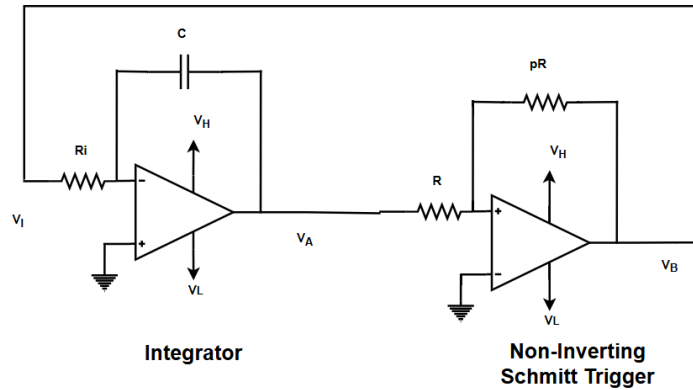


Question 01.

Answer the following question for the Triangular wave generator.

Given, $V_L = -V_H$

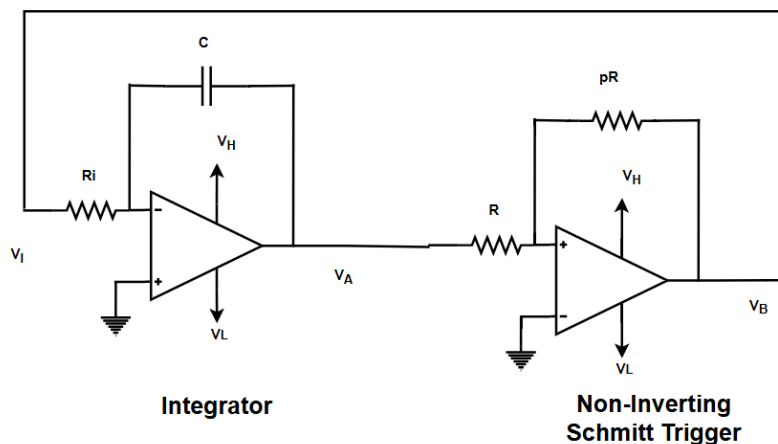


(a)	Prove that the frequency of the triangular wave, $f = \frac{P}{4R_iC}$.
(b)	Find the duty cycle of the triangular wave and find the duty cycle of the square wave. Is there any relation between these two duty cycles?
(c)	Draw the wave form of the square wave (V_A) and triangular wave (V_B).

Question 02.

Answer the following question for the Triangular wave generator.

Given, $R_i = 10k$, $C = 10 \mu F$, $R_2 = pR = 20k$, $R_1 = R = 10k$, $V_L = -V_H$ or $V_H = 15 V$, $V_L = -15 V$



(a)	Find the value of upper threshold and lower threshold value of the Schmitt trigger used in the above triangular wave generator.
(b)	Draw the VTC of the Schmitt trigger used in the above triangular wave generator.
(c)	What is the frequency and time period of the triangular wave generator?

Question 03

Suppose you want to design a triangular wave generator circuit. Required frequency of the wave is 1 kHz.

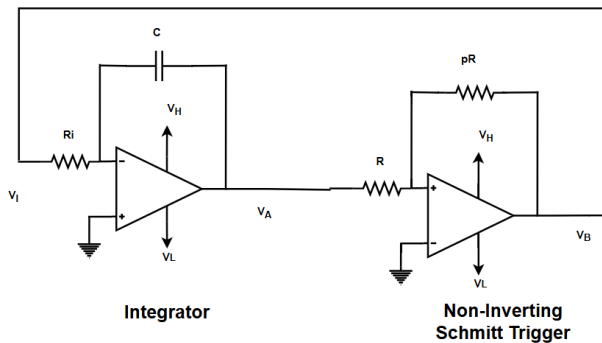
Duty cycle should be close to 50 %. You have +15V, -15 V power supply, $0.47 \mu F$ capacitor and different resistors.

(a)	Find the time period, rising time and falling time of the desired triangular wave.
(b)	Design a circuit to generate the required wave.
(c)	Suppose you have replaced the power supply of your designed circuit with +5V and -5V what will be new frequency and duty cycle of the triangular wave?

Question 04.

Answer the following question for the Triangular wave generator.

