

# LR(0) Parser

**Course Name: Compiler Design**

**Course Code: CSE331**

**Level:3, Term:3**

**Department of Computer Science and Engineering**

**Daffodil International University**

Given That,  $S \rightarrow A A$   
 $A \rightarrow a A \mid b$

We will denote an expression as  $S' \rightarrow .S$

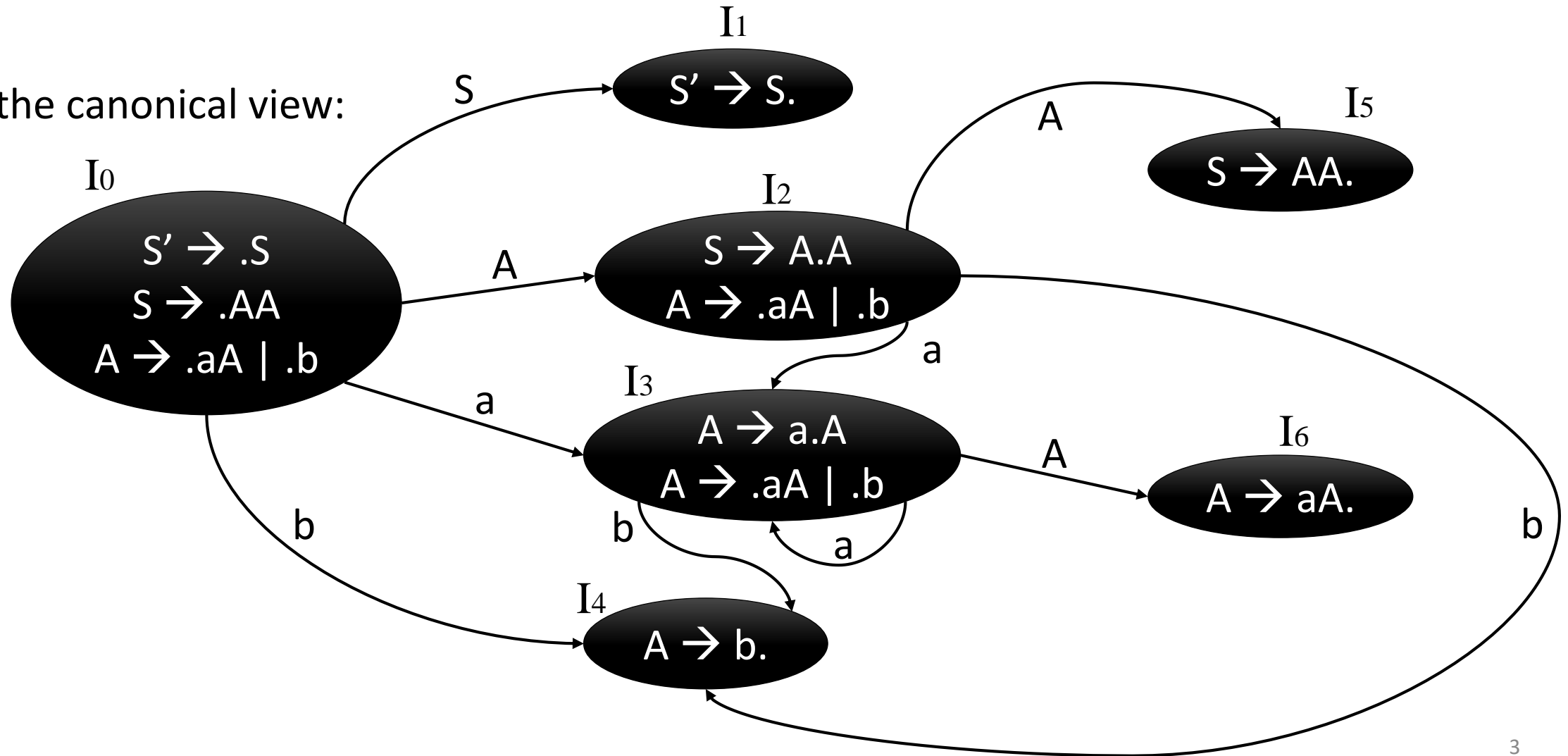
$S \rightarrow .A A$   
 $A \rightarrow .a A \mid .b$

