

Here are the answers to the algebra practice questions.

## Solutions

### 1. Solve the following simultaneous equations:

The solution is  $x = 2$ ,  $y = -1$ .

- Rearrange the second equation to make  $y$  the subject:  $y = 2x - 5$ .
- Substitute this into the first equation:  $3x + 2(2x - 5) = 4$ .
- Solve for  $x$ :  $3x + 4x - 10 = 4$   
 $\text{implies } 7x = 14$   
 $\text{implies } x = 2$ .
- Substitute  $x = 2$  back into  $y = 2x - 5$  to find  $y$ :  $y = 2(2) - 5 = 4 - 5 = -1$ .

### 2. Express as a single fraction in its simplest form:

The answer is

$\frac{1}{2}$ .

- Invert the second fraction and multiply:  
 $\frac{x^2 - 4x + 3}{x^2 - 9}$   
 $\text{times}$   
 $\frac{x + 3}{x - 3}$ .
- Factorise each expression:  
 $\frac{(x - 3)(x - 1)(x - 3)(x + 3)}{(x - 3)(x + 3)}$   
 $\text{times}$   
 $\frac{x + 3}{x - 3}$ .
- Cancel the common factors  $(x - 3)$ ,  $(x - 1)$ , and  $(x + 3)$  to get  
 $\frac{1}{2}$ .

### 3. Solve the equation $3x^2 - 7x - 5 = 0$ :

[cite\_start]The solutions are  $x = 2.91$  and  $x = -0.57$ . [cite: 687]

- [cite\_start]Using the quadratic formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  with  $a = 3$ ,  $b = -7$ ,  $c = -5$ . [cite: 1953]

- $x =$   
 $\frac{7 \pm \sqrt{(-7)^2 - 4(3)(-5)}}{2(3)} =$   
 $\frac{7 \pm \sqrt{49 + 60}}{6} =$   
 $\frac{7 \pm \sqrt{109}}{6}.$
- $x$   
 $\approx$   
 $\frac{7 \pm 10.446}{6}.$
- $x$   
 $\approx 2.91$  or  $x$   
 $\approx -0.57.$

#### 4. Make x the subject of the formula:

The answer is  $x =$

$$\frac{3y + 1}{y - 2}.$$

- $y(x - 3) = 2x + 1$   
 $\implies yx - 3y = 2x + 1.$
- Gather the x terms on one side:  $yx - 2x = 3y + 1.$
- [cite\_start]Factor out x:  $x(y - 2) = 3y + 1.$  [cite: 493]
- Divide to solve for x:  $x =$   
 $\frac{3y + 1}{y - 2}.$

#### 5. Find their present ages:

The **father is 40 years old** and the **son is 18 years old**.

- Let the father's age be F and the son's age be S.
- Equations:  $F + S = 58$  and  $F + 4 = 2(S + 4).$
- From the first equation,  $F = 58 - S.$
- Substitute this into the second equation:  $(58 - S) + 4 = 2S + 8$   
 $\implies 62 - S = 2S + 8$   
 $\implies 54 = 3S$   
 $\implies S = 18.$
- $F = 58 - 18 = 40.$

## 6. Simplify the expression:

The answer is  **$16x^3$** .

- $(16x^8)^{\frac{3}{4}} = 16^{\frac{3}{4}} \times (x^8)^{\frac{3}{4}} = ( \sqrt[4]{16} )^3 \times x^{8 \times \frac{3}{4}} = 2^3 \times x^6 = 8x^6$ . [cite: 809, 811]
- $8x^6 \times 2x^{-3} = 16x^{6-3} = 16x^3$ . [cite: 803]

## 7. How long would it take for 6 workers?

It would take **1 hour and 20 minutes**.

- The relationship is  $t = \frac{w^2}{4}$ . [cite: 701]
- Substitute the known values:  $3 = \frac{4^2}{t}$   
 $\implies 3 = \frac{16}{t}$   
 $\implies t = 48$ .
- The formula is  $t = \frac{4w^2}{t}$ .
- For 6 workers:  $t = \frac{4 \times 6^2}{t} = \frac{4 \times 36}{t} = \frac{144}{t}$  hours.
- $\frac{144}{t}$  hours is 1 hour and  $\frac{1}{3}$  of an hour, which is 20 minutes.

## 8. Solve the equation:

There are **no real solutions**.

- Multiply all terms by the common denominator  $x(x+2)$ :  $5x - 3(x+2) = 1x(x+2)$ .
- $5x - 3x - 6 = x^2 + 2x$

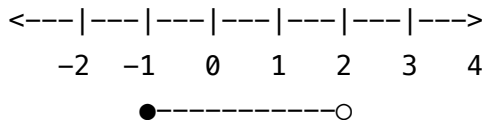
$$\text{implies } 2x - 6 = x^2 + 2x.$$

- $x^2 = -6$ . It is not possible to find a real square root of a negative number.

## 9. Solve the inequality and represent the solution on a number line:

The solution is  $-1 \leq x < 3$ .

- [cite\_start]Add 2 to all parts of the inequality: **ParseError: KaTeX parse error: Undefined control sequence: \< at position 14: -5+2 \le 3x \le 7+2 \implies ...** [cite: 1067]
- [cite\_start]Divide all parts by 3: **ParseError: KaTeX parse error: Undefined control sequence: \< at position 11: -1 \le x \le 3.** [cite: 1064]
- The number line representation is:



[cite\_start](A filled circle at -1 indicates it is included, and an open circle at 3 indicates it is not included). [cite: 1051, 1052, 1055]

## 10. Find the width of the garden:

The width of the garden is **6.25 meters**.

- Using Pythagoras' theorem:  $x^2 + (x + 4)^2 = 12^2$ .
- $x^2 + x^2 + 8x + 16 = 144$   
 $\text{implies } 2x^2 + 8x - 128 = 0$ .
- Simplify by dividing by 2:  $x^2 + 4x - 64 = 0$ .
- Using the quadratic formula:  $x =$   
 $\frac{-4 \pm \sqrt{4^2 - 4(1)(-64)}}{2(1)} =$   
 $\frac{-4 \pm \sqrt{16 + 256}}{2} =$   
 $\frac{-4 \pm \sqrt{272}}{2}$ .
- Since length must be positive, we take the positive root:  $x$   
 $\approx$   
 $\frac{-4 + 16.4922}{2}$   
 $\approx 6.246$ .
- Correct to 3 significant figures, the width is 6.25 m.