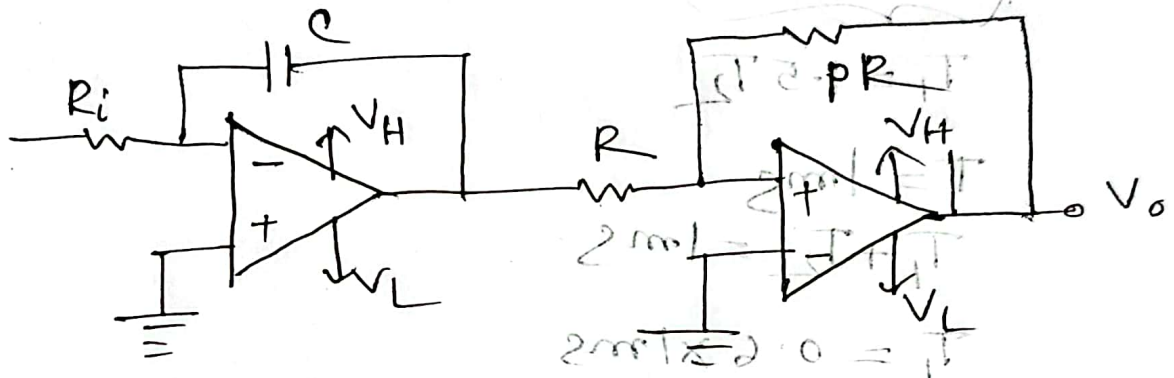
Given, $R_i = 10k$, $C = 10 \mu F$, $R_2 = pR = 20k$, $R_1 = R = 10k$, or $V_H = 10 V$, $V_L = -8 V$



(a)	Find the values of V_{TH} , V_{TL} , <i>Falling time</i> and <i>Rising Time</i> of the triangular wave generator.
(b)	What will be the duty cycle of the triangular wave and the square wave?

Triangular Wave Generator

Q1. a) Triangular wave generator,



Given, $V_L = -V_H$

$$V_{TH} = -\frac{V_L}{p} = \frac{V_H}{p} \quad [V_L = -V_H]$$

$$V_{TL} = -\frac{V_H}{p}$$

$$\text{Now, } T_1 = R_i C \frac{V_{TH} - V_{TL}}{V_H} = R_i C \frac{\frac{V_H}{p} + \frac{V_H}{p}}{V_H} = \frac{2 R_i C}{p}$$

$$T_2 = R_i C \frac{V_{TL} - V_{TH}}{V_L} = R_i C \frac{-\frac{V_H}{p} - \frac{V_H}{p}}{-V_H} [V_L = -V_H] = \frac{2 R_i C}{p}$$

$$T = T_1 + T_2 = \frac{2 R_i C}{p} + \frac{2 R_i C}{p} = \frac{4 R_i C}{p}$$

$$\therefore f = \frac{1}{T} = \frac{p}{4 R_i C} \quad [\text{proved}]$$

Q1. b) We know,

$$T_{01} = R_i C \frac{V_{TH} - V_{TL}}{\frac{V_H}{P} + \frac{V_H}{P}}$$

$$= R_i C \frac{V_H}{V_H}$$

$$= \frac{2 R_i C}{P}$$

$$V_H = -V_L$$

$$V_{TH} = \frac{V_H}{P}$$

and, $V_{TL} = -\frac{V_H}{P}$

$$T_2 = R_i C \frac{V_{TL} - V_{TH}}{-\frac{V_H}{P} - \frac{V_H}{P}} = \frac{2 R_i C}{P}$$

$$D.C. (T_{ri}) = \frac{T_2}{T_1 + T_2} \times 100\%$$

$$= \frac{\frac{2 R_i C}{P}}{\frac{2 R_i C}{P} + \frac{2 R_i C}{P}} \times 100\% = 50\%$$