We will denote an expression as  $S' \rightarrow .S$

$S \rightarrow .AA$

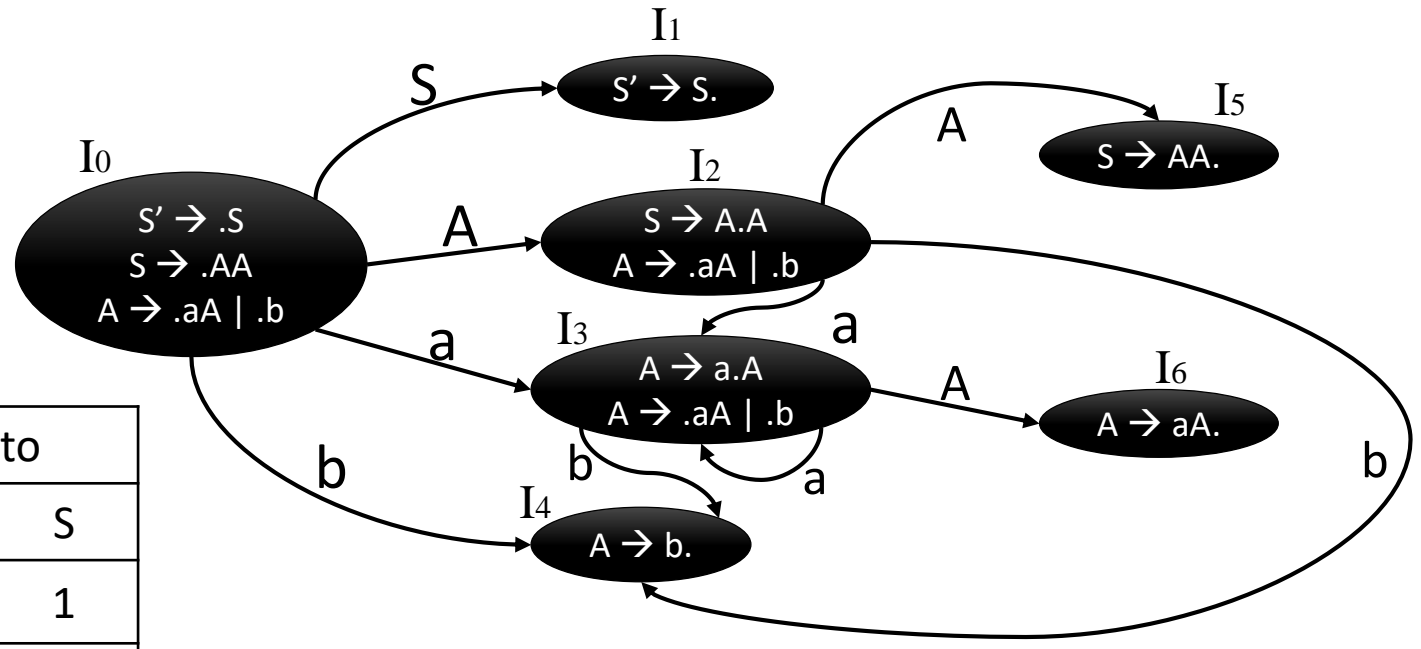
$A \rightarrow .aA \mid .b$

So, the canonical view:



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

States	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Shift (S) = Si (1,2,3)  
Reduce (r) = ri (1,2,3)

Here we can say,

$$S \rightarrow . A A \text{ -----1}$$

$$A \rightarrow . a A \text{ -----2}$$

$$A \rightarrow . b \text{ -----3}$$

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a a b b \$

0 a 3

Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a **a** **b** **b** \$

0 a 3 a 3

Here we can say,

$$S \rightarrow . A A \text{ -----1}$$

$$A \rightarrow . a A \text{ -----2}$$

$$A \rightarrow . b \text{ -----3}$$

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a a **b** b \$

0 a 3 a 3 b 4

Here we can say,  $S \rightarrow . A A$  -----1

$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

Reduce 3, as there is one element b in right, (2x1=) 2 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a a b **b** \$

0 a 3 a 3 b 4



Here we can say,  $S \rightarrow . A A$  -----1

$A \rightarrow . a A$  -----2

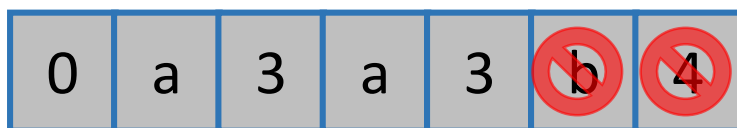
$A \rightarrow . b$  -----3

Reduce 3, as there is one element b in right, (2x1=) 2 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a a b b \$



Here we can say,

$$S \rightarrow . A A \text{ -----1}$$

$$A \rightarrow . a A \text{ -----2}$$

$$A \rightarrow . b \text{ -----3}$$

Now, push A into stack

Shift (S) = Si (1,2,3)  
Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

Input: a a b b \$

A  
↑  
b would be reduced by A

0 a 3 a 3 ~~b~~ ~~4~~ A

Here we can say,

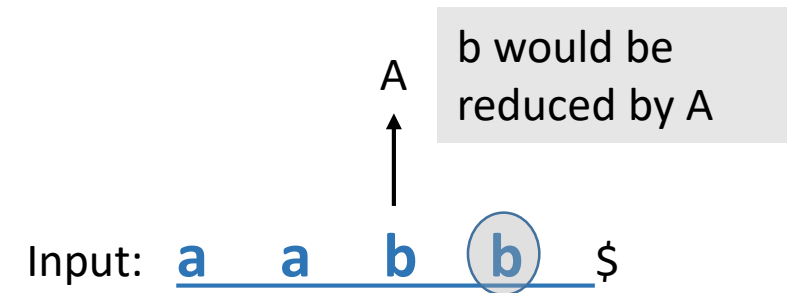
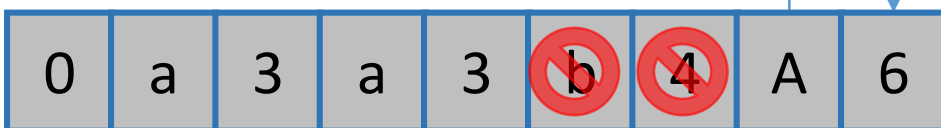
$$S \rightarrow . A A \text{ -----1}$$

