      1
// 1)      1 1
// 2)      1 2 1
// 3)      1 3 3 1
// 4)      1 4 6 4 1
// 5) 1 5 10 10 5 1
int PascalsTriangle(int r, int c) {
    return nCr(r, c);
}
// 0)      1
// 1)      1 1
// 2)      1 2 [1]
// 3)      1 3 [3] 1
// 4)      1 4 [6] 4 1
// 5) 1 5 10 (10) 5 1
// sum of (0Cr, 1Cr, 2Cr, 3Cr, 4Cr) -> 5C(r + 1)
int HockeyStickIdentity(int n, int r) {
    return nCr(n + 1, r + 1);
}
// Vandermonde's identity: sum_{i=0}^{r-1} C(m, i) *
// C(n, r-i) = C(m+n, r)

```

```

// Counts ways to pick r items from two sets by
// summing over all splits.
int vandermondeIdentity(int n, int k) {
    return nCr(n + k, k);
}

```

12 Compress Array

```

void CompressArray(vector<int>& a) {
    auto b = a; sort(b.begin(), b.end());
    b.erase(unique(b.begin(), b.end()), b.end());
    for (auto& ai : a)
        ai = lower_bound(b.begin(), b.end(), ai) -
            b.begin();
}

```

13 Convex Hull

```

const double PI = acos((double)-1.0);
using ll = long long;
struct PT {
    ll x, y;
    bool operator < (const PT &p) const {
        return x == p.x ? y < p.y : x < p.x;
    }
};
11 area(PT a, PT b, PT c) { // twice of area
    return (b.x - a.x) * (c.y - a.y) - (b.y - a.y) *
        (c.x - a.x);
}
vector<PT> ConvexHull(vector<PT> p) {
    int n = p.size(), m = 0;
    if (n < 3) return p;
    vector<PT> hull(n + n);
    sort(p.begin(), p.end());
    for (int i = 0; i < n; ++i) {
        while (m > 1 and area(hull[m - 2], hull[m - 1],
                    p[i]) <= 0) --m;
        hull[m++] = p[i];
    }
    for (int i = n - 2, j = m + 1; i >= 0; --i) {
        while (m >= j and area(hull[m - 2], hull[m - 1],
                    p[i]) <= 0) --m;
        hull[m++] = p[i];
    }
    hull.resize(m - 1);
    return hull;
}
11 convexHullArea() {
    int n = hull.size();
    ll totalArea = 0;
    for (int i = 0; i < n; ++i) {
        int j = (i + 1) % n;
        totalArea += hull[i].x * hull[j].y - hull[j].x *
            hull[i].y;
    }
    return llabs(totalArea); // twice of area
    return llabs(totalArea) / 2.0;
}

```

```

11 f(int i, PT P, int n) {
    return area(hull[i], hull[(i + 1) % n], P);
}
1d minTriangleArea(PT P) {
    int n = hull.size(), l = 0, r = n - 1;
    while (r - l > 5) {
        int m1 = l + (r - l) / 3;
        int m2 = r - (r - l) / 3;
        if (f(m1, P, n) < f(m2, P, n)) r = m2 - 1;
        else l = m1 + 1;
    }
    11 ans = 1.1e17;
    for (int i = l; i <= r; i++)
        ans = min(ans, f(i, P, n));
    return ans; // twice of area
    return (1d)ans / 2.0;
}

```

14 Coin Piles

```

// Remove (1,2) or (2,1) coins from the two piles per
// move.
int main() {
    int t;
    cin >> t;
    while (t--) {
        ll a, b;
        cin >> a >> b;
        if ((a + b) % 3 == 0 && min(a, b) * 2 >= max(a,
                b))
            cout << "YES\n";
        else
            cout << "NO\n";
    }
}

```

15 Dfs With Lca

```

struct DFS {
    int n, k, t = 0;
    vector<int> tin, tout, depth, height, subtree_size,
        heavy;
    vector<bool> is_leaf;
    vector<vector<int>> parent;
    DFS() {}
    DFS(vector<vector<int>>& adj, int root = 1) {
        n = (int)adj.size() + 1;
        k = __lg(n) + 1;
        tin.resize(n), tout.resize(n), depth.resize(n),
        height.resize(n), subtree_size.resize(n),
        heavy.assign(n, -1), is_leaf.assign(n, 1);
        parent = vector<vector<int>> (n, vector<int> (k));
        dfs(root, root, adj);
    }
    void dfs(int u, int p, vector<vector<int>>& adj) {
        tin[u] = ++t;
        subtree_size[u] = 1;
        parent[u][0] = p;
        for (int i = 1; i < k; i++)
            parent[u][i] = parent[parent[u][i - 1]][i - 1];
        for (int v : adj[u])
            if (v != p)
                dfs(v, u, adj);
    }
}

```

```

for (int i = 1; i < k; i++) {
    if (parent[u][i - 1] != -1) parent[u][i] =
        parent[parent[u][i - 1]][i - 1];
    else parent[u][i] = -1;
}
for (auto& v : adj[u]) {
    if (v != p) {
        depth[v] = depth[u] + 1;
        is_leaf[u] = 0;
        dfs(v, u, adj);
        height[u] = max(height[u], height[v] + 1);
        subtree_size[u] += subtree_size[v];
        if (heavy[u] == -1 || subtree_size[heavy[u]] < subtree_size[v]) {
            heavy[u] = v;
        }
    }
}
tout[u] = ++t;
}

bool is_ancestor(int u, int v) {
    return tin[u] <= tin[v] && tout[v] <= tout[u];
}

int kth_parent(int u, int kth) {
    for (int i = k - 1; i >= 0; i--) {
        if (kth & (1 << i)) {
            u = parent[u][i];
            if (u == -1) return u;
        }
    }
    return u;
}

int lca(int u, int v) {
    if (is_ancestor(u, v)) return u;
    for (int i = k - 1; i >= 0; i--) {
        if (!is_ancestor(parent[u][i], v))
            u = parent[u][i];
    }
    return parent[u][0];
}

int dis(int u, int v)
    return depth[u] + depth[v] - 2 * depth[lca(u, v)];
};

```

16 Digit Dp

```

// optimized - final
// count of 11, from 0 to n
// first reverse the string, then cal f(s.size() - 1,
// → 0, 10, 1)
// memset only once
11 dp[32][32][3];
11 f(int i, int cnt, int last, int tight) {
    if (i < 0) return cnt;
    auto ret = dp[i][cnt][last];
    if (~ret && !tight) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 1;
    for (int d = 0; d <= limit; d++) {
        int nTight = tight && (d == limit);
        int nCnt = cnt + (last == d && d == 1);
        ret += f(i - 1, nCnt, d, nTight);
    }
}

```

```

    }
    if (!tight) dp[i][cnt][last] = ret;
    return ret;
}
// handle case of '0' -> no two adjacent digits are
// → the same.
// int nLast = (last == 10 && d == 0) ? 10 : d;
// or use started state for keep track that if number
// → has started
11 dp[20][11];
11 f(int i, int last, int tight) {
    if (i < 0) return 1;
    auto ret = dp[i][last];
    if (~ret && !tight) return ret;
    ret = 0;
    int limit = tight ? s[i] - '0' : 9;
    for (int d = 0; d <= limit; d++) {
        if (d == last) continue;
        int nTight = tight && (d == limit);
        int nLast = (last == 10 && d == 0) ? 10 : d;
        ret += f(i - 1, nLast, nTight);
    }
    if (!tight) dp[i][last] = ret;
    return ret;
}

#2 countWithExactDigitCount // f(0, 0, 1, 0)
int dp[11][11][2][2];
int targetDigit, targetCnt;
int f(int i, int digitCnt, int tight, int started) {
    if (i == n) {
        return targetCnt == digitCnt;
    }
    auto& ret = dp[i][digitCnt][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newDigitCnt = digitCnt;
        if (newStarted) newDigitCnt += (d == targetDigit);
        ret += f(i + 1, newDigitCnt, newTight,
            → newStarted);
    }
    return ret;
}
#6 countNumbersWithOnly1234 // f(0, 1, 0)
int dp[11][2][2];
int f(int i, int tight, int started) {
    if (i == n) {
        return started;
    }
    auto& ret = dp[i][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}
#11 count Numbers Divisible By k and Contains No Digit
// → m // f(0, 0, 1, 0)
int dp[11][100][2][2];
int k, m;
int f(int i, int rem, int tight, int started) {
    if (i == n) return started && (rem == 0);
    auto& ret = dp[i][rem][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}

```

```

if (d > 4) continue;
if (!newStarted && d == 0) ret += f(i + 1,
    → newTight, newStarted);
else if (d >= 1 && d <= 4) ret += f(i + 1,
    → newTight, newStarted);
}
return ret;
}
#8 countDistinctDigitNumbers // f(0, 0, 1, 0)
int dp[11][1025][2][2];
int f(int i, int mask, int tight, int started) {
    if (i == n) return started;
    auto& ret = dp[i][mask][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) {
            if (mask & (1 << d)) continue;
            newMask |= (1 << d);
        }
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}
#9 countWithAnyRepeatedDigits -> n -
// → f(countDistinctDigitNumbers)
#10 countNumbersWithKDistinctDigits // f(0, 0, 1, 0)
int k, dp[11][1025][2][2];
int f(int i, int mask, int tight, int started) {
    if (i == n) return started &&
        → (_builtin_popcount(mask) == k);
    auto& ret = dp[i][mask][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        ret += f(i + 1, newMask, newTight, newStarted);
    }
    return ret;
}
#11 count Numbers Divisible By k and Contains No Digit
// → m // f(0, 0, 1, 0)
int dp[11][100][2][2];
int k, m;
int f(int i, int rem, int tight, int started) {
    if (i == n) return started && (rem == 0);
    auto& ret = dp[i][rem][tight][started];
    if (~ret) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;

```

```

for (int d = 0; d <= limit; d++) {
    if (d == m) continue;
    int newTight = tight && (d == limit);
    int newStarted = started || (d > 0);
    int newRem = (rem * 10 + d) % k;
    ret += f(i + 1, newRem, newTight, newStarted);
}
return ret;
}

--> find sum of integers and conunt at same time
#12 sum and count of all numbers x that has at most k
→ distinct digits // f(0, 0, 1, 0)
const int mod = 998244353;
ll n, k, Pow10[20];
array<ll, 2> dp[20][1025][2][2]; // dp[0] -> cnt,
→ dp[1] -> sum;
string s;
array<ll, 2> f(int i, int mask, int tight, int
→ started) {
    if (i == n) {
        return {started && (_builtin_popcount(mask) <=
            → k), 0};
    }
    auto& ret = dp[i][mask][tight][started];
    if (!ret[0]) return ret;
    ret = {0, 0};
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        int newStarted = started || (d > 0);
        int newMask = mask;
        if (newStarted) newMask |= (1 << d);
        auto [currCnt, currSum] = f(i + 1, newMask,
            → newTight, newStarted);
        auto& [cnt, sum] = ret;
        cnt = (cnt + currCnt) % mod;
        sum = (sum + (currCnt * d % mod) * Pow10[n - i -
            → 1] % mod);
        sum = (sum + currSum) % mod;
    }
    return ret;
}
ll Cnt(ll num) {
    if (num <= 0) return 0;
    memset(dp, -1, sizeof dp);
    s = to_string(num);
    n = s.size();
    Pow10[0] = 1;
    for (int i = 1; i < 20; i++) {
        Pow10[i] = (Pow10[i - 1] * 10) % mod;
    }
    return f(0, 0, 1, 0)[1];
}

--> find digit sum upto n, this is optimized version,
→ use memset just once
string s;
ll dp[20][2][2];
ll cnt[20][2][2];
pair<ll, ll> f(int i, int tight, int started) {

```

```

if (i < 0) return {0, started ? 1 : 0}; // {sum,
→ count of valid numbers}
if (~dp[i][tight][started] && !tight) return
→ {dp[i][tight][started], cnt[i][tight][started]};
ll totalSum = 0, totalCount = 0;
int limit = tight ? (s[i] - '0') : 9;
for (int d = 0; d <= limit; d++) {
    int newTight = tight && (d == limit);
    int newStarted = started || (d > 0);
    auto [nextSum, nextCount] = f(i - 1, newTight,
        → newStarted);
    if (newStarted) {
        totalSum += d * nextCount + nextSum;
        totalCount += nextCount;
    } else {
        totalSum += nextSum;
        totalCount += nextCount;
    }
}
dp[i][tight][started] = totalSum;
cnt[i][tight][started] = totalCount;
return {totalSum, totalCount};

ll sumOfAllDigits(ll num) {
    if (num < 0) return 0;
    s = to_string(num);
    reverse(s.begin(), s.end());
    return f(s.size() - 1, 1, 0).first;
}
memset(dp, -1, sizeof dp);
memset(cnt, -1, sizeof cnt);

// Optimized versions -->
## with only 1 memset, reverse the number then
→ calculate from (n - 1) ->
## so when some state is already calculated and tight
→ == 0, then return 'ret', or else again calculate
→ the state
#13 count of 3 = 6 = 9, and count of 3 > 0
const int mod = 1e9 + 7, N = 17;
string s;
int dp[51][N][N][N][2]; // f(s.size() - 1, 0, 0, 0, 1)
int f(int i, int three, int six, int nine, int tight)
→ {
    if (three > 16 || six > 16 || nine > 16) return 0;
    if (i < 0) {
        return (three > 0) && (three == six) && (six ==
            → nine);
    }
    auto& ret = dp[i][three][six][nine][tight];
    if (ret != -1 && !tight) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        ret = (ret + f(i - 1, three + (d == 3), six + (d
            → == 6), nine + (d == 9), newTight)) % mod;
    }
    return ret;
}

// optimized, without tight state
// when the state is not tight then return 'ret' also
→ memoize the dp;
int dp[51][N][N][N];
int f(int i, int three, int six, int nine, int tight)
→ {
    if (three > 16 || six > 16 || nine > 16) return 0;
    if (i < 0) {
        return (three > 0) && (three == six) && (six ==
            → nine);
    }
    auto ret = dp[i][three][six][nine];
    if (ret != -1 && !tight) return ret;
    ret = 0;
    int limit = tight ? (s[i] - '0') : 9;
    for (int d = 0; d <= limit; d++) {
        int newTight = tight && (d == limit);
        ret = (ret + f(i - 1, three + (d == 3), six + (d
            → == 6), nine + (d == 9), newTight)) % mod;
    }
    if (!tight) dp[i][three][six][nine] = ret;
    return ret;
}

int Cnt(string a) {
    reverse(a.begin(), a.end());
    s = a;
    return f(s.size() - 1, 0, 0, 0, 1);
}

int check(string& s) {
    // problem condition
}

void solve() {
    string a, b;
    cin >> a >> b;
    cout << Cnt(b) - Cnt(a) + check(a); // check if only
    → string a can satisfy the condition
}