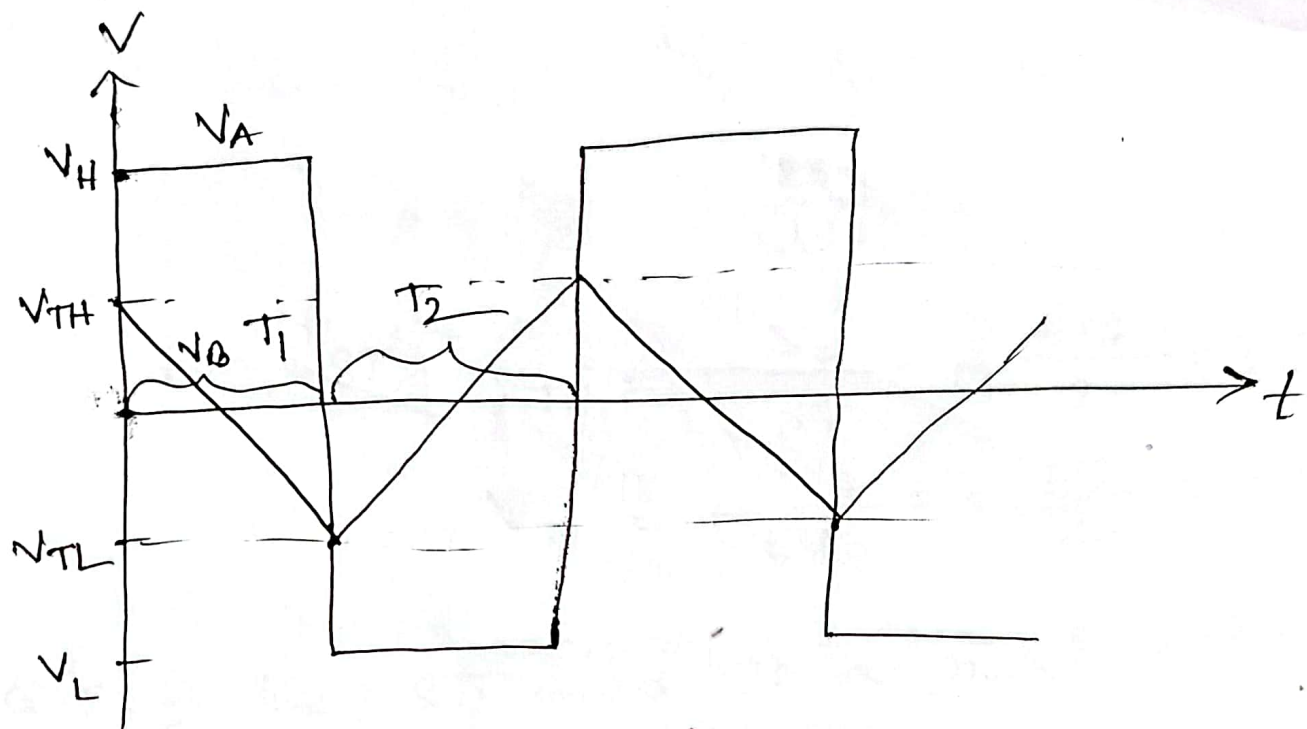
$$D.C. (S_q) = \frac{T_1}{T_1 + T_2} \times 100\%$$

$$= \frac{\frac{2 R_i C}{P}}{\frac{2 R_i C}{P} + \frac{2 R_i C}{P}} \times 100\% = 50\%$$

Yes, sum of the two duty cycles is 100%.

$$D.C. (T_{ri}) + D.C. (S_q) = 100\%$$

Q.1.(c)



