

Day 5

Historical figure

Turn to someone sitting near you. Take about 3 minutes to discuss:

If you could meet any historical figure, who would you choose and why?

Groups

1. On the set of integers, consider the binary operation of exponentiation. This operation is...

- (A) Both associative and commutative.
- (B) Associative, but not commutative.
- (C) Commutative, but not associative.
- (D) Neither associative nor commutative.

Recall: A *left identity* for a binary operation on a set S is an element e such that $es = s$ for all $s \in S$. A *right identity* is an element e such that $se = s$ for all $s \in S$.

2. On the set of integers, consider the binary operation of exponentiation. This operation has...

- (A) both a left identity and a right identity.
- (B) a left identity, but no right identity.
- (C) a right identity, but no left identity.
- (D) neither a right identity nor a left identity.

3. Consider the set $\{1, 2, 3\}$ equipped with the binary operation of multiplication modulo 4. This set is not a group because...

- (A) The set is not closed under the given operation.
- (B) The operation is not associative.
- (C) There is no identity element.
- (D) Not every element has an inverse.