// calculate between l and r in one function
int dp[51][2][2][18][18][18];
string l, r;
int f(int i, int tightLower, int tightUpper, int c3,
→ int c6, int c9) {
    if (c3 >= 17 || c6 >= 17 || c9 >= 17) return 0;
    if (i < 0) {
        return c3 && c3 == c6 && c6 == c9;
    }
    int& ret =
        → dp[i][tightLower][tightUpper][c3][c6][c9];
    if (~ret && !tightLower && !tightUpper) return ret;
    int lo = tightLower ? l[i] - '0' : 0;
    int hi = tightUpper ? r[i] - '0' : 9;
    ret = 0;
    for (int d = lo; d <= hi; d++) {
        int newTightLower = tightLower && (d == lo);
        int newTightUpper = tightUpper && (d == hi);

```

```

    ret = (ret + f(i - 1, newTightLower,
    ↵ newTightUpper, c3 + (d == 3), c6 + (d == 6),
    ↵ c9 + (d == 9))) % mod;
}
return ret;
}
// optimized, without (tightLower, tightUpper) state
int f(int i, int tightLower, int tightUpper, int c3,
    ↵ int c6, int c9) {
if (c3 >= 17 || c6 >= 17 || c9 >= 17) return 0;
if (i < 0) {
    return c3 && c3 == c6 && c6 == c9;
}
int ret = dp[i][c3][c6][c9];
if (!ret && !tightLower && !tightUpper) return ret;
int lo = tightLower ? l[i] - '0' : 0;
int hi = tightUpper ? r[i] - '0' : 9;
ret = 0;
for (int d = lo; d <= hi; d++) {
    int newTightLower = tightLower && (d == lo);
    int newTightUpper = tightUpper && (d == hi);
    ret = (ret + f(i - 1, newTightLower,
    ↵ newTightUpper, c3 + (d == 3), c6 + (d == 6),
    ↵ c9 + (d == 9))) % mod;
}
if (!tightLower && !tightUpper) dp[i][c3][c6][c9] =
    ↵ ret;
return ret;
}
void solve() {
    cin >> l >> r;
    int n = r.size();
    while (l.size() < n) l = "0" + l;
    reverse(l.begin(), l.end());
    reverse(r.begin(), r.end());
    cout << f(n - 1, 1, 1, 0, 0, 0) << '\n';
}

```

17 Dijkstra

```
const ll INF = 1.1e17;
vector<ll> Dijkstra(vector<vector<array<ll, 2>>&
→ adj, int source = 1) {
    int n = (int)adj.size();
    vector<ll> dis(n, INF);
    vector<bool> vis(n);
    dis[source] = 0;
    priority_queue<array<ll, 2>, vector<array<ll, 2>>
    → greater<array<ll, 2>>> pq;
    pq.push({0, source});
    while (!pq.empty()) {
        auto [d, u] = pq.top();
        pq.pop();
        if (vis[u]) continue;
        vis[u] = 1;
        for (auto& [v, c] : adj[u]) {
            if (dis[v] > d + c) {
                dis[v] = d + c;
                pq.push({dis[v], v});
            }
        }
    }
}
```

```

    }
}
} return dis;
}



## 18 Dinic Max Flow



---



```

// complexity: O(E.V^2)
struct edge {
 int u, v;
 ll cap, flow;
 edge(int u, int v, ll cap) : u(u), v(v), cap(cap)
 ~> flow(0) {}
};

struct Dinic {
 int N;
 vector<edge> E;
 vector<vector<int>> g;
 vector<int> d, pt;
 Dinic(int N) : N(N), E(0), g(N), d(N), pt(N) {}
 void AddEdge(int u, int v, ll cap) {
 if (u == v) {
 E.emplace_back(u, v, cap);
 g[u].emplace_back(E.size() - 1);
 E.emplace_back(v, u, 0);
 g[v].emplace_back(E.size() - 1);
 }
 }
 bool BFS(int S, int T) {
 queue<int> q({S});
 fill(d.begin(), d.end(), N + 1);
 d[S] = 0;
 while (!q.empty()) {
 int u = q.front();
 q.pop();
 if (u == T) break;
 for (int k : g[u]) {
 edge &e = E[k];
 if (e.flow < e.cap and d[e.v] > d[e.u] + 1) {
 d[e.v] = d[e.u] + 1;
 q.emplace(e.v);
 }
 }
 }
 return d[T] != N + 1;
 }
 ll DFS(int u, int T, ll flow = -1) {
 if (u == T or flow == 0) return flow;
 for (int &i = pt[u]; i < g[u].size(); ++i) {
 edge &e = E[g[u][i]];
 edge &oe = E[g[u][i] ^ 1];
 if (d[e.v] == d[e.u] + 1) {
 ll amt = e.cap - e.flow;
 if (flow != -1 and amt > flow) amt = flow;
 if (ll pushed = DFS(e.v, T, amt)) {
 e.flow += pushed;
 oe.flow -= pushed;
 return pushed;
 }
 }
 }
 return 0;
 }
}

```


```

18 Dinic Max Flow

```

    }
    ll MaxFlow(int S, int T) {
        ll total = 0;
        while (BFS(S, T)) {
            fill(pt.begin(), pt.end(), 0);
            while (ll flow = DFS(S, T)) total += flow;
        } return total;
    }
};

/*
Dinic dinic(N);
dinic.AddEdge(u - 1, v - 1, cap);
dinic.AddEdge(v - 1, u - 1, cap); // for undirected
dinic.MaxFlow(0, N - 1);
*/

```

19 Distinct Subsequence

```

int distinctSubseq(string &a) {
    vector<int> last(26); // for array, use map
    int res = 1;
    for(auto& ai : a) {
        int curr = (2LL * res - last[ai - 'a']) % mod;
        if (curr < 0) curr += mod;
        last[ai - 'a'] = res;
        res = curr;
    } return (res - 1 + mod) % mod; // without empty set
}

```

20 Dp Path Print Recursive

```

// LIS
const int N = 1001;
int n, m, a[N], b[N], dp[N][N];
int f(int i, int j) {
    if (i >= n || j >= m) return 0;
    auto& ret = dp[i][j];
    if (~ret) return ret;
    if (a[i] == b[j]) {
        ret = f(i + 1, j + 1) + 1;
    } else {
        ret = max(ret, f(i + 1, j));
        ret = max(ret, f(i, j + 1));
    }
    return ret;
}
void g(int i, int j, int len) {
    if (len == 0 || i >= n || j >= n) return;
    if (a[i] == b[j]) {
        cout << a[i] << ' ';
        g(i + 1, j + 1, len - 1);
    } else {
        if (f(i + 1, j) >= f(i, j + 1)) g(i + 1, j, len);
        else g(i, j + 1, len);
    }
}
f(0, 0);
g(0, 0, len);

```

21 Dsu

```
struct DSU {
    vector<int> parent, sz;
    DSU(int n) {
        parent.resize(n + 1), sz.resize(n + 1, 1);
        iota(parent.begin(), parent.end(), 0);
    }
    int Find(int u) {
        if (u == parent[u]) return u;
        return parent[u] = Find(parent[u]);
    }
    bool Is_connected(int u, int v) {
        return Find(u) == Find(v);
    }
    void Merge(int u, int v) {
        u = Find(u), v = Find(v);
        if (u != v) {
            if (sz[u] < sz[v]) swap(u, v);
            parent[v] = u;
            sz[u] += sz[v];
        }
    }
};
```

22 Digit Queries

```
char find_digit(ll k) {
    ll len = 1, count = 9, start = 1;
    while (k > len * count) {
        k -= len * count;
        len++, count *= 10, start *= 10;
    }
    ll num = start + (k - 1) / len;
    string s = to_string(num);
    return s[(k - 1) % len];
}
int main() {
    int q; cin >> q;
    while (q--) {
        ll k;
        cin >> k;
        cout << find_digit(k) << '\n';
    }
}
```

23 Exclusion Dp

```
vector<int> f(n), g(n);
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) f[i] += cnt[j];
    f[i] = nc2(f[i]);
}
for (int i = N - 1; i > 0; i--) {
    g[i] = f[i];
    for (int j = i * 2; j < N; j += i) g[i] -= g[j];
}
// g[i] = how many pairs have gcd i
```

24 Extended Gcd Crt

```
// returns gcd(a, b) and sets x, y such that a*x + b*y
// = gcd(a,b)
ll extendedGCD(ll a, ll b, ll &x, ll &y) {
    if (b == 0) { x = 1, y = 0; return a; }
    ll x1, y1;
    ll d = extendedGCD(b, a % b, x1, y1);
    x = y1, y = x1 - (a / b) * y1;
    return d;
}
// a*x ≡ 1 (mod m) -> x is the modular inverse of a
// modulo m
ll modInv(ll a, ll m) {
    ll x, y;
    ll g = extendedGCD(a, m, x, y);
    if (g != 1) return -1;
    return (x % m + m) % m;
}
// returns all solutions to a*x ≡ b (mod m) -> (g
// should be small)
vector<ll> solveModEquation(ll a, ll b, ll m) {
    ll x, y;
    ll g = extendedGCD(a, m, x, y);
    vector<ll> sol;
    if (b % g != 0) return sol;
    ll x0 = (x * (b / g)) % m;
    if (x0 < 0) x0 += m;
    ll mod = m / g;
    for (int k = 0; k < g; k++) {
        sol.push_back((x0 + k * mod) % m);
    }
    return sol;
}
// Merge two congruences: x ≡ a1 mod m1, x ≡ a2 mod
// m2
pair<ll, ll> merge(ll a1, ll m1, ll a2, ll m2) {
    ll x, y;
    ll g = extendedGCD(m1, m2, x, y);
    if ((a2 - a1) % g != 0) return {-1, -1};
    ll lcm = m1 / g * m2;
    ll k = ((a2 - a1) / g % (m2 / g) + (m2 / g)) % (m2
        / g);
    k = k * ((x % (m2 / g) + (m2 / g)) % (m2 / g)) %
        (m2 / g);
    ll res = (a1 + m1 * k) % lcm;
    if (res < 0) res += lcm;
    return {res, lcm};
}
// Returns {x, mod} or {-1, -1} if no solution
// ans.first = the smallest non-negative solution x
// ans.second = the modulus of the solution, i.e., the
// LCM of all input moduli
pair<ll, ll> CRT(const vector<ll> &a, const vector<ll>
&m) {
    ll x = a[0], mod = m[0];
    for (int i = 1; i < a.size(); i++) {
        auto res = merge(x, mod, a[i], m[i]);
        if (res.first == -1) return {-1, -1};
        x = res.first;
        mod = res.second;
    }
    return {x, mod};
}
```

```
/*
    x ≡ a1 (mod m1)
    x ≡ a2 (mod m2)
    ...
    x ≡ an (mod mn)
*/
vector<long long> a = {2, 3, 2};
vector<long long> m = {3, 5, 8};
auto ans = CRT(a, m);
```

25 Farthest Index Where Each Element Is Distinct

```
// 0 based, farthest index where each element is
// distinct
array<vector<int>, 2>
farthestDistinctElementIndex(vector<int>& a) {
    int n = a.size(), mxIdx = -1;
    map<int, int> mp;
    vector<int> l(n);
    for (int i = 0; i < n; i++) {
        if (mp.count(a[i])) mxIdx = max(mxIdx, mp[a[i]]);
        mp[a[i]] = i, l[i] = mxIdx + 1;
    }
    mp.clear(), mxIdx = n;
    vector<int> r(n);
    for (int i = n - 1; i >= 0; i--) {
        if (mp.count(a[i])) mxIdx = min(mxIdx, mp[a[i]]);
        mp[a[i]] = i, r[i] = mxIdx - 1;
    }
    return {l, r};
}
```

26 Fenwick Tree 2d

```
struct FenWick2D {
    int n, m;
    vector<vector<ll>> ft;
    FenWick2D(int _n, int _m) {
        n = _n, m = _m;
        ft.assign(n + 1, vector<ll> (m + 1));
    }
    void Add(int x, int y, ll val) {
        for (int i = x; i <= n; i += i & -i)
            for (int j = y; j <= m; j += j & -j)
                ft[i][j] += val;
    }
    ll Csum(int x, int y) {
        ll res = 0;
        for (int i = x; i > 0; i -= i & -i)
            for (int j = y; j > 0; j -= j & -j)
                res += ft[i][j];
        return res;
    }
    ll Rsum(int x1, int y1, int x2, int y2) {
        return Csum(x2, y2) - Csum(x1 - 1, y2) - Csum(x2,
            - y1 - 1) + Csum(x1 - 1, y1 - 1);
    }
};
```

27 Fenwick Tree Bit

```

struct FenwickTree {
    int n;
    vector<ll> ft;
    FenwickTree(vector<int>& a) {
        Initial((int)a.size());
        Build(a);
    }
    void Initial(int _n) {
        n = _n;
        ft.assign(n + 1, 0);
    }
    void Build(vector<int>& a) {
        for (int i = 0; i < (int)a.size(); i++) Add(i, i, a[i]); #change
    }
    void Add(int idx, ll val) {
        for (int i = idx; i <= n; i += i & -i) ft[i] += val;
    }
    void Add(int l, int r, ll val) {
        Add(l, val);
        Add(r + 1, -val);
    }
    ll Csum(int idx) {
        ll res = 0;
        for (int i = idx; i > 0; i -= i & -i) res += ft[i];
        return res;
    }
    ll Rsum(int l, int r) {
        return Csum(r) - Csum(l - 1);
    }
};

```

28 Fft

```

struct cplx {
    long double a, b;
    cplx(long double a = 0, long double b = 0) : a(a),
    → b(b) {}
    const cplx operator + (const cplx &c) const {
        → return cplx(a + c.a, b + c.b); }
    const cplx operator - (const cplx &c) const {
        → return cplx(a - c.a, b - c.b); }
    const cplx operator * (const cplx &c) const {
        → return cplx(a * c.a - b * c.b, a * c.b + b *
        → c.a); }
    const cplx operator / (const long double &d) const
    → { return cplx(a / d, b / d); }
};

const long double PI = acos(-1);
vector<int> rev;
void Preprocess(int sz) {
    if ((int)rev.size() == sz) return;
    rev.resize(sz);
    rev[0] = 0;
    int lg_n = __builtin_ctz(sz);

```

