Active Learning for Text Classification

Aktivní učení pro klasifikaci textů

Masters's Degree Project

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Academic year: 2019/2020

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Název práce:

Aktivní učení pro klasifikaci textů

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Obor: Aplikované matematicko-stochastické metody

Druh práce: Diplomová práce

Vedoucí práce: **doc. Ing. Václav Šmídl, Ph.D.**, Ústav teorie informace a automatizace

Abstrakt: Modely strojového učení pro klasifikaci jsou založené na učení parametrů black box modelu, které popisují vztah mezi vzorky dat a jejích třídou. Proces sběru dat a jejích labelů pro účely trénování modelu může být komplikovaný a drahý. Množina dat je v mnoha případech větší než množina dostupných labelů, ale našim předpokladem je to, že nové labely můžou být obdržené prostřednictvím dotazu anotátorovi. Aktivní učení je proces výběru takových dat pro anotování, které povedou ke zvýšení diskriminability datasetu. Mnoho různých metod aktivního učení v mnoha různých odvětvích bylo navrženo pro úlohy v nichž se používá učení s učitelem. V tomto projektu jsou popsané a ukázané různé metody aktivního učení pro klasifikaci textů. Navíc jsou porovnávané už existující black box modely a jejích reprezentace neurčitosti. Modely aktivního učení jsou formalizované pomocí teorie rozhodování, kde rozhodnutím je výběr dat bez labelů pro získávání anotace a neurčitost je v parametrech klasifikátorů. Entropie predikce klasifikátoru je vybrána jako očekávaná ztrátová funkce pro rozhodovací úlohu. Modely hlubokého učení dosáhli state-of-the-art výsledků v různých odvětvích zpracování přirozeného jazyka a také v klasifikaci textu. Kombinace aktivního učení pro výběr dat a navržené reprezentace neurčitosti založené na ensemblech hlubokých neuronových sítí dosáhla výrazně lepších výsledků než strategie náhodného výběru nebo aktivní učení s alternativní reprezentací neurčitosti.

Klíčová slova: Aktivní učení, ensemble modely hlubokého učení, ensemble modely neuronových sítí, klasifikace textu, teorie rozhodování, zpracování přirozeného jazyka.

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Abstract: Machine learning approach to classification is based on learning parameters of black box model describing relation between the recorded data samples and their class labels. The process of data labels collection for the purposes of model training can be complex and costly. Therefore, the number of data record is often much higher than the number of labels, but the labels can be obtained by querying an annotator. Active learning is a process of selection of unlabeled data records for which knowledge of the label would bring the highest discriminability of the dataset. Various methods for active learning have been proposed in many different fields that use supervised learning models. In this project, we study suitability of various approaches for active learning of a text classification problem. We compare existing black box classifiers, and representations of their uncertainty. We formalize active learning using decision theory under uncertainty where the decision is which unlabeled data to select for annotation and the uncertainty is in the parameters of the classifier. The expected loss function of the

decision making is chosen as entropy of the classifier predictions. Neural networks have showed state-of-the-art performance in different natural language processing tasks, including text classification. The proposed combination of active learning data selection and uncertainty representation, based on deep learning ensembles algorithm achieves significantly better results than random data selection strategy or active learning with other types of uncertainty represenattion.

Key words: Active learning, decision theory, deep learning ensembles, natural language processing, neural network ensembles, text classification.

Contents

Notation

Symbol	Definition
$\mathbf{x} \in \mathcal{X}$	vector features, i.e. the instance
$\mathbf{y} \in \mathcal{Y}$	one hot encoded label of a specific instance
$\mathbf{X} = \{\mathbf{x}_1, \ldots \mathbf{x}_M\}$	set of available instances
$\mathbf{Y} = \{\mathbf{y}_1, \ldots, \mathbf{y}_M\}$	set of labels that can be provided by an annotator
$\tilde{\mathbf{X}}$	set of training instances
$\tilde{\mathbf{Y}}$	set of training labels
$[x_1, x_2, ..., x_S]^T$	transposed vector
$(\mathbf{x}, \mathbf{y})$	tuple of elements x and y
$\{\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_R\}$	set of vectors $x_1, \ldots x_R$
$a \in \mathcal{A}$	action from a set of all possible actions
$\theta \in \Theta$	decision theory uncertainty parameter
L	loss function
π^*	probability density function of variable θ
$p(\mathbf{y}|\mathbf{x})$	conditional probability density function of label $\mathbf{y}$ given instance $\mathbf{x}$
$\hat{\mathbf{y}}$	expected value of $\mathbf{y}$ given $\mathbf{x}, \mathbf{X}$
$\mathbf{w}$	vector of parameters of a classifier (e.g. SVM or decision tree)
b	SVM bias (scalar)
$\mathbf{W}$	tuple of parameters of a classifier (e.g. Naive Bayes, random forest or neural network (single layer))
$\mathbf{b}$	vector of neural network single layer biases
Ω	tuple of neural network parameters (all weights and biases)
δ	Dirac delta function

Introduction

Active learning strategy lets the machine learning models iteratively and strategically query the labels of some instances for reducing human labeling efforts. This project shows how it is possible to connect active learning and text data. People have already been solving the same problem for anomaly detection [6], image processing [8], etc.

If we take a look at the modern approach of automating the labeling process of a huge amount of unlabeled data, it is not optimal. People are randomly choosing unlabeled text data. These data are annotated by the subject matter experts, and used for training and testing the models. If the model performance is weak after the training, more text documents are selected and annotated. This approach is costly because nobody knows how many text documents must be selected to have good model scores. Our active learning strategy proposes a selection of unlabeled text data that the model is not certain about. Unlabeled text data are given to a subject matter expert to provide the labels. Discussed problem was introduced almost two decades ago. Some active learning approaches for text classification dates back to 2001 [24], where are shown different querying strategies, and superiority of results of the active learning over random sampling strategies is demonstarted. There is no doubt that active learning strategy brings a lot of advantages. First of all, we are able to start with lower amount of training data, and iteratively extend the dataset. The dataset is extended using the data, which the model is not certain about. In this work, we are extending our dataset with only one sample per active learning iteration. However, it was also shown that the strategies, which sample batches with more than one sample, also perform good results [2]. Thus, based on the active learning approach, the model will get much more information from non-randomly chosen text samples.

The project describes different algorithms formulation with respect to decision theory, and then the connection of all the methods to active learning theory. The main focus of this work is on deep neural networks and ensemble models of their uncertainty. It was shown in [23] that ensemble deep learning algorithms give the best performance both for text and image processing data. Plenty of alternative models for active learning for text classifications exits such [8], with use of acquisition functions and dropout, for uncertainty representation e.g. named entity recognition [22] and text classification [13], [5]. We will investigate if the ensembles outperform dropout uncertainty representation for text data, as it was shown in [11] for image classification.

This project also provides the link to Python implementation of active learning algorithms and a comparison of different results gathered with respect to different data. We believe, that the active learning approach is able to significantly reduce the amount of time and expenses needed for automating the text labeling process.

Chapter 1

Introduction to Decision Theory

The process of decision making is defined as a selection of the optimal action from a set of possibilities that can be applied at some operating conditions. The criteria of optimality are formalized by a loss function. The process of selection of the optimal action is, thus, formalized as the optimization problem. However, the operating conditions are often not known exactly, since we have incomplete information about them. Therefore, we will use the theory of decision making under uncertainty [3], where the uncertainty is represented by probability density functions. We will now briefly review the theoretical background.

1.1 Decision Theory

The theory of decision making has three basic elements: i) the set of possible actions $\mathcal{A}$ from which we should select an optimal action $a^* \in \mathcal{A}$, ii) the vector $\theta \in \Theta$ defining operating conditions under which we make the decision, where Θ is the parameter space, iii) the loss function

$$L = L(\theta, a), \tag{1.1}$$

that defines our preference of the action, in the sense that action a which has the lowest value from the action set of the loss function is preferred. For complete knowledge of the operating conditions θ, the task is turned into simple optimization of (1.1). However, with incomplete information, we have to consider a range of possible states θ. The theory of decision making under uncertainty [3] defines the expected loss function that takes into account the uncertainty.

Definition 1. [3]If $\pi^*(\theta)$ is the probability distribution of θ at the time of decision making, the *Bayesian expected loss* of an action a is

$$\rho(\pi^*, a) = \mathbb{E}_{\pi^*}[L(\theta, a)] = \int_{\Theta} L(\theta, a)\pi^* d\theta. \tag{1.2}$$

Based on definition 1.2, the optimal action is defined as the one that minimizes the expected loss:

$$a^* = \underset{a \in \mathcal{A}}{\operatorname{argmin}} \, \mathbb{E}_{\pi^*}[L(\theta, a)]. \tag{1.3}$$

The key task of the application of decision theory is the choice of the action space, parameter space, loss function, and method of evaluating the probability measure. In the following sections, we discuss examples of the application of the theory to the problem of supervised learning and active learning, respectively.

1.2 Decision Theory for Supervised Learning

Supervised learning is defined as learning from the data with a known target value. Specifically, for the classification problem, the target value is the class, where each data point belongs.

We would like to commence our formal definition with the data. Let $\mathbf{x} \in \mathcal{X} \subset \mathbb{R}^n$ and $\mathbf{y} \in \mathcal{Y} = \{[0, 1]^T, [1, 0]^T\}$, where $\mathbf{x}$ is the feature vector of size n, and $\mathbf{y}$ is its label assigned to the data instance $\mathbf{x}$ from space $\mathcal{X}$. Each value from space $\mathcal{Y}$ can be represented using one hot representation, which is a vector consisting of ones and zeros. In the case of binary classification $\mathbf{y} \in \{[0, 1]^T, [1, 0]^T\}$, where the first class is represented as $\mathbf{y} = [1, 0]^T$ and the second class is represented as $\mathbf{y} = [0, 1]^T$. As a good example of the previous definition, $\mathbf{x}$ can be a text document (represented as a vector in order to meet the definition above) and $\mathbf{y}$ can be its category, such as sports or comedy. As seen from this example, the label and the text are forming a tuple. In this work we are considering our data as tuples of variables $(\mathbf{x}, \mathbf{y}) \in \mathcal{X} \times \mathcal{Y}$.

Basing on the data definitions from the previous part, we can assume that $\mathcal{X} \times \mathcal{Y}$ is an infinite set and $(\mathbf{x}, \mathbf{y})$ is a sample from this set. We assume, that all available data tuples are sampled independently from a joint probability density function $p(\mathbf{x}, \mathbf{y})$. If $p(\mathbf{x}, \mathbf{y})$ was known, the optimal classifier $p(\mathbf{y}|\mathbf{x})$ can be obtained by the chain rule of probability

$$p(\mathbf{x}, \mathbf{y}) = p(\mathbf{y}|\mathbf{x})p(\mathbf{x}). \tag{1.4}$$

However, since we do not know the analytical form of the joint probability distribution, we aim at selecting the best possible approximation within a chosen class. Specifically, we choose a parametric form $p(\mathbf{y}|\mathbf{x}, a)$, where a is the parameter to be optimized.

It remains to choose the form of representation of the joint probability distribution. We will consider the uncertainty θ to be represented by empirical distribution:

$$\pi^* = p(\mathbf{x}, \mathbf{y}) = \frac{1}{N} \sum_{i=1}^{N} \delta(\mathbf{x} - \mathbf{x}_i, \mathbf{y} - \mathbf{y}_i) \tag{1.5}$$

where $\mathbf{x}_i, \mathbf{y}_i$ are elements of training set $(\tilde{\mathbf{X}} \subset \mathcal{X}, \tilde{\mathbf{Y}} \subset \mathcal{Y})$. The training set is usually a subset of all available data on which the optimization is performed, the rest of the data is used for validation [26].

1.2.1 Decision Theory and Support Vector Machine Algorithm

In this subsection, we will continue the construction of the decision theory on the example of Support Vector Machine (SVM) method. For simplicity, let us consider a linearly separable dataset. From the theoretical perspective, SVM constructs a hyperplane in high dimensional space. In this case, our decision (action) is a hyperplane that will separate two classes. Equation of the hyperplane can be written as $f(\mathbf{x}, \mathbf{w}, b) = \mathbf{w}^T \mathbf{x} + b$, where $\mathbf{w} \in \mathbb{R}^n$ is a set of hyperplane parameters and $b \in \mathbb{R}$ is a bias. As a result, action space is represented as $(\mathbb{R}^n, \mathbb{R}) = \mathcal{A}$ and as a consequence tuple $(\mathbf{w}, b) \in \mathcal{A}$. From this knowledge, we consider the uncertainty θ described with (1.5) that meets the condition of the limitation on $\Theta = (\tilde{\mathbf{X}} \subset \mathcal{X}, \tilde{\mathbf{Y}} \subset \mathcal{Y})$. Consider loss function (1.1) that can be written as

$$L = L(\mathbf{x}, \mathbf{y}, \mathbf{w}, b). \tag{1.6}$$

The following task is to understand how good is our action (hyperplane estimation) with respect to the dataset. We can choose different types of loss functions, such as cross entropy, hinge loss, etc.. The most basic approach for SVM method is the hinge loss function [20] which is defined as

$$L(\mathbf{x}, \mathbf{y}, \mathbf{w}, b) = \max(0, 1 - y\hat{y}(\mathbf{x}, \mathbf{w}, b)), \tag{1.7}$$

where $\hat{y}(\mathbf{x}, \mathbf{w}, b) = \mathbf{w}^T \mathbf{x} + b$ and $y = \mathbf{y}_1$.

In terms of the SVM method, we want to find such a hyperplane that will label input values as the first class, if it is "above" the hyperplane and as the second class, if it is "below" the hyperplane. At this point, a very important assumption will be introduced. In order to find an optimal hyperplane, we assume, that the data $\tilde{\mathbf{X}}$ and its labels $\tilde{\mathbf{Y}}$ fully describe spaces $\mathcal{X}$ and $\mathcal{Y}$. Thus, the uncertainty of the decision task can be defined as (1.5).

Using (1.2) we can evaluate expected loss function for SVM as follows

$$\mathbb{E}_{\pi^*} L = \int_{\mathcal{X} \times \mathcal{Y}} L(\mathbf{x}, \mathbf{y}, \mathbf{w}, b) p(\mathbf{x}, \mathbf{y}) d(\mathbf{x}, \mathbf{y}),$$

$$= \int_{\mathcal{X} \times \mathcal{Y}} \max(0, 1 - y_1 \hat{y}(\mathbf{x}, \mathbf{w}, b)) \frac{1}{N} \sum_{i=1}^{N} \delta(\mathbf{x} - \mathbf{x}_i, \mathbf{y} - \mathbf{y}_i) d(\mathbf{x}, \mathbf{y}),$$

$$= \frac{1}{N} \sum_{i=1}^{N} \max(0, 1 - y_{1,i} \hat{y}(\mathbf{x}_i, \mathbf{w}, b)),$$

where $\hat{y}(\mathbf{x}_i, \mathbf{w}, b) = \mathbf{w}^T \mathbf{x}_i + b$ and $y_{1,i}$ is first component of $i - $th vector $\mathbf{y}_i$. Expect loss function for SVM can be written as

$$\rho(\mathbf{x}_i, \mathbf{w}, b) = \frac{1}{N} \sum_{i=1}^{N} \max(0, 1 - y_i(\mathbf{w}^T \mathbf{x}_i + b)). \tag{1.8}$$

1.2.2   Decision Theory and Algorithm Based on Neural Network Function

1.2.2.1   Neural Network

Neural Network (NN) is a mapping that has the instance $\mathbf{x} \in \mathcal{X}$ on its input predicted value of the label $\hat{\mathbf{y}}$ on the output. In this part of the work, our prior interest is focused around Feed Forward Neural Network algorithm, that assigns input value to a specific class.

The first layer of NN is defined as

$$\mathbf{a}_1 = \mathbf{W}_1^T \mathbf{x} + \mathbf{b}_1, \tag{1.9}$$

where $\mathbf{W}_1$ is matrix of weights and $\mathbf{b}_1$ is a vector of bias values. The first layer is called the input layer.

Further layers of NN are formed as

$$\mathbf{a}_k = \mathbf{W}_k^T f(\mathbf{a}_{k-1}) + \mathbf{b}_k, \ k = \{2, ..., K - 1\}. \tag{1.10}$$

As seen from equation (1.10), neurons from each layer (except input layer) take linear combination of the neurons from the previous layer. Function f is an activation function. The activation function is defined as a non-decreasing, continuous function. The most commonly used activation functions are sigmoid, relu, elu, and hyperbolic tangence functions [4].