Q2. a) Here, $V_H = +15V$, $V_L = -15V$,

$$p = \frac{R_2}{R_1} = \frac{20k}{10k} = 2$$

$$\text{For, ST, } V_{TH} = -\frac{V_L}{p} = -\frac{-15}{2} = 7.5V$$

$$V_{TL} = -\frac{V_H}{p} = -\frac{15}{2} = -7.5V$$

Q2. b) The ST used is a non-inverting ST,

$$\text{From (a), } V_{TH} = 7.5V,$$

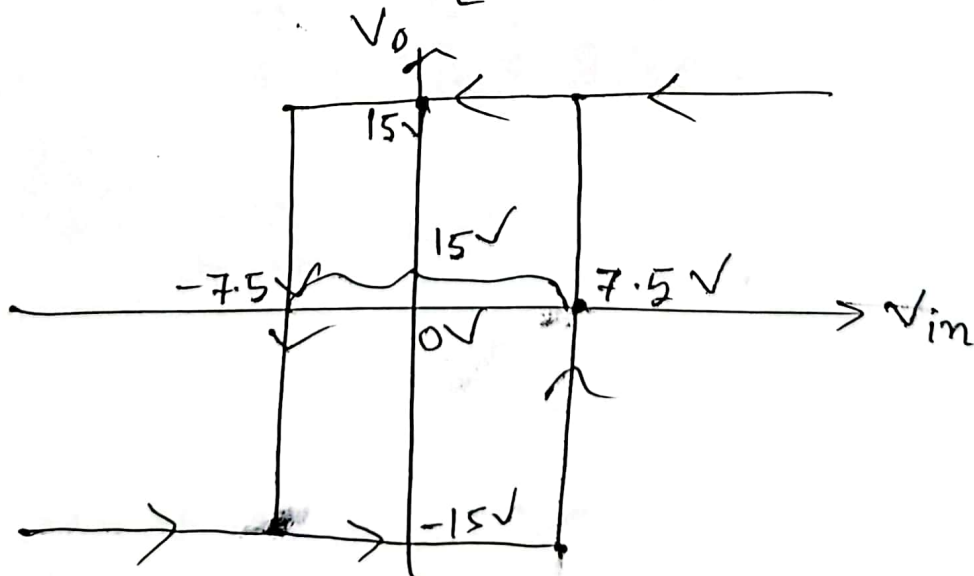
$$V_{TL} = -7.5V,$$

$$V_S = \frac{V_{TH} + V_{TL}}{2} = 0$$

$$V_{HW} = V_{TH} - V_{TL} = 15V$$

$$V_H = +15V$$

$$V_L = -15V$$



Q.2(c) As the power supply is symmetrical,

$$f = \frac{P_{oc}}{4 R_C} = \frac{2.5}{19} = P_9 = \frac{R_2}{R_1} = 2$$

$$V_{2F} = \frac{V_{21}}{5} = \frac{2V}{5} = 0.4V$$

$$f = \frac{V_{21}}{5} = 5Hz = 5V$$

$$T_2 \text{ period} = \frac{1}{f} = \frac{1}{5} = 0.2s$$

$$V_{2F} = 4V$$

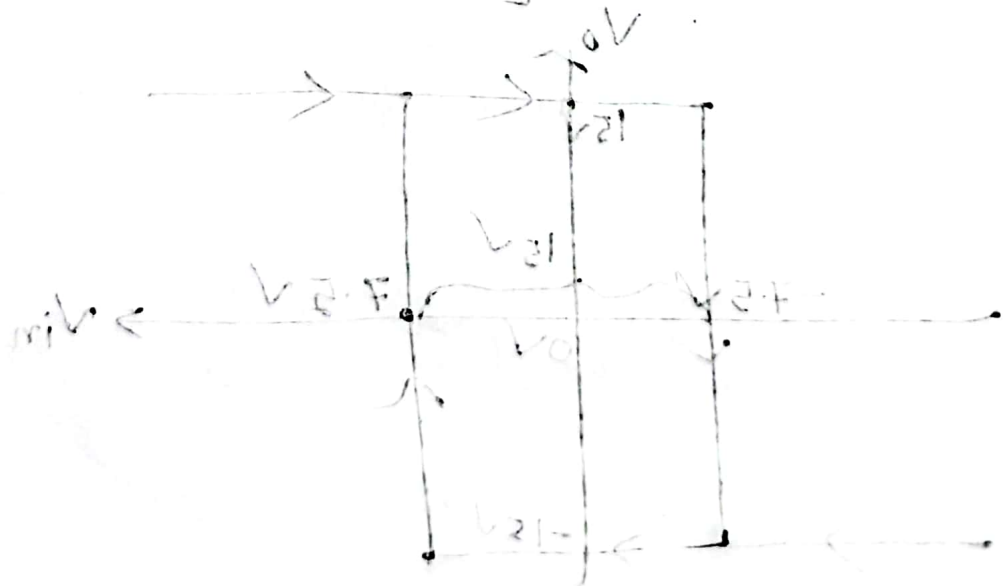
$$V_{2F} = 1V$$

$$0 = \frac{V_{2F} + V_{21}}{5} = 2V$$

$$V_{21} = 1V - 4V = -3V$$

$$V_{21} = 4V$$

$$V_{21} = -12V$$



Q.3. a) We know,

t_1 = Falling time

t_2 = Rising time

$$T = \frac{1}{f} = \frac{1}{1k} = 1ms$$