```

        for (int i = 1; i < sz; ++i)
            rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (lg_n -
            → 1));
    }
    void fft(vector<cplx> &a, bool inv = 0) {
        int n = a.size();
        for (int i = 1; i < n - 1; ++i) {
            if (i < rev[i]) swap(a[i], a[rev[i]]);
        }
        for (int len = 2; len <= n; len <= 1) {
            long double t = 2 * PI / len * (inv ? -1 : 1);
            cplx wlen = {cosl(t), sinl(t)};
            for (int st = 0; st < n; st += len) {
                cplx w(1);
                for (int i = 0; i < len / 2; ++i) {
                    cplx ev = a[st + i], od = a[st + i + len / 2]
                    → * w;
                    a[st + i] = ev + od;
                    a[st + i + len / 2] = ev - od;
                    w = w * wlen;
                }
            }
            if (inv)
                for (cplx& z : a) z = z / n;
        }
        vector<long long> multiply(vector<int> &a,
        → vector<int> &b) {
            int n = a.size(), m = b.size(), sz = 1;
            while(sz < n + m - 1) sz <= 1;
            vector<cplx> x(sz), y(sz), z(sz);
            for(int i = 0 ; i < sz; i++) {
                x[i] = i < n ? cplx(a[i], 0) : cplx(0, 0);
                y[i] = i < m ? cplx(b[i], 0) : cplx(0, 0);
            }
            Preprocess(sz);
            fft(x), fft(y);
            for(int i = 0; i < sz; i++) z[i] = x[i] * y[i];
            fft(z, 1);
            vector<long long> c(n + m - 1);
            for(int i = 0; i < n + m - 1; i++) c[i] =
            → round(z[i].a);
            return c;
        }
        auto c = multiply(a, b);
    }

```

29 Fibonacci Log N

```

pair<ll, ll> fib_pair(ll n) {
    if (n == 0) return {0, 1};
    auto p = fib_pair(n >> 1);
    ll c = p.first * ((2 * p.second - p.first + mod) %
    → mod) % mod;
    ll d = (p.first * p.first % mod + p.second *
    → p.second % mod) % mod;
    if (n & 1) return {d, (c + d) % mod};
    return {c, d};
}
ll fibonacci(ll n) {

```

```

    return fib_pair(n).first;
}

```

30 Floyd Warshall

```

void FloydWarshall(vector<vector<long long>>& adj) {
    int n = (int)adj.size();
    for (int k = 0; k < n; k++) {
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                adj[i][j] = min(adj[i][j], adj[i][k] +
                → adj[k][j]);
                adj[i][i] = 0;
            }
        }
    }
}

```

31 Geometry

```

const double PI = acos((double)-1.0);
using ld = long double;
using ll = long long;
struct point { ld x, y; }
point operator+(const point& a, const point& b){  

    → return {a.x+b.x, a.y+b.y}; }
point operator-(const point& a, const point& b){  

    → return {a.x-b.x, a.y-b.y}; }
point operator*(const point& a, ld k){ return {a.x*k,
    → a.y*k}; }
point operator/(const point& a, ld k){ return {a.x/k,
    → a.y/k}; }
void manhattanToChebychev(int& x, int& y) {  

    int X = x + y, Y = x - y;  

    x = X, y = Y;
}
void chebyshevToManhattan(int& x, int& y) {  

    int X = (x + y) / 2, Y = (x - y) / 2;  

    x = X, y = Y;
}
ll manhattanDistance(point& p1, point& p2) {
    return abs(p1.x - p2.x) + abs(p1.y - p2.y);
}
/*
    Calculates the minimum time to move between two
    → points
    when diagonal movement is allowed.
    This uses Chebyshev distance.
*/
ll chebyshevDistance(point& p1, point& p2) {
    return max(abs(p1.x - p2.x), abs(p1.y - p2.y));
}
// distance of two points
ld distance(point& p1, point& p2) {
    return sqrt((p2.x - p1.x) * (p2.x - p1.x) + (p2.y -
    → p1.y) * (p2.y - p1.y));
}
ld dot(point a, point b){ return a.x*b.x + a.y*b.y; }

```

```

ld cross(point a, point b){ return a.x*b.y - a.y*b.x;
}
ld pointLineDistance(point p, point a, point b){
    return abs(cross(b-a, p-a) / distance(a, b));
}
point project(point p, point a, point b){
    ld t = dot(p-a, b-a) / dot(b-a, b-a);
    return a + (b-a)*t;
}
/*
    determines the relative position (cross product) of
    a point (p3)
    with respect to the line passing through (p1) and
    (p2)
    if (d > 0): point (p3) is to the left of the line
    if (d < 0): point (p3) is to the right of the line
    if (d == 0): point (p3) lies exactly on the line.
*/
ld determinant(point p1, point p2, point p3) {
    ld d = (p2.x - p1.x) * (p3.y - p1.y) - (p2.y -
    p1.y) * (p3.x - p1.x);
    return d;
}
bool arePointsOnSameSide(point p1, point p2, point
    p3, point p4) {
    ld d1 = determinant(p1, p2, p3);
    ld d2 = determinant(p1, p2, p4);
    return (d1 * d2) > 0;
}
bool doLinesIntersect(point p1, point p2, point p3,
    point p4) {
    ld d1 = determinant(p3, p4, p1);
    ld d2 = determinant(p3, p4, p2);
    ld d3 = determinant(p1, p2, p3);
    ld d4 = determinant(p1, p2, p4);
    return (d1 * d2 < 0) && (d3 * d4 < 0);
}
// a point inside circle
// x1, y1 = point of circle, r = radius of circle
// x2, y2 = target point
bool isInside(int x1, int y1, int x2, int y2, int r) {
    return ((x2 - x1) * (x2 - x1)) + ((y2 - y1) * (y2 -
    y1)) <= r * r;
}
ld toDegrees(ld radians) {
    return radians * (180.0 / PI);
}
point rotate(point p, ld theta){ // theta in radians
    return {p.x*cos(theta) - p.y*sin(theta),
            p.x*sin(theta) + p.y*cos(theta)};
}
// circle with radius r
struct Circle {
    ld r;
    Circle(ld _r) { r = _r; }
    ld Diameter() { return 2 * r; }
    ld Circumference() { return 2 * PI * r; }
    ld Area() { return PI * r * r; }
    // if theta in radians, make it to degrees
}

```

```

// all the calculations are in degree
ld Sector_Area(ld theta) { return (theta / 360.0) *
    Area(); }
ld Arc_Length(ld theta) { return (theta / 360.0) *
    Circumference(); }
ld Chord_Length(ld theta) { return 2 * r *
    sin((theta * PI) / 360.0); }
ld Segment_Area(ld theta) { return
    Sector_Area(theta) - (0.5 * r * r * sin((theta *
    PI) / 180.0)); }
ld Circumscribed_Square_Area() { return 4 * r * r; }
ld Inscribed_Square_Area() { return 2 * r * r; }
ld Sphere_Surface_Area() { return 4 * PI * r * r; }
ld Sphere_Volume() { return (4.0 / 3.0) * PI * r *
    r * r; }
ld Cylinder_Surface_Area(ld h) { return 2 * PI * r *
    (r + h); }
ld Cylinder_Volume(ld h) { return PI * r * r * h; }
ld Cone_Surface_Area(ld l) { return PI * r * (r +
    l); }
ld Cone_Volume(ld h) { return (1.0 / 3.0) * PI * r *
    r * h; }
ld Annulus_Area(ld R) { return PI * (r * r - R *
    R); }
}
// triangle with three sides: a, b, c
struct Triangle {
    ld a, b, c, s;
    Triangle(point x, point y, point z) {
        a = distance(x, y);
        b = distance(y, z);
        c = distance(z, x);
        s = (a + b + c) / 2;
    }
    Triangle(ld _a, ld _b, ld _c) {
        a = _a, b = _b, c = _c;
        s = (a + b + c) / 2;
    }
    ld Area() { return sqrt(s * (s - a) * (s - b) * (s -
        c)); }
    ld Perimeter() { return a + b + c; }
    ld Angle_A_Radians() { return acos((b * b + c * c -
        a * a) / (2 * b * c)); }
    ld Angle_B_Radians() { return acos((a * a + c * c -
        b * b) / (2 * a * c)); }
    ld Angle_C_Radians() { return acos((a * a + b * b -
        c * c) / (2 * a * b)); }
    ld Angle_A_Degrees() { return
        toDegrees(Angle_A_Radians()); }
    ld Angle_B_Degrees() { return
        toDegrees(Angle_B_Radians()); }
    ld Angle_C_Degrees() { return
        toDegrees(Angle_C_Radians()); }
    ld Inradius() { return sqrt((s - a) * (s - b) * (s -
        c) / s); }
    ld Circumradius() { return (a * b * c) / (4 *
        Area()); }
}

```

```

ld Exradius_A() { return Area() / (s - a); }
ld Exradius_B() { return Area() / (s - b); }
ld Exradius_C() { return Area() / (s - c); }
ld Altitude_A() { return 2 * Area() / a; }
ld Altitude_B() { return 2 * Area() / b; }
ld Altitude_C() { return 2 * Area() / c; }
ld Median_A() { return sqrt((2 * b * b + 2 * c * c -
    - a * a) / 4); }
ld Median_B() { return sqrt((2 * a * a + 2 * c * c -
    - b * b) / 4); }
ld Median_C() { return sqrt((2 * a * a + 2 * b * b -
    - c * c) / 4); }
}
point circumcenter(point a, point b, point c){ //
    triangle
    ld D =
        2*(a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y));
    ld Ux = ((a.x*a.x + a.y*a.y)*(b.y-c.y)+(b.x*b.x +
        b.y*b.y)*(c.y-a.y)+(c.x*c.x +
        c.y*c.y)*(a.y-b.y))/D;
    ld Uy = ((a.x*a.x + a.y*a.y)*(c.x-b.x)+(b.x*b.x +
        b.y*b.y)*(a.x-c.x)+(c.x*c.x +
        c.y*c.y)*(b.x-a.x))/D;
    return {Ux, Uy};
}
// n sided polygon (n-gon) with side length a
struct Polygon {
    int n;
    ld a;
    Polygon(int _n, ld _a) { n = _n, a = _a; }
    ld Perimeter() { return n * a; }
    ld Exterior_Angle_Degrees() { return 360.0 / n; }
    ld Exterior_Angle_Radians() { return (2 * PI) / n; }
    ld Interior_Angle_Degrees() { return (n - 2) *
        180.0 / n; }
    ld Interior_Angle_Radians() { return PI - (2 * PI /
        n); }
    ld Circumradius() { return a / (2 * sin(PI / n)); }
    ld Inradius() { return a / (2 * tan(PI / n)); }
    ld Area() { return (n * a * a) / (4 * tan(PI / n));
    }
    ld Central_Angle_Degrees() { return 360.0 / n; }
    ld Central_Angle_Radians() { return (2 * PI) / n; }
    ld Diagonals_count() { return n * (n - 3) / 2; }
    ld Diagonal_length() { return a / sin(PI / n); }
    ld Height() {
        if (n & 1) return 2 * Inradius();
        else return Inradius() + Circumradius();
    }
    ld Width() {
        if (n & 1) {
            return 2 * Circumradius() * sin((n - 1) * PI /
                (2 * n));
        } else {
            if ((n / 2) & 1) return 2 * Circumradius();
            else return 2 * Inradius();
        }
    }
}

```

};

32 Gray Code

```
// Generate all 2^n n-bit strings so consecutive ones
// differ in exactly one bit.
int main() {
    int n; cin >> n;
    for (int i = 0; i < (1 << n); i++) {
        bitset<16> b(i ^ (i >> 1));
        for (int j = n - 1; j >= 0; j--) cout << b[j];
        cout << '\n';
    }
}
```

33 Hashing With Update

```
const int MAX = int(1e6) + 9;
vector<long long> MOD = {1909999999, 1999990999};
vector<array<long long, 2>> pw(MAX), ipw(MAX);
array<long long, 2> bs = {137, 277};
int BinExp(long long a, long long b, int mod) {
    a %= mod;
    int res = 1;
    while (b) {
        if (b & 1) res = (res * a) % mod;
        a = (a * a) % mod;
        b >>= 1;
    }
    return res;
}
void Preprocess() {
    pw[0][0] = pw[0][1] = 1;
    for (int i = 1; i < MAX; i++) {
        pw[i][0] = (pw[i - 1][0] * bs[0]) % MOD[0];
        pw[i][1] = (pw[i - 1][1] * bs[1]) % MOD[1];
    }
    ipw[0][0] = ipw[0][1] = 1;
    long long ip1 = BinExp(bs[0], MOD[0] - 2, MOD[0]);
    long long ip2 = BinExp(bs[1], MOD[1] - 2, MOD[1]);
    for (int i = 1; i < MAX; i++) {
        ipw[i][0] = (ipw[i - 1][0] * ip1) % MOD[0];
        ipw[i][1] = (ipw[i - 1][1] * ip2) % MOD[1];
    }
}
struct Hashing {
    int n;
    vector<array<long long, 2>> hs;
    Hashing(string& s) {
        if (pw[2][0] == 0) Preprocess();
        n = s.size();
        hs.resize(n + 1);
        for (int i = 0; i < n; i++) {
            hs[i + 1][0] = (hs[i][0] + (pw[i][0] * s[i])) %
                MOD[0];
            hs[i + 1][1] = (hs[i][1] + (pw[i][1] * s[i])) %
                MOD[1];
        }
    }
}
```

```
array<long long, 2> get_hash(int l, int r) { // 0
    // based query
    l++, r++; // 1 based hashing
    long long res1 = ((hs[r][0] - hs[l - 1][0]) +
        MOD[0]) % MOD[0];
    long long res2 = ((hs[r][1] - hs[l - 1][1]) +
        MOD[1]) % MOD[1];
    res1 = (res1 * ipw[l - 1][0]) % MOD[0];
    res2 = (res2 * ipw[l - 1][1]) % MOD[1];
    //return res1 << 31 | res2;
    return {res1, res2};
}
auto Hash_Merge(array<long long, 2> left, array<long
    long, 2> right, int left_sz) {
    for (int i = 0; i < 2; i++) {
        (right[i] *= pw[left_sz][i]) %= MOD[i];
        (left[i] += right[i]) %= MOD[i];
    }
    return left;
}
// # with update, find palindrome O(nlogn)
const int N = 1e6 + 9;
int power(long long n, long long k, const int mod) {
    int ans = 1 % mod;
    n %= mod;
    if (n < 0) n += mod;
    while (k) {
        if (k & 1) ans = (long long) ans * n % mod;
        n = (long long) n * n % mod;
        k >>= 1;
    }
    return ans;
}
using T = array<int, 2>;
const T MOD = {127657753, 987654319};
const T p = {137, 277};
T operator + (T a, int x) {return {(a[0] + x) %
    MOD[0], (a[1] + x) % MOD[1];}}
T operator - (T a, int x) {return {(a[0] - x +
    MOD[0]) % MOD[0], (a[1] - x + MOD[1]) % MOD[1];}}
T operator * (T a, int x) {return {(int)((long long)
    a[0] * x % MOD[0]), (int)((long long) a[1] * x %
    MOD[1]);}}
T operator + (T a, T x) {return {(a[0] + x[0]) %
    MOD[0], (a[1] + x[1]) % MOD[1];}}
T operator - (T a, T x) {return {(a[0] - x[0] +
    MOD[0]) % MOD[0], (a[1] - x[1] + MOD[1]) %
    MOD[1];}}
T operator * (T a, T x) {return {(int)((long long)
    a[0] * x[0] % MOD[0]), (int)((long long) a[1] *
    x[1] % MOD[1]);}}
ostream& operator << (ostream& os, T hash) {return os
    << "(" << hash[0] << ", " << hash[1] << ")";}
T pw[N], ipw[N];
void prec() {
    pw[0] = {1, 1};
    for (int i = 1; i < N; i++) {
```

