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# Hydrogen separation from reforming gas using organic templating silica/alumina composite membrane

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#### Abstract

The separation characteristics and dynamics of hydrogen mixture produced from natural gas reformer were studied on methyltriethoxysilane (MTES) templating silica membrane. The permeation and separation of CO pure gas,  $H_2/CO$  (50/50, vol.%) binary mixture and  $H_2/CH_4/CO/CO_2$  (69/3/2/26, vol.%) quaternary mixture were investigated both experimentally and theoretically. Since the permeance of pure CO on the MTES membrane was very low ( $CO \approx 4.79-6.46 \times 10^{-11}$  mol m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>), comparatively high hydrogen selectivity could be obtained from the  $H_2/CO$  mixture (separation factor = 93–110). This implies that CO, which should be eliminated prior to use in fuel cells, can be separated from hydrogen mixtures using MTES membranes. The permeance of the  $H_2$  quaternary mixture on the MTES membrane was  $2.07-3.37 \times 10^{-9}$  mol m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup> and the separation factor of  $H_2/(CO+CH_4+CO_2)$  was 6–24 at 323–473 K. Since the permeation flux in the MTES membrane was affected by both molecular sieving and surface diffusion, high  $H_2$  selectivity could be obtained at elevated temperatures. The transient permeation/separation behaviours of hydrogen multi-component systems on the MTES membrane were predicted by the Generalized Maxwell–Stefan model incorporating the dusty gas model and Langmuir isotherm model. © 2008 Elsevier B.V. All rights reserved.

Keywords: MTES templating; Silica membrane; Hydrogen; Carbon monoxide; Carbon dioxide; Methane

#### 1. Introduction

Hydrogen is considered to be one of the most important chemicals used in the chemical and petroleum industries. Furthermore, hydrogen can be used as a general purpose energy source for space heating, electric power generation, and transportation fuel. These potential uses have resulted in a huge increase in hydrogen demand.

The current emphasis on hydrogen fuel cells has driven the technological development of hydrogen stations to commercialize fuel cells and fuel cell powered vehicles. Generally, hydrogen stations produce hydrogen on-site. The hydrogen production process requires several units, including desulfurizers, reformers, water gas shift reactors, and  $H_2$  separation apparatuses.

However, in addition to hydrogen, the reformate gas produced by the hydrogen production process also contain by-products, such as carbon monoxide. These by-products tend to contaminate the anode catalysts of polymer electrolyte membrane (PEM)

fuel cells. The removal of carbon monoxide in the hydrogen stream is a critical yet challenging issue. Many strategies have

been applied to facilitate reformate cleaning, including the appli-

cation of membrane technology [1–4].

is a simple and low-energy method. In particular, ceramic composite membranes have high thermal, chemical, and mechanical stabilities than those of polymeric membranes and thus have been expected to more suitable for high temperature and sever conditions. Therefore, this can be accomplished by performing the separation process using tubular-type inorganic membranes,

high temperature conditions. Membrane separation technology

In order to be considered practical, hydrogen stations require small to medium sized hydrogen plants, small spatial occupancy, quick installation, and compact modular configurations. Constructing stations that can continuously generate hydrogen can improve efficiency and limit spatial restrictions. In addition, because the temperature of H<sub>2</sub> mixture produced from reaction is high, the separation technology is needed to work well at

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such as those made from silica or zeolite. Recent transient permeation experiments involving single gases [2] and binary mixtures [1,5] have also raised the possibility of using silica membranes for hydrogen separation.

This study investigated the permeation and separation of reforming gas from natural gas ( $H_2/CH_4/CO/CO_2$ : 69/3/2/26, vol.%) in tubular-type MTES (methyltriethoxysilane) templating silica/ $\alpha$ -alumina composite membrane at transient and steady-state conditions. Since the removal of CO in the reforming gas is quite important, experiments of CO single gas and  $H_2/CO$  (50/50, vol.%) binary mixture were performed separately. In order to depict the permeation and separation mechanisms of multi-component theoretically, the GMS (generalized Maxwell–Stefan) model incorporating the DGM (dust gas model) and Langmuir isotherm model were applied to the experimental results.

#### 2. Theory

A quantitative description of mass transfer in porous media must ensure the local conservation of mass for each participating species. In this study, a dynamic model incorporating mass and energy balances were adopted to analyze the permeation mechanism.