Output values are computed with

$$\hat{\mathbf{y}} = f_{sm} \left(\mathbf{W}_K^T f(\mathbf{a}_{K-1}) + \mathbf{b}_K \right), \tag{1.11}$$

where f_{sm} is the softmax function, that is typically used for classification problems. The softmax function is defined as

$$f_{sm,i} = \frac{\exp(\mathbf{z}_i)}{\sum_{i=1}^{2} \exp(\mathbf{z}_i)},$$

where

$$\mathbf{z} = \mathbf{W}_K^T f(\mathbf{a}_{K-1}) + \mathbf{b}_K$$

is an output vector before the activation function is applied. The output vector has the same size as label $\mathbf{y}$.

1.2.2.2 Decision Theory

Decision theory construction for the algorithm, based on a neural network function, is mostly the same as in 1.2.1. However, in this case, our decision is to find estimate $\hat{\mathbf{y}} = \hat{\mathbf{y}}(\mathbf{x}, \Omega)$ of the probability density function $p(\mathbf{y}|\mathbf{x})$, where $\mathbf{x}$ is the input data, $\Omega = (\mathbf{W}_1, ...\mathbf{W}_K, \mathbf{b}_1..., \mathbf{b}_K)$ is a collection of all neural network function parameters and biases. Action space $\mathcal{A}$ will be the parameters' and biases' space of $\hat{\mathbf{y}}$. Same as in 1.2.1 we can define $(\mathbf{x}, \mathbf{y})$ are parameters of the loss function and $\mathcal{X} \times \mathcal{Y}$ is a parameters' space. Another example of loss functions that we will use is the cross entropy loss function, which is defined as

$$L(\mathbf{x}, \mathbf{y}, \Omega) = -y_1 \ln\left(\hat{y}_1(\mathbf{x}, \Omega)\right) - y_2 \ln\left((\hat{y}_2(\mathbf{x}, \Omega)\right), \tag{1.12}$$

where $\mathbf{y} = [y_1, y_2]^T$ and $\hat{\mathbf{y}} = [\hat{y}_1, \hat{y}_2]^T$. With the usage of the given dataset, where $\forall i \in \{1, .., N\}$, $(\mathbf{x}_i, \mathbf{y}_i) \in (\tilde{\mathbf{X}} \subset \mathcal{X}, \tilde{\mathbf{Y}} \subset \mathcal{Y})$ are independent identically distributed, we can approximate $p(\mathbf{x}, \mathbf{y})$ as (1.5). Applying definition (1), expected loss for the algorithm based on a neural network function is evaluated as

$$\mathbb{E}_{\pi^*} L = \int_{\mathcal{X} \times \mathcal{Y}} L(\mathbf{x}, y, \Omega) p(\mathbf{x}, \mathbf{y}) d(\mathbf{x}, \mathbf{y}),$$

$$= -\int_{\mathcal{X} \times \mathcal{Y}} \left(y_1 \ln\left(\hat{y}_1(\mathbf{x}, \Omega)\right) + y_2 \ln\left((\hat{y}_2(\mathbf{x}, \Omega)\right)\right) \frac{1}{N} \sum_{i=1}^{N} \delta(\mathbf{x} - \mathbf{x}_i, \mathbf{y} - \mathbf{y}_i) d(\mathbf{x}, \mathbf{y}),$$

$$= -\frac{1}{N} \sum_{i=1}^{N} \left(y_1 \ln\left(\hat{y}_1(\mathbf{x}, \Omega)\right) + y_2 \ln\left((\hat{y}_2(\mathbf{x}, \Omega)\right)\right), \tag{1.13}$$

where $\mathbf{y} = [y_1, y_2]^T$ and $\hat{\mathbf{y}} = [\hat{y}_1, \hat{y}_2]^T$.

1.2.2.3 Parameters Estimation

In further sections, we are going to introduce more methods based on Neural Networks, which will slightly differ between each other. Thus, we would like to cover more theory around parameters estimation. The very simple, but efficient method is Gradient Descent. This method is based on equation

$$\hat{\Omega}_{n+1} = \hat{\Omega}_n - \eta_n \nabla L(\tilde{\mathbf{X}}, \tilde{\mathbf{Y}}, \hat{\Omega}_n, Z_n), \tag{1.14}$$

where $\hat{\mathbf{\Omega}}_n$ is the $n-$th iteration value of gradient descent of NN weights and its biases that converges to $\hat{\Omega}$. Value of $\nabla L(\mathbf{X}, \mathbf{Y}, \hat{\Omega}_n, Z_n)$ is a gradient of a loss function and η_n is the $n-$th iteration of value, that in terms of NN is defined as learning rate with a decay. Term Z_n represents indices from X and Y, that are used in the $n-$th iteration of a loss function. Learning rate decay is not an obligatory feature. It can be constant as well. However, the best performance is obtained when the learning rate is estimated from the data, which is the main idea of adaptive methods, such as RMSProp or ADAM [10].

The usual gradient descent is an efficient method for complex $\hat{\mathbf{y}}(\mathbf{x}, \Omega)$ but may struggle with local minima. In this case, the algorithm may stop iterating even in a very shallow local minimum. Due to the complex functions $\hat{\mathbf{y}}(\mathbf{x}, \Omega)$, the loss function of its approximation will be non-convex with a large amount of local minima and maxima. Multiple solutions to this problem have been proposed in the form of Gradient Descent with momentum, or Stochastic Gradient Descent (SGD) [4]. In comparison to standard Gradient Descent, the key difference is that SGD allows us to use only a small subset of all data points (minibatch) from the full training dataset in order to calculate the step [4]. The minibatch is represented with value Z_n that says which training indices to use. The data samples (minibatch) are picked randomly at each step.

In this work, we are using the ADAM optimization [10], which is a stochastic gradient optimization, including an adaptation of the learning rate as well as the coefficient of the momentum.

1.2.3 Decision Theory and Naive Bayes Algorithm

Naive Bayes algorithm is a bit different from the algorithm based on neural networks and SVM. In the case of Naive Bayes, we want to estimate $p(\mathbf{W}|\mathbf{x}, \mathbf{y})$, where $\mathbf{W} = (\mathbf{w}_1, \mathbf{w}_2, ..., \mathbf{w}_n) \subset \mathcal{W}$ is a collection of parameters of individual classifiers, and will be used as an action ($a = \mathbf{W}$, $a \in \mathcal{A}$) it the following decision task. The reason why we look for an estimate of the $p(\mathbf{W}|\mathbf{x}, \mathbf{y})$ but not $p(\mathbf{y}|\mathbf{x}, \mathbf{W})$ is due to $p(\mathbf{y}|\mathbf{x}, \mathbf{W})$ normalization constant. The normalization constant would be dependent on the set of parameters $\mathbf{W}$. That fact would make our computations very complicated. In order to proceed with the loss function construction, we would like to go through Naive Bayes (NB) method.

1.2.3.1 Naive Bayes

Consider a binary classification problem. With the usage of the Bayes rule, we can rewrite $p(\mathbf{W}|\mathbf{x}, \mathbf{y})$ as follows

$$p(\mathbf{W}|\mathbf{x}, \mathbf{y}) = \frac{p(\mathbf{y})p(\mathbf{x}|\mathbf{y}, \mathbf{W})p(\mathbf{W})}{\int_{\mathcal{W}} p(\mathbf{x}, \mathbf{y}|\mathbf{W})p(\mathbf{W})d\mathbf{W}}, \tag{1.15}$$

where $\mathcal{W}$ is the space of possible values of $\mathbf{W}$.

Naive Bayes method introduces a very strong assumption in equation (1.15). This assumption says that features of vector $\mathbf{x} = [x_1, x_2, ..., x_n]^T$ are conditionally independent. As a result, the estimation of $p(\mathbf{W}|\mathbf{x}, \mathbf{y})$ can be written as

$$\tilde{p}(\mathbf{W}|\mathbf{x}, \mathbf{y}) = \frac{1}{Z}p(\mathbf{y})p(\mathbf{W})\prod_{i=1}^{n} (p(x_i|y_1, \mathbf{w}_i)^{y_1} p(x_i|y_2, \mathbf{w}_i)^{y_2}), \tag{1.16}$$

where $\mathbf{y} = [y_1, y_2]$, $\mathbf{W} = \{\mathbf{w}_1, \mathbf{w}_2, ..., \mathbf{w}_n\}$, and Z is a normalizing constant.

1.2.3.2 Decision Theory

We want to maximize probability $\tilde{p}(\mathbf{W}|\mathbf{x}, \mathbf{y})$. As a result, using (1.16) loss function L will be represented as

$$L(\mathbf{y}, \mathbf{x}, \mathbf{w}) = -\log(\tilde{p}(\mathbf{W}|\mathbf{x}, \mathbf{y}), \tag{1.17}$$

$$= \log(Z) - \log(p(\mathbf{y})) - \log(p(\mathbf{W})) - \sum_{i=1}^{n} \log(p(x_i|y_1, \mathbf{w}_i)^{y_1} p(x_i|y_2, \mathbf{w}_i)^{y_2}). \tag{1.18}$$

Same as in 1.2.1 and 1.2.2, we will assume that we can approximate $p(\mathbf{x}, \mathbf{y})$ as 1.5. From this moment, everything is ready for expected loss function derivation. The expected loss function for Naive Bayes method is derived as

$$\mathbb{E}_{\pi^*}L = \int_{X \times \mathcal{Y}} L(\mathbf{x}, \mathbf{y}, \mathbf{w})p(\mathbf{x}, \mathbf{y})d(\mathbf{x}, \mathbf{y}),$$

$$\int_{X \times \mathcal{Y}} \left(\xi(\mathbf{W}, \mathbf{y}) - \sum_{i=1}^{n} \log(p(x_i|y_1, \mathbf{w}_i)^{y_1} p(x_i|y_2, \mathbf{w}_i)^{y_2})\frac{1}{N}\sum_{j=1}^{N}\delta(\mathbf{x} - \mathbf{x}_j, \mathbf{y} - \mathbf{y}_j)d(\mathbf{x}, \mathbf{y}),$$

$$\frac{1}{N}\sum_{j=1}^{N}\left(\xi_j(\mathbf{W}, \mathbf{y}_j) - \sum_{i=1}^{n} \log(p(x_{i,j}|y_{1,j}, \mathbf{w}_i)^{y_{1,j}} p(x_{i,j}|y_{2,j}, \mathbf{w}_i)^{y_{2,j}})\right), \tag{1.19}$$

where $\xi(\mathbf{W}, \mathbf{y}) = \log(Z) - \log(p(\mathbf{y})) - \log(p(\mathbf{W}))$ and $\xi_j(\mathbf{W}, \mathbf{y}_j) = \log(Z) - \log(p(\mathbf{y}_j)) - \log(p(\mathbf{W}))$.

1.2.4 Decision Theory and Random Forest Algorithm

In order to work with random forests, we must precisely define decision trees and only then construct a random forest theory.

1.2.4.1 Decision Tree

In this section, we expect our decision tree to give us an estimate $\hat{\mathbf{y}}(\mathbf{x}, \mathbf{w}) \in \{[0, 1]^T, [1, 0]^T\}$, where $\mathbf{w}$ is a vector that describes tree (depth, branches, etc.), for each $\mathbf{x} \in \mathcal{X}$ and $\mathbf{y} \in \mathcal{Y}$. It is very important to mention that for different trees $\mathbf{w}$ can have different dimensionality. Thus, for consistency, we will assume that for all $\mathbf{w} \in \mathcal{W}$ exist a single upper bound, where $\mathcal{W}$ is redefined as a space of tree parameters. As a result, we will make all $\mathbf{w}$ to have the same length. If $\mathbf{w}$ has spare elements, they will be filled with zeros. Decision tree parameters space is $\mathcal{W}$. The loss function action $a \in \mathcal{A}$ will be represented as elements of the action space $\mathcal{A} = \mathcal{W}$. The loss function of a decision tree is a zero-one loss function, defined as

$$L(\mathbf{x}, \mathbf{y}, \mathbf{w}) = \begin{cases} 1, & \mathbf{y} \neq \hat{\mathbf{y}}(\mathbf{x}, \mathbf{w}) \\ 0, & \mathbf{y} = \hat{\mathbf{y}}(\mathbf{x}, \mathbf{w}) \end{cases}. \tag{1.20}$$

With the use of the given data, where $\forall i \in \{1, .., N\}$, $(\mathbf{x}_i, \mathbf{y}_i) \in \tilde{\mathbf{X}} \times \tilde{\mathbf{Y}}$ are independent identically distributed, we can approximate $p(\mathbf{x}, \mathbf{y})$ as (1.5). As a result, the expected loss function for a decision tree can be derived as

$$\mathbb{E}_{\pi^*} L = \int_{\mathcal{X} \times \mathcal{Y}} L(\mathbf{x}, \mathbf{y}, \mathbf{w}) p(\mathbf{x}, \mathbf{y}) d(\mathbf{x}, \mathbf{y}),$$

$$= \int_{\mathcal{X} \times \mathcal{Y}} L(\mathbf{x}, \mathbf{y}, \mathbf{w}) \frac{1}{N} \sum_{i=1}^{N} \delta(\mathbf{x} - \mathbf{x}_i, \mathbf{y} - \mathbf{y}_i) d(\mathbf{x}, \mathbf{y}),$$

$$= \frac{1}{N} \sum_{i=1}^{N} L(\mathbf{x}_i, \mathbf{y}_i, \mathbf{w}),$$

where $\sum_{i=1}^{N} L(\mathbf{x}_i, \mathbf{y}_i, \mathbf{w})$ is (1.20).

The conventional optimization procedure for decision trees is a heuristic, that works as follows. In the process of constructing a decision tree, we choose such feature $x_i \in [x_1, ..., x_n]^T = \mathbf{x}$ that will bring the highest information about the system (e.g. highest entropy of the features). This feature will form the first layer on which a classification rule is designed. Then we add another feature with the highest information gain and construct the second layer. Using this method, we construct nodes and add more and more layers (branches). However, such a procedure can be sub-optimal, and improvement was achieved using a set of decision trees. For this purpose, we will define our decision tree $T(\mathbf{x}, \mathbf{w}_l)$, which has a one-hot encoded classification, i.e. two-dimensional vector $\hat{\mathbf{y}}$ for the binary classification problem. Index l represents the set of parameters for the l-th three.

1.2.4.2 Random Forest

Consider $\mathbf{x} \in \mathcal{X}$ and $\mathbf{y} \in \mathcal{Y}$ as random variables with joint probability density function $p(\mathbf{x}, \mathbf{y})$. We will also assume that $\forall i \in \{1, ..., N\}$, $(\mathbf{x}_i, \mathbf{y}_i) \in \tilde{\mathbf{X}} \times \tilde{\mathbf{Y}}$ are independent identically distributed.

We will use the training set ($\tilde{\mathbf{X}}$ and $\tilde{\mathbf{Y}}$), as a set from which we sample $V \in \mathbb{N}$ sets, $\tilde{\mathbf{X}}_v \subset \tilde{\mathbf{X}}$ and $\tilde{\mathbf{Y}}_v \subset \tilde{\mathbf{Y}}$, $\forall v \in \{1, ..., V\}$. The data $\tilde{\mathbf{X}}_v$ and $\tilde{\mathbf{Y}}_v$ are created with random uniform sampling of indices of instances in $\tilde{\mathbf{X}}$ and $\tilde{\mathbf{Y}}$ without repetition. We, also, want each subset to contain strictly 80% of the data

from $\tilde{\mathbf{X}}$ and $\tilde{\mathbf{Y}}$. As a result, the parameters space for random forests will form tuples of sets $(\tilde{\mathbf{X}}_v, \tilde{\mathbf{Y}}_v)$. Using this theory, we will construct V decision trees $\hat{\mathbf{y}}_v = T(\mathbf{x}, \mathbf{w}_v)$. As a result, the expected loss is

$$\mathbb{E}_{\pi^*} L = \frac{1}{V} \sum_{v=1}^{V} \frac{1}{N_v} \sum_{i=1}^{N_v} L(\mathbf{x}_{i,v}, \mathbf{y}_{i,v}, \mathbf{w}_v) \delta(\mathbf{x} - \mathbf{x}_{i,v}, \mathbf{y} - \mathbf{y}_{i,v}), \tag{1.21}$$

where $(\mathbf{x}_{i,v}, \mathbf{y}_{i,v}) \in (\tilde{\mathbf{X}}_v, \tilde{\mathbf{Y}}_v)$ and N_v is the number of the data samples in $\tilde{\mathbf{X}}_v$ and $\tilde{\mathbf{Y}}_v$. If we assume $\mathbf{w}_v$ to be a random variable, then V decision trees form samples from the probability density function $p(\mathbf{y}|\mathbf{x}, \mathbf{w})$. In other words

$$p(\mathbf{y}|\mathbf{x}, \mathbf{w}_v) = \hat{y}_{v,1}^{y_1} \hat{y}_{v,2}^{y_2}, \tag{1.22}$$

where label $\mathbf{y}$ is written as a one-hot representation, and the estimate is in the same form $\hat{\mathbf{y}}_v = [\hat{y}_{v,1}, \hat{y}_{v,2}]^T$. Thus, we can say that classification probability $p(\mathbf{y}|\mathbf{x})$ can be written as

$$p(\mathbf{y}|\mathbf{x}) = \int_{\mathbf{w} \in \mathcal{A}} p(\mathbf{y}|\mathbf{x}, \mathbf{w}) p(\mathbf{w}) d\mathbf{w}, \tag{1.23}$$

where $\mathcal{A}$ is an action space. With the usage of samples $\mathbf{w}_v$ we can approximate $p(\mathbf{y}|\mathbf{x})$ as

$$p(\mathbf{y}|\mathbf{x}) = \frac{1}{V} \sum_{l=1}^{V} \hat{y}_{v,1}^{y_1} \hat{y}_{v,2}^{y_2}, \tag{1.24}$$

where each decision tree $T(\mathbf{x}, \mathbf{w}_v)$ is constructed with the use of (1.21).