```
        pw[i] = pw[i - 1] * p;
    }
    ipw[0] = {1, 1};
    T ip = {power(p[0], MOD[0] - 2, MOD[0]),
        power(p[1], MOD[1] - 2, MOD[1])};
    for (int i = 1; i < N; i++) {
        ipw[i] = ipw[i - 1] * ip;
    }
}
struct Hashing {
    int n;
    string s; // 1 - indexed
    vector<array<T, 2>> t; // (normal, rev) hash
    array<T, 2> merge(array<T, 2> l, array<T, 2> r) {
        l[0] = l[0] + r[0];
        l[1] = l[1] + r[1];
        return l;
    }
    void build(int node, int b, int e) {
        if (b == e) {
            t[node][0] = pw[b] * s[b];
            t[node][1] = pw[n - b + 1] * s[b];
            return;
        }
        int mid = (b + e) >> 1, l = node << 1, r = l + 1;
        build(l, b, mid);
        build(r, mid + 1, e);
        t[node] = merge(t[l], t[r]);
    }
    void upd(int node, int b, int e, int i, char x) {
        if (b > i || e < i) return;
        if (b == e && b == i) {
            t[node][0] = pw[b] * x;
            t[node][1] = pw[n - b + 1] * x;
            return;
        }
        int mid = (b + e) >> 1, l = node << 1, r = l + 1;
        upd(l, b, mid, i, x);
        upd(r, mid + 1, e, i, x);
        t[node] = merge(t[l], t[r]);
    }
    array<T, 2> query(int node, int b, int e, int i,
        int j) {
        if (b > j || e < i) return {T{0, 0}, T{0, 0}};
        if (b >= i && e <= j) return t[node];
        int mid = (b + e) >> 1, l = node << 1, r = l + 1;
        return merge(query(l, b, mid, i, j), query(r, mid
            + 1, e, i, j));
    }
    Hashing() {}
    Hashing(string _s) {
        n = _s.size();
        s = "." + _s;
        t.resize(4 * n + 1);
        build(1, 1, n);
    }
    void upd(int i, char c) {
        upd(1, 1, n, i, c);
        s[i] = c;
    }
}
```

```

T get_hash(int l, int r) { // 1 - indexed
    return query(1, 1, n, l, r)[0] * ipw[l - 1];
}
T rev_hash(int l, int r) { // 1 - indexed
    return query(1, 1, n, l, r)[1] * ipw[n - r];
}
T get_hash() return get_hash(1, n);
bool is_palindrome(int l, int r) return get_hash(l,
    → r) == rev_hash(l, r);
}

```

34 Hash Map

```

#include <ext/pb_ds/assoc_container.hpp>
struct splitmix64_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbfb58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            std::chrono::steady_clock::now().time_since_epoch()
            .count();
        return splitmix64(x + FIXED_RANDOM);
    }
};

template <typename K, typename V, typename Hash =
    splitmix64_hash>
using hash_map = __gnu_pbds::gp_hash_table<K, V,
    → Hash>;
template <typename K, typename Hash = splitmix64_hash>
using hash_set = hash_map<K, __gnu_pbds::null_type,
    → Hash>;

```

35 Hld

```

// weight in the edges
int t = 0, a[N];
int tin[N], depth[N], par[N], head[N], heavy[N],
    → sz[N], values[N];
vector<array<int, 2>> adj[N];
void dfs(int u, int p) {
    par[u] = p, sz[u] = 1;
    for (auto& [v, w] : adj[u]) {
        if (v != p) {
            depth[v] = depth[u] + 1;
            values[v] = w; // when weight in edges
            dfs(v, u);
            sz[u] += sz[v];
            if (heavy[u] == -1 || sz[heavy[u]] < sz[v]) {
                heavy[u] = v;
            }
        }
    }
}
void decompose(int u, int h) {
    head[u] = h;

```

```

tin[u] = ++t;
a[t] = values[u];
if (heavy[u] != -1) decompose(heavy[u], h);
for (auto& [v, w] : adj[u]) {
    if (v != par[u] && v != heavy[u]) {
        decompose(v, v);
    }
}
// exclude LCA, then eLca = 1
// Update and Query are operations of segmentTree
void UpdatePath(int a, int b, int val, int eLca = 0) {
    for (; head[a] != head[b]; b = par[head[b]]) {
        if (depth[head[a]] > depth[head[b]]) swap(a, b);
        Update(tin[head[b]], tin[b], val);
    }
    if (depth[a] > depth[b]) swap(a, b);
    if (a != b) Update(tin[a] + eLca, tin[b], val);
}
int QueryPath(int a, int b, int eLca = 0) {
    int res = 0;
    for (; head[a] != head[b]; b = par[head[b]]) {
        if (depth[head[a]] > depth[head[b]]) swap(a, b);
        res = (res + Query(tin[head[b]], tin[b])) % mod;
    }
    if (depth[a] > depth[b]) swap(a, b);
    if (a != b) res = (res + Query(tin[a] + eLca,
        → tin[b])) % mod;
    return res;
}
void BuildHLD() {
    t = 0;
    for (int i = 0; i <= n; i++) heavy[i] = -1;
    dfs(1, 1);
    decompose(1, 1);
    BuildSeg();
}

```

36 Hopcroft Karp

```

// O(√V * E)
// works for only directed graph, or on two graphs
// 1 to n is left graph, n + 1 to n + m is right graph
// make directed edges for two graph
// match pairs -> if (i < match[i]) (i <-> match[i])
const int N = 2e5 + 9, INF = 1.1e9;
vector<int> adj[N];
int n, m, match[N], dist[N];
bool bfs() {
    queue<int> q;
    for (int i = 1; i <= n; ++i) {
        if (!match[i]) dist[i] = 0, q.emplace(i);
        else dist[i] = INF;
    }
    dist[0] = INF;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        if (!u) continue;
        for (int v : adj[u]) {
            if (dist[match[v]] == INF) {

```

```

                dist[match[v]] = dist[u] + 1,
                q.emplace(match[v]);
            }
        }
    }
    if (dist[0] != INF) {
        return dist[0];
    }
    bool dfs (int u) {
        if (!u) return 1;
        for (int v : adj[u]) {
            if (dist[match[v]] == dist[u] + 1 and
                → dfs(match[v])) {
                match[u] = v, match[v] = u;
                return 1;
            }
        }
        dist[u] = INF;
        return 0;
    }
    int max_matching() {
        int ret = 0;
        while (bfs()) {
            for (int i = 1; i <= n; ++i)
                ret += !match[i] and dfs(i);
        }
        return ret;
    }
    void printPairs() {
        for (int i = 1; i <= n + m; ++i)
            if (match[i] && i < match[i])
                cout << i << " " << match[i] << "\n";
    }
}

```

37 Hungarian Min Assignment

```

/*
Hungarian Algorithm: max weight assignment (rows →
    → distinct columns)
Input: cost matrix a[i][j] (0-based)
Output: {max_sum, ans}, where ans[i] = column
    → assigned to row i
To get minimum assignment, negate the matrix values
*/
template<typename T>
pair<T, vector<int>> hungarian(const
    → vector<vector<T>> &a) {
    if (a.empty()) return {0, {}};
    int n = a.size() + 1, m = a[0].size() + 1;
    vector<int> p(m), ans(n - 1);
    vector<T> u(n), v(m);
    for (int i = 1; i < n; i++) {
        p[0] = i;
        int now = 0;
        vector<int> pre(m, -1), vis(m + 1);
        vector<T> dis(m, numeric_limits<T>::max());
        do {
            vis[now] = true;
            int t = p[now], nxt;
            T d = numeric_limits<T>::max();
            for (int j = 1; j < m; j++) {
                if (!vis[j]) {

```

```

T cur = -a[t - 1][j - 1] - u[t] - v[j];
if (cur < dis[j]) dis[j] = cur, pre[j] =
    now;
if (dis[j] < d) d = dis[j], nxt = j;
}
for (int j = 0; j < m; j++) {
    if (vis[j]) u[p[j]] += d, v[j] -= d;
    else dis[j] -= d;
}
now = nxt;
} while (p[now]);
while (now) {
    int t = pre[now];
    p[now] = p[t], now = t;
}
for (int i = 1; i < m; i++)
    if (p[i]) ans[p[i] - 1] = i - 1;
return {v[0], ans};
}

```

38 Kmp And Functions

```

// length of longest proper prefix of P[0...i] that is
// also a suffix of P[0...i]
// Pattern: a b a b a c a
// Index:   0 1 2 3 4 5 6
// LPS[]:   0 0 1 2 3 0 1
vector<int> get_pi(string& s) {
    int n = s.size();
    vector<int> pi(n);
    for (int i = 1, j = 0; i < n; i++) {
        if (s[i] == s[j]) pi[i] = ++j;
        else if (j == 0) pi[i] = 0;
        else j = pi[j - 1], i--;
    }
    return pi;
}
// count the number of p occurs in s
string s, p;
s = p + "#" + s;
vector<int> pi = get_pi(s);
int ans = 0;
for (auto& i : pi) ans += (i == p.size());

int KMPSearch(string& text, string& pattern) {
    int n = text.size(), m = pattern.size();
    auto lps = get_pi(pattern);
    int total = 0;
    for (int i = 0, j = 0; i < n; ) {
        if (pattern[j] == text[i]) j++, i++;
        if (j == m) {
            total++, j = lps[j - 1];
        } else if (i < n && pattern[j] != text[i]) {
            if (j != 0) j = lps[j - 1];
            else i = i + 1;
        }
    }
    return total;
}

```

```

const int N = 1e5 + 9;
int aut[N][26];
void compute_automaton(const string& s) {
    string t = s + '#';
    int n = t.size();
    auto pi = get_pi(t);
    for (int i = 0; i < n; i++) {
        for (int c = 0; c < 26; c++) {
            char ch = 'a' + c; // change if capital
            if (i > 0 && ch != t[i])
                aut[i][c] = aut[pi[i - 1]][c];
            else
                aut[i][c] = i + (ch == t[i]);
        }
    }
    /*
    substring containing at least once
    i → number of characters placed so far
    state → how many characters of pattern matched so far
    */
    int n, m, dp[1009][N][2];
    int f(int i = 0, int state = 0, int found = 0) {
        if (i == n) return found;
        auto& ret = dp[i][state][found];
        if (~ret) return ret;
        ret = 0;
        for (int c = 0; c < 26; c++) {
            int nState = aut[state][c];
            int nFound = found || nState == m;
            ret = (ret + f(i + 1, nState, nFound)) % mod;
        }
        return ret;
    }
    /*
    Border = prefix which is also suffix (≠ whole string)
    Example: "abcababcab" → ab, abcab
    */
    vector<int> borders(string& s) {
        auto pi = get_pi(s);
        int n = s.size(), i = pi[n - 1];
        vector<int> a;
        while (i > 0) {
            a.push_back(i);
            i = pi[i - 1];
        }
        reverse(a.begin(), a.end());
        return a;
    }
    /*
    Period = prefix that generates the string by
    → repetition
    (last repetition may be partial)
    Example: "abcabca" → abc, abcabc, abcabca
    */
    vector<int> periods(string& s) {
        auto pi = get_pi(s);
        int n = s.size(), i = pi[n - 1];
        vector<int> a;
        while (i > 0) {

```

```

            a.push_back(n - i);
            i = pi[i - 1];
        }
        a.push_back(n);
        return a;
    }

```

39 Largest Rectangle In Histogram

```

int64_t largestRectangleInHistogram(vector<int>& a) {
    int64_t n = a.size(), mx = 0;
    stack<int> st;
    for (int i = 0; i <= n; i++) {
        int cur = (i == n ? 0 : a[i]);
        while (!st.empty() && a[st.top()] >= cur) {
            int64_t h = a[st.top()];
            st.pop();
            int left = st.empty() ? -1 : st.top();
            mx = max(mx, h * (i - left - 1));
        }
        st.push(i);
    }
    return mx;
}

```

40 Linear Sieve

```

vector<int> lpf(N), phi(N), mu(N), primes;
void linear_sieve() {
    phi[1] = mu[1] = 1;
    for (int i = 2; i < N; i++) {
        if (lpf[i] == 0) {
            lpf[i] = i, phi[i] = i - 1, mu[i] = -1;
            primes.push_back(i);
        }
        for (int p : primes) {
            if (p > lpf[i] || i * p >= N) break;
            lpf[i * p] = p;
            if (i % p == 0) {
                phi[i * p] = phi[i] * p;
                mu[i * p] = 0;
                break;
            } else {
                phi[i * p] = phi[i] * (p - 1);
                mu[i * p] = -mu[i];
            }
        }
    }
}

```

41 Longest Path In Dag

```

vector<int> adj[N];
int dp[N], vis[N], n;
int dfs (int u) {
    vis[u] = dp[u] = 1;
    for (int v : adj[u]) {
        if (!vis[v]) dfs(v);
        dp[u] = max(dp[u], dp[v] + 1);
    }
    return dp[u];
}

```

```

}
int longestpath() {
    int ans = 0;
    for (int i = 1; i <= n; i++) {
        if (!vis[i]) ans = max(ans, dfs(i));
    }
    return ans;
}

```

42 Manacher

```

struct Manacher { // 0 based
    int n; vector<int> p;
    Manacher(string& s) {
        n = s.size(); p.resize(2 * n);
        for (int i = 0, j = 0, k; i < n * 2; i += k, j =
            → max(j - k, 0)) {
            while (i >= j && i + j + 1 < n * 2 && s[(i - j)
            → / 2] == s[(i + j + 1) / 2]) ++j;
            p[i] = j;
            for (k = 1; i >= k && j >= k && p[i - k] != j -
            → k; ++k) {
                p[i + k] = min(p[i - k], j - k);
            }
        }
        bool is_palindrome(int l, int r) {
            int len = (r - l + 1), idx = -1;
            if (len & 1) idx = (l + len / 2) * 2;
            else idx = (l + len / 2 - 1) * 2 + 1;
            return p[idx] >= len;
        }
        int odd_length_of_center_i(int i) { return p[i * 2]; }
        int even_length_of_center_i(int i) { return p[i * 2 + 1]; }
        vector<int> mxR, mxL;
        void longestPalindromeEndingAtEachPosition() {
            mxR.assign(n, 1);
            for (int i = 0; i < n; i++) {
                int l = p[i * 2];
                mxR[i + l / 2] = max(mxR[i + l / 2], 1);
                l = p[i * 2 + 1];
                mxR[i + l / 2] = max(mxR[i + l / 2], 1);
            }
            for (int i = n - 2; i >= 0; i--) {
                mxR[i] = max(mxR[i], mxR[i + 1] - 2);
            }
        }
        void longestPalindromeStartingAtEachPosition() {
            mxL.assign(n, 1);
            for (int i = n - 1; i >= 0; i--) {
                int l = p[i * 2];
                mxL[i - l / 2] = max(mxL[i - l / 2], 1);
                l = p[i * 2 + 1];
                int idx = min(n - 1, i - l / 2 + 1);
                mxL[idx] = max(mxL[idx], 1);
            }
            for (int i = 1; i < n; i++)
                mxL[i] = max(mxL[i], mxL[i - 1] - 2);
        }
    };
}

```

43 Matrix Expo

