

In Example 2 in 2.8, are we supposed to attempt to simplify the equations or compute the Grobner basis like normal? It seemed like the equations could have been found using substitution.

I don't totally understand the solving of the equations in Example 2. . .

You're right that the original system could have been solved directly by substitution in this case! In general, though, you might not be able to solve a polynomial system by substitution right away. But computing a Gröbner basis with respect to lex order will always get you to a place where you might be able to solve by substitution.

[I'm] still a little unsteady on Grobner bases because I don't quite know the order I should be computing  $S(f_i, f_j)$ .

It doesn't really matter what order you use. Just be systematic about it and make sure you compute the S-polynomial for all pairs! For instance, you might do the order  $(i, j) = (1, 2), (1, 3), \dots, (1, t), (2, 3), (2, 4), \dots, (2, t), \dots$