In order to proceed with further sections we define the output of Random Forest as $\hat{\mathbf{y}} = \hat{\mathbf{y}}(\mathbf{x}, \mathbf{W})$, where $\mathbf{W} = \{\mathbf{w}_1, ..., \mathbf{w}_V\} \in \mathcal{W}$ is a set of parameters of specific Random Forest algorithm. We define vector $\hat{\mathbf{y}}$ as

$$\hat{\mathbf{y}} = \frac{1}{V} \sum_{l=1}^{V} \hat{\mathbf{y}}_v. \tag{1.25}$$

1.3 Decision Theory for Active Learning

As mentioned in previous sections, the training set $\tilde{\mathbf{X}} \times \tilde{\mathbf{Y}}$ is only a subset of all available data. It is important that each point $\mathbf{x}$ in the training set has a label $\mathbf{y}$. The labels are expensive to obtain in many situations, and the number N of all available samples $\mathbf{x} \in \mathbf{X}$ is large, while labels are available only for the initial subset $J_0 = \{1, \ldots, N_0\}, N_0 \ll N$. This problem is known as semi-supervised learning.

We consider a setup in which we can ask for a label for an arbitrary $\mathbf{x}$, that can be provided for example by a human (annotator). We assume that getting labels needs some time and is very expensive. The task is to choose which sample we will ask to label.

The active learning problem is defined as a sequence of supervised learning problems. Specifically, we assume that the initial sets for supervised learning are $\mathbf{X}_0 = \{\mathbf{x}_i\}_{i \in J_0}$ and $\mathbf{Y}_0 = \{\mathbf{y}_i\}_{i \in J_0}$. We consider a sequence of U questions $u = \{1, \ldots, U\}$, in each question we select an index j_u and ask to obtain the label $\mathbf{y}_{j_u}$ for data record $\mathbf{x}_{j_u}$. The index set and the data sets are extended as follows

$$J_u = \{J_{u-1}, j_u\}, \qquad\qquad \mathbf{X}_u = \{\mathbf{X}_{u-1}, \mathbf{x}_{j_u}\}, \qquad\qquad \mathbf{Y}_u = \{\mathbf{Y}_{u-1}, \mathbf{y}_{j_u}\}.$$

The task of active learning is to optimize the selection of indices j_u to reach as good classification metrics with as low number of questions as possible. As a result, we have to define the expected loss for each question u that will be dependent on the action and parameter spaces. In this case, we can define our action space as a space of the data indices of the unlabeled data $\mathbf{x}$, $a = j_u \in \mathcal{A}_u = J \backslash J_u$. The

uncertainty of the decision task, if the parameter space Θ of the used classifiers, i.e. $\theta = (\mathbf{w}, \mathbf{b})$ for SVM, $\theta = \Omega$ for NN, $\theta = \mathbf{W}$ for RF and NB. It is very vital to understand, that point estimate of the parameters that was designed in supervised learning is not sufficient for this task. We need full distribution on the parameters because we will integrate over the parameters space. As an example, if we talk about the SVM method, then parameters space for active learning problem will be defined as a set of weights that form a hyperplane. If we talk about the algorithm that is based on a neural network function, then parameters space of the active learning problem will form weights from neurons. We wanted to highlight that parameters space will be different for each problem but the idea for each algorithm is the same.

The decision task for this particular problem can be written as

$$j_u^* = \operatorname*{argmin}_{j_u \in J \setminus J_u}(\mathbb{E}_{\pi_u^*} L^*), \tag{1.26}$$

where $\mathbb{E}_{\pi_u^*} L^*$ is the expected loss that is dependent on an action given question u, and J is the space of all indices. The expected loss for the active learning problem is defined as

$$\mathbb{E}_{\pi_u^*} L^* = \int_{\Theta} L^*(j_u, \theta) \pi_u^* d\theta, \tag{1.27}$$

where $j_u \in J \setminus J_u$, $\theta \in \Theta$ and L^* is a loss function for the active learning problem. Character "$*$" is used only for distinguishing active learning loss from the loss function which is used for different models.

Using this approach, we will be able sequentially select indices from $\mathbf{X}$ and ask for a label from $\mathbf{Y}$, that will help us to get higher scores faster than in the case of a random choice of indices.

1.3.1 Bayesian Approach of Classifiers' Parameters Sampling

Consider that $\mathbf{y} \in \mathcal{Y}$. Let $\hat{\mathbf{y}} = \hat{\mathbf{y}}(\mathbf{x}_{j_u}, \theta_u)$ is an estimate of $\mathbf{y}$. However, in this case output estimate $\hat{\mathbf{y}}$ is represented as a vector of probabilities that $\mathbf{x}_{j_u}$ is assigned to different classes. As an example for a well trained binary classifier, for specific $\mathbf{x}$ that is assigned to $\mathbf{y} = [1, 0]^T$, classifiers estimate of $\mathbf{x}$ can be $\hat{\mathbf{y}} = [0.95, 0.05]^T$. It is interesting that before we can solve the optimization problem with choosing the index j_u, we have to solve the optimization problem of finding $\hat{\mathbf{y}}$. This leads us to supervised learning models that we have discussed in previous sections.

In this section, we would like to construct a theory around π_u^* from equation (1.27). The mentioned distribution is a distribution of the models' parameters, given the training data that can be written as

$$\pi_u^* = p_u(\theta_u | \mathbf{X}_u, \mathbf{Y}_u). \tag{1.28}$$

We do not have explicit form of the pdf. However, we assume that we have Q_u samples $\theta_{u,q} \in \{1_u, ..., Q_u\}$ from $p_u(\theta_u | \mathbf{X}_u, \mathbf{Y}_u)$. As a result $p_u(\theta_u | \mathbf{X}_u, \mathbf{Y}_u)$ can be approximated as

$$\pi_u^* = \frac{1}{Q_u} \sum_{q=1}^{Q_u} \delta(\theta_u - \theta_u^{(q)}), \tag{1.29}$$

where $\delta(\theta_u - \theta_u^{(q)})$ is Dirac delta function centered in $\theta_u^{(q)}$.

1.3.1.1 Parameters Sampling Based on Training Data Subsets

This method is quite general and can be applied to all types of classifiers in this work (Random Forest, SVM, neural network). The idea is very simple. We consider that some data samples in training dataset $\tilde{\mathbf{X}} \times \tilde{\mathbf{Y}}$ are noise corrupted. Thus, it is obvious that we do not want our models to learn from noise

corrupted data. As a result, we would like to randomly sample Q_u subsets from $\tilde{\mathbf{X}}$ with their labels from $\tilde{\mathbf{Y}}$. Let us rewrite it in a more mathematical form.

Assume N_u is the number of samples in $\mathbf{X}_u$. Let $Z_u = \{z_1, ..., z_{N_u^{sub}}\} \subset J_u$, where $N_u^{sub} < N_u$. Let $p(\theta_u|\mathbf{X}_u, \mathbf{Y}_u, Z_u)$ be a probability of model parameters θ_u given $\mathbf{X}_u, \mathbf{Y}_u$ and Z_u. The conditioning in the pdf is defined as a restriction of sets $\mathbf{X}_u$, $\mathbf{Y}_u$ on indices from Z_u. As a result, we can approximate (1.28) as

$$\pi_u^* = p(\theta_u|\mathbf{X}_u, \mathbf{Y}_u) \tag{1.30}$$

$$= \int p(\theta_u|\mathbf{X}_u, \mathbf{Y}_u, Z_u)p(Z_u)dZ_u \tag{1.31}$$

$$= \frac{1}{Q_u} \sum_{q=1}^{Q_u} p(\theta_u|\mathbf{X}_u, \mathbf{Y}_u, Z_u^{(q)}) \tag{1.32}$$

$$= \frac{1}{Q_u} \sum_{q=1}^{Q_u} \delta(\theta_u - \theta_u^{(q)}). \tag{1.33}$$

Sampling from $p(Z_u)$ is very simple. The only thing that must be predefined is N_u^{sub}. After training the model using $\mathbf{X}_u$ and Y_u under restriction Z_u, the vector of model parameters will represent a single sample from π_u^*.

1.3.1.2 SGLD

Unlike the previous section method, SGLD sampling is designed only for neural network based classifiers. SGLD modifies neural network learning algorithm by adding noise in Stochastic Gradient Descent. The conventional stochastic gradient descent of Feed Forward Neural Network was extended in [28] by an additive white noise, which is know as the Stochastic Gradient Langevin Dynamics (SGLD) algorithm. This algorithm provides Bayesian estimate of Neural Network parameters [28]. In essence, when the algorithm is almost trained, the additional noise samples i.i.d parameter values in a neighborhood of the minimum. Using the Bayes rule we can rewrite (1.28) as

$$\pi_u^* = p(\theta_u|\mathbf{X}_u, \mathbf{Y}_u)$$
$$\propto p(\mathbf{X}_u, \mathbf{Y}_u|\theta_u)p(\theta_u). \tag{1.34}$$

Next, we can approximate (1.34) as

$$\pi_u^* = \frac{1}{Q_u} \sum_{q=1}^{Q_u} p(\mathbf{X}_u, \mathbf{Y}_u|\theta_u^{(q)}) \tag{1.35}$$

that results in (1.33). However, for this case, θ must meet some constraints. If we want to sample parameters from its distribution, θ must be independent identically distributed. Based on [28], the updated gradient for SGLD can be written as

$$\hat{\Omega}_{n+1} = \hat{\Omega}_n - \frac{N}{N_{minibatch}} \frac{\eta_n}{2} \Big(\nabla L(\tilde{\mathbf{X}}, \tilde{\mathbf{Y}}, \hat{\Omega}_n, Z_n) \Big) + \epsilon_n, \tag{1.36}$$

$$\epsilon_n \sim \mathcal{N}(0, \eta_n I), \tag{1.37}$$

where N is the number of training data, $N_{minibatch}$ is the number of samples in the minibatch and η_n is the learning rate in $n-$th iteration of the algorithm.

1.3.1.3 Dropout

Dropout is another technique similar to SGLD designed to sample from a neural network parameters distribution [8]. The idea is randomly turn off some neurons while training. Thus, an estimate of $\pi_u^* = p(\theta_u | \mathbf{X}_u, \mathbf{Y}_u)$ is the Dirac function as well 1.29. When the algorithm is almost trained, we are able to start sampling the i.i.d. parameter masks. Samples $\theta^{(q)}$ are generated after each step of the SGD, where the different mask of neural weight and biases is sampled for each q.

1.3.1.4 Deep Ensemble Filter

Deep Ensemble Filter (DENFI) algorithm is an extension of deep ensembles [11]. In case of DENFI algorithm [25], we can approximate (1.28) with the usage of equations (1.34) and (1.33). The equations are the same but a sampling from $p(\theta_u)$ is different. In this work, we propose a modification of the initial DENFI algorithm. The idea of this algorithm is to train an ensemble of Q_u Feed Forward Neural Networks using Stochastic Gradient Descent. In theory, each neural network will find a different local minimum due to different initial weights of neurons and Stochastic Gradient Descent. The beauty of this algorithm is in further training iterations that will be described and shown in further sections. For now, we are only interested in parameters sampling from $p(\theta_u)$, that has been already covered and described.

1.3.2 Active Learning Loss Function

The acquisition function is a function that helps us to decide which data sample is the best for model learning given the model's uncertainty. A wide overview of different acquisition functions is shown in [8] e.g. entropy, information, or mean standard deviation maximization. However, in our work, we decided to use only the entropy loss.

1.3.2.1 Entropy Based Active Learning Loss

The first approach of defining the Active Learning loss function is negative entropy. Basing on the formal entropy definition [21], we can write it as

$$-H(\hat{\mathbf{y}}|\mathbf{x}_{j_u}, \theta_u) = \sum_{r=1}^{R} \hat{y}_r(\mathbf{x}_{j_u}, \theta_u) \log\left(\hat{y}_r(\mathbf{x}_{j_u}, \theta_u)\right), \qquad (1.38)$$

where $\hat{y}_r$ is $r-$th element of the output estimate $\hat{\mathbf{y}}$, and θ is a vector of parameters for specific model. As done in Passive Learning sections we want to find expected loss based on entropy function.

With the usage of previous knowledge, we can derive expected entropy loss as

$$\begin{aligned}
\mathbb{E}_{\pi_u^*} L^* &= \int_{\Theta_u} -H(\hat{\mathbf{y}}|\mathbf{x}_{j_u}, \theta_u) p_u(\theta_u | \mathbf{X}_u, \mathbf{Y}_u) d\theta_u \\
&= \int_{\Theta_u} -H(\hat{\mathbf{y}}|\mathbf{x}_{j_u}, \theta_u) \frac{1}{Q_u} \sum_{q=1}^{Q_u} \delta(\theta_u - \theta_{u,q}) d\theta_u \\
&= \frac{1}{Q_u} \sum_{q=1}^{Q_u} -H(\hat{\mathbf{y}}|\mathbf{x}_{j_u}, \theta_{u,q})) \\
&= \frac{1}{Q_u} \sum_{q=1}^{Q_u} \sum_{r=1}^{R} \hat{y}_r(\mathbf{x}_{j_u}, \theta_{u,q}) \log\left(\hat{y}_r(\mathbf{x}_{j_u}, \theta_{u,q})\right).
\end{aligned} \qquad (1.39)$$

As a result, the minimization of the given expected loss will lead us to a sample with the highest entropy. Thus, we are seeking for the index of the data instance that has maximum predictive entropy. In other words $j_u^* = \operatorname{argmin}_{j \in J \setminus J_u}(\mathbb{E}_{\pi_u^*} L^*)$.

1.3.3 Active Learning

We would like to generalize the active learning part for all described algorithms, in order to estimates $p(\mathbf{y}|\mathbf{x}, \mathbf{X}_u, \mathbf{Y}_u)$ basing on samples from π_u^* in (1.28). In the Supervised Learning section we have derived estimate $\hat{\mathbf{y}}$ of $\mathbf{y}$ for SVMs, Random Forests and Feed Forward Neural Networks. Active Learning algorithm requires distribution over the parameters of the algorithms. We will solve this problem the way that we will get samples from π_u^*, and then approximate probability distribution as (1.28).

In order to estimate $p(\mathbf{y}|\mathbf{x}, \mathbf{X}_u, \mathbf{Y}_u)$, we define Generalized Ensembles Algorithm. SGLD and DENFI can be also represented as generalized ensembles models because parameters sampling (neuron weights sampling) represents different configurations of neural networks. Thus, each sample from π_u^* can be assumed as i.i.d. ensemble. As a result, we will use Q_u ensembles in each step of Active Learning algorithm. Therefore, basing on the previous theory we can approximate $p(\mathbf{y}|\mathbf{x}, \mathbf{X}_u, \mathbf{Y}_u)$ as

$$p(\mathbf{y}|\mathbf{x}, \mathbf{X}_u, \mathbf{Y}_u) = \frac{1}{Q_u} \sum_{q=1}^{Q_u} \hat{\mathbf{y}}_{q,u}. \tag{1.40}$$

1.4 Conclusion

In this section, we have covered the decision theory for both passive and active learning with respect to different algorithms and ensemble approaches. Passive Learning section showed how it is possible to represent SVM, Random Forest, and neural networks in terms of decision theory problem setup. In addition to this, the Active Learning section showed how to represent the uncertainty of the model and parameters sampling for ensembles representation.