$$A \rightarrow . a A \text{ -----2}$$

$$A \rightarrow . b \text{ -----3}$$

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

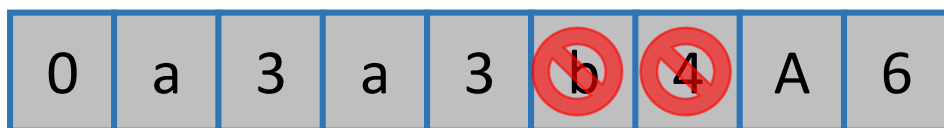
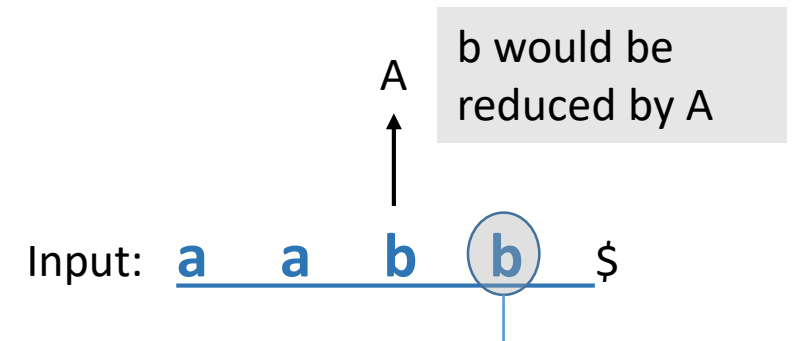
	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1  
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Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1

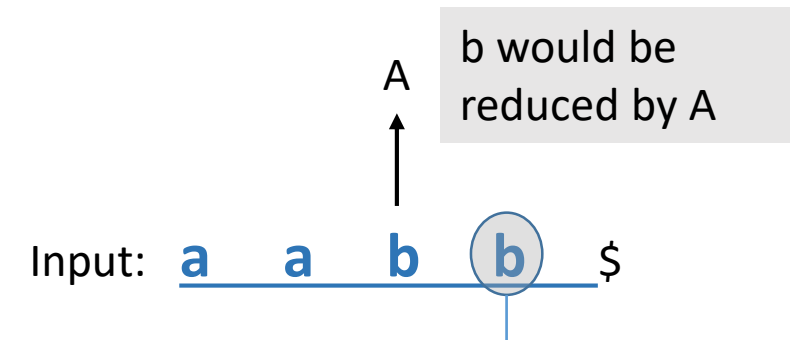
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

Reduce 2, as there is two elements (a,A) in right, (2x2=) 4 elements would pop up

Shift (S) = Si (1,2,3)  
Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1

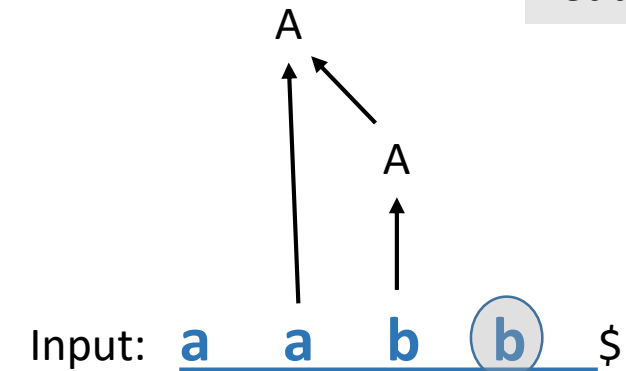
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

Reduce 2, as there is two elements (a,A) in right, (2x2=) 4 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



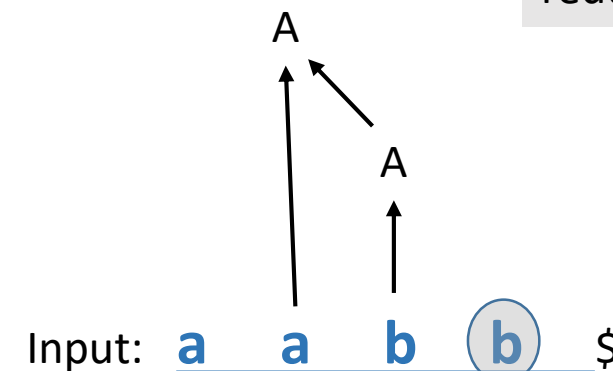
Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Now, push A into stack