```

// 0 based
typedef vector<int> row;
typedef vector<row> matrix;
inline int add(const int &a, const int &b) {
    int c = a + b;
    if (c >= MOD) c -= MOD;
    return c;
}
inline int mult(const int &a, const int &b) {
    return (long long)a * b % MOD;
}
matrix operator*(const matrix &m1, const matrix &m2) {
    int r = m1.size(), m = m1.back().size(), c =
        → m2.back().size();
    matrix ret(r, row(c, 0));
    for (int i = 0; i < r; i++)
        for (int k = 0; k < m; k++)
            for (int j = 0; j < c; j++)
                ret[i][j] = add(ret[i][j], mult(m1[i][k],
                → m2[k][j]));
    return ret;
}
matrix one(int dim) {
    matrix ret(dim, row(dim, 0));
    for (int i = 0; i < dim; i++)
        ret[i][i] = 1;
    return ret;
}
matrix operator^(const matrix &m, const int &e) {
    if (e == 0) return one(m.size());
    matrix sqrtm = m ^ (e / 2);
    matrix ret = sqrtm * sqrtm;
    if (e & 1) ret = ret * m;
    return ret;
}
// adj^k = number of walks of length k between nodes
int n, m, k; cin >> n >> m >> k; // nodes, edges,
→ steps
matrix adj(n, row(n, 0));
for (int i = 0; i < m; i++) {
    int u, v; cin >> u >> v; u--; v--;
    adj[u][v] = add(adj[u][v], 1);
}
matrix ans = adj ^ k; // number of walks of length k
// print matrix of walks
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++)
        cout << ans[i][j] << " ";
    cout << "\n";
}

```

44 Max Element Index In Range Static

```

int n, a[N], st[N][LOG], lg[N]; // LOG = 20
void Preprocess() {
    for (int i = 2; i < N; ++i) lg[i] = lg[i / 2] + 1;
}
// max element index in (l to r)

```

```

void build() {
    if (lg[2] == 0) Preprocess();
    for (int j = 0; j < LOG; j++) {
        for (int i = 0; i + (1 << j) - 1 <= n; i++) {
            if (j == 0) st[i][j] = i;
            else {
                if (a[st[i][j - 1]] > a[st[i + (1 << (j - 1))][j - 1]]) st[i][j] = st[i][j - 1];
                else st[i][j] = st[i + (1 << (j - 1))][j - 1];
            }
        }
    }
}
int query(int l, int r) {
    if (l > r) return -1;
    int k = lg[r - l + 1];
    if (a[st[l][k]] > a[st[r - (1 << k) + 1][k]])
        → return st[l][k];
    return st[r - (1 << k) + 1][k];
}

```

45 Merge Sort Tree

```

// add ordered multiset
struct MergeSortTree {
    int size = 1;
    vector<ordered_multiset<int>> st; #change
    MergeSortTree(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(1, 1, size, a);
    }
    void Initial(int _n) {
        size = _n;
        int tree_size = 1;
        while (tree_size < _n) tree_size *= 2;
        st.resize(tree_size * 2);
    }
    void Build(int u, int s, int e, vector<int>& a) {
        if (s == e) { #change
            st[u].insert(a[s]);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
        Build(v, s, m, a);
        Build(w, m + 1, e, a);
        for (int i = s; i <= e; i++) st[u].insert(a[i]);
    }
    void Update(int u, int s, int e, int k, int prev,
    → int curr) {
        if (s == e) { #change
            st[u].erase(st[u].find_by_order(st[u].order_of_-
            → key(prev)));
            st[u].insert(curr);
            return;
        }
        int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;

```

```

    if (k <= m) Update(v, s, m, k, prev, curr);
    else Update(w, m + 1, e, k, prev, curr);
    #change
    st[u].erase(st[u].find_by_order(st[u].order_of_key
        ↪ y(prev)));
    st[u].insert(curr);
}

void Update(int k, int prev, int curr) {
    Update(1, 1, size, k, prev, curr);
}

int Query(int u, int s, int e, int l, int r, int
    ↪ val) {
    if (e < l || r < s) { #change
        return 0;
    }
    if (l <= s && e <= r) { #change
        return st[u].order_of_key(val);
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    int lsum = Query(v, s, m, l, r, val);
    int rsum = Query(w, m + 1, e, l, r, val);
    return lsum + rsum; #change
}

int Query(int l, int r, int val) {
    return Query(1, 1, size, l, r, val);
}
};

46 Mex With Trie

```

```

const int N = 2e5 * 22 + 9;
int nxt[N][2], cnt[N], intCntr[N], node = 2;
void insert(int x, int u = 1) {
    for (int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        if (!nxt[u][bit]) nxt[u][bit] = node++;
        u = nxt[u][bit];
        cnt[u]++;
    } intCntr[u]++;
}

int find(int x, int u = 1) {
    for (int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        if (!nxt[u][bit]) return 0;
        u = nxt[u][bit];
    } return intCntr[u];
}

void erase(int x, int u = 1) {
    if (find(x) == 0) return;
    for (int i = 20; i >= 0; i--) {
        int bit = (x >> i) & 1;
        int v = nxt[u][bit];
        cnt[v]--;
        u = v;
    } intCntr[u]--;
}

int mex() {
    int u = 1, ret = 0;
    for (int i = 20; i >= 0; i--) {
        if (u == 0 || !nxt[u][0]) return ret;

```

```

        if (cnt[nxt[u][0]] >= (1 << i)) {
            u = nxt[u][1];
            ret |= (1 << i);
        } else {
            u = nxt[u][0];
        }
    } return ret;
}

// only insert the distinct element for mex after xor
int mexAfterXor(int num) {
    int u = 1, ret = 0;
    for (int i = 20; i >= 0; i--) {
        int bit = (num >> i) & 1;
        if (u == 0 || !nxt[u][bit]) return ret;
        if (cnt[nxt[u][bit]] >= (1 << i)) {
            u = nxt[u][bit ^ 1];
            ret |= (1 << i);
        } else {
            u = nxt[u][bit];
        }
    } return ret;
}

```

47 Minimum Expression

```

// lexicographically smallest rotation
int minimumExpression(string s) {
    s = s + s;
    int i = 0, j = 1, k = 0, len = s.size();
    while (i + k < len && j + k < len) {
        if (s[i + k] == s[j + k]) k++;
        else if (s[i + k] < s[j + k]) { j = max(j + k + 1,
            ↪ i + 1); k = 0; }
        else { i = max(i + k + 1, j + 1); k = 0; }
    } return min(i, j);
}

```

48 Next Perv Permutation

```

void next_permutation(vector<int>& a) {
    int n = a.size(), i = n - 2;
    while (i >= 0 && a[i] >= a[i + 1]) i--;
    if (i < 0) {
        reverse(a.begin(), a.end());
        return;
    }
    int j = n - 1;
    while (a[j] <= a[i]) j--;
    swap(a[i], a[j]);
    reverse(a.begin() + i + 1, a.end());
}

void prev_permutation(vector<int>& a) {
    int n = a.size(), i = n - 2;
    while (i >= 0 && a[i] <= a[i + 1]) i--;
    if (i < 0) {
        reverse(a.begin(), a.end());
        return;
    }
    int j = n - 1;
    while (a[j] >= a[i]) j--;

```

```

    swap(a[i], a[j]);
    reverse(a.begin() + i + 1, a.end());
}

```

49 Number Theory

```

using ll = ll;
const int N = 1e6 + 9;
vector<int> lpf(N), gpf(N);
vector<array<int, 2>> factors[N];
// sieve for finding lowest prime and highest prime
↪ upto N
for (int i = 2; i < N; i++) {
    if (lpf[i] == 0) {
        for (int j = i; j < N; j += i) {
            gpf[j] = i;
            if (!lpf[j]) lpf[j] = i;
        }
    }
}

// find all factors upto N
for (int i = 2; i < N; i++) {
    int num = i;
    while (num > 1) {
        int p = lpf[num], cnt = 0;
        while (num > 1 && num % p == 0) {
            cnt++;
            num /= p;
        }
        factors[i].push_back({p, cnt});
    }
}

int num = 10;
int total_divisors = 1;
ll sum_of_divisors = 1;
for (auto& [p, c] : factors[num]) {
    total_divisors *= (c + 1);
    sum_of_divisors *= (pow(p, c + 1) - 1) / (p - 1);
}

// phi of single integer
int n = 10;
ll num = n;
ll phi_of_n = n;
for (ll i = 2; i * i <= num; i++) {
    if (num % i == 0) {
        while (num % i == 0) num /= i;
        phi_of_n -= phi_of_n / i;
    }
}
if (num > 1) phi_of_n -= phi_of_n / num;

// phi upto N
vector<int> phi(N);
// initial 0 to N
iota(phi.begin(), phi.end(), 0);
for (int i = 2; i < N; i++) {
    if (phi[i] == i) {
        for (int j = i; j < N; j += i) {
            phi[j] -= phi[j] / i;
        }
    }
}

```

```

    }
}

// gcd sum ->  $\sum \gcd(i, n)$  for  $1 \leq i \leq n$ ; ( $n \leq 1e9$ )
//  $\gcd(1, n) + \gcd(2, n) + \dots + \gcd(n, n)$ 
ll sum = 0;
for (int i = 1; 1LL * i * i <= n; i++) {
    if (n % i == 0) {
        sum += i * phi(n / i);
        if (n / i != i) sum += (n / i) * phi(n / (n / i));
    }
}
// all pair gcd sum from 1 to N ( $N \leq 4e6$ )
//  $\sum_{i=1}^{N-1} \sum_{j=i+1}^N [\gcd(i, j)]$ 
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) sum[j] += i * phi[j
        / i];
}
for (int i = 1; i < N; i++) sum[i] += sum[i - 1] - i;
// lcm sum ->  $\sum \text{lcm}(i, n)$  for  $1 \leq i \leq n$ ; ( $n \leq 1e6$ )
//  $\text{lcm}(1, n) + \text{lcm}(2, n) + \dots + \text{lcm}(n, n)$ 
phi[1] = 2; // phi[1] should be 2 for this algorithm
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) lcm_sum[j] += 1LL *
        j * phi[i] * i / 2;
}
// all pair lcm sum from 1 to N ( $N \leq 1e6$ )
//  $\sum_{i=1}^{N-1} \sum_{j=i+1}^N [\text{lcm}(i, j)]$ 
phi[1] = 2; // phi[1] should be 2 for this algorithm
for (int i = 1; i < N; i++) {
    for (int j = i; j < N; j += i) lcm_sum[j] += (ll) j
        * (1LL * i * phi[i] / 2);
}
for (int i = 1; i < N; i++) lcm_sum[i] += lcm_sum[i -
    1] - i;

```

50 Offline Range Mex Query

```

struct SegmentTree {
    int n; vector<int> st;
    SegmentTree(int sz) {
        n = 1;
        while (n < sz) n *= 2;
        st.assign(n * 2, 0);
    }
    void update(int idx, int val) {
        st[idx += n] = val;
        for (idx /= 2; idx; idx /= 2)
            st[idx] = min(st[idx << 1], st[idx << 1 | 1]);
    }
    int mex(int l) {
        int u = 1;
        while (u < n) {
            int lc = u << 1;
            if (st[lc] < 1) u = lc;
            else u = lc + 1;
        }
        return u - n;
    }
};

```

```

// 1 based array
// update last occurence of each value with index of
// array
// find the lowest segmentree index which is less than
// current range "L"
const int N = 2e5 + 9;
vector<array<int, 2>> queries[N];
int n, a[N], res[N];
void getMex() {
    SegmentTree sg(N);
    for (int i = 1; i <= n; i++) {
        sg.update(a[i], i);
        for (auto& [l, idx] : queries[i]) res[idx] =
            sg.mex(l);
    }
}

```

51 Ordered Set

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <class T> using ordered_set = tree<T,
    null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T> using ordered_multiset = tree<T,
    null_type, less_equal<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T, class R> using ordered_map =
    tree<T, R, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
// Sorting Descending (or Equal)
template <class T> using ordered_set = tree<T,
    null_type, greater<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T> using ordered_multiset = tree<T,
    null_type, greater_equal<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
template <class T, class R> using ordered_map =
    tree<T, R, greater<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
// Fucntions
st.order_of_key(k); // count of elements smaller than
    k. - O(log n)
st.find_by_order(k); // Returns the iterator for the
    kth element (0 based index). - O(log n)
st.size() - st.order_of_key(k + 1); // count of
    elements greater than k. - O(log n)
st.order_of_key(r + 1) - st.order_of_key(l); // count
    of elements between l to r
st.erase(st.find_by_order(st.order_of_key(k))); // 
    erase in multiset

```

52 Rope

```

/*
 * Problem: Given an array of length n, you will be
 * given q queries

```

Each query will contain two indexes L and R ($L \geq R$)
 You have to move the segment [L, R] to the beginning of the array
 * All the indices are 0 based

```

*/
#include <bits/stdc++.h>
using namespace std;
#include <ext/rope>
using namespace __gnu_cxx;
rope<int> R; // use as usual STL container
int main() {
    int n, q;
    cin >> n >> q;
    for (int i = 0; i < n; i++) {
        int a;
        cin >> a;
        R.push_back(a);
    }
    int l, r;
    for (int i = 0; i < q; ++i) {
        cin >> l >> r;
        l--;
        rope<int> cur = R.substr(l, r - l + 1);
        R.erase(l, r - l + 1);
        R.insert(0, cur);
    }
    for (auto it = R.mutable_begin(); it != R.mutable_end(); ++it) cout << *it << " ";
    cout << "\n";
    return 0;
}
/*
* Initialization: rope<int> R(n, 0);
* R.push_back(x) O(log N).
* R.pop_back() O(log N).
* R.insert(pos, nr) inserts rope nr into R at
    position pos (the first element of nr will be in
    position pos).
    Time Complexity: For Best Case: O(log N) and For
        Worst Case: O(N).
* R.erase(pos, cnt) deletes segment [pos, pos + cnt)
    from R.
    Time Complexity: O(log N).
* R.substr(pos, cnt) = segment[pos, pos + cnt].
    Time Complexity: O(log N).
* R.replace(pos, cnt, nr) replaces the segment [pos,
    pos + cnt) with the rope nr.
    Time Complexity: O(log N).
* R1 + R2: concatenate two ropes using the '+',
    symbol.
    Time Complexity: O(1).
* R.size(): Returns the length of the rope R.
* R.mutable_begin(): Returns an iterator pointing to
    the beginning of the rope R.
* R.mutable_end(): Returns an iterator pointing to
    the end of the rope R.
* R.mutable_reference_at(pos): Mutable reference
    pointing at pos