Chapter 2

Natural Language Processing Theory

2.1 Text Representation

According to [12], Natural Language Processing (NLP) is a theoretically motivated range of computational techniques for analyzing and representing naturally occurring texts at one or more levels of linguistic analysis for the purpose of achieving human-like language processing for a range of tasks or applications.

In this work we are focused on two techniques, such as TF-IDF [19] and Fast Text Word Embeddings [15]. These methods are used for representation of text in a mathematical form (vectors, matrices). Even though TF-IDF is quite old method for text representation, it is still widely used. However, primary method, that is used in the thesis is the Fast Text Word Embeddings. In this project we are working with text documents (articles and tweets) and their labels. In the beginning of chapter 1 we defined value $\mathbf{x} \in X$ as text features vector. By features vector we mean any kind of text encoding (TF-IDF, Fast Text Word Embedding, etc..).

2.1.1 TF-IDF

Term Frequency - Inverse Document Frequency (TF-IDF) is extremely powerful tool. This text encoding tool is quite simple and efficient. Method's advantage is its popularity. Plenty of packages in different programming languages have implementations of this algorithm. As mentioned in the name of this method, it is composed of two parts as Term Frequency and Inverse Document Frequency. Term Frequency is defined as

$$TF(t, d) = \frac{f_{t,d}}{\sum_{t'} f_{t',d}},$$

where $f_{t,d}$ is number of times of word t in a document d. Inverse Document Frequency is defined as

$$IDF(t, d) = \log \frac{|D|}{|\{d \in D : t \in d\}|},$$

where numerator stand for total number of documents in the corpus and denominator is number of documents where the term t appears. We assume words from corpus D. Thus, the denominator is always greater than zero.

Finally,

$$TF - IDF(t, d) = TF(t, d) \cdot IDF(t, d).$$

2.1.1.1 TF-IDF and Information Theory

In this part is shown the connection of TF-IDF to information theory [1]. Let us first take a look on documents' entropy given word t,

$$
\begin{aligned}
H(D|T = t) &= -\sum_d p(d|t) \log p(d|t) \\
&= \log \frac{1}{|\{d \in D : t \in D\}|} \\
&= -\log \frac{|\{d \in D : t \in D\}|}{D|} + \log |D| \\
&= -IDF(t,d) + \log |D|,
\end{aligned}
\tag{2.1}
$$

where D is a documents' random variable and T is words' random variable. Equation (2.1) is correct under the condition that we have no duplicate documents in the text corpus. Next step is to derive an equation of mutual information of documents and words as follows

$$
\begin{aligned}
M(D,T) &= H(D) - H(D|T) \\
&= -\sum_d p(d) \log p(d) - \sum H(D|T = t) \cdot p(t)_t \\
&= \sum_t p(t) \cdot \left(\log \frac{1}{|D|} + IDF(t,d) - \log |D| \right) \\
&= \sum_t p(t) \cdot IDF(t,d) \\
&= \sum_{t,d} p(t|d) \cdot p(d) \cdot IDF(t,d) \\
&= \frac{1}{|D|} \sum_{t,d} TF(t,d) \cdot IDF(t,d).
\end{aligned}
\tag{2.2}
$$

As seen from (2.2) TF-IDF has really good explanatory definition based on information theory. As a result, it is one more advantage of this method usage. However, here is one big disadvantage that can be very crucial. The higher amount of words is, the bigger and sparser the vectors that represent each document, will be.

2.1.2 Fast Text and CBOW Word Embeddings

Term "embedding" means a set of language modeling and feature learning techniques in natural language processing, where words or phrases from the vocabulary are mapped to vectors of real numbers. Plenty of word embedding methods based on neural networks and co-occurrence matrices exist nowadays. Word embeddings are used as pretrained models. Words' encoding is used to encode the text, and then text encoding is used for different purposes, such as classification, clustering, etc..

The principle of word embeddings based on neural networks is explained in this section. We decided to describe Continuous Bag of Words Model (CBOW) because Fast Text word embeddings model is a modification of this method, and CBOW covers all main theoretical aspects.

2.1.2.1 CBOW Word Embeddings

The CBOW embeddings have been introduced in [14]. Consider the sentence "A beautiful cat jumped over a puddle". We choose the window of $2m + 1$, $m \in \mathbb{N}$ words and try to predict the word with index

$m + 1$, basing on the context of size $2m$, where m words are before the prediction word and m words are after the prediction word. We would like to treat tuple ("a", "beautiful", "cat", 'over', "a', "puddle") as a context, and based on the context we would like to predict or generate the word "jumped". This type of model is the Continuous Bag of Words (CBOW) model. Let the known parameters in our model be the contexts, represented with one-hot encoded word vectors. The input one hot encoded word vector is denoted as $\mathbf{c}^{(c)}$, where c is the position of the word in the context. The predicted context word is defined as $\mathbf{c}_{\text{pred}}$. We create two matrices, $\mathbf{E} \in \mathbb{R}^{E \times |\mathbf{v}|}$ and $\mathbf{U} \in \mathbb{R}^{|\mathbf{v}| \times E}$. Where E is an arbitrary size which defines the size of our embedding space and $|\mathbf{v}|$ is a vocabulary size of all words from all contexts. $\mathbf{E}$ is the input word matrix, such that the i-th column of $\mathbf{E}$ is the E-dimensional embedded vector for word $\mathbf{c}_i$. We denote this $E \times 1$ vector as $\mathbf{e}_i$. Similarly, $\mathbf{U}$ is the output word matrix. The k-th row of $\mathbf{U}$ is an E-dimensional embedded vector for word $\mathbf{c}_{\text{pred},k}$ when it is an output of the model. We denote this row of $\mathbf{U}$ as $\mathbf{u}_k$.

The matrices $\mathbf{E}$ and $\mathbf{U}$ are obtained by the following sequence of actions:

- We generate our one hot word vectors $(\mathbf{c}^{(c-m)}, ..., \mathbf{c}^{(c)}, ..., \mathbf{c}^{(c+m)})$ for the input context of size $2m$

- We get our embedded word vectors for the context $(\mathbf{e}_{c-m} = \mathbf{E}\mathbf{c}^{(c-m)}, \mathbf{e}_{c-m+1} = \mathbf{E}\mathbf{c}^{(c-m+1)}, ..., \mathbf{e}_{c+m} = \mathbf{E}\mathbf{c}^{(c+m)})$

- Average these vectors to get $\tilde{\mathbf{e}} = \frac{\mathbf{e}_{c-m}+\mathbf{e}_{c-m+1}+...+\mathbf{e}_{c+m}}{2m}$

- Generate a score vector $\mathbf{z} = \mathbf{U}\tilde{\mathbf{e}}$

- Turn the scores into probabilities

$$\hat{\mathbf{c}}_{\text{pred}} = \text{softmax}(\mathbf{z}) \tag{2.3}$$

- We optimize $\mathbf{E}$ and $\mathbf{U}$ to maximize the match between the predicted vector $\hat{\mathbf{c}}_{\text{pred}}$, and the true vector $\mathbf{c}_{\text{pred}}$, which also happens to be the one hot vector of the actual word.

The described method can be interpreted as a Feed Forward Neural Network with only input and output layers. The optimization is provided with respect to cross entropy loss function

$$L = \sum_{i=1}^{|\mathbf{v}|} \mathbf{c}_{\text{pred},i} \log(\hat{\mathbf{c}}_{\text{pred},i}), \tag{2.4}$$

where $\hat{\mathbf{c}}_{\text{pred}}$ is softmax (2.3) function. When the weights in a neural network are trained, matrix $\mathbf{E}$ represents $|\mathbf{v}|$ word embeddings where i-th word from vocabulary $\mathbf{v}$ is i-th row in $\mathbf{E}$.

Previously, we mentioned that all the methods take an instance (text) $\mathbf{x}$ as an input value and predict its class. Instance $\mathbf{x}$ is calculated as a mean value from all words embeddings in the text

$$\mathbf{x}_i = \frac{1}{|\mathcal{D}_i|} \sum_{j \in \mathcal{D}_i} \mathbf{E}\mathbf{c}^{(j)},$$

where $\mathcal{D}_i$ is the set of indices of all words in i-th document in the common vocabulary.

2.1.2.2 Fast Text Word Embeddings

As mentioned previously, the Fast Text method is a CBOW modification. The main modification is that Fast Text is taking into account not only words but also suffixes of words. The words are split into suffixes and as a result, they can handle understanding of the context better.

In this thesis, we used pretrained Fast Text models [15] consisting of 1 million word vectors trained on Wikipedia 2017, UMBC web base corpus and statmt.org news dataset (16B tokens).

Chapter 3

Data and Evaluation Metrics

3.1 Evaluation Metrics

When the models are implemented and trained we have to compare them. This part is very important because we want to define such metrics that will not be biased and which will have high discriminability. In this project, experiments are separated into two parts. The first part is a supervised classification with a big amount of the training data. This is done for classifiers' maximal upper bound understating. The upper bounds are used as maxima to which our active learning algorithms should be converging.

3.1.1 Receiver Operating Characteristic Metric

In section 1 we mentioned that we are limiting our problem only on binary classification. Plenty of metrics, such as recall, accuracy, precision, etc. exists for binary classification scoring. However, we decided to find a metric that is able to unify all metrics discussed before and do not underperform each of them. For these purposes, we chose the Receiver Operating Characteristic (ROC) metric. ROC visualizes the tradeoff between the true positive rate (TPR)

$$\text{TPR} = \frac{\text{true positive}}{\text{true positive} + \text{false negative}}$$

and the false positive rate (FPR)

$$\text{FPR} = \frac{\text{false positive}}{\text{false positive} + \text{true negative}},$$

where terminology true/false positive/negative refers to assigned classification being correct or incorrect with respect to positive or negative category [7]. This means that for every threshold we are able to calculate TPR and FPR, and plot it in one figure.

We are working with balanced datasets. Thus, there is no problem with using ROC metric. ROC metric is also quite efficient when we care equally about positive and negative classes. Another advantage is that if we notice small changes in ROC, it will not result in big changes in other binary classification metrics.

The metric results should be aggregated into a single number in order to obtain a unique comparison value. This is typically done as calculation of the area under the ROC, which is known as the area under the curve (AUC) metric. The probabilistic interpretation of ROC score means that if a positive case and a negative case are chosen randomly, the probability that the positive case outranks the negative case, according to the classifier, is given by the AUC [7].

3.1.2 Supervised Learning Results Validation

As mentioned above, supervised learning results are used as a maximal upper bound of the specific classifier. In order to make results statistically valid, we used k-fold cross validation. For each batch from k-fold cross validation we calculated both ROC and AUC. As an output result of a classifier performance we calculated mean value over all ROC and AUC scores. All results are calculated with respect to balanced data classes.

3.1.3 Active Learning Results Validation

Active learning model evolution is based on supervised learning algorithms that are sequentially retrained. Thus, we are not able to display ROC for active learning algorithms because the amount of results is too big. We decided to aggregate results and display the evolution of AUC metric for each step of the active learning sequence. AUC sequences can be well compared over different classifiers. Another aspect of data validation is making the results statistically significant. We are not able to use k-fold cross validation for active learning algorithms. Therefore, we run the active learning algorithm $H \in \mathbb{N}$ times with different random selection of the initial training set. Due to the random initializations, we are able to determine uncertainty bounds that are calculated as standard deviations from the mean values.

3.2 Data

This chapter is dedicated to the dataset description. We used two datasets for algorithms training and testing. We consider these datasets big and diverse enough for getting unbiased results. We took into account the size of texts (articles and tweets), diversity and at the same time, similarity of topics.

3.2.1 HuffPost 200k Articles Dataset

HuffPost 200k Articles Dataset is publicly available at Kaggle competition webpage and can be found as News Category Dataset [16] here `https://www.kaggle.com/rmisra/news-category-dataset`. The described dataset contains around 200k news headlines from the year 2012 to 2018 obtained from HuffPost web journal. The following dataset includes a url address and a label for each article. HuffPost dataset has 200k articles assigned to 41 categories. We used only 10 categories. We are interested in binary classification, as a result we have to make pairs from chosen categories. These categories and pairs are listed in table 3.1.

Tuple Id	Category Pairs	
1	Crime	Good News
2	Sports	Comedy
3	Politics	Business
4	Science	Tech
5	Education	College

Table 3.1: HuffPost Dataset Categories which were chosen for algorithms' training and testing

Due to the fact that there is no raw article included in the dataset, we used url links in order to find the articles. For each category, we scraped 500 original articles from `www.huffpost.com`. Listed categories are chosen with respect to diversity and classification complexity. We sorted the categories in table 3.1 with respect to the ascending classification complexity order. By classification complexity we mean two

sets intersection in feature space. If the classification complexity is high, the majority of feature space dimensions have intersections between two datasets. Thus, it is harder to find such set of features that can be used for high classification performance.

3.2.2   1600k Tweets Dataset

Another dataset that is used in this work is 1600k tweets dataset, which is publicly available and is also taken from Kaggle competition webpage. The dataset can be found as sentiment140 dataset [9] at `https://www.kaggle.com/kazanova/sentiment140`. This dataset contains 1,600,000 tweets extracted using Twitter API. The tweets have been annotated as negative (0), positive (4) and they are used for sentiment detection. Same as with HuffPost dataset we used 500 records for each category, for training and testing purposes. The reason of choosing this dataset is that we wanted to show how our algorithms can handle data that consist of little texts.

Chapter 4

Project Implementation and Architecture

Even though this work is quite theoretical with experiments that prove theoretical concepts, we consider the implementational part interesting as well. In this chapter, we show the architecture of the project and explain how different dependencies cooperate with each other. The codebase of this project can be easily found at `https://github.com/sahanmar/Peony`. We expect this project to grow continuously and be used not only in terms of master thesis.

This project was written in Python 3.7 programming language with the usage of Conda environment. The project combines a lot of different tools and programs such as Docker, Docker-Compose, MongoDb, Jupyter, etc..

In this thesis, we used two main components that represent the database and a computational part. We tried to unify all methods as much as possible and make the utilization process very easy.

4.1 Database

In order to make everything consistent and let the models work with the same input and output format we decided to create a database that will store all the data in JSON format. This unification lets us connect the database to machine learning and visualization components. In this project we decided to work with NoSQL database. Our choice was MongoDb. The reason why we have chosen MongoDb is because of its simplicity and possibility of maintaining through Docker. Since Docker and MongoDb is a perfect combination, the database can be deployed with two lines of code through Docker-Compose as explained in documentation on GitHub. Of course, it is easier to use MongoDb without Docker but our motivation was measured on the simplicity of creating and working with the database. All experiments were run on Google Cloud Platform virtual machine instance. Thus, we could start working with the models right away without any complications with the installation.

4.1.1 MongoDb Data Format

MongoDb represents the data in BSON format behind the scenes but we insert and get the data in JSON format. Despite the fact that we are having different text datasets which we store in the database, we decided to create a unified JSON scheme that will let us preserve the structure of the data stored in MongoDb. JSON schema of how the data are stored and what a user will get as an output from a database is shown in figure 4.1. Deeper explanation of JSON schema format can be found at `https://json-schema.org/understanding-json-schema/`.

```
{
  "title": "Database",
  "type": "object",
  "properties": {
    "datasetName": {
      "type": "string",
      "description": "Name of the dataset"
    },
    "datasetId": {
      "type": "int",
      "description": "Unique hash id that will be created automatically"
    },
    "record": {
      "type": "object",
      "description": "All the information about an instance",
      "properties": {
        "id": {
          "type": "string",
          "description": "Unique hash id that will be created automatically
            "
        },
        "snippet": {
            "type": "string",
            "description": "Snippet of a text. Can be empty"
        },
        "text": {
          "type": "object",
          "description": "Text instance that is used for a model",
          "properties" : {
            "title": {
              "type": "string",
              "description": "Title of a text. Can be empty"
            },
            "body": {
              "type": "string",
              "description": "Body of a text"
            },
          },
        },
        "label": {
          "type": "string",
          "description": "Label for an instance. Can be empty if this is
            not a validation data"
        },
        "metadata": {
          "type": "object",
          "description": "Any additional metadata. Can be empty"
        },
      },
    },
  },
}
```

Figure 4.1: MongoDb JSON schema visualization

4.2   Computations

All computations were done with the usage of virtual instance on Google Cloud Platform. We used configuration with 2 CPU, 7.5Gb memory that was running on Debian GNU/Linux 10. All versions of python, python packages, docker, mongo, etc. can be found in .yml files in GitHub folder with the project.