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

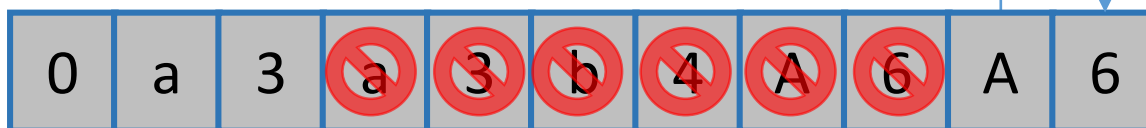
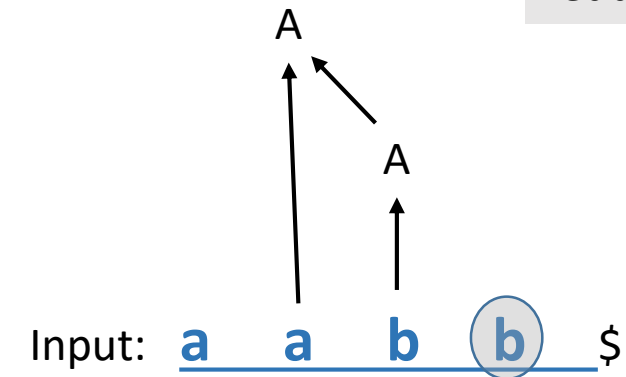
a and A would be reduced by A



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		





Here we can say,  $S \rightarrow . A A$  -----1

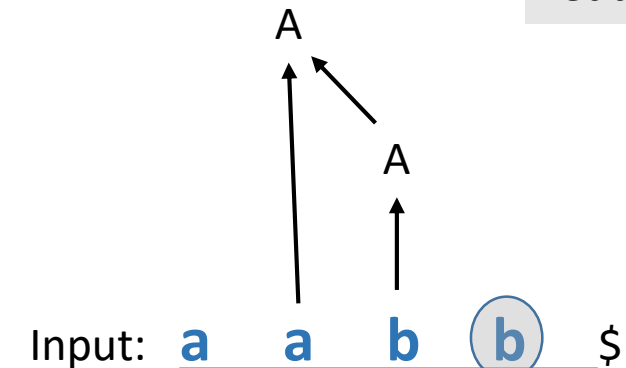
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

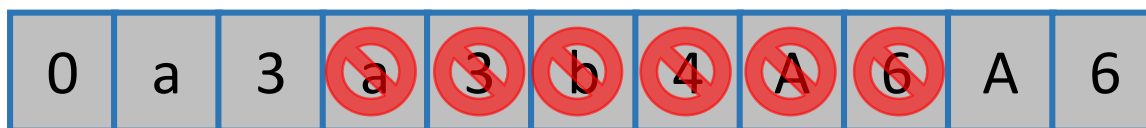
Reduce 2, as there is two elements (a,A) in right, (2x2=) 4 elements would pop up

Shift (S) = Si (1,2,3)  
Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



a and A would be reduced by A



Here we can say,  $S \rightarrow . A A$  -----1

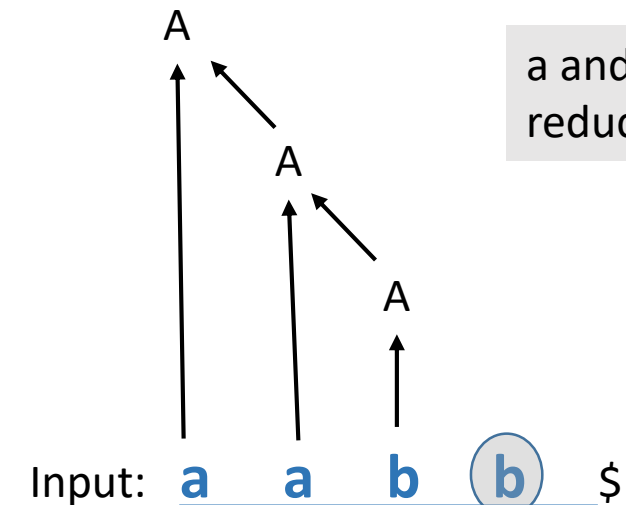
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

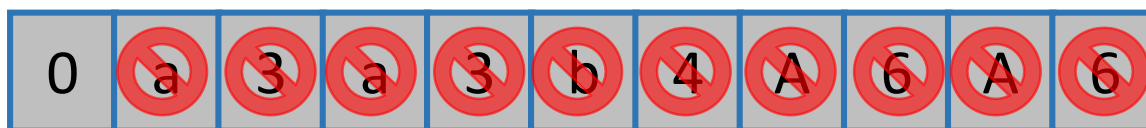
Reduce 2, as there is two elements (a,A) in right, (2x2=) 4 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