### 2.1. Transient permeation

The mass balance of a component, i, in an infinitesimal volume can be presented as follows [6,7]:

$$\frac{\varepsilon}{RT}\frac{\partial P_i}{\partial t} + (1 - \varepsilon)\frac{\partial q_i}{\partial t} = -\frac{1}{r}\frac{\partial (rN_i^{\text{tot}})}{\partial r} \quad (i = 1, \dots, n)$$
 (1)

where  $P_i$  is the partial pressure,  $q_i$  is the adsorbed phase concentration,  $\varepsilon$  is the porosity and  $N_i^{\text{tot}}$  is the total molar flux. Eq. (1) states that the local partial pressure and concentration of the adsorbed species change with time, depending on the transport rate of the components.

#### 2.2. Total permeation

The total permeation flux is composed of pore diffusion and surface diffusion:

$$N_i^{\text{tot}} = \left(\frac{\varepsilon}{\tau}\right) \cdot N_i^{\text{P}} + (1 - \varepsilon) \cdot N_i^{\text{S}}$$
 (2)

where  $N_i^P$  is the flux by pore diffusion,  $N_i^S$  is the flux by surface diffusion, and  $\tau$  is the tortuosity factor of the membrane layer.

### 2.3. Pore diffusion (DGM)

The multi-component macro- or meso-pore diffusion consisting of Knudsen diffusion and Poiseuille diffusion can be expressed by the DGM (Dusty gas model) [6–8].

$$N_i^{\rm P} = -\frac{\varepsilon}{\tau} \frac{1}{RT} \left( D_i^{\rm Kn} + \frac{B_i^0}{\eta_i} P_i \right) \cdot \frac{\partial P_i}{\partial r}$$
 (3)

For a homogeneous porous structure, the pore diffusion contains the two parameters,  $D_i^{\text{Kn}}$  (Knudsen diffusivity: Eq. (4)) and  $B_i^0$  (viscous diffusion parameter: Eq. (5)). These can be determined by the following equations [9,10]:

$$D_i^{\text{Kn}} = \frac{2r_{\text{P}}}{3} \cdot \sqrt{\frac{8RT}{\pi M_i}} \tag{4}$$

$$B_i^0 = \frac{r_{\rm P}^2}{8} \tag{5}$$

where  $r_P$  is the pore radius, R is the ideal gas constant, T is temperature, M is molecular weight, and  $\eta_i$  is the viscosity of each gas [10,11].

#### 2.4. Surface diffusion (generalized Maxwell–Stefan model)

The molar flux by surface diffusion can be calculated by the GMS model combined with surface coverage. The surface fluxes through a membrane in a single (Eq. (6)) and binary (Eq. (7)) systems are described as below:

$$N_1^{\mathbf{S}} = -\rho \cdot (1 - \varepsilon) \cdot q_1^{\mathbf{Sat}} \cdot \frac{\mathbf{D}_1^{\mathbf{S}}}{1 - \theta_1} \cdot \nabla \theta_1 \quad (i = 1, 2, \dots, n) \quad (6)$$

$$\begin{split} N_{1}^{S} &= -\rho \cdot (1 - \varepsilon) \cdot q_{1}^{\text{sat}} \cdot \frac{\mathbf{D}_{1}^{S}}{1 - \theta_{1} - \theta_{2}} \\ &\cdot \frac{[(1 - \theta_{2}) + \theta_{1}(\mathbf{D}_{2}^{S}/\mathbf{D}_{12}^{S})]\nabla\theta_{1} + [\theta_{1} + \theta_{1}(\mathbf{D}_{2}^{S}/\mathbf{D}_{12}^{S})]\nabla\theta_{2}}{\theta_{2}(\mathbf{D}_{1}^{S}/\mathbf{D}_{12}^{S}) + \theta_{1}(\mathbf{D}_{2}^{S}/\mathbf{D}_{12}^{S}) + 1} \end{split}$$

A special case of Eq. (7) is that friction between molecules is less important than friction with the wall. In that case,  $D_{ij}^{S}$  (= $\infty$ ) is much higher than  $D_{i}^{S}$ , and Eq. (7) is reduced to

$$N_1^{S} = -\rho \cdot (1 - \varepsilon) \cdot q_1^{\text{sat}} \cdot \frac{\mathbf{D}_1^{S}}{1 - \theta_1 - \theta_2} \cdot [(1 - \theta_2)\nabla\theta_1 + \theta_1\nabla\theta_2]$$
(8)

And the surface flux of quaternary mixture can be also described as follows:

$$N_1^{S} = -\rho(1-\varepsilon)q_{\text{sat}} \frac{\Phi_1^{S}}{1-\theta_1-\theta_2-\theta_3-\theta_4} \times \left[ (1-\theta_2-\theta_3-\theta_4)\nabla\theta_1 + \theta_1(\nabla\theta_2 + \nabla\theta_3 + \nabla\theta_4) \right]$$
(9)