$$50\% = \frac{t_2}{t_1 + t_2} \times 100\%$$

$$\Rightarrow \frac{1}{2} = \frac{t_2}{t_1 + t_2}$$

$$\Rightarrow t_1 + t_2 = 2t_2$$

Since $t_1 = t_2$ we have

$$\text{Again, } T = t_1 + t_2$$

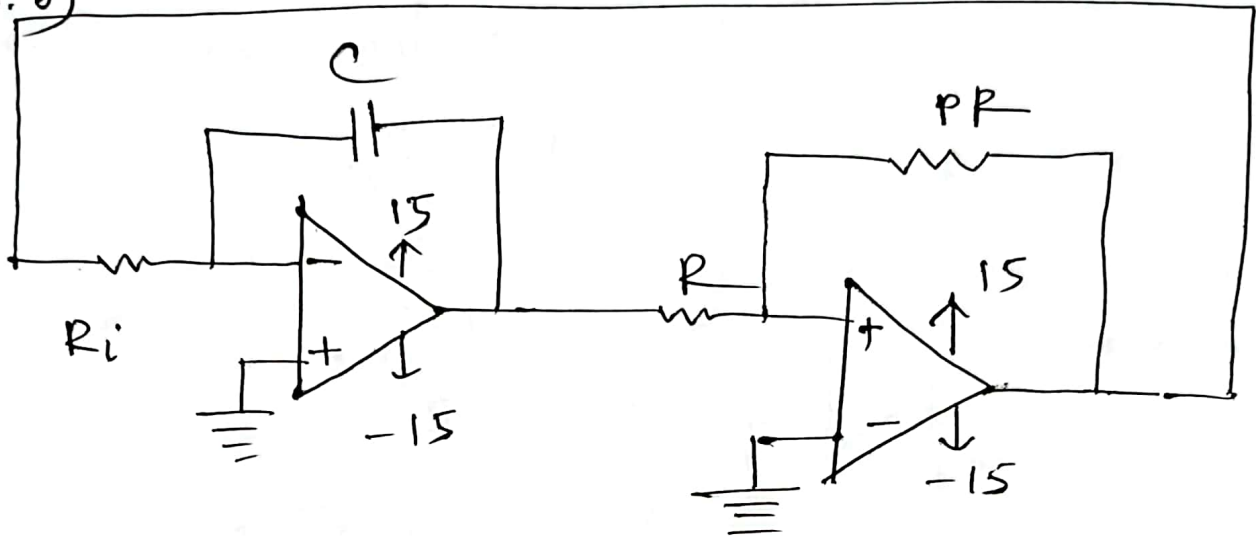
$$\Rightarrow T = t_1 + t_2 \quad [t_1 = t_2]$$

$$\Rightarrow t_1 = \frac{T}{2} = \frac{1ms}{2} = 0.5ms$$

$$t_1 = t_2 = 0.5ms$$

$$\frac{0.5ms}{1} = T$$

Q 3. b)



Given, $C = 0.47 \mu F$,
 $V_L = -V_H$, $V_H = 15V$, $V_L = -15V$

$$f = 1000 \text{ Hz}$$

From, symmetrical power supply,

$$f = \frac{p}{4 R_i C}$$

$$\Rightarrow 1000 = \frac{p}{4 \times R_i \times 0.47 \times 10^{-6}}$$

Now, we can assume, $p = 4$

$$1000 = \frac{4}{4 \times R_i \times 0.47 \times 10^{-6}}$$

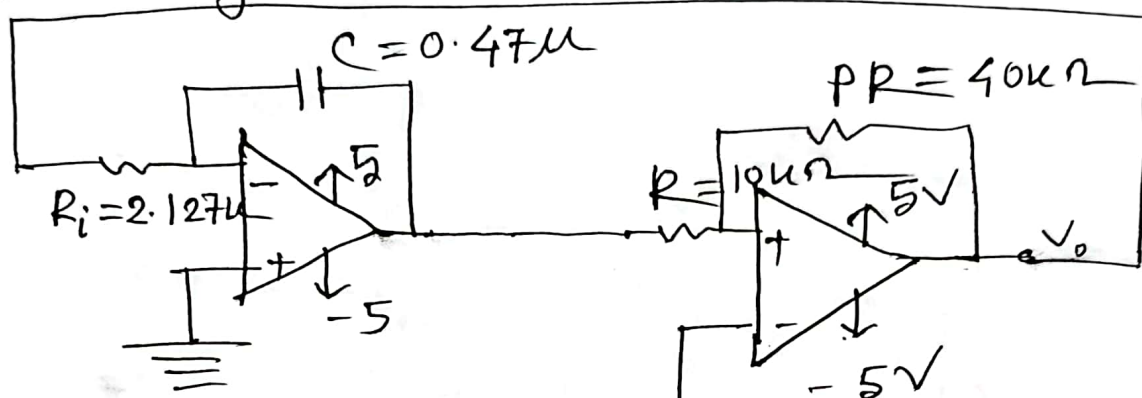
$$\Rightarrow R_i = 2.127 \text{ k}\Omega$$

As, $p = \frac{R_2}{R_1}$, Assuming, $R_1 = 10 \text{ k}\Omega$,

$$\frac{R_2}{10 \text{ k}} = 4, \Rightarrow R_2 = 40 \text{ k}\Omega$$

Now, $R_i = 2.127 \text{ k}\Omega$, $R_1 = 10 \text{ k}\Omega$, $R_2 = 40 \text{ k}\Omega$, $C = 0.47 \mu F$