a and A would be reduced by A again

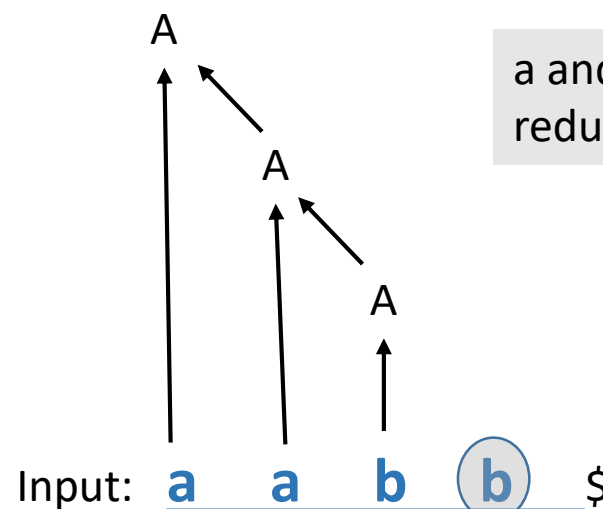


Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Now, push A into stack

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

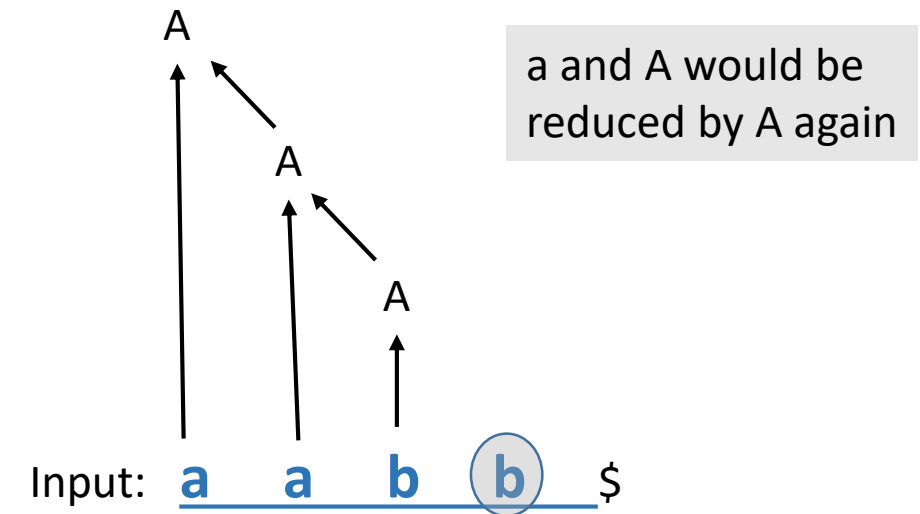
	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

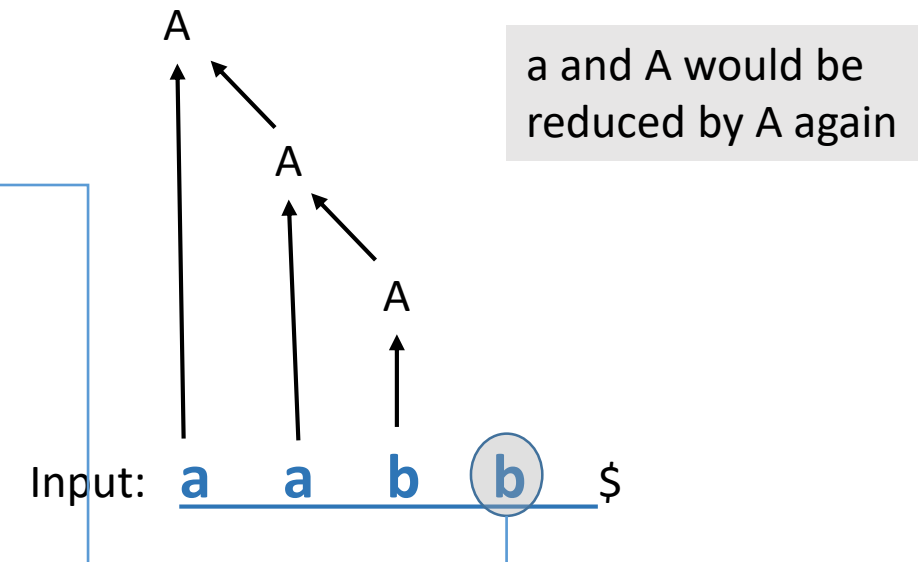
	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1

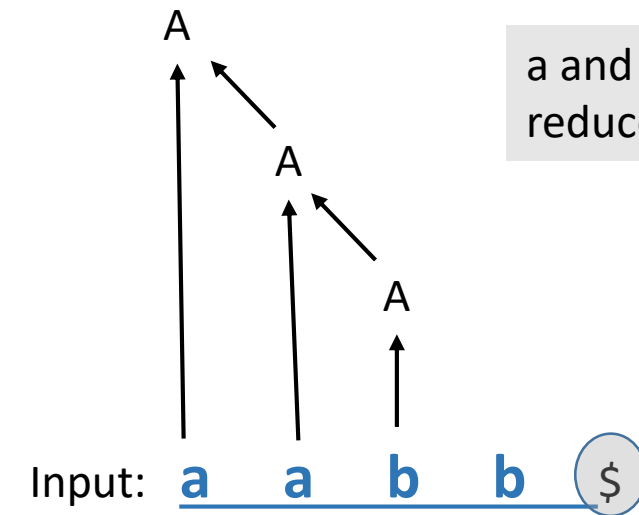
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

Reduce 3, as there is one element (b) in right, (2x1=) 2 elements would pop up

Shift (S) =  $S_i$  (1,2,3)  
Reduce (r) =  $r_i$  (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1