In this study, the surface coverage,  $\theta_i$ , was calculated by the following Langmuir isotherm model:

$$\theta_i = \frac{q_i}{q_i^{\text{sat}}} = \frac{b_i P_i}{1 + \sum_{j=1}^n b_j P_j}$$
 (10)

If molecule–molecule interactions cannot be ignored, Eq. (7) should be used.  $D_{ij}^{S}$  from the single component diffusivities can be determined by using the empirical relation [10,11]:

$$\mathbf{D}_{ij}^{\mathbf{S}} = \mathbf{D}_{i}^{\mathbf{S}\theta_{i}/(\theta_{i}+\theta_{j})} \mathbf{D}_{i}^{\mathbf{S}\theta_{j}/(\theta_{i}+\theta_{j})} \tag{11}$$

The cross-term diffusivities satisfy the Onsager reciprocity relation [10,12]:

$$\mathbf{D}_{ij}^{\mathbf{S}} = \mathbf{D}_{ii}^{\mathbf{S}} \tag{12}$$

### 2.5. Heat effect

The overall energy balance can be expressed as follows [13,14]:

$$\Delta H_{\text{ads}} \cdot A(N_{i,\text{in}}^{\text{tot}} - N_{i,\text{out}}^{\text{tot}}) = \rho C_{\text{p}} V \frac{\partial T}{\partial t} + h_i A(T_{\text{in}} - T_{\text{out}}) \quad (13)$$

where  $\Delta H_{\rm ads}$  is the heat of adsorption on the membrane, A is the effective membrane area,  $C_{\rm p}$  is the heat capacity, V is the volume of the layer,  $h_i$  is the convective heat transfer coefficient of the feed gas and  $T_{\rm out}$  is the feed temperature.

# 2.6. Temperature dependencies on parameters

The change of temperature leads to variation of surface diffusivity and adsorption equilibrium. The temperature dependency of surface diffusivity can be expressed by the following Arrhenius-type relationship [12,15]:

$$\Phi_i^{\rm S} = \Phi_{0,i}^{\rm S} \, \exp\left(\frac{-E_{\rm D}}{RT}\right) \tag{14}$$

where  $E_D$  is the diffusional activation energy and  $\mathfrak{D}_{0,i}$  is the diffusivity at infinite temperature. The temperature dependency of adsorption parameters,  $q_i^{\text{sat}}$  and  $b_i$ , can be calculated with the LRC (loading ratio correlation) using the Langmuir isotherm [9] and  $b_i$  is related to heat of adsorption using the van't Hoff equation [10]

$$q_i^{\text{sat}} = \frac{k_1}{T^{k_2}} \tag{15}$$

$$b_i = b_{i,0} \exp\left(\frac{\Delta H_{\text{ads}}}{RT}\right) \tag{16}$$

where  $k_1$  and  $k_2$  are the fitting parameters and  $b_{i,0}$  is the Langmuir parameter at zero loading.

# 3. Experimental

# 3.1. Membrane preparation

A MTES sol as the structure-directing agent was used for the templating material in the fabrication of a nano-porous silica/ $\alpha$ -alumina composite membrane. The SiO<sub>2</sub>/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> composite support (1.6 nm mean pore diameter) was prepared using a pressurized coating of colloidal silica sol inside the tubular  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> supports (7.8 mm outside diameter, 6.2 mm inside diameter, 0.8 mm thickness, 100 mm length, and 0.1  $\mu$ m mean pore diameter). The organic templating silica sol was prepared from the mixture of silica sol and organic template MTES. The organic templating silica composite membrane was then fabricated by dip-coating the SiO<sub>2</sub>/ $\alpha$ -Al<sub>2</sub>O<sub>3</sub> composite supports in the templating silica sols. The whole process of dip-coating, drying, and calcining was repeated several

times to repair any defects in the silica layer. The pore size of the silica composite membrane was controlled using the TEOS-EtOH solution. In this study, to identify the mechanical strength of the membrane, the burst strength of the membrane was measured by using the hydraulic pressure (water at room temperature) of  $10\,{\rm kg_f\,cm^{-2}}$ , under which condition the membrane showed no damage. The synthesis and characteristics of the membrane have previously been described in detail [5,16,17]