```

*/

53 Scc

```
// clear everything first, 1 based
// reverse scc for topological order
const int N = 5e5 + 10;
vector<int> adj[N], trans[N], scc[N];
int col[N], vis[N], idx = 0, n, m;
stack<int> st;
void dfs(int u) {
    vis[u] = 1;
    for (int v : adj[u]) if (!vis[v]) dfs(v);
    st.push(u);
}
void dfs2(int u) {
    col[u] = idx;
    scc[idx].push_back(u);
    for (int v : trans[u]) if (!col[v]) dfs2(v);
}
void findSCC() {
    for (int i = 1; i <= n; i++)
        if(!vis[i]) dfs(i);
    for (int u = 1; u <= n; u++)
        for (int v : adj[u])
            trans[v].push_back(u);
    while (!st.empty()) {
        int u = st.top(); st.pop();
        if (col[u]) continue;
        idx++; dfs2(u);
    }
}
// take input and call findSCC();
```

54 Segment Tree

```
struct node { #change
    long long sum, pref, suff, ans;
    node() {
        sum = pref = suff = ans = 0;
    }
};
struct SegmentTree {
    int size = 1;
    vector<node> st;
    SegmentTree(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(1, 0, size, a);
    }
    void Initial(int _n) {
        size = _n;
        int tree_size = 1;
        while (tree_size <= size) tree_size *= 2;
        st.resize(tree_size * 2);
    }
    node Make_node(int val) { #change
        node res;
        res.sum = val;
        res.pref = res.suff = res.ans = max(0, val);
        return res;
    }
```

```
}
```

```
node Merge(node& l, node& r) { #change
    node res;
    res.sum = l.sum + r.sum;
    res.pref = max(l.pref, l.sum + r.pref);
    res.suff = max(r.suff, r.sum + l.suff);
    res.ans = max(max(l.ans, r.ans), l.suff + r.pref);
    return res;
}
void Build(int u, int s, int e, vector<int>& a) {
    if (s == e) {
        st[u] = Make_node(a[s]);
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    Build(v, s, m, a);
    Build(w, m + 1, e, a);
    st[u] = Merge(st[v], st[w]);
}
void Update(int u, int s, int e, int k, long long
    val) {
    if (s == e) { #change
        st[u] = Make_node(val);
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    if (k <= m) Update(v, s, m, k, val);
    else Update(w, m + 1, e, k, val);
    st[u] = Merge(st[v], st[w]);
}
void Update(int k, long long val) {
    Update(1, 0, size, k, val);
}
node Query(int u, int s, int e, int l, int r) {
    if (e < l || r < s) { #change
        return node();
    }
    if (l <= s && e <= r) return st[u];
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    node lsum = Query(v, s, m, l, r);
    node rsum = Query(w, m + 1, e, l, r);
    return Merge(lsum, rsum);
}
node Query(int l, int r) {
    return Query(1, 0, size, l, r);
}
```

55 Segment Tree Iterative Pointupdate Rangequery

```
template <class T> struct SegmentTreeIterative {
    int n = 1;
    vector<T> st;
    SegmentTreeIterative(vector<int>& a) {
        Initial((int)a.size() - 1);
        Build(a);
    }
    void Initial(int _n) {
        n = _n;
```

```
int tree_size = 1;
while (tree_size <= n) tree_size *= 2;
st.resize(tree_size * 2);
}
T neutral = INT_MAX; #change
T Merge(T& a, T& b) { #change
    return min(a, b);
}
void Build(vector<int>& a) {
    for (int i = 1; i <= n; ++i)
        st[n + i] = a[i];
    for (int u = n - 1; u > 0; --u)
        st[u] = Merge(st[u < 1], st[u < 1 | 1]);
}
void Update(int idx, T val) {
    st[idx += n] = val;
    for (idx /= 2; idx >= 1; idx /= 2)
        st[idx] = Merge(st[idx < 1], st[idx < 1 | 1]);
}
T Query(int l, int r) {
    T res = neutral;
    for (l += n, r += n + 1; l < r; l >= 1, r >= 1)
        if (l & 1) res = Merge(res, st[l++]);
        if (r & 1) res = Merge(res, st[-r]);
    return res;
};
```

56 Segment Tree Lazy

```
int64_t sum[4 * N], lz[4 * N];
void Apply(int u, int v) {
    if (lz[v] != INF) lz[v] = (lz[v] * lz[u]) % mod;
    else lz[v] = lz[u];
}
void Push(int u, int l, int r) {
    if (lz[u] == INF) return;
    if (l != r) {
        Apply(u, 2 * u);
        Apply(u, 2 * u + 1);
    }
    sum[u] = (sum[u] * lz[u]) % mod;
    lz[u] = INF;
}
void Merge(int u, int v, int w) {
    sum[u] = (sum[v] + sum[w]) % mod;
}
void Build(int u = 1, int s = 0, int e = n) {
    if (s == e) {
        sum[u] = a[s]; // change
        lz[u] = INF;
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    Build(v, s, m);
    Build(w, m + 1, e);
    Merge(u, v, w);
}
```

```

void Update(int l, int r, int64_t val, int u = 1, int
→ s = 0, int e = n) {
    Push(u, s, e);
    if (e < l || r < s) return;
    if (l <= s && e <= r) { // change
        if (lz[u] != INF) lz[u] = (lz[u] * val) % mod;
        else lz[u] = val;
        Push(u, s, e);
        return;
    }
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    Update(l, r, val, v, s, m);
    Update(l, r, val, w, m + 1, e);
    Merge(u, v, w);
}
int64_t Query(int l, int r, int u = 1, int s = 0, int
→ e = n) {
    Push(u, s, e);
    if (e < l || r < s) return 0;
    if (l <= s && e <= r) return sum[u]; // change
    int v = 2 * u, w = 2 * u + 1, m = (s + e) / 2;
    int64_t lSum = Query(l, r, v, s, m);
    int64_t rSum = Query(l, r, w, m + 1, e);
    return (lSum + rSum) % mod; // change
}
void BuildSeg() {
    for (int i = 0; i <= 4 * n; i++) {
        sum[i] = 0;
        lz[i] = INF;
    }
    Build();
}
int Idx_query(int l, int r, int u, int s, int e) {
    Push(u, s, e);
    if (e < l || r < s) return -1;
    if (s == e) return st[u].mn == 0 ? s : -1;
    int v = u << 1, w = v | 1, m = s + e >> 1;
    int lq = Idx_query(l, r, v, s, m);
    if (lq == -1) return Idx_query(l, r, w, m + 1, e);
    return lq;
}

```

57 Sorting Methods

```

// choose two adjacent elements and swap them /
→ inversions count
vector<int> a;
int64_t mergeSort(int l, int r) {
    if (l >= r) return 0;
    int m = (l + r) / 2;
    int64_t ret = mergeSort(l, m) + mergeSort(m + 1, r);
    int i = l, j = m + 1;
    while (i <= m || j <= r) {
        if (j > r || (i <= m and a[i] < a[j])) i++;
        else j++, ret += m - i + 1;
    }
    inplace_merge(a.begin() + l, a.begin() + m + 1,
    → a.begin() + r + 1);
    return ret;
}
int invCnt = mergeSort(0, n - 1);

```

```

// choose any element and move it to another position:
→ n - LIS.
int lis(vector<int> p) {
    int n = p.size();
    vector<int> sorted;
    for (int i = 0; i < n; ++i) {
        auto it = lower_bound(sorted.begin(),
        → sorted.end(), p[i]);
        if (it == sorted.end()) sorted.push_back(p[i]);
        else *it = p[i];
    }
    return sorted.size();
}
// choose any two elements and swap them: n -
→ number_of_cycles.
int cyclesInPermutation(vector<int>& p) {
    int n = p.size(), cnt = 0;
    vector<bool> vis(n + 1);
    for (int i = 0; i < n; ++i) {
        if (vis[i]) continue;
        int j = i, cnt++;
        while (!vis[j]) {
            vis[j] = 1, j = p[j];
        }
    }
    return cnt;
}
// choose any element and move it to the front of the
→ array: n - suffix_length
int longestSortedSuffix(vector<int>& p) {
    int n = p.size(), cnt = 0, curr = n - 1;
    for (int i = n - 1; i >= 0; i--) {
        if (p[i] == curr) curr--, cnt++;
    }
    return cnt;
}

```

58 Sos Dp

```

const int mod = 1e9 + 7;
const int B = 20, N = (1 << B) + 9;
int f[N], g[N], pairF[N], pairG[N], subseqF[N],
→ subseqG[N], Pow2[N];
void sub(int& a, int& b) { // a = a - b
    a -= b;
    if (a < 0) a += mod;
}
int nC2(int n) {
    return (n * 1LL * (n - 1) / 2) % mod;
}
void forward1() { // sum over subset
    for (int bit = 0; bit < B; bit++) {
        for (int i = 0; i < N; i++) {
            if (i & (1 << bit)) f[i] += f[i ^ (1 << bit)];
        }
    }
}
void backward1() { // exclude subset sum
    for (int bit = 0; bit < B; bit++) {
        for (int i = N - 1; i >= 0; i--) {
            if (i & (1 << bit)) {
                // f[i] -= f[i ^ (1 << bit)];
                sub(pairF[i], pairF[i ^ (1 << bit)]);
            }
        }
    }
}

```

```

sub(subseqF[i], subseqF[i ^ (1 << bit)]);
}
}
void forward2() { // sum over superset
    for (int bit = 0; bit < B; bit++) {
        for (int i = N - 1; i >= 0; i--) {
            if (i & (1 << bit)) g[i ^ (1 << bit)] += g[i];
        }
    }
}
void backward2() { // exclude superset sum
    for (int bit = 0; bit < B; bit++) {
        for (int i = 0; i < N; i++) {
            if (i & (1 << bit)) {
                // g[i ^ (1 << bit)] -= g[i];
                sub(pairG[i ^ (1 << bit)], pairG[i]);
                sub(subseqG[i ^ (1 << bit)], subseqG[i]);
            }
        }
    }
}
void sosDP(vector<int>& a) {
    Pow2[0] = 1;
    for (int i = 1; i < N; i++) Pow2[i] = (Pow2[i - 1]
    → * 2) % mod;
    for (auto& ai : a) f[ai]++, g[ai]++;
    forward1(); forward2();
    for (int i = 0; i < N; i++) {
        // all pair (i < j)
        pairF[i] = nC2(f[i]), pairG[i] = nC2(g[i]);
        // subsequence
        subseqF[i] = Pow2[f[i]] - 1, subseqG[i] =
        → Pow2[g[i]] - 1;
    }
    backward1(); backward2();
}
// x | y = x
int subMaskOf(int x) return f[x];
// x & y = x
int superMaskOf(int x) return g[x];
// y & z = x (i < j)
int countPairsWithAnd(int x) return pairG[x];
// y | z = x (i < j)
int countPairsWithOr(int x) return pairF[x];
int countSubseqWithAnd(int x) return subseqG[x];
int countSubseqWithOr(int x) return subseqF[x];
sosDP(a); // clear everything before use

```

59 Sparse Table Rmq

```

const int N = (int)2e5 + 9;
int lg[N];
void Preprocess() {
    for (int i = 2; i < N; ++i) lg[i] = lg[i / 2] + 1;
}

```

```

}
template <class T> struct RMQ {
    int n = 1, LOG = 1;
    vector<vector<T>> st;
    T Merge(T& a, T& b) {
        return min(a, b); #change
    }
    RMQ(vector<T>& a) {
        if (lg[2] == 0) Preprocess();
        n = (int)a.size(), LOG = _lg(n) + 1;
        st.assign(n, vector<T> (LOG));
        for (int j = 0; j < LOG; j++) {
            for (int i = 0; i + (1 << j) - 1 < n; i++) {
                if (j == 0) st[i][j] = a[i];
                else st[i][j] = Merge(st[i][j - 1], st[i + (1 << (j - 1))][j - 1]);
            }
        }
    }
    T Query(int l, int r) {
        // if (l > r) return 0;
        int k = lg[r - l + 1];
        return Merge(st[l][k], st[r - (1 << k) + 1][k]);
    }
};

```

60 Stress Testing

```

// rename file -> testing.sh
set -e
g++ -std=c++17 gen.cpp -o gen
g++ -std=c++17 main.cpp -o main
g++ -std=c++17 brute.cpp -o brute
for((i = 1; ; ++i)); do
    echo $i
    ./gen $i > in
    ./main < in > out
    ./brute < in > out2
    diff -w out out2 || break
done

```

61 String Stream

```

string s;
getline(cin, s);
stringstream custom_in(s);
string word;
int count_word = 0;
while (custom_in >> word) {
    count_word++;
}

```

62 Sublime Build

```

// check the gcc version and replace
// name the file -> cp.sublime-build
{ // ubuntu
    "cmd" : ["g++ -std=c++14 $file_name -o
        $file_base_name && timeout 4s
        ./$file_base_name<input.txt>output.txt"],

    "selector" : "source.c",
    "shell": true,
    "working_dir" : "$file_path"
}

// windows
"cmd": ["g++.exe", "-std=c++14", "${file}", "-o",
    "${file_base_name}.exe", "&&",
    "${file_base_name}.exe<input.txt>output.txt"],
"selector": "source.cpp",
"shell": true,
"working_dir": "$file_path"
}

```

```

63 Suffix Array
/*
for integer, just change string to vector<int> and
minimum value of vector must be >= 1
for integer, lim will be the maximum value of the
array
LCP of suffix (sa[i], sa[i + 1]) = lcp[i]
0(nlogn)
*/
array<vector<int>, 2> get_sa(string& s, int lim =
    128) {
    int n = s.size() + 1, k = 0, a, b;
    vector<int> x(begin(s), end(s) + 1), y(n), sa(n),
    lcp(n), ws(max(n, lim)), rank(n);
    x.back() = 0;
    iota(begin(sa), end(sa), 0);
    for (int j = 0, p = 0; p < n; j = max(1, j * 2),
    lim = p) {
        p = j, iota(begin(y), end(y), n - j);
        for (int i = 0; i < n; ++i) if (sa[i] >= j)
            y[p++] = sa[i] - j;
        fill(begin(ws), end(ws), 0);
        for (int i = 0; i < n; ++i) ws[x[i]]++;
        for (int i = 1; i < lim; ++i) ws[i] += ws[i - 1];
        for (int i = n; i--;) sa[-ws[x[y[i]]]] = y[i];
        swap(x, y), p = 1, x[sa[0]] = 0;
        for (int i = 1; i < n; ++i) a = sa[i - 1], b =
            sa[i],
            x[b] = (y[a] == y[b] && y[a + j] == y[b + j]) ?
                p - 1 : p++;
    }
    for (int i = 1; i < n; ++i) rank[sa[i]] = i;
    for (int i = 0, j; i < n - 1; lcp[rank[i + 1]] = k)
        for (k && k--, j = sa[rank[i] - 1]; s[i + k] ==
            s[j + k]; k++);
    sa.erase(sa.begin()), lcp.erase(lcp.begin());
    lcp.push_back(lcp[0]), lcp.erase(lcp.begin());
    return {sa, lcp};
}

/*
0(|S| + |alphabet|) Suffix Array
LIM := max{s[i]} + 2
LCP of suffix (sa[i], sa[i + 1]) = lcp[i]
*/