4.3   Machine Learning Component

Machine Learning (ML) Component is fully implemented in Python with the usage of open source libraries. In order to understand how to use the models, it is possible to find the code and its usage in Jupyter notebook that is stored in the showcase folder. Showcase folder has four Jupyter notebooks that show both how to get the data for the models from the database and how to start using the models.

4.3.1   Data Transformers

Before models training and testing, the user has to fit the data transformer that transforms text into tensors form. Tensors are used as input values for models. As mentioned in chapter 2, we are working only with Fast Text and TF-IDF text encodings. Both TF-IDF and Fast Text models are fitted from the documents that are given to the transformer.

4.3.1.1   TF-IDF Transformer

Basic concept is that TF-IDF transformer represents one article as a vector. TF-IDF encoding for a single document is calculated on the basis of all extracted words that exist in the vocabulary. As a result, if we make TF-IDF encoding of a set of articles, we will get a matrix where each row represents a specific document and each column represents a word from a dictionary.

4.3.1.2   Fast Text Transformer

Fast Text model is a pretrained model that consists of one million words mapped to vectors. These words are stored in MongoDb. When a user starts to use the Fast Text model, ML component creates a words' vocabulary from the texts taken for model training/testing. This vocabulary is created in the form of a hash map (word -> vector) where word embeddings are downloaded from MongoDb. It is important to remember that Fast Text encoding represents each word as a vector with predefined number of components. We are using word embeddings that represent each word with 300 float values. We introduce article encoding as a mean value through all words from a text that is given for encoding. Thus, if we make Fast Text encoding of a set of articles, we will get a matrix where each row represents a specific document. A huge advantage of this method in comparison to TF-IDF is that we are working only with 300 float values than with huge vocabulary (all unique words from a text corpus). Therefore, we get both lower features dimensionality and better context understanding.

4.3.2   Machine Learning

In this work, we created the Generalized Model that unifies all models. Generalized Model allows us to work with each Machine Learning algorithm in the same way. Generalized Model is able to take a data transformer as an input argument. This feature makes it easier to work with models. In the first chapter of this thesis, we introduced our models the way that we want to sample from their parameters'

distributions. In other words, we defined ensembles models. In figure 4.2 is shown a generalized diagram of a machine learning structure.
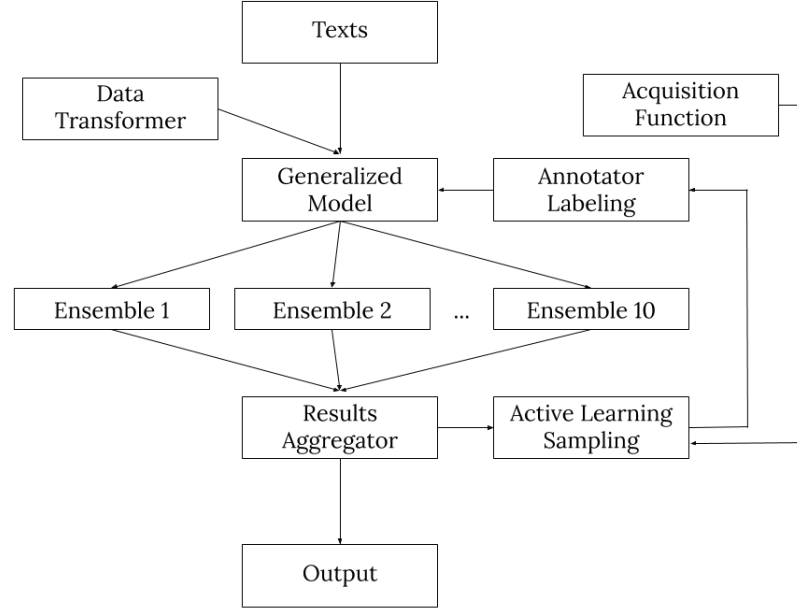

Figure 4.2: Machine Learning Workflow

We used scikit-learn [18] for basic algorithms such as Random Forests and SVMs. However, the core of this project is constructed around neural networks. We used PyTorch [17] as a neural networks framework. In this work, we have implemented and tested five classification algorithms. Three of them, such as SVM, Random Forest, and Feed Forward Neural Network ensembles are trained on randomly chosen subsets from the training data. For each ensemble are randomly chosen 80% from training data that are used for training. Two algorithms such as SGLD and DENFI are using a full training dataset for their ensembles. The variability in SGLD and DENFI ensembles is reached through adding Gaussian noise while ensembles training. We hardcoded amount of ensembles for all models to 10, except SGLD where are used 50 ensembles.

4.3.2.1 SVM and Random Forest Ensemble Setup

Both SVM and Random Forest models were taken and used out of the box. We created 10 SVM and 10 Random Forest ensembles with default scikit-learn setting. No modifications were provided.

4.3.2.2 Feed Forward Neural Network

Despite the fact that we used very simple neural network architecture it showed great results. We implemented Feed Forward Neural Network with the usage of PyTorch python package with only an input layer that consists of 100 neurons with a sigmoid activation function. We chose the softmax activation function for an output layer.

Algoritmus 4.1 DENFI modification algorithm pseudocode

```
def active_learning_iteration_training(all_ensembles, training_data):
  for ensemble in all_ensembles:
    if first_active_learning_iteration is False:
      ensemble.weights = ensemble.weights_prev_iteration
      training_epochs = 500
    else:
      ensemble.weights = gaussian_initialization(mean=0, var=0.1)
      training_epochs = 2000
    ensemble.train(training_data)
        ensemble.weights = ensemble.weights
                      + gaussian_noise(mean=0, var=0.1)
```

4.3.2.3 SGLD

For SGLD we used the same configuration as for Feed Forward Neural Network. One significant difference is that we used the whole training dataset and were adding Gaussian noise to a Gradient Descent [28] as shown in (1.36). We used 2000 epochs in order to train the model. Next, we started a sampling procedure. Each sample was generated with a 50 epochs interval. The precise configuration of SGLD can be found in GitHub project here `https://github.com/sahanmar/Peony/blob/master/Peony_project/Peony_box/src/peony_adjusted_models/sgld_nn.py`.

4.3.2.4 DENFI

In this work, we have simplified the original DENFI algorithm. The pseudocode of this algorithm is shown in algorithm 4.1. The main idea is that the algorithm finds different local minimums due to the random weights initialization in the first active learning iteration. We used 2000 epochs in order to train the model. When the training is finished, Gaussian noise is added to the output weights in order to increase the variability. In further active learning iterations, weights from previous iterations with extended training dataset are used. After the training, we also add Gaussian noise to the weights. We have empirically discovered that the model shows the best performance with 0.1 variance of an additive noise. We have also tried different noise configurations with 0.2 and 0.3 variance. However, Gaussian noise with 0.1 variance has shown the best scores. The amount of training epochs in hot start loop equals to 500 epochs. When the learning iterations are done, we can use the algorithm for predicting.

Chapter 5

Passive Learning Classification

Before we can start the active learning part, we have to understand if the implemented algorithms are capable to solve the classification task. Thus, we decided to test the models on Sports and Comedy categories from the HuffPost Dataset and on tweets from the Tweets Dataset. The classification was done both for the TF-IDF and Fast Text encodings. We separated experiments with respect to the dataset types.

5.1   Passive Learning HuffPost Dataset

In this section, we are illustrating ROC and AUC metrics with respect to 10-fold cross validation and 500 Sports, 500 Comedy articles. Vocabulary, that is created from 1000 articles corpus consists of 20 thousand unique words. We would like to mention that all algorithms are trained and tested with respect to 10 ensembles. We decided to test the ensemble models on a passive learning problem in order to see the limit that an active learning strategy will converge to. Moreover, the ratio of randomly chosen training data for ensembles (SMV, Random Forest, Feed Forward NN ensembles) is set to 80%.

5.1.1   SVM Ensembles

Results for SVM Ensembles are shown in figures 5.1 and 5.2. These are results both for TF-IDF and Fast Text encodings. As seen on these plots, ROC and AUC values of 10-fold cross validation are very high. This means that our model works very good. Another interesting point is that the standard deviation with respect to all runs is very low. It means that SVM ensembles could linearly separate Sports and Comedy sets with an acceptable classification error.

It is also seen that ROC and AUC metrics are almost the same for TF-IDF and Fast Text encodings. However, there is one significant difference. The difference is in computational time because Fast Text encoded text document consists of 300 float components and the TF-IDF encoded text document consists of 20 thousand float components. Even though we are using algorithms for sparse matrix computations for the TF-IDF method, computations for Fast Text encoding are approximately five times faster. The higher amount of unique words is, the higher elapsed time per article for TF-IDF based encoding algorithm will be. Another good aspect of SVM is the algorithm's simplicity. SVM is trained much faster than neural network based models.

It is possible to conclude that the model achives good results for this classification problem and can be used for active learning experiments.
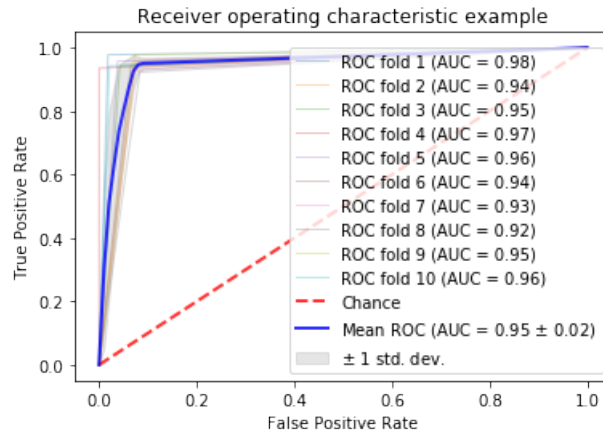
Figure 5.1: TF-IDF ROC and AUC for 10 SVM ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data
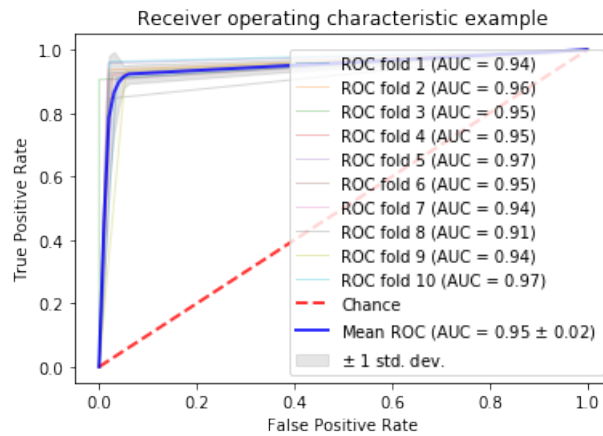

Figure 5.2: Fast Text ROC and AUC for 10 SVM ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data
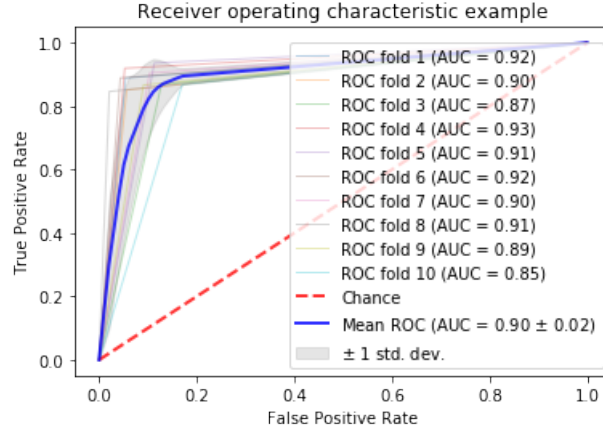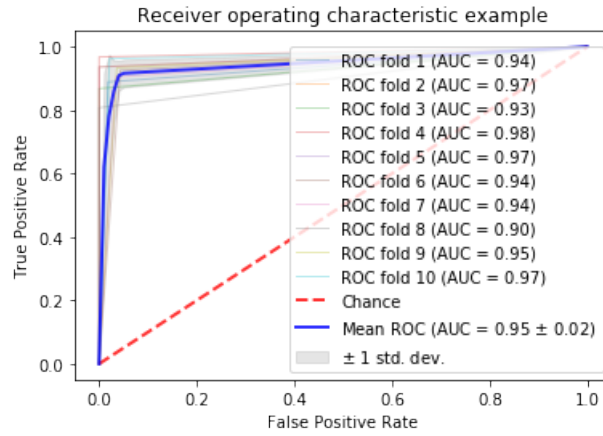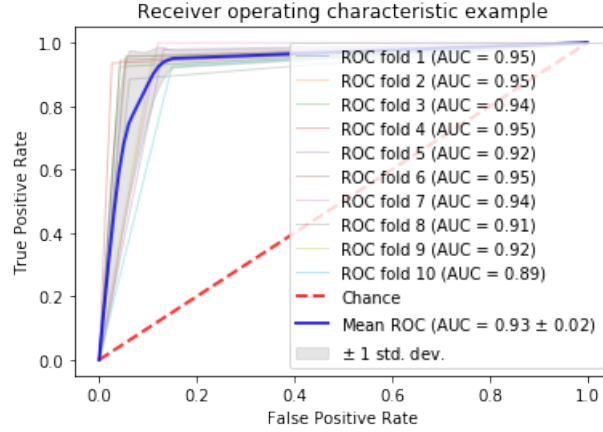
Figure 5.3: TF-IDF ROC and AUC for 10 Random Forest ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data

Figure 5.4: Fast Text ROC and AUC for 10 Random Forest ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data

5.1.2   Random Forest Ensembles

Results for the Random Forest ensembles are shown in figures 5.3 and 5.4. The displayed results are both for the TF-IDF and the Fast Text encodings. Same as in the SVM section, ROC and AUC values of 10-fold cross validation for Random Forest are high as well. This means that our model works well. ThesStandard deviation with respect to all runs is also low.

If we compare the results for TF-IDF and Fast Text encodings, it is seen that the Fast Text based model outperforms the TF-IDF encoding model. ThemMean AUC value for the Fast Text article encoding model is higher by 5%. It is interesting that the TF-IDF sparse matrix algorithm application in Random Forest ensembles model results in almost the same computational time for Fast Text and TF-IDF encoding algorithms. This observation was made on the basis of processing 1000 articles from the Comedy and Sports categories. As mentioned in the SVM section, we can also say that the Random Forest algorithm is trained much faster than the neural network based models.

It is possible to conclude that the model shows good results for this classification problem and can be used for active learning experiments.

Figure 5.5: TF-IDF ROC and AUC for 10 neural networks ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data
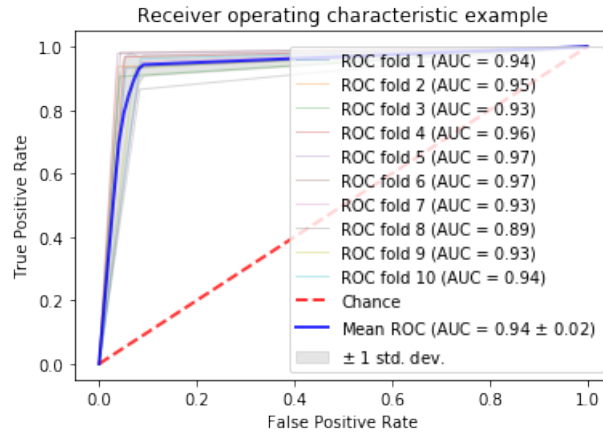

Figure 5.6: Fast Text ROC and AUC for 10 neural networks ensembles trained and tested on Sports and Comedy data where each ensemble is trained on 80% of randomly chosen training data

5.1.3 Feed Forward Neural Network Ensembles

In this work, we have implemented three algorithms based on neural networks, such as neural networks ensembles, SGLD, and DENFI algorithms. The difference between these methods is in parameters sampling. Neural networks ensembles take a randomly selected subset from the training data for each ensemble. On the other hand, SGLD and DENFI require special training. Thus, we decided not to show SGLD and DENFI results in this section. Consequently, if neural networks ensembles achieve good results, we assume that SGLD and DENFI will also perform well for the passive learning scenario.

Results for the neural networks ensembles are shown in figures 5.5 and 5.6. The displayed results are both for the TF-IDF and Fast Text encodings. As seen in the previous section, ROC and AUC values of 10-fold cross validation for neural networks are high as well.