Q3.c) Designed circuit, with $\pm 5V$ supply



$$V_H = +5V, V_L = -5V, p = \frac{R_2}{R_1} = 4$$

$$V_{TH} = -\frac{V_L}{p}$$

$$= -\frac{-5}{4}$$

$$= 1.25V$$

$$V_{TL} = -\frac{V_H}{p} = -\frac{5}{4} = -1.25V$$

$$T_1 = R_i C \frac{V_{TH} - V_{TL}}{V_H}$$

$$= R_i C \frac{1.25 + 1.25}{5} = \frac{R_i C}{2}$$

$$T_2 = R_i C \frac{V_{TL} - V_{TH}}{V_L}$$

$$= R_i C \frac{-1.25 - 1.25}{-5}$$

$$= \frac{R_i C}{2}$$

$$T = T_1 + T_2$$

$$= \frac{R_i C}{2} + \frac{R_i C}{2}$$

$$= R_i C$$

$$f = \frac{1}{T} = \frac{1}{R_i C} = \frac{1}{2.127 \times 10^3 \times 0.47 \times 10^{-6}}$$

Same as before, $\approx 1000 \text{ Hz}$

Q4. a) Power supply not symmetrical,

$$\text{Here, } p = \frac{R_2}{R_1} = \frac{20\mu}{10\mu} = 2$$

$$V_H = 10V, V_L = -8V$$

$$\begin{aligned} V_{TH} &= -\frac{V_L}{p} \\ &= -\frac{-8}{2} \\ &= 4V, \end{aligned}$$

$$\begin{aligned} V_{TL} &= -\frac{V_H}{p} \\ &= -\frac{10}{2} \\ &= -5V \end{aligned}$$

$$\text{Here, } \tau = R_i C = 10\mu \times 10\mu = 100 \text{ ms}$$

$$T_1 = 100 \text{ ms} \times \frac{4 - (-5)}{10} = 90 \text{ ms}$$

$$T_2 = 100 \text{ ms} \times \frac{-5 - 4}{-8} = 112.5 \text{ ms}$$

$$V_{TH} = 4V, V_{TL} = -5V, T_1 = 90 \text{ ms}, T_2 = 112.5 \text{ ms}$$

$T_1 \rightarrow$ falling time

$T_2 \rightarrow$ rising time

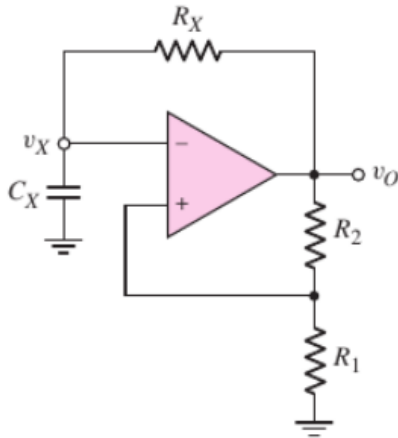
Q4. b) From (a), $T_1 = 90 \text{ ms}$, $T_2 = 112.5 \text{ ms}$

$$DC (T_{ri}) = \frac{T_2}{T_1 + T_2} \times 100\% = 55.55\%$$

$$DC (S_f) = \frac{T_1}{T_1 + T_2} \times 100\% = 44.44\%$$

Square Wave Generator

1.

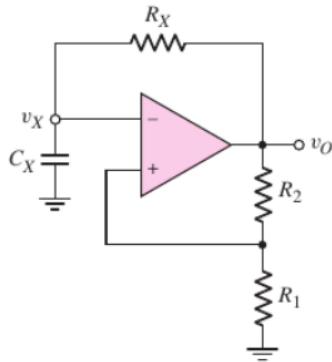


Here suppose $R_1 = 10k$, $R_2 = 20k$, $R_X = 1k$, $C_X = 1 \text{ mF}$, $V_H = 10V$ and $V_L = -10V$

a. Find the period and frequency of the square wave?

- b. What will be the value of the duty cycle of the square wave?
- c. Draw the output waveform with proper labeling.

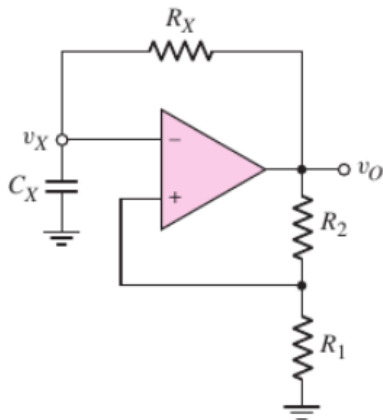
2.



Here $V_H = 10\text{ V}$ and $V_L = -10\text{ V}$

Design the circuit so that it can generate a square wave with 1 kHz frequency and 50% duty cycle.