```

```

void inducedSort(const vector<int>& vec, int
    val_range, vector<int>& SA, const vector<int>&
    sl, const vector<int>& lms_idx) {
    vector<int> l(val_range, 0), r(val_range, 0);
    for (int c : vec) {
        ++r[c];
        if (c + 1 < val_range) ++l[c + 1];
    }
    partial_sum(l.begin(), l.end(), l.begin());
    partial_sum(r.begin(), r.end(), r.begin());
    fill(SA.begin(), SA.end(), -1);
    for (int i = lms_idx.size() - 1; i >= 0; --i)
        SA[--r[vec[lms_idx[i]]]] = lms_idx[i];
    for (int i : SA) if (i > 0 and sl[i - 1])
        SA[l[vec[i - 1]]] = i - 1;
    fill(r.begin(), r.end(), 0);
    for (int c : vec) ++r[c];
    partial_sum(r.begin(), r.end(), r.begin());
    for (int k = SA.size() - 1, i = SA[k]; k; --k, i =
        SA[k]) {
        if (i and !sl[i - 1]) SA[--r[vec[i - 1]]] = i - 1;
    }
}
vector<int> suffixArray(const vector<int>& vec, int
    val_range) {
    const int n = vec.size();
    vector<int> sl(n), SA(n), lms_idx;
    for (int i = n - 2; i >= 0; --i) {
        sl[i] = vec[i] > vec[i + 1] or (vec[i] == vec[i +
            1] and sl[i + 1]);
        if (sl[i] and !sl[i + 1]) lms_idx.emplace_back(i
            + 1);
    }
    reverse(lms_idx.begin(), lms_idx.end());
    inducedSort(vec, val_range, SA, sl, lms_idx);
    vector<int> new_lms_idx(lms_idx.size()),
    lms_vec(lms_idx.size());
    for (int i = 0, k = 0; i < n; ++i) {
        if (SA[i] > 0 and !sl[SA[i]] and sl[SA[i] - 1])
            new_lms_idx[k++] = SA[i];
    }
    int cur = 0; SA[n - 1] = 0;
    for (int k = 1; k < new_lms_idx.size(); ++k) {
        int i = new_lms_idx[k - 1], j = new_lms_idx[k];
        if (vec[i] ^ vec[j]) {
            SA[j] = ++cur; continue;
        }
        bool flag = 0;
        for (int a = i + 1, b = j + 1; ; ++a, ++b) {
            if (vec[a] ^ vec[b]) {
                flag = 1; break;
            }
            if ((!sl[a] and sl[a - 1]) or (!sl[b] and sl[b -
                1])) {
                flag = (!sl[a] and sl[a - 1] and !sl[b] and
                    sl[b - 1]); break;
            }
        }
    }
}

```

```

    }
    SA[j] = flag ? ++cur : cur;
}
for (int i = 0; i < lms_idx.size(); ++i) lms_vec[i]
→ = SA[lms_idx[i]];
if (cur + 1 < lms_idx.size()) {
    auto lms_SA = suffixArray(lms_vec, cur + 1);
    for (int i = 0; i < lms_idx.size(); ++i)
        new_lms_idx[i] = lms_idx[lms_SA[i]];
}
inducedSort(vec, val_range, SA, sl, new_lms_idx);
→ return SA;
}
vector<int> getSuffixArray(const string& s, const int
→ LIM = 128) { // change limit for integer array,
→ (integer > 0)
    vector<int> vec(s.size() + 1);
    copy(begin(s), end(s), begin(vec)); vec.back() =
→ '!';
    auto ret = suffixArray(vec, LIM);
    ret.erase(ret.begin()); return ret;
}
// build RMQ on it to get LCP of any two suffix
vector<int> getLCPArray(const string& s, const
→ vector<int>& SA) {
    int n = s.size(), k = 0;
    vector<int> lcp(n), rank(n);
    for (int i = 0; i < n; ++i) rank[SA[i]] = i;
    for (int i = 0; i < n; ++i, k ? --k : 0) {
        if (rank[i] == n - 1) {
            k = 0; continue;
        }
        int j = SA[rank[i] + 1];
        while (i + k < n and j + k < n and s[i + k] ==
→ s[j + k]) ++k;
        lcp[rank[i]] = k;
    }
    lcp[n - 1] = 0; return lcp;
}
int lower_bound(string& s, string& t, vector<int>&
→ sa) {
    int n = s.size(), m = t.size(), lo = 0, hi = n - 1;
    while (lo <= hi) {
        int mid = (lo + hi) / 2;
        if (s.substr(sa[mid], m) < t) lo = mid + 1;
        else hi = mid - 1;
    }
    return lo;
}
int upper_bound(string& s, string& t, vector<int>&
→ sa) {
    int n = s.size(), m = t.size(), lo = 0, hi = n - 1;
    while (lo <= hi) {
        int mid = (lo + hi) / 2;
        if (s.substr(sa[mid], m) <= t) lo = mid + 1;
        else hi = mid - 1;
    }
    return lo;
}

```

```

int find_occurrence(string& s, string& t,
→ vector<int>& sa) {
    return upper_bound(s, t, sa) - lower_bound(s, t,
→ sa);
}
const int N = 1e6 + 9;
int64_t distPref[N];
void kthSubstringDistinctPreprocess(vector<int>& sa,
→ vector<int>& lcp) {
    int last = 0, n = sa.size();
    for (int i = 0; i < n; i++) {
        distPref[i] = n - sa[i] - last;
        if (i) distPref[i] += distPref[i - 1];
        last = lcp[i];
    }
}
array<int, 2> kthSubstringDistinctPos(string& s,
→ int64_t k, vector<int>& sa, vector<int>& lcp) {
    int n = s.size(); k--;
    int i = upper_bound(distPref, distPref + n, k) -
→ distPref;
    int len = k - (i == 0 ? 0 : distPref[i - 1]) + (i
→ == 0 ? 0 : lcp[i - 1]) + 1;
    return {i, len};
}
string kthSubstringDistinct(string& s, int64_t k,
→ vector<int>& sa, vector<int>& lcp) {
    auto [i, len] = kthSubstringDistinctPos(s, k, sa,
→ lcp);
    return s.substr(sa[i], len);
}
int64_t pref[N];
void kthSubstringPreprocess(vector<int>& sa) {
    int n = sa.size();
    for (int i = 0; i < n; i++) {
        pref[i] = n - sa[i];
        if (i) pref[i] += pref[i - 1];
    }
}
string kthSubstring(string& s, int64_t k,
→ vector<int>& sa, vector<int>& lcp) {
    int n = s.size();
    int64_t lo = 1, hi = distPref[n - 1];
    while (lo <= hi) {
        int64_t mid = (lo + hi) >> 1;
        auto [i, len] = kthSubstringDistinctPos(s, mid,
→ sa, lcp);
        int64_t totCnt = (i == 0 ? 0 : pref[i - 1]) + len;
        int mn = len;
        for (int j = i; j < n; j++) {
            mn = min(mn, lcp[j]);
            if (mn == 0) break;
            totCnt += mn;
        }
        if (totCnt < k) lo = mid + 1;
        else hi = mid - 1;
    }
    return kthSubstringDistinct(s, lo, sa, lcp);
}

```

```

int main() {
    string s;
    auto sa = getSuffixArray(s);
    auto lcp = getLCPArray(s, sa);
    kthSubstringDistinctPreprocess(sa, lcp);
    kthSubstringPreprocess(sa);
}

```

64 String Reorder Lexicographically Minimal

```

int n, la, A[36]; // no two adjacent characters are
→ the same
string s, ans;
int main() {
    cin >> s; n = s.size(); s = "0" + s;
    for (int i = 1; i <= n; i++) A[s[i] - 'A' + 1]++;
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= 26; j++) {
            if (!A[j] || j == la) continue;
            A[j]--;
            int maxn = 0;
            for (int k = 1; k <= 26; k++) maxn = max(maxn,
→ A[k]);
            if (maxn * 2 > n - i + 1) { A[j]++; continue; }
            ans += char(j + 'A' - 1), la = j;
            break;
        }
        if (ans.size() != i) { cout << "-1\n"; return 0; }
    } cout << ans << "\n";
}

```

65 Topological Sort

```

bool topological_sort(vector<vector<int>>& adj) {
    int n = adj.size();
    vector<int> in_degree(n + 1);
    for (int u = 1; u <= n; u++) {
        for (auto& v : adj[u]) in_degree[v]++;
    }
    // without sorting the order
    queue<int> q;
    // sort with lexicographically
    // priority_queue<int, vector<int>, greater<int>> q;
    for (int u = 1; u <= n; u++) {
        if (in_degree[u] == 0) q.push(u);
    }
    if (q.empty()) return 0;
    vector<int> order;
    while (!q.empty()) {
        # change the queue operation
        int u = q.front();
        q.pop();
        for (auto& v : adj[u]) {
            in_degree[v]--;
            if (in_degree[v] == 0)
                q.push(v);
        }
        order.push_back(u);
    }
}

```

```

} return (int)order.size() == n;
}

```

66 Trie

```

// iterative
const int N = 1e6 + 9, A = 26;
int nxt[N][A], pref_cnt[N], word_cnt[N], node = 2;
void insert(string& s, int u = 1) {
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) nxt[u][idx] = node++;
        u = nxt[u][idx];
        pref_cnt[u]++;
    } word_cnt[u]++;
}
int countPref(string& s, int u = 1) {
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) return 0;
        u = nxt[u][idx];
    } return pref_cnt[u];
}
int find(string& s, int u = 1) {
    for (auto& c : s) {
        int idx = c - 'a';
        if (!nxt[u][idx]) return 0;
        u = nxt[u][idx];
    } return word_cnt[u];
}
void erase(string& s, int u = 1) {
    if (find(s) == 0) return;
    for (auto& c : s) {
        int idx = c - 'a';
        int v = nxt[u][idx];
        pref_cnt[v][idx]--;
        u = v;
    } word_cnt[u]--;
}

// trie integer iterative (max xor, min xor)
const int N = 2e5 * 31 + 9, A = 2;
int nxt[N][A], pref_cnt[N], int_cnt[N], node = 2;
void insert(int num, int u = 1) {
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (!nxt[u][idx]) nxt[u][idx] = node++;
        u = nxt[u][idx];
        pref_cnt[u]++;
    } int_cnt[u]++;
}

int find(int num, int u = 1) {
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (!nxt[u][idx]) return 0;
        u = nxt[u][idx];
    } return int_cnt[u];
}
void erase(int num, int u = 1) {
    if (find(num) == 0) return;
}

```

```

for(int bit = 30; bit >= 0; bit--) {
    int idx = (num >> bit) & 1;
    int v = nxt[u][idx];
    pref_cnt[v]--;
    u = v;
} int_cnt[u]--;
}

int maxXor(int num) {
    int res = 0, u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        int flip = idx ^ 1;
        if (nxt[u][flip] && pref_cnt[nxt[u][flip]]) {
            res += (1 << bit);
            u = nxt[u][flip];
        } else {
            u = nxt[u][idx];
        }
    } return res;
}

int minXor(int num) {
    int res = 0, u = 1;
    for (int bit = 30; bit >= 0; bit--) {
        int idx = (num >> bit) & 1;
        if (nxt[u][idx] && pref_cnt[nxt[u][idx]]) {
            u = nxt[u][idx];
        } else {
            res += (1 << bit);
            u = nxt[u][idx ^ 1];
        }
    } return res;
}

```

67 Tower Of Hanoi

```

void hanoi(int n, int a, int b, int c) {
    if (n == 0) return;
    hanoi(n - 1, a, c, b);
    cout << a << " " << c << '\n';
    hanoi(n - 1, b, a, c);
}

int main() {
    int n; cin >> n;
    int k = (1LL << n) - 1;
    cout << k << '\n';
    hanoi(n, 1, 2, 3);
}

```

68 Wavelet Matrix

```

struct bitVec {
    vector<pair<ll, int>> b;
    bitVec(const vector<bool> &a): b((int)(a).size() / 
→ 64 + 1) {
        for (int i = 0; i < (int)(a).size(); ++i)
            b[i >> 6].first |= (ll)(a[i]) << (i & 63);
        for (int i = 0; i < (int)(b).size() - 1; ++i)
            b[i + 1].second =
                __builtin_popcountll(b[i].first) +
                b[i].second;
    }
}

```

```

}
int cnt0(int r) {
    pair<ll, int> p = b[r >> 6];
    ll x = p.first;
    int y = p.second;
    return r - y - __builtin_popcountll(x & ((1ULL <<
→ (r & 63)) - 1));
}
};

struct WaveletMatrix {
    int n; vector<bitVec> bv;
    vector<vector<ll>> pref;
    WaveletMatrix(vector<ll> a, ll max_val):
        n((int)(a).size()), bv(1 + __lg(max_val),
        { }), pref(1 + __lg(max_val)) {
        vector<ll> nxt(n);
        for (int h = (int)(bv).size(); h--;) {
            vector<bool> b(n);
            for (int i = 0; i < n; ++i) b[i] = ((a[i] >> h)
                & 1);
            bv[h] = b;
            int cnt0 = bv[h].cnt0(n);
            ll* it[2] = {nxt.data(), nxt.data() + cnt0};
            for (int i = 0; i < n; ++i) *it[b[i]]++ = a[i];
            pref[h].resize(n + 1);
            pref[h][0] = 0;
            for (int i = 0; i < n; ++i) pref[h][i + 1] =
                pref[h][i] + nxt[i];
            swap(a, nxt);
        }
    }
    // count i s.t. (l <= i < r) && (v[i] == x)
    int rank(int l, int r, ll x) {
        for (int h = (int)(bv).size(); h--;) {
            int lo = bv[h].cnt0(l), ro = bv[h].cnt0(r);
            if ((x >> h) & 1) {
                l += bv[h].cnt0(n) - 10;
                r += bv[h].cnt0(n) - ro;
            } else {
                l = 10, r = ro;
            }
        }
        return r - l;
    }
    // k-th (0-indexed) largest number in a[l, r]
    ll kthSmallest(int l, int r, int k) {
        ll res = 0;
        for (int h = (int)(bv).size(); h--;) {
            int lo = bv[h].cnt0(l), ro = bv[h].cnt0(r);
            if (k < ro - 10) l = 10, r = ro;
            else {
                k -= ro - 10, res |= 1ULL << h,
                l += bv[h].cnt0(n) - 10, r += bv[h].cnt0(n)
                → - ro;
            }
        }
        return res;
    }
    int kthLargest(int l, int r, int k) {