Comparing the results between the TF-IDF and Fast Text encoding based models we can observe that the Fast Text based model gives slightly better results. We have already discussed the fastness of algorithm training with respect to different embedding models in the Random Forest section. In the case of neural networks, this difference is even more significant. The model that is based on the Fast

Text word embeddings takes approximately 20 times less computational time than the TF-IDF encoding based model.

5.2 Conclusion

All of the tested models achieved really good results in the task of classification documents into the Sports and Comedy categories. We can not rule out any of them as irrelevant and we will test these algorithms in the active learning section. We would like to highlight that the Fast Text encoding based algorithms showed a bit better results than TF-IDF. Fast Text based algorithms also showed significant improvement in the evaluation speed of algorithm training.

Chapter 6

Active Learning Classification

In the Passive Learning section, we showed that all implemented algorithms are achieve good results for solving passive text classification tasks. The results of Active Learning are the main contribution of this thesis. Therefore, we tested all five algorithms on the data mentioned in the Data section. The results are shown and described in further subsections. However, before starting with text classification results, we would like to show how our models represent uncertainty. As written in the theoretical introduction to active learning, we use models' uncertainty for an active learning loop.

6.1 Active Learning Models' Uncertainty

Due to the fact that dimensionality of the feature space of both text encoding approaches is extremely high, we introduce a 2-dimensional toy problem for uncertainty visualization. In figure 6.1 is shown a conventional two-moon dataset that is used for the toy problem classification. We generated this dataset by adding Gaussian noise in order to make the task similar to real-world problems.

We generated 1000 data points where 500 are assigned to class 0 and another 500 points are assigned to class 1. We used 50% randomly chosen data samples as the training dataset. The next step was creating a two-dimensional grid that will be used for model predictions. We assign data sample to class 1 if the prediction value is higher than 0.5. If the prediction value is lower than 0.5, then the value is assigned to class 0. We consider that the model is uncertain about a specific data sample if its prediction values
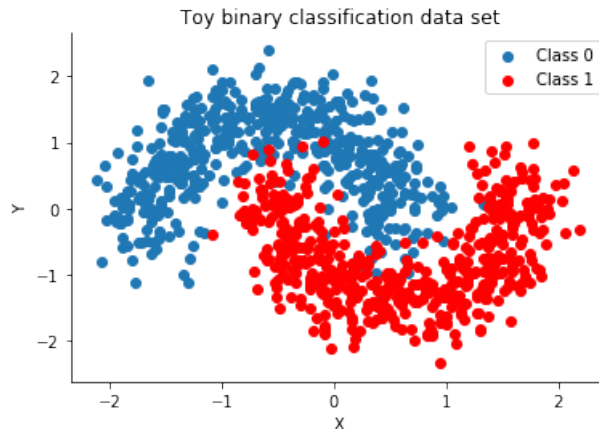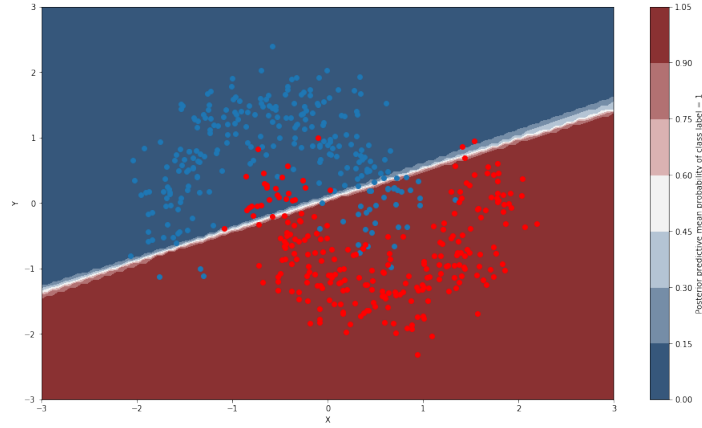

Figure 6.1: Visualization of the toy problem dataset.

Figure 6.2: Mean value of posterior prediction of class 1 for SVM ensembles.

is close to 0.5. As a result, sampling values from the maximal uncertainty region will bring maximum information about the dataset. Setup of models for the toy problem is the same as it is defined in section 4.3 .

6.1.1   SVM Ensembles

Uncertainty for SVM ensembles model is visualized in figure 6.2. Uncertainty bounds are linear and quite narrow. The linearity of uncertainty bounds is explained with the fact that we are using SVMs with a linear kernel. Narrowness can be explained with the richness of the training dataset and linear limitations of the SVM decision boundary.

6.1.2   Random Forest Ensembles

Model uncertainty of the Random Forest ensembles is visualized in figure 6.3. In the case of Random Forest ensembles, we can see that uncertainty bounds are not linear and lay near the region where the two classes are split. We see that the uncertainty region is becoming wider near the places where datapoint of two different classes lay close to each other. This is a behavior that we wanted to observe.

It is also seen that the curve is not smooth enough. This is caused by the shape of the Random Forest decision boundary.

6.1.3   Neural Network Ensembles

Model uncertainty of the neural network ensembles is visualized in figure 6.4. In comparison to the methods that were shown above, uncertainty bounds are quite smooth. We can also observe that uncertainty bounds become wider when they go further away from the data points. This behavior can be explained by the fact that in these places the algorithm did not get any training data samples. We could also see this behavior in SVM ensembles, but the neural network models represent the uncertainties much better.

6.1.4   SGLD

Model uncertainty of neural network estimated by SGLD is visualized in In figure 6.5. We see that SGLD algorithm has similar behavior to neural network ensembles. The difference is that all uncertainty
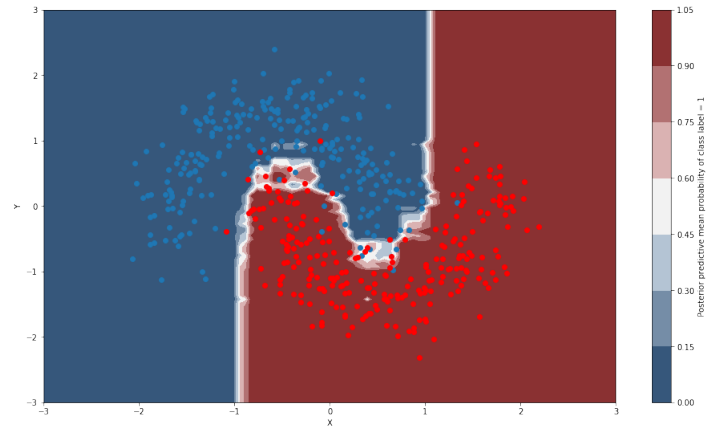
Figure 6.3: Mean value of posterior prediction of class 1 for Random Forest ensembles.
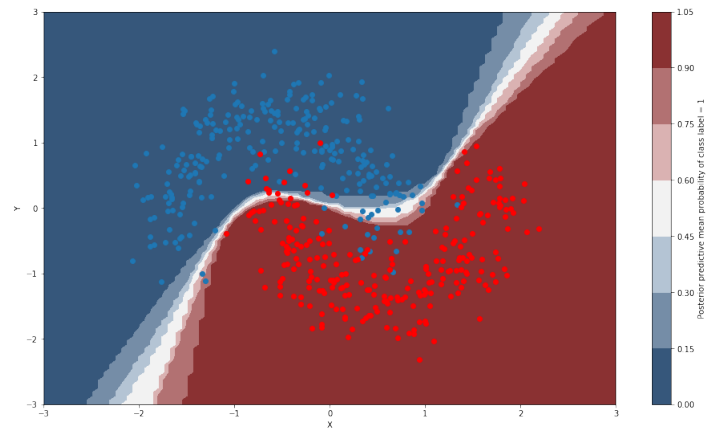

Figure 6.4: Neural network ensembles posterior predictive mean probability of class 1
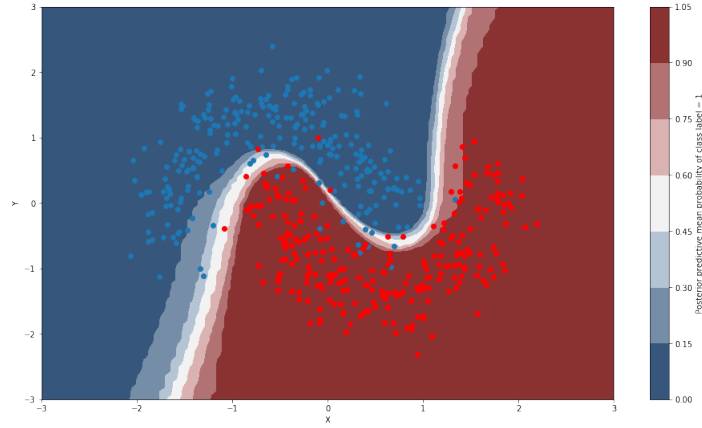
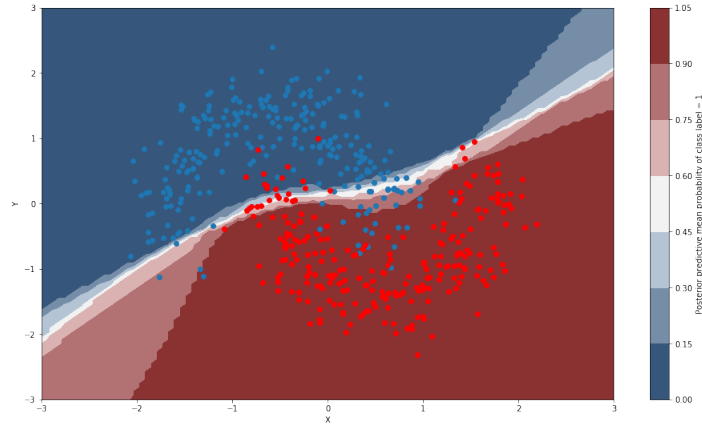Figure 6.5: SGLD posterior predictive mean probability of class 1

Figure 6.6: DENFI posterior predictive mean probability of class 1

bound curves have similar curvature. This is happening due to the fact that SGLD finds a loss function minimum and then samples parameters' values in a neighborhood of the minimum. As a result, we expect decision bound for each parameters sample to be quite similar to each other.

6.1.5 DENFI

In figure 6.6 is visualized DENFI model uncertainty. We see that uncertainty bounds are very similar to neural network ensembles algorithms but still a bit different. As told in pseudocode 4.1, algorithm founds different local minimums and then we add some Gaussian noise to parameters values. In further learning iterations the algorithm continues training using the weights from the previous step.

The last 100 loss function values with respect to each DENFI ensemble are shown in figure 6.7. It is seen that each ensemble found its own local minimum. Additional Gaussian noise adds more variability to the algorithm that makes samples more diverse.

6.1.6 Conclusion

To conclude, we can say that the best variability representation was seen in neural network models. Obviously, we could test SVM algorithm with different kernels but our prior interest was concentrated
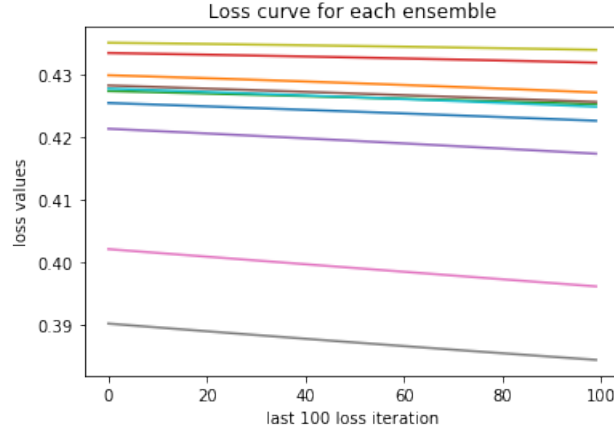
Figure 6.7: The last 100 loss function values with respect to each DENFI ensemble

on neural networks due to their scalability to larger datasets. We have shown that all models are able to represent variability and can be used for further tests.

6.2 Active Learning Simulation Set Up

6.2.1 Simulation Loop

The active learning simulation is designed to compare two strategies: i) random, and ii) active (smart) selection of text documents. We randomly choose an initial training set that has 10 samples. These 10 random samples are chosen from 1000 text documents (500 text documents per category). We reduce the size of all the above-mentioned datasets to 1000 documents. Each dataset is split into the testing and training data.

Next, we initialize two runs. The first run is based on a random selection of the text documents and the second run is based on acquisition function selection of the documents. Both runs start with the same training dataset, and then they choose additional training documents based on their strategies. We consider continuous new data selection from 1000 documents dataset and imitating the annotators labeling process. All in all, we repeat selection of text samples 200 times ($U = 200$). We select 10 random samples in the beginning, train our model, and make a prediction on the complement to the training dataset (990 text documents from validation set). As a further step, we select 1 new sample from the set on which the prediction was done. A new text sample for labeling is chosen with respect to acquisition function or random choice. Before we extend our training dataset with a new labeled sample, we calculate the AUC metrics on the complement to the dataset (990 text documents). Thus, by the end of the simulation, our training set will have 210 text documents and the testing set (complement to a training set) will have 790 data samples. In order to make our results statistically valid, we repeat the described simulation loop 10 times.

6.2.2 Epsilon Greedy Strategy

In this work, we decided that we do not want to sample with respect to an acquisition function from the beginning but follow the epsilon greedy strategy [27]. We decided that both active learning and random strategy are going to start with random sampling. The algorithms have a coefficient $\epsilon \in [0, 1)$ that represents a probability of the data sampling with respect to the acquisition function. In this work,
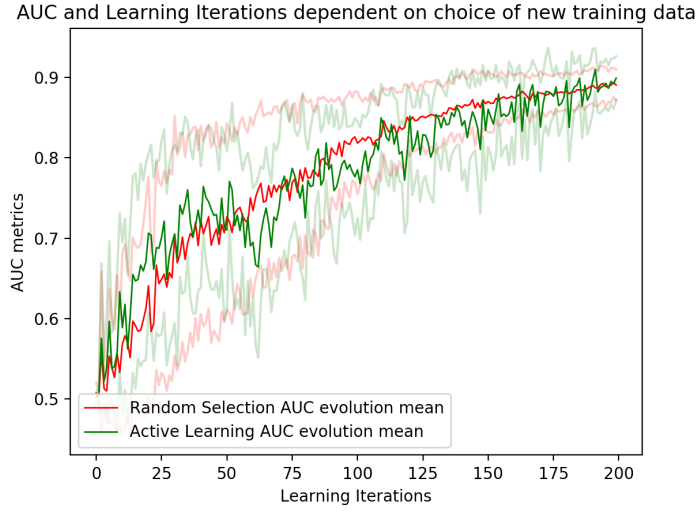
Figure 6.8: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SVM ensembles algorithm with TF-IDF encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

we define ϵ as

$$\epsilon = \begin{cases} \frac{\exp(u-40)}{\exp(u-40)+1}, & u \in \{1, ..., U\} \\ 0, & u = 0, \end{cases} \tag{6.1}$$

where $u = \{0, 1, ..., U\}$ is set of questions that results in the number of text documents which will be labeled by an annotator. As mentioned in the previous section, the number of iterations (questions U) is set to 200. From the equation 6.1 is seen that when we reach $40-$th document, the probability of random sampling is 50%. This strategy provides good results which will be shown in further sections.

6.3 Active Learning on Texts with TF-IDF Encoding Based Models

We decided to show the results for the TF-IDF encoding based model because this text encoding provides high discriminability and it is relatively simple at the same time. However, as mentioned in the passive learning section, models that are using this type of encoding are harder to train due to the high dimensionality of features. We were not able to train neural network ensembles because of the high dimensional feature space. Thus, we decided to show the results only with respect to SVM, Random Forest and Sports, Comedy categories. Therefore, there is no need to split further section for different datasets because all the experiments based on TF-IDF encoding are assumed to be done only for the Sports and Comedy categories.

6.3.1 SVM Ensembles

In figure 6.8 are shown simulation results of active learning for SVM ensembles with TF-IDF encoding. The active learning strategy is based on the entropy acquisition function.