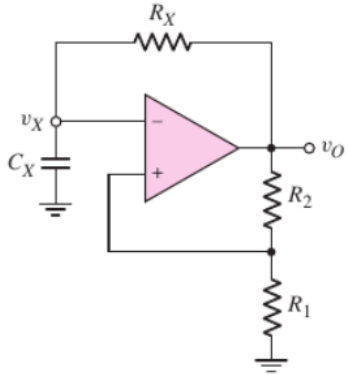
3.



suppose $R_1 = 10\text{ k}$, $R_2 = 20\text{ k}$, $R_X = 1\text{ k}$, $C_X = 1\text{ mF}$

Design the circuit so that it can generate square wave with a 30% duty cycle. Find the frequency of your designed circuit.

4.



Here suppose $R_1 = 10k$, $R_2 = 20k$, $R_x = 1k$, $C_x = 1 \text{ mF}$, $V_H = 10V$ and $V_L = -5V$

Find out the duty cycle of inverted output signal of the above circuit.

$$1. a) R_1 = 10k, R_2 = 20k, R_x = 1k, C_x = 1mF,$$

$$V_H = +10V, V_L = -10V$$

$$V_{TH} = \cancel{10} V_H \times \frac{R_1}{R_1 + R_2}$$

$$= 10 \times \frac{10}{10 + 20} = 3.33$$

$$V_{TL} = V_L \times \frac{R_1}{R_1 + R_2} = -3.33$$

$$\tau = R_x C_x = 1k \times 1m = 1s$$

$$T_1 = \tau \ln \frac{V_H - V_{TL}}{V_H - V_{TH}}$$

$$= 1 \times \ln \frac{10 - (-3.33)}{10 - 3.33}$$

$$= 0.69s$$

$$T_2 = \tau \ln \frac{V_L - V_{TH}}{V_L - V_{TL}}$$

$$= 1 \times \ln \frac{-10 - 3.33}{-10 - (-3.33)}$$

$$= 0.69s$$

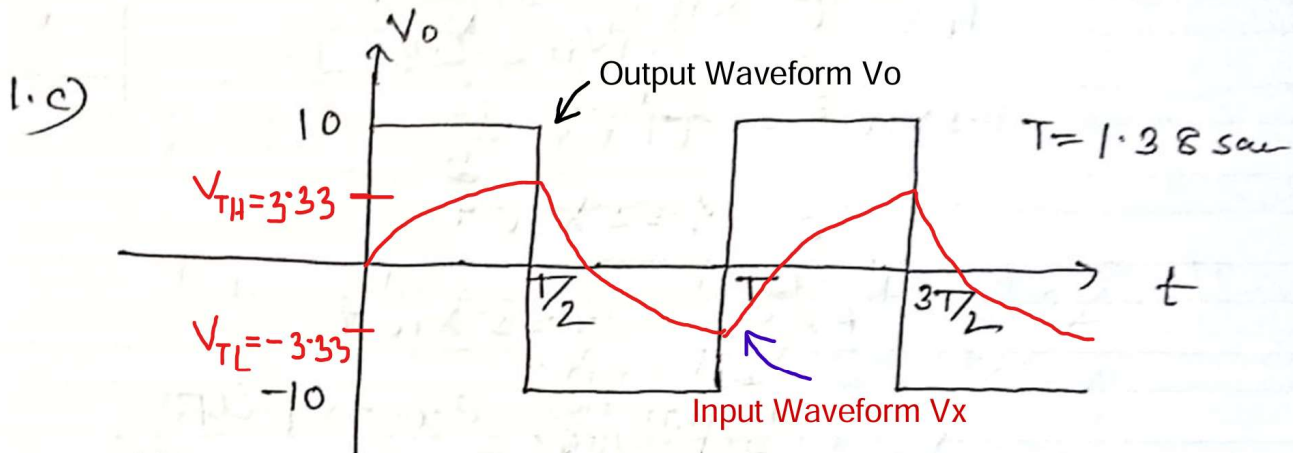
$$T = T_1 + T_2 = 0.69 + 0.69 = 1.38s$$

$$f = \frac{1}{T} = 0.72 \text{ Hz}$$

1. b) Duty cycle $= \frac{T_1}{T_1 + T_2} \times 100\%$

$$= \frac{0.69}{0.69 + 0.69} \times 100\%$$

$$= 50\%$$



2. $V_H = 10V$, $V_L = -10V$

Assuming, $R_1 = R_2 = 10k\Omega$

$$V_{TH} = V_H \times \frac{R_1}{R_1 + R_2} = 5V$$

$$V_{TL} = V_L \times \frac{R_1}{R_1 + R_2} = -5V$$

given, $f = 1kHz$, $T = \frac{1}{f} = 1ms$

Duty cycle = 50% and, $T = T_1 + T_2$

$$\therefore \frac{T_1}{T_1 + T_2} = 0.5, \Rightarrow T_1 = T_2 = \frac{T}{2} \\ = 0.5 \times 10^{-3}$$