```

```

        return kthSmallest(l, r, r - l - k - 1);
    }
    // count i s.t. (l <= i < r) && (v[i] < upper)
    int rangeFreq(int l, int r, ll ub) {
        int res = 0;
        for (int h = (int)(bv).size(); h--;) {
            int l0 = bv[h].cnt0(1), r0 = bv[h].cnt0(r);
            if ((~ub >> h) & 1) l = l0, r = r0;
            else
                res += r0 - l0, l += bv[h].cnt0(n) - l0,
                r += bv[h].cnt0(n) - r0;
        }
        return res;
    }
    // count i s.t. (l <= i < r) && (lower <= v[i] <
    ↪ upper)
    int rangeFreq(int l, int r, ll lower, ll upper) {
        if (lower > upper) swap(lower, upper);
        return rangeFreq(l, r, upper) - rangeFreq(l, r,
    ↪ lower);
    }
    // sum of v[i] s.t. (l <= i < r) && (v[i] <= k)
    ll sumLTE(int l, int r, ll k) {
        ll res = 0;
        for (int h = (int)(bv).size(); h--;) {
            int l0 = bv[h].cnt0(1), r0 = bv[h].cnt0(r);
            if ((k >> h) & 1) {
                res += pref[h][r0] - pref[h][l0];
                l += bv[h].cnt0(n) - l0;
                r += bv[h].cnt0(n) - r0;
            } else {
                l = l0, r = r0;
            }
            if (l < r) res += pref[0][r] - pref[0][l];
        }
        return res;
    }
    // sum of v[i] s.t. (l <= i < r) && (lower <= v[i]
    ↪ <= upper)
    ll sumBetween(int l, int r, ll lower, ll upper) {
        return sumLTE(l, r, upper) - sumLTE(l, r, lower -
    ↪ 1);
    }
    // max v[i] s.t. (l <= i < r) && (v[i] < upper)
    ll prevValue(int l, int r, ll upper) {
        int cnt = rangeFreq(l, r, upper);
        return cnt == 0 ? -1 : kthSmallest(l, r, cnt - 1);
    }
    // min v[i] s.t. (l <= i < r) && (lower <= v[i])
    ll nextValue(int l, int r, ll lower) {
        int cnt = rangeFreq(l, r, lower);
        return cnt == r - l ? -1 : kthSmallest(l, r, cnt);
    }
}

```

69 Xor Basis

```

// XorBasis on Bitset
const int D = 5009;
struct XorBasis {

```

```

    bitset<N> basis[D];
    int sz = 0, n = 0;
    void insert(bitset<N> x) {
        for (int i = D - 1; i >= 0; i--) {
            if (!(x[i] & 1)) continue;
            if (basis[i].none()) {
                basis[i] = x;
                sz++;
                break;
            }
            x ^= basis[i];
        }
        n++;
    }
    bool canRepresent(bitset<N> x) {
        for (int i = D - 1; i >= 0; i--) {
            if (x[i] & 1) x ^= basis[i];
        }
        return x == 0;
    }
    int countSubsetsWithXor(bitset<N> x) {
        if (!canRepresent(x)) return 0;
        return BinExp(2, n - sz);
    }
};

// integer
using ll = long long;
const int D = 60;
struct XorBasis {
    // number of subsequences of xor-sum X, for ith
    ↪ prefix -> 2 ^ (i - sz);
    ll basis[D] = {};
    int sz = 0, n = 0;
    void insert(ll x) {
        for (int i = D - 1; i >= 0; i--) {
            if (!((x >> i) & 1)) continue;
            if (!basis[i]) {
                basis[i] = x;
                sz++;
                break;
            }
            x ^= basis[i];
        }
        n++;
    }
    bool canRepresent(ll x) {
        for (int i = D - 1; i >= 0; i--)
            if ((x >> i) & 1) x ^= basis[i];
        return x == 0;
    }
    ll maxXor(ll x = 0) {
        for (int i = D - 1; i >= 0; i--)
            if ((x ^ basis[i]) > x) x ^= basis[i];
        return x;
    }
    ll minXor() { // except xor 0
        for (int i = 0; i < D; i++)
            if (basis[i]) return basis[i];
        return 0;
    }
    ll maxXorWith(ll x) {
        return maxXor(x);
    }
    ll minXorWith(ll x) {
        for (int i = D - 1; i >= 0; i--) {
            if ((x ^ basis[i]) < x) x ^= basis[i];
        }
        return x;
    }
    ll countDistinctXors() {
        return 1LL << sz;
    }
    ll kthXor(ll k) { // returns k + 1 th xor, 1st xor
    ↪ is 0
        ll res = 0;
        ll tot = countDistinctXors();
        if (tot < k) return -1;
        for (int i = D - 1; i >= 0; i--) {
            if (basis[i]) {
                ll low = tot / 2;
                if ((low < k && (res & 1 << i) == 0) ||
                    (low >= k && (res & 1 << i) > 0)) res ^=
                ↪ basis[i];
                if (low < k) k -= low;
                tot /= 2;
            }
        }
        return res;
    }
    ll kthLargestXor(ll k) {
        return kthXor(countDistinctXors() - 1 - k);
    }
    ll kthXorAllCombinations(ll k) {
        if (n - sz > 60) return kthXor(1);
        ll totComb = 1LL << n;
        ll disComb = countDistinctXors();
        ll dupPerDis = totComb / disComb;
        ll disIdx = (k - 1) / dupPerDis + 1;
        return kthXor(disIdx);
    }
    ll kthLargestXorAllCombinations(ll k) {
        if (n - sz > 60) return
        ↪ kthXor(countDistinctXors());
        ll totComb = 1LL << n;
        ll disComb = countDistinctXors();
        ll dupPerDis = totComb / disComb;
        ll disIdx = (k - 1) / dupPerDis + 1;
        ll desIdx = disComb - disIdx + 1;
        return kthXor(desIdx);
    }
    ll countSubsetsLessThan(ll x) {
        ll lo = 0, hi = countDistinctXors();
        while (lo <= hi) {
            ll mid = (lo + hi) / 2;
            if (kthXor(mid) < x) lo = mid + 1;
            else hi = mid - 1;
        }
        return hi;
    }
    ll countSubsetsWithXor(ll x) {

```

```

    if (!canRepresent(x)) return 0;
    return 1LL << (n - sz); // if n > 60 use mod
}

```

70 Z Function

```

// 0 based, longest substring lenght starting at
// position i that is also a prefix
// String: a b c a b c b b
// Index: 0 1 2 3 4 5 6 7
// Z[]:      - 0 0 3 0 0 0 0
vector<int> get_z(string& s) {
    int n = s.size(), l = 0, r = 0;
    vector<int> z(n); z[0] = n;
    for (int i = 1; i < n; i++) {
        if (i < r) z[i] = min(r - i, z[i - 1]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]]);
        z[i]++;
        if (i + z[i] > r) l = i, r = i + z[i];
    }
    return z;
}

```

71 Mathematical Formulas & Notes

- PI up to 31:** 3.1415926535897932384626433832795
- PI value in CPP:** $2 * \text{acos}(0), 2 * \text{asin}(1), M_PI$
- Formula for angle C using the Law of Cosines**
 $C = \cos^{-1}\left(\frac{a^2+b^2-c^2}{2ab}\right)$
- Sum remainder: n mod 1+n mod 2+ n mod 3 +.....+n mod m :** n^*m -sum of divisors from 1 to n
- A number is divisible by 60 if and only if it is divisible by 3 and 20**
- All numbers greater than 1099 can be written as a sum of 11 and 111**
- Legendre's formula:** $\nu_p(n!) = \sum_{i=1}^L \left\lfloor \frac{n}{p^i} \right\rfloor$, where $L = \lfloor \log_p n \rfloor$
- $nC_r = \binom{n}{r} = \frac{n!}{r!(n-r)!}, nP_r = \frac{n!}{(n-r)!}$
- $(a-b)\%M = (a\%M - b\%M + M)\%M$
- $(a/b)\%M = (a\%M * b^{-1}\%M)\%M$
- $(a^b)\%M = ((a\%M)^b)\%M$

12. Euler's Totient Function (ETF): Count of numbers less than n that are co-prime to n is,
 $\phi(n) = n * \prod_{p|n} \left(1 - \frac{1}{p}\right)$
Here, p = distinct prime factors of n

- Congruence:** $a \equiv b \pmod{M}$
if $a\%M = b\%M$ and $M | (a - b)$
- Euler's Theorem:** $a^{\phi(M)} \equiv 1 \pmod{M}$, where a and M are co-prime
- Fermat's Little Theorem:** $a^{M-1} \equiv 1 \pmod{M}$, where M is prime
- $a^b \equiv a^b \pmod{\phi(M)}$ (mod M) or it can be written that,
 $a^b \pmod{M} = a^b \pmod{\phi(M)} \pmod{M}$ or,
 $a^b \pmod{M} = a^b \pmod{M-1} \pmod{M}$
- x steps forward or backward in a circular number range:**
 $newPos = l + ((pos - l + x)\%N) + N)\%N$
Where $N = l - r + 1$ (total numbers in range)
- Stars & Bars:** $x_1 + x_2 + \dots + x_k = n$ with $x_i \geq 0$ has $\binom{n+k-1}{n}$ solutions and with $x_i > 0$ has $\binom{n-1}{k-1}$ solutions.
- Number of subsequences of length k from an array of size n such that x appears at least once in the subsequence, where that x appears c times in the array:
 $nC_k - n^{-c} C_k$
- Hockey-stick Identity:** $n > r, \sum_{i=r}^n \binom{i}{r} = \binom{n+1}{r+1}$
- $a^k - b^k = (a - b) \cdot (a^{k-1}b^0 + a^{k-2}b^1 + \dots + a^0b^{k-1})$
- $ab \pmod{ac} = a(b \pmod{c})$
- $|a - b| + |b - c| + |c - a| = 2(\max(a, b, c) - \min(a, b, c))$
- if $a \cdot b \leq c$ then $a \leq \left\lfloor \frac{c}{b} \right\rfloor$ Same for $<, \leq, >, \geq$
- For positive integer n & arbitrary real numbers m, x,
 $\left\lfloor \frac{\lfloor x/m \rfloor}{n} \right\rfloor = \left\lfloor \frac{x}{mn} \right\rfloor$ and $\left\lceil \frac{\lceil x/m \rceil}{n} \right\rceil = \left\lceil \frac{x}{mn} \right\rceil$
- $1 + 2 + \dots + n = \frac{n(n+1)}{2}$

$$27. 1^2 + 2^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$

$$28. 1^3 + 2^3 + \dots + n^3 = \left(\frac{n(n+1)}{2}\right)^2$$

$$29. \text{Arithmetic Progression (AP): } a + (a+d) + \dots + (a + (n-1)d) = \frac{n}{2}(2a + (n-1)d)$$

$$30. \text{Geometric Progression (GP): } 1+r+r^2+\dots+r^n = \frac{r^{n+1}-1}{r-1}, \text{ for } r \neq 1$$

$$31. \text{Infinite GP } (|r| < 1): 1 + r + r^2 + \dots = \frac{1}{1-r}$$

$$32. \text{Quadratic Formula: } ax^2 + bx + c = 0 \Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Simple Formulas

- $(a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3$
- $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$
- $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
- $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
- $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
- $\sin A \pm \sin B = 2 \sin\left(\frac{A \pm B}{2}\right) \cos\left(\frac{A \mp B}{2}\right)$
- $\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
- $\cos A - \cos B = 2 \sin\left(\frac{A+B}{2}\right) \sin\left(\frac{B-A}{2}\right)$
- $\sin A \sin B = -\frac{1}{2}[\cos(A+B) - \cos(A-B)]$
- $\cos A \cos B = \frac{1}{2}[\cos(A+B) + \cos(A-B)]$
- $\sin A \cos B = \frac{1}{2}[\sin(A+B) + \sin(A-B)]$
- $\sin 2\theta = 2 \sin \theta \cos \theta = \frac{2 \tan \theta}{1 + \tan^2 \theta}$
- $\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1$
 $= 1 - 2 \sin^2 \theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$
- $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$
- $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$
- $\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$
- $\tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$
- $1 + \cos 2\theta = 2 \cos^2 \theta$
- $1 - \cos 2\theta = 2 \sin^2 \theta$
- $1 \pm \sin 2\theta = (\cos \theta \pm \sin \theta)^2$

21. $\sin^{-1} x = \cos^{-1} \sqrt{1-x^2}$
 22. $2 \sin^{-1} x = \sin^{-1}(2x\sqrt{1-x^2})$
 23. $2 \cos^{-1} x = \cos^{-1}(2x^2 - 1)$
 24. $2 \tan^{-1} x = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$
 25. $2 \tan^{-1} x = \sin^{-1}\left(\frac{2x}{1+x^2}\right)$
 26. $2 \tan^{-1} x = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$
 27. $3 \sin^{-1} x = \sin^{-1}(3x - 4x^3)$
 28. $3 \cos^{-1} x = \cos^{-1}(4x^3 - 3x)$
 29. $3 \tan^{-1} x = \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$
 30. $\sin^{-1} x \pm \sin^{-1} y = \sin^{-1} \left[x\sqrt{1-y^2} \pm y\sqrt{1-x^2} \right]$
 31. $\cos^{-1} x \pm \cos^{-1} y = \cos^{-1} \left[xy \mp \sqrt{1-x^2}\sqrt{1-y^2} \right]$
 32. $\tan^{-1} x \pm \tan^{-1} y = \tan^{-1}\left(\frac{x \pm y}{1 \mp xy}\right)$
 33. $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \tan^{-1}\left(\frac{x+y+z-xyz}{1-xy-yz-zx}\right)$

Short Formulas

- | | |
|---|---|
| 1. $\sin(-\theta) = -\sin \theta$ | 2. $\cos(-\theta) = \cos \theta$ |
| 3. $\tan(-\theta) = -\tan \theta$ | 4. $\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$ |
| 5. $\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$ | 6. $\tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta$ |
| 7. $\cot\left(\frac{\pi}{2} - \theta\right) = \tan \theta$ | 8. $\csc\left(\frac{\pi}{2} - \theta\right) = \sec \theta$ |
| 9. $\sec\left(\frac{\pi}{2} - \theta\right) = \csc \theta$ | 10. $\sin\left(\frac{\pi}{2} + \theta\right) = \cos \theta$ |
| 11. $\cos\left(\frac{\pi}{2} + \theta\right) = -\sin \theta$ | 12. $\tan\left(\frac{\pi}{4} + \theta\right) = \frac{1+\tan \theta}{1-\tan \theta}$ |
| 13. $\tan\left(\frac{\pi}{4} - \theta\right) = \frac{1-\tan \theta}{1+\tan \theta}$ | 14. $\sin(\pi + \theta) = -\sin \theta$ |
| 15. $\cos(\pi + \theta) = -\cos \theta$ | 16. $\sin(\pi - \theta) = \sin \theta$ |
| 17. $\cos(\pi - \theta) = -\cos \theta$ | 18. $\log_a a = 1$ |
| 19. $a^{\log_a b} = b$ | 20. $\log_b a = \frac{\log a}{\log b}$ |
| 21. $\log a^m = m \log a$ | |