As seen in figure 6.8, the results for entropy are not better than for random selection. This can be explained due to the low variability of SVM ensembles. In this case, we can conclude that there is
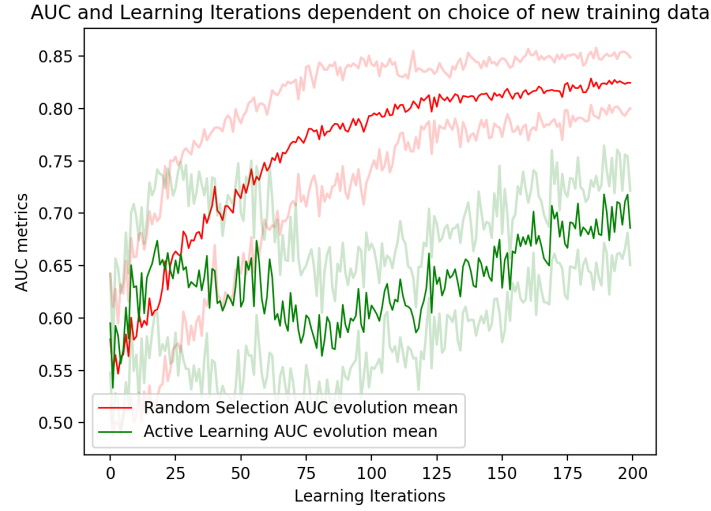
Figure 6.9: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the Random Forest ensembles algorithm with TF-IDF encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

no significant difference between entropy and random data selection strategy. The first and the second strategy has almost the same uncertainty bounds and converges to the same AUC results.

6.3.2   Random Forest Ensembles

In figure 6.9 are shown simulation results of active learning for the Random Forest ensembles with TF-IDF encoding. The active learning strategy is based on the entropy acquisition function.

In comparison to SVM ensembles, the active learning strategy for Random Forest ensembles shows really poor results. Random data selection overcomes the entropy selection, and it can be said that the active learning strategy is not working at all for this algorithm. The reason of such behavior can be explained due to the little amount of training data in the beginning. This fact may make the algorithm to start selecting the data which have high entropy but are close to each other. As a result, it will not lead to high-performance results.

6.3.3   Conclusion

Even though we were able to see extremely good results for TF-IDF encoding in the Passive Learning section, we were not able to train neural networks models and test active learning there, due to the high dimensionality of the feature space. Moreover, the results of the SVM and Random Forest ensembles were unsatisfying, and the active learning strategy did not show good results in comparison to random sampling.

6.4   Active Learning on Texts with Fast Text Encoding Based Models

In this section we show results of all models because the Fast Text encoding maps the texts to a 300-dimensional feature space. This is much lower than in the case of the TF-IDF encoding. Thus, we
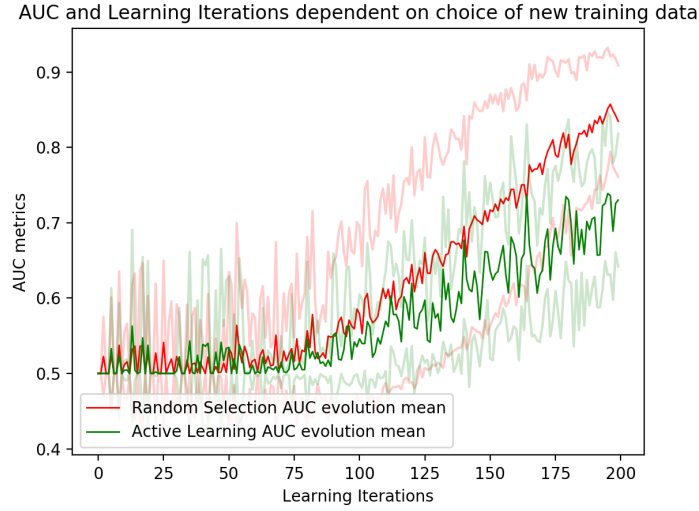
Figure 6.10: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SVM ensembles algorithm with Fast Text encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

were able to provide computations with respect to all models.

6.4.1 SVM Ensemble

6.4.1.1 Sports and Comedy Categories

In figure 6.10 are shown simulation results of active learning for the SVM ensembles with the Fast Text encoding. The active learning strategy is based on the entropy acquisition function.

The behavior which we observe in figure 6.10 is similar to figure 6.8. We can see that the active learning strategy is not working for the case of the Fast Text encoding as well.

6.4.1.2 Conclusion

We can conclude that even despite good performance in the Passive Learning section, the active learning algorithm is not working as expected. Thus, we will not continue testing this algorithm on other datasets.

6.4.2 Random Forest Ensembles

6.4.2.1 Sports and Comedy Categories

In figure 6.11 are shown simulation results of active learning for the Random Forest ensembles with the Fast Text encoding. The active learning strategy is based on the entropy acquisition function.

As illustrated in figure 6.10, we can see the strategies results are similar to each other but in active learning case, the entropy based sampling is outperforming the random sampling strategy. We can also see that the uncertainty bounds are much more narrow in the active learning case .
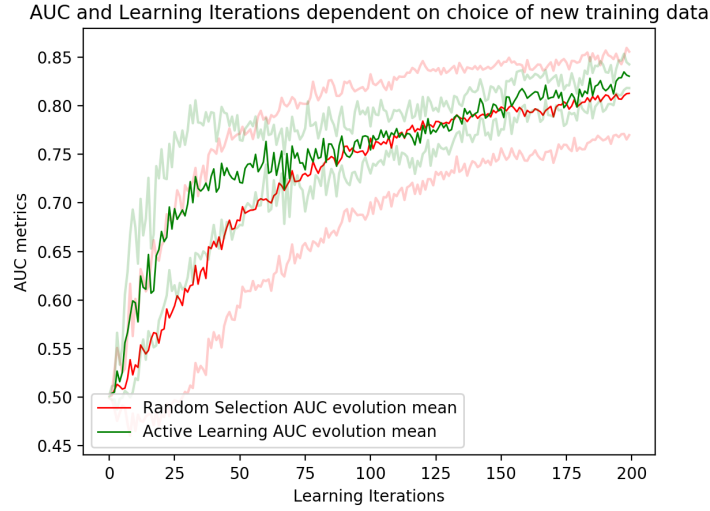
Figure 6.11: .Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the Random Forest ensembles algorithm with Fast Text encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

6.4.2.2 Conclusion

Even though we could observe that the active learning strategy achieves better results than the random sampling strategy, we do not continue with further experiments because the results are not significant enough.

6.4.3 Neural Network Ensembles

6.4.3.1 Sports and Comedy Categories

In figure 6.12 are shown simulation results of active learning for neural networks ensembles with the Fast Text encoding. The active learning strategy is based on the entropy acquisition function.

If we compare output metrics from figure 6.12 and figures 6.10, 6.10, we can see a significant difference in performance of the algorithms. In comparison to previous methods, the algorithm based on neural networks achieves the same AUC at 50-th iteration. It means that the probability of using non-random acquisition function equals to 50%. We are able to observe significant improvement of the entropy based sampling over the random sampling strategy. We can also see, that the random sampling strategy is converging very slow to the results of the active learning strategy. Moreover, uncertainty bounds of the active learning strategy are much more narrow than the uncertainty bounds of the random sampling algorithm.

6.4.3.2 Conclusion

One significant disadvantage of this method is that it is very slow and hard to train. Each time, we have to train 10 neural networks with a cold start. That means training neural networks with random weights initialization and no prior information from the previous training. Despite the fact, that the results are really good, we decided not to continue with the algorithm testing because it is very slow and
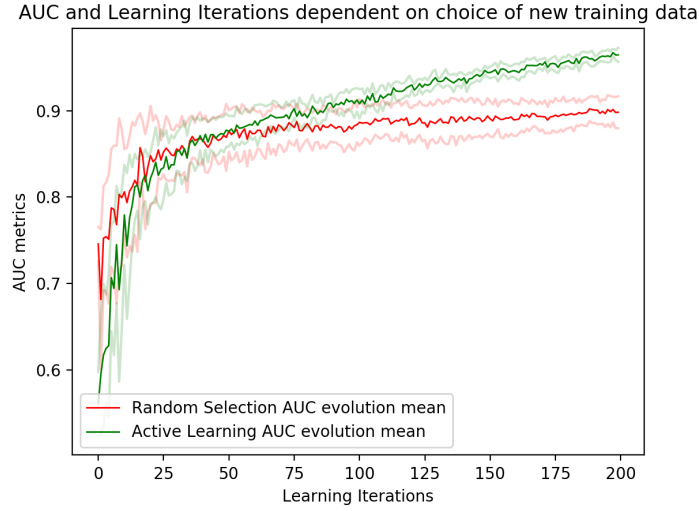
Figure 6.12: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the Feed Forward Neural Network ensembles algorithm with Fast Text encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

computationally costly. In the next sections we introduce results based on neural networks but with a different way of uncertainty representation.

6.4.4 SGLD

Stochastic Gradient Langevin Dynamics algorithm [28] is one of the two algorithms that are assumed to improve the ratio of training time consumption and performance. As mentioned previously, Gaussian noise is added to the gradient while training. This approach helps us to sample different parameters vectors around the loss minimum by simply continuing training. In comparison to neural networks ensembles, we do not have to train neural network ensembles separately, but train only one neural network with some additional training epochs.

6.4.4.1 Sports and Comedy Categories

In figure 6.13 are shown simulation results for active learning for SGLD with the Fast Text encoding and Sport vs. Comedy categories dataset. The active learning strategy is based on the entropy acquisition function.

We can see that in figure 6.13 both mean and uncertainty bound curves are not smooth enough in comparison to neural network ensembles. This behavior can be explained with a low number of samples from the SGLD training. However, we are able to observe the same analogy as with neural network ensembles. The active learning strategy improves over the random sampling and has narrower uncertainty bounds. Moreover, the SGLD was trained almost three times faster than the neural network ensembles algorithm.
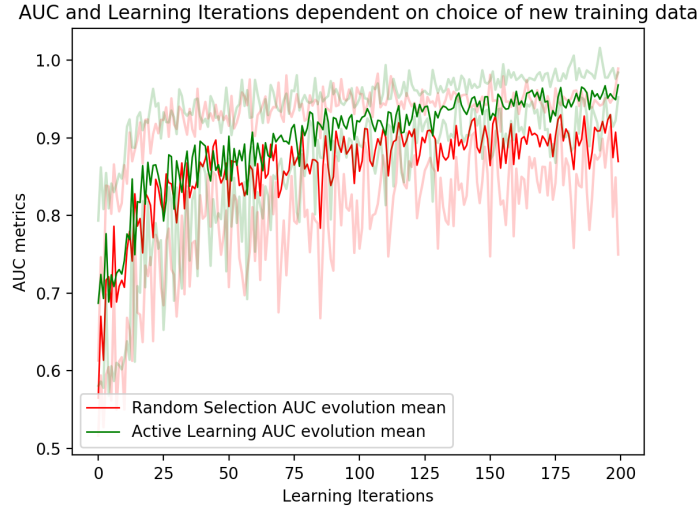
Figure 6.13: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed

6.4.4.2 Crime and Good News Categories

In figure 6.14 are shown simulation results of active learning for SGLD with the Fast Text encoding and the Crime vs. Good News datasets. The active learning strategy is based on the entropy acquisition function.

We expect the Crime and Good News categories to have only a small intersection. As seen from 6.14 it is really true, because the first iteration of the simulation starts at around $85\% - 90\%$ AUC. It means that only 10 training data samples algorithm could reach high-performance results. The evolution of the two strategies is quite the same as in figure 6.13. We would like to pay attention to the place where the upper uncertainty bound reaches the value that is greater than one. It is not possible for the AUC to be greater than one because AUC $\in [0, 1]$. However, as mentioned previously, we construct uncertainty bounds as one standard deviation from the mean value. In this case, it is possible that the upper uncertainty bound is greater than one. Thus, while interpreting the results, a reader has to keep in mind that AUC metric must be truncated to one.

6.4.4.3 Politics and Business Categories

In figure 6.15 are shown simulation results for active learning for SGLD with the Fast Text encoding and the Politics vs. Business datasets. The active learning strategy is based on the entropy acquisition function.

These two categories have a larger intersection, what means that it is a harder classification task. The results show again that the active learning strategy easily exceeds the random sampling strategy. Even though the topics are harder to distinguish, the active learning strategy finds the patterns in the data and shows much better results with narrower uncertainty bounds.
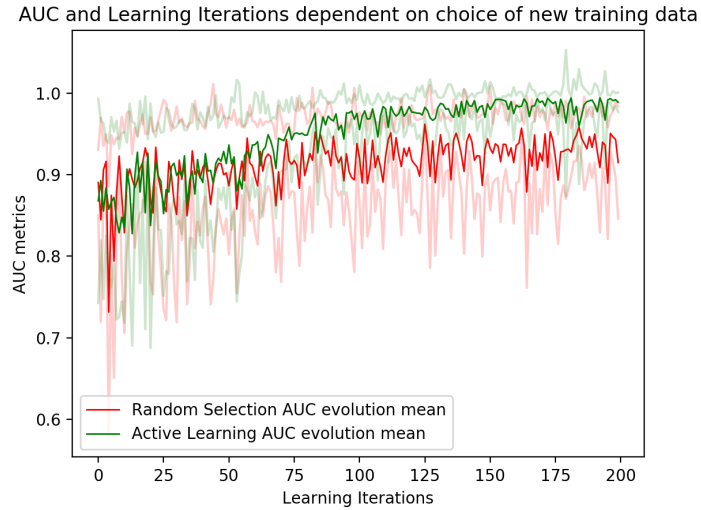
Figure 6.14: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the Crime vs. Good News categories 200 queries for data annotation were performed
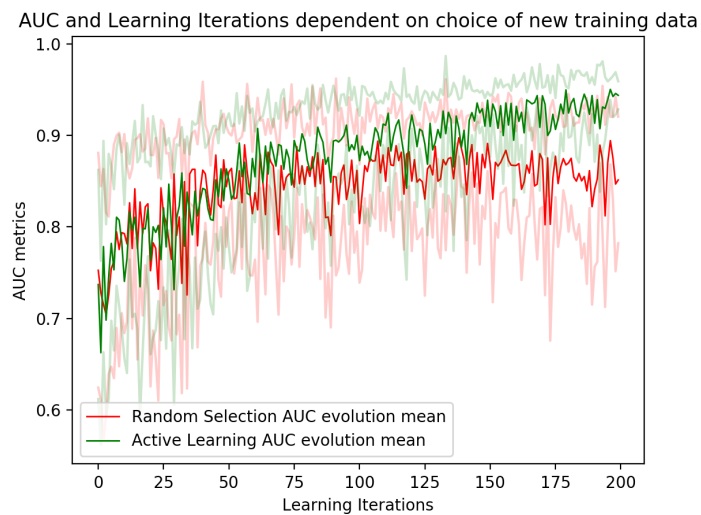

Figure 6.15: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the Politics vs. Business categories 200 queries for data annotation were performed
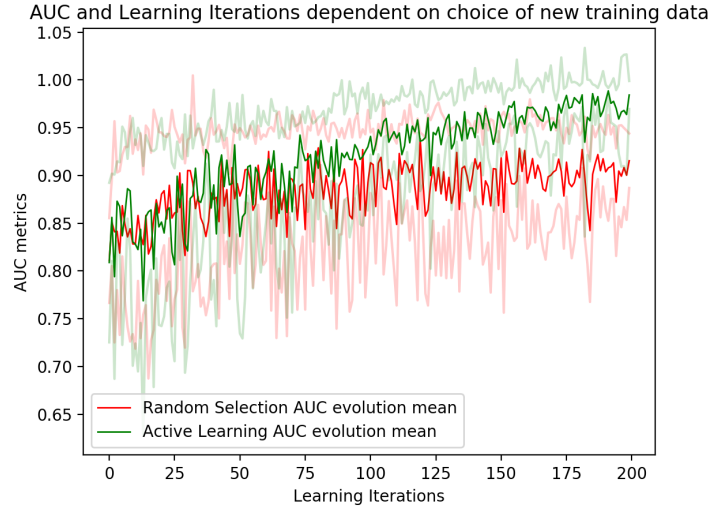
Figure 6.16: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the Tech vs. Science categories 200 queries for data annotation were performed

6.4.4.4 Tech and Science Categories

In figure 6.16 are shown simulation results for active learning for SGLD with the Fast Text encoding and Tech vs. Science categories. The active learning strategy is based on the entropy acquisition function.

We observe once again that the active learning strategy is better even though the categories are quite similar. As seen from the plot, the upper uncertainty bound reaches the values which is greater than one. This is exactly the case which was already covered in 6.4.4.2.

6.4.4.5 College and Education Categories

In figure 6.17 are shown simulation results of active learning for SGLD, with the Fast Text encoding and the College vs. Education categories. The active learning strategy is based on the entropy acquisition function.

The collected results based on the College and Education category do not differ from the results from the previous experiment with the SGLD algorithm. We can still see that active learning strategy outperforms the random sampling, even despite the fact that these categories are very similar.

6.4.4.6 Positive and Negative Tweets Categories

In figure 6.18 are shown simulation results of active learning for SGLD with the Fast Text encoding and the Positive vs. Negative tweets categories. The active learning strategy is based on the entropy acquisition function.