$$T_1 = \tau \ln \frac{V_H - V_{TL}}{V_H - V_{TH}}$$

$$0.5 \times 10^{-3} = \tau \ln \frac{15}{5}$$

$$\tau = 4.55 \times 10^{-4}$$

$$R_x C_x = 4.55 \times 10^{-4}$$

assuming, $C_x = 1 \mu\text{F}$

$$R_x = \frac{4.55 \times 10^{-4}}{C_x} \\ = 455 \Omega$$

3. time constant $\Rightarrow \tau = R_x \cdot C_x = 1k\Omega \times 1mF$
 $= 1 \times 10^3 \times 1 \times 10^{-3} = 1 \text{ sec}$

given, square wave duty cycle $\Rightarrow 30\%$

means, $\frac{\tau_1}{\tau_1 + \tau_2} \times 100\% = 30\%$

$\Rightarrow \frac{\tau_1}{\tau_1 + \tau_2} = 0.3$

$\Rightarrow \tau_1 = 0.3 \tau_1 + 0.3 \tau_2$

$\Rightarrow 0.7 \tau_1 = 0.3 \tau_2$

$\Rightarrow \boxed{7\tau_1 = 3\tau_2} \rightarrow \text{Relation between high \& low times}$

we know, $\tau_1 = \tau \ln \frac{V_H - V_{TL}}{V_H - V_{TH}}$

$R_1 = 10k\Omega$

$R_2 = 20k\Omega$

$\therefore \frac{R_1}{R_1 + R_2} = \frac{10}{30}$
 $= \frac{1}{3} = 0.33$

$= \tau \ln \frac{V_H - \left(\frac{R_1}{R_1 + R_2}\right) \times V_L}{V_H - \left(\frac{R_1}{R_1 + R_2}\right) \times V_H}$

$= 1 \times \ln \frac{V_H - \frac{V_L}{3}}{V_H - \frac{V_H}{3}}$

$= 1 \times \ln \frac{3V_H - V_L}{2V_H}$

$\boxed{\tau_1 = 1 \times \ln \frac{3V_H - V_L}{2V_H}}$

$\tau_2 = \tau \ln \frac{V_L - V_{TH}}{V_L - V_{TL}}$

$= \tau \ln \frac{V_L - \left(\frac{R_1}{R_1 + R_2}\right) V_H}{V_L - \left(\frac{R_1}{R_1 + R_2}\right) V_L}$

$\boxed{\tau_2 = 1 \ln \frac{3V_L - V_H}{2V_L}}$

Now, $7T_1 = 3T_2$

$$7 \ln \frac{3V_H - V_L}{2V_H} = 3 \ln \frac{3V_L - V_H}{2V_L}$$

as, there is two unknowns
 V_H and V_L in the equation,

let's suppose $\rightarrow V_H = 10V$

$$7 \ln \frac{30 - V_L}{20} = 3 \ln \frac{3V_L - 10}{2V_L}$$

using calculator, we get \rightarrow

$$V_L = 10$$

$$\begin{aligned} \therefore T_1 &= 1 \times \ln \frac{30-10}{20} \\ &= 0 \text{ sec} \end{aligned}$$

$$\begin{aligned} \therefore T_2 &= 1 \times \ln \frac{30-10}{20} \\ &= 0 \text{ sec} \end{aligned}$$

$$\therefore T = T_1 + T_2 = 0 \text{ sec}$$

$$f = \frac{1}{0} = \infty \text{ Hz}$$

$$4. \quad \tau = R \times C = 1s$$

$$V_H = +10V, \quad V_L = -5V$$

$$V_{TH} = V_H \frac{R_1}{R_1 + R_2} = 10 \times \frac{10}{10 + 20} = 3.33$$

$$V_{TL} = V_L \frac{R_1}{R_1 + R_2} = -5 \times \frac{10}{10 + 20} = -1.67$$

$$\begin{aligned} T_1 &= \tau \ln \frac{V_H - V_{TL}}{V_H - V_{TH}} \\ &= 1 \times \ln \frac{10 - (-1.67)}{10 - 3.33} = 0.559 \end{aligned}$$

$$\begin{aligned} T_2 &= \tau \ln \frac{V_L - V_{TH}}{V_L - V_{TL}} = 1 \times \ln \frac{-5 - 3.33}{-5 - (-1.67)} \\ &= 0.913s \end{aligned}$$

$$\text{Duty Cycle} = \frac{T_1}{T_1 + T_2} \times 100\% = 37.9\%$$