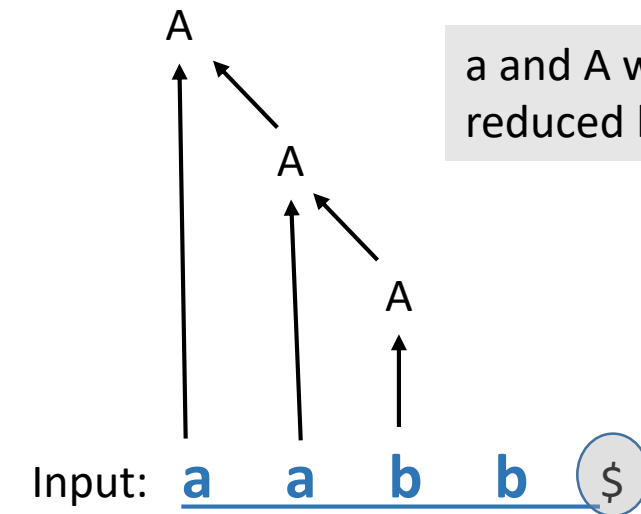
$A \rightarrow . a A$  -----2

$A \rightarrow . b$  -----3

Reduce 3, as there is one element (b) in right, (2x1=) 2 elements would pop up

Shift (S) =  $S_i$  (1,2,3)  
Reduce (r) =  $r_i$  (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



a and A would be reduced by A again

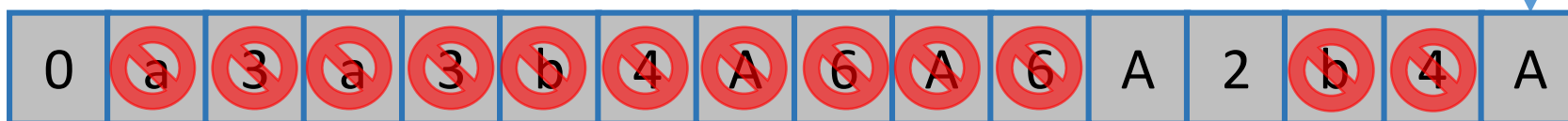
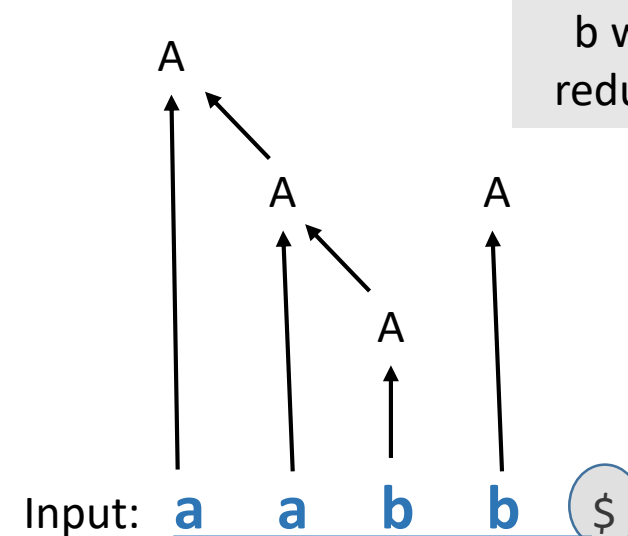


Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Now, push A into stack

Shift (S) = Si (1,2,3)  
 Reduce (r) = ri (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

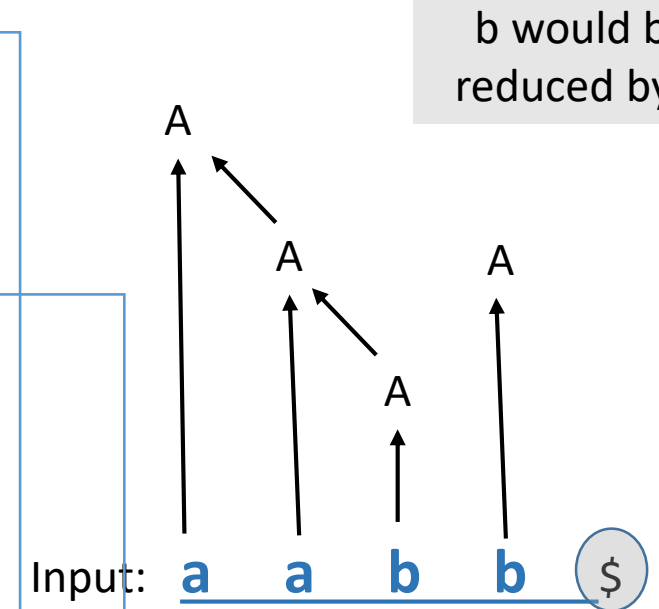




Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) =  $S_i$  (1,2,3)  
 Reduce (r) =  $r_i$  (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