In previous sections, we tested the SGLD algorithm on the data from the HuffPost dataset. In figure 6.18 are illustrated results with respect to the tweets dataset. Due to the fact that the tweets are really short, it is quite hard to find the patterns that can be used for high performance separation of categories. Thus, we can see that our classification results (AUC) are not as high as they were in previous datasets.
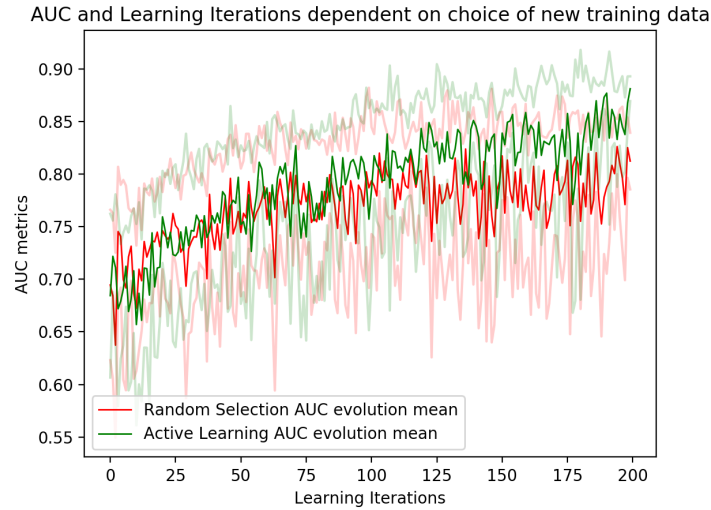
Figure 6.17: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the College vs. Education categories 200 queries for data annotation were performed
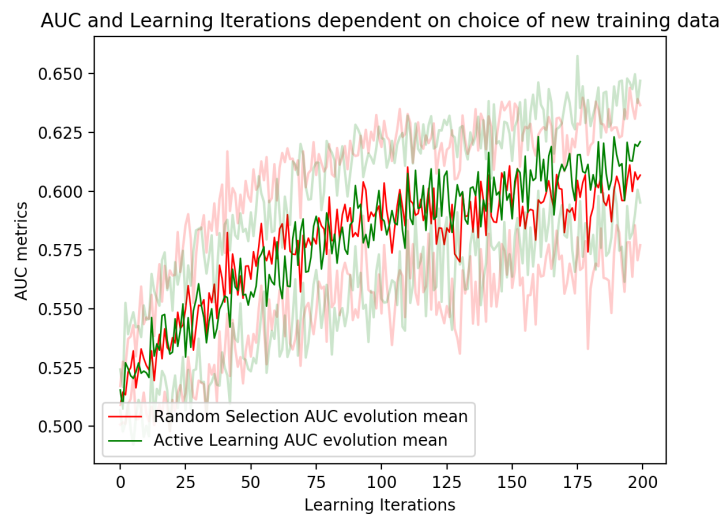

Figure 6.18: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the SGLD algorithm with Fast Text encoding. The initial training set contains 10 samples from the Positive vs. Negative tweet categories 200 queries for data annotation were performed

Moreover, we observed that for this dataset there is no difference between active learning and random sampling strategy.

6.4.4.7 Conclusion

To sum up, we can say that the SGLD algorithm exhibit really impressive results and proved that the active learning strategy outperforms the random sampling. However, there are several disadvantages. The first disadvantage is that the resulted curves were not smooth. We think that this problem can be eliminated by sampling more parameters vectors while training the model. Another problem is that the algorithm does not show better active learning results when it is tested on short and quite general text data. We believe that this problem can be solved with a different encoding approach.

6.4.5 Deep Ensemble Filter

Deep Ensemble Filter (DENFI) algorithm is the second algorithm which is not partitioning the training dataset. In addition to this, we use a modification of the DENFI algorithm. A huge advantage of this algorithm is that it uses prior information from the previous training round. In the first training round, the DENFI algorithm follows almost the same strategy as the neural network ensembles method. It trains 10 ensembles with respect to all training data. The variability in ensembles is reached with different weights initialization. After the training is finished, we add some Gaussian noise in order to increase the variability. When we add some training samples, we continue training using the weights from the previous iteration with the addition of Gaussian noise in the end. Moreover, we are using a lower number of epochs. The hot start approach gives sufficient variability that is manifested in the quality of results in the subsequent sections.

6.4.5.1 Sports and Comedy Categories

In figure 6.19 are shown simulation results of active learning for DENFI with the Fast Text encoding and the Sport vs. Comedy categories. The active learning strategy is based on the entropy acquisition function.

The active learning result, displayed in figure 6.19, outperforms all the algorithms that were tested before. We observe that the uncertainty bounds are extremely narrow. In addition to this, we see that the active learning strategy has much higher AUC metrics and the curves are quite smooth. Moreover, due to the hot start training, the time needed to fit the algorithm is much lower in comparison to neural network ensembles.

6.4.5.2 Crime and Good News Categories

In figure 6.20 are shown simulation results of active learning for the DENFI with Fast Text encoding and the Crime vs. Good News categories. The active learning strategy is based on the entropy acquisition function.

We have already discussed in the SGLD section that the Crime and Good news categories can be well separated from each other. In this case, we see the same behavior for active learning strategy as in the previous section. The uncertainty bounds are narrow and the AUC scores are very high in comparison to the random sampling strategy.
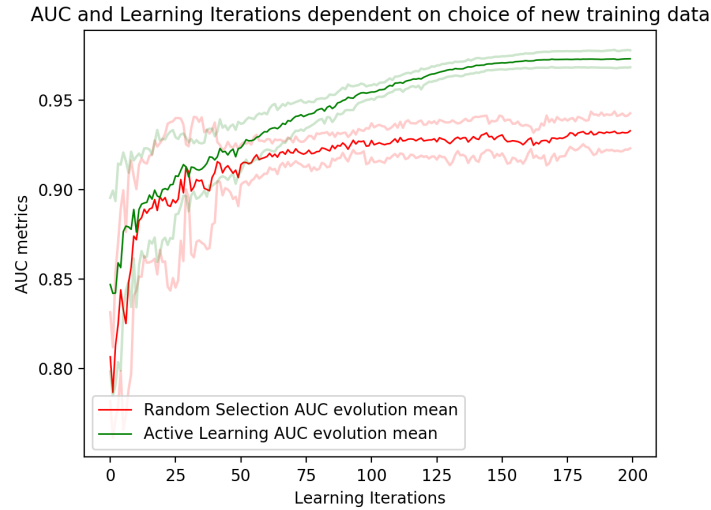
Figure 6.19: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the Sports vs. Comedy categories 200 queries for data annotation were performed
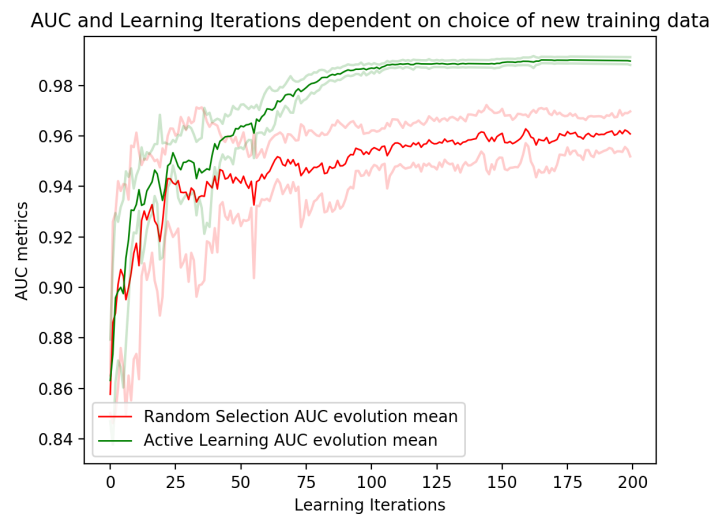

Figure 6.20: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the Crime vs. Good News categories 200 queries for data annotation were performed
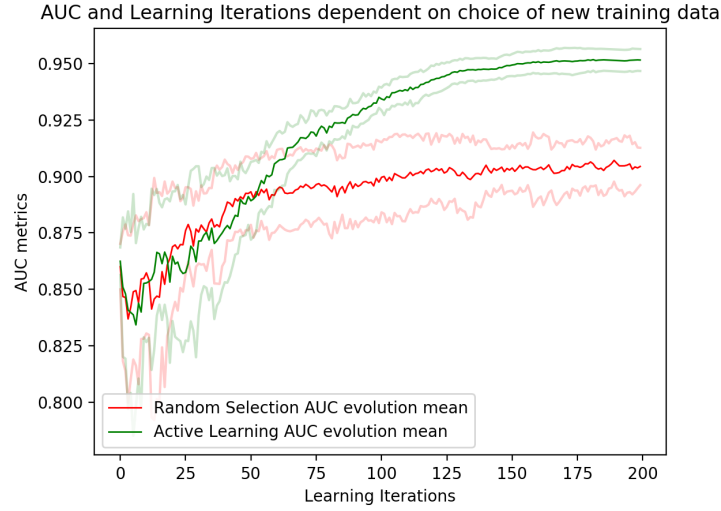
Figure 6.21: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the Politics vs. Business categories 200 queries for data annotation were performed

6.4.5.3 Politics and Business Categories

In figure 6.21 are shown simulation results of active learning for the DENFI with Fast Text encoding and the Politics vs. Business categories. The active learning strategy is based on the entropy acquisition function.

The behavior, observed in figure 6.21, is the same as in the previous DENFI results. Moreover, we see good active learning performance, even though it is not easy to separate these categories. If we compare the results in figure 6.21 to the SGLD results in figure 6.15, we can see the DENFI is better not only because its less corrupted with noise but also in terms of higher AUC scores.

6.4.5.4 Tech and Science Categories

In figure 6.22 are shown simulation results of active learning for the DENFI with Fast Text encoding and the Tech vs. Science categories. The active learning strategy is based on the entropy acquisition function.

The active learning strategy results for the DENFI algorithm are much better in comparison to the SGLD method that are shown in figure 6.16. We see that for the active learning strategy, the DENFI easily found the patterns which helped it to learn faster and show better scores with narrower uncertainty bounds.

6.4.5.5 College and Education Categories

In figure 6.23 are shown simulation results of active learning for the DENFI with Fast Text encoding and the College vs. Education categories. The active learning strategy is based on the entropy acquisition function.

Last but not least of the Huffpost dataset, results for the College and Education categories also prove that success of the DENFI active learning strategy is not dependent on size of the intersection between
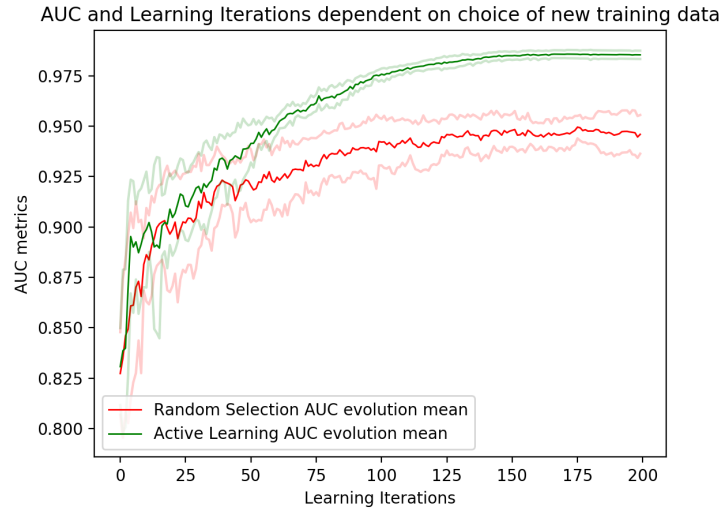
Figure 6.22: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the Tech vs. Science categories 200 queries for data annotation were performed
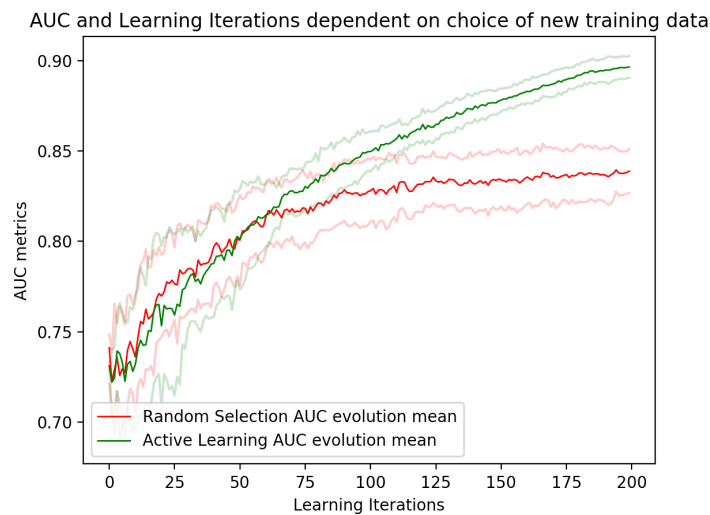

Figure 6.23: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the College vs. Education categories 200 queries for data annotation were performed
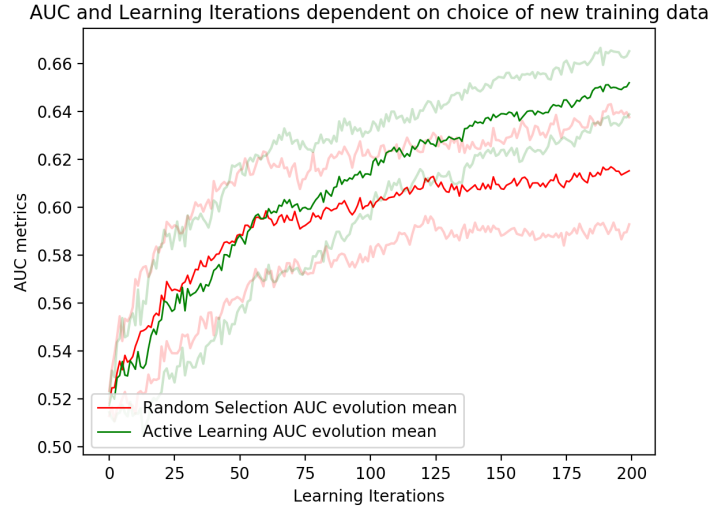
Figure 6.24: Comparison of the random and active learning strategies for semi-supervised learning in terms of the mean and one standard deviation of 10 runs of the DENFI algorithm with Fast Text encoding. The initial training set contains 10 samples from the Positive vs. Negative tweets categories 200 queries for data annotation were performed

the categories. The uncertainty bounds for the active learning strategy are still narrow and the AUC score is much higher than for the random sampling case.

6.4.5.6 Positive and Negative Tweets Categories

In figure 6.24 are shown simulation results of active learning for the DENFI with Fast Text encoding and the Positive vs. Negative tweets categories. The active learning strategy is based on the entropy acquisition function.

In comparison to SGLD, the DENFI algorithm shows better active learning performance for the tweets dataset. The DENFI active learning strategy is also working on tweets whereas the SGLD active learning strategy was not able to overcome the random sampling. We can also see that the DENFI AUC scores for active learning are higher with narrower uncertainty bounds than those for thes SGLD.

6.4.5.7 Conclusion

To conclude we can say that the DENFI algorithm achieved by far the best results for all problems which it was tested on. In all cases, the active learning strategy outperformed the random sampling. The algorithm was tested both on the data that are easy and hard to separate. In addition to this, the AUC scores for all active learning results with the DENFI were higher than for all other algorithms. That makes the DENFI algorithm the best one, with the highest performance and the lowest uncertainty bounds, from all approaches tested within this project.

Conclusion

This project demonstrate how an active learning strategy of querying unlabeled text documents for further labeling and training can beat the random selection strategy. We have provided not only a high-level theoretical description of the problem but also testing results that cover different scenarios and text document categories. Github link for Python implementation is also available in this project.

Based on the achieved results that were gathered from testing on 12 different categories, we were able to see that a modification of the DENFI algorithm shows excellent performance and overcomes other algorithms in all aspects. The DENFI algorithm outperforms all other models, both in higher AUC scores and narrower uncertainty bounds. Another considerable advantage of DENFI is that it is the fastest neural network model that was implemented and tested in this thesis.

We see a plenty of further opportunities how to improve the algorithm, starting from a better text representation and ending using other modification of the DENFI algorithm. To conclude, we would like to say that the ensembles showed their power in solving an active learning problem, and in our opinion, it is a good field for continuing the research.

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