b would be reduced by A



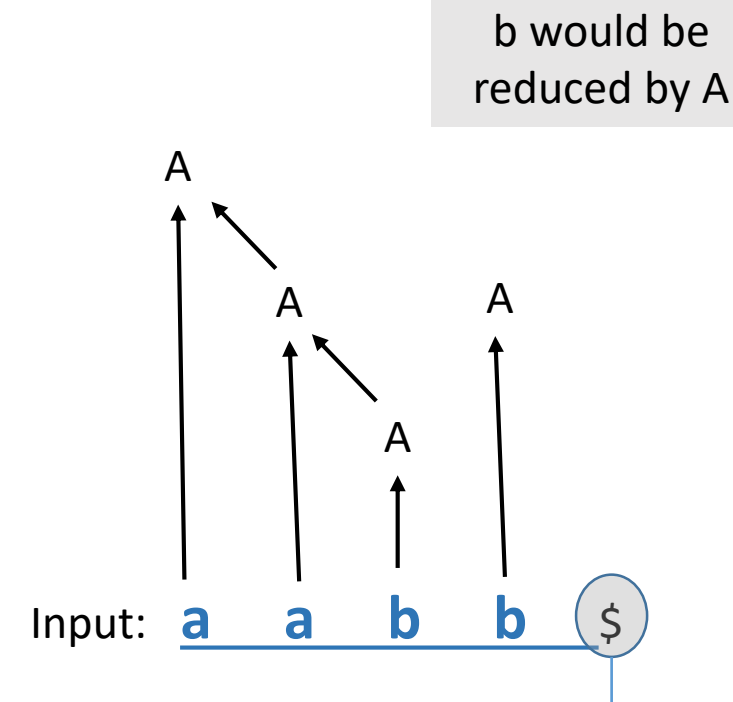
Here we can say,

$S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Reduce 1, as there are two elements (A,A) in right, (2x2=) 4 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,

$$S \rightarrow . A A \text{ -----} 1$$

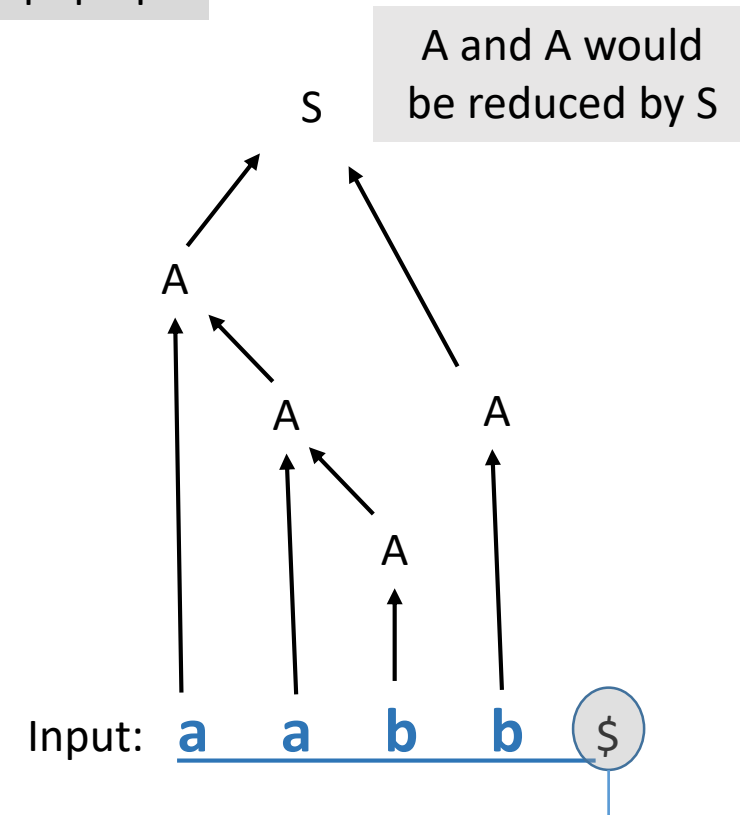
$$A \rightarrow . a A \text{ -----} 2$$

$$A \rightarrow . b \text{ -----} 3$$

Reduce 1, as there are two elements (A,A) in right, (2x2=) 4 elements would pop up

Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		

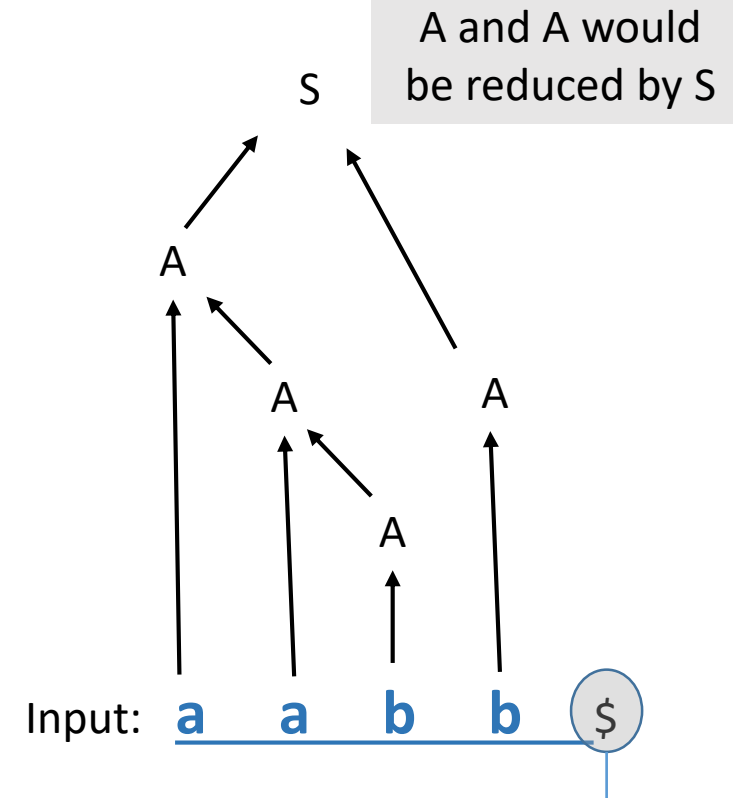


Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Now, push S into stack

Shift (S) =  $S_i$  (1,2,3)  
 Reduce (r) =  $r_i$  (1,2,3)

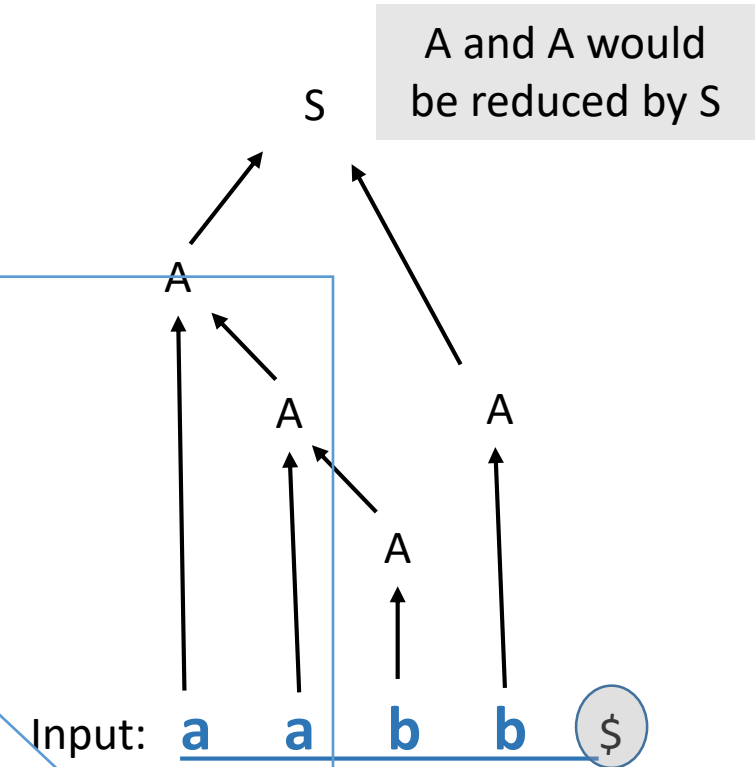
	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) =  $S_i (1,2,3)$   
 Reduce (r) =  $r_i (1,2,3)$

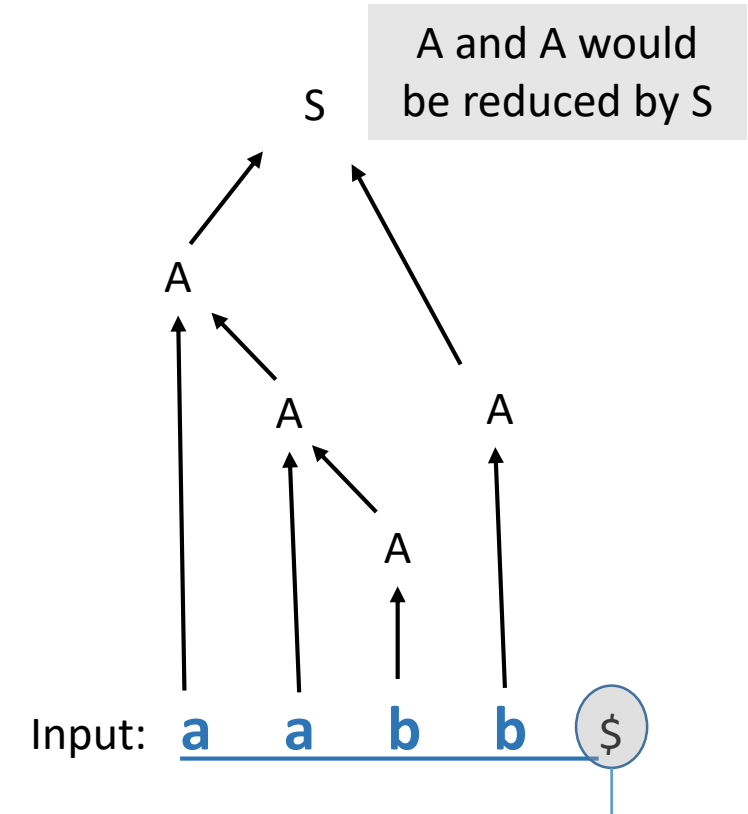
	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



Here we can say,  $S \rightarrow . A A$  -----1  
 $A \rightarrow . a A$  -----2  
 $A \rightarrow . b$  -----3

Shift (S) =  $S_i$  (1,2,3)  
 Reduce (r) =  $r_i$  (1,2,3)

	Action			Goto	
	a	b	\$	A	S
I <sub>0</sub>	S3	S4		2	1
I <sub>1</sub>			Accepted		
I <sub>2</sub>	S3	S4		5	
I <sub>3</sub>	S3	S4		6	
I <sub>4</sub>	r3	r3	r3		
I <sub>5</sub>	r1	r1	r1		
I <sub>6</sub>	r2	r2	r2		



THANK YOU