### 3.2. Permeation experiments

The permeation experiments in the inorganic membranes were performed at temperatures between 323 and 473 K and pressures of 100-600 kPa The permeation experiments of pure gas (CO, 99.99% purity) were measured in dead-end mode without the retentate stream, and the permeation/separation experiments of binary (H<sub>2</sub>/CO, 50/50, vol.%) and quaternary (H<sub>2</sub>/CH<sub>4</sub>/CO/CO<sub>2</sub>, 69/3/2/26, vol.%) mixtures were measured in stage-cut mode by controlling feed and retentate flow rates. The permeation flux and composition were measured using a mass flow meter and an online quadrupole mass spectrometer (QMG 422, Balzers Co., Germany). Experiments involving a depressurization (DP, feed pressure → atmospheric pressure) step and a pressurization (PR, atmospheric pressure → feed pressure) step were performed to investigate permeation/separation mechanism. In general, the pores in inorganic membranes become occupied by contaminating molecules due to their adsorption at low temperature, resulting in the hindrance of permeation of desired molecules. In order to alleviate this problem, a backwashing (DP) step was added to the experimental process. In addition, the permeation mechanism can be confirmed by DP experimental results. The detailed experimental system and the permeation measurement procedure were described in a previous study [2,5].

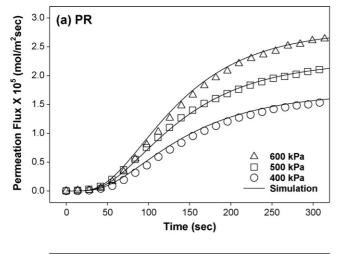
#### 3.3. Numerical simulation

In this study, the gPROMS modeling tool (Process Systems Enterprise Ltd.) was used to obtain the solution of dynamic simulation from the mathematical model mentioned above. A centered finite difference method (CFDM) of the second order was applied to the spatial partial derivatives. The DAEs (differential-algebraic equations) for temporal domain were subsequently integrated by employing an integrator, called DASOLV, included in the gPROMS library. The results of numerical simulation were stable for the range of conditions used in this study.

#### 4. Results and discussion

# 4.1. Transient permeations of pure CO: pressure and temperature effect

Since CO acts as a poison for fuel cells, it is important to remove CO from reforming gas before use. Elucidating the permeation mechanisms of pure CO is needed in order to understand



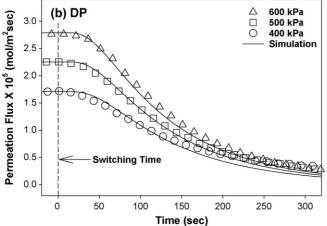
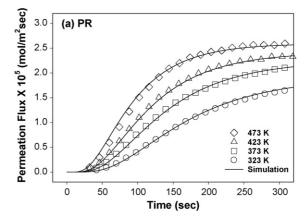


Fig. 1. Pressure effect of transient permeation flux of CO on a MTES templating silica/ $\alpha$ -alumina composite membrane: (a) PR step and (b) DP step at 373 K: dead end (stage cut = 1) and sweeping gas (flow rate =  $0.68 \times 10^{-6}$  m<sup>3</sup> s<sup>-1</sup>) condition.

the process by which hydrogen is separated from natural gas. Fig. 1 shows the effect of pressure on transient permeation flux of CO at 373 K. Increased pressure caused the occupancy of CO on the membrane layer to increase and the time to reach the steady state to decrease slightly. This is because the chemical potential gradient of the adsorbed phase decreases as coverage approaches saturation at higher pressure. In addition, the time to reach the steady state of desorption in MTES membrane was similar at all pressure ranges during the depressurization (DP) step (Fig. 1b).

Temperature changes can also have a great influence on CO permeation behavior. Fig. 2 shows the effect of temperature on transient permeation flux of CO at 500 kPa. As shown in Fig. 2, the time required to reach steady-state flux at both PR and DP steps decreased with increasing temperature due to the activation of molecules [2]. Moreover, as shown in Fig. 2b, the desorption rate at the DP step became faster at higher temperature in the adsorptive porous membrane layer. Therefore, the transient permeation flux curves at low and high temperatures crossed during the time interval between 50 and 100 s.



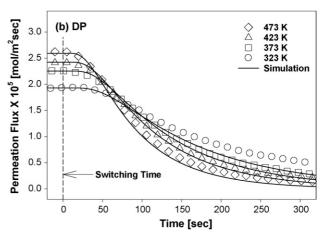


Fig. 2. Temperature effect of transient permeation flux of CO on a MTES templating silica/ $\alpha$ -alumina composite membrane: (a) PR step and (b) DP step at 500 kPa: dead end (stage cut=1) and sweeping gas (flow rate=0.68 × 10<sup>-6</sup> m<sup>3</sup>s<sup>-1</sup>) condition.

# 4.2. Comparison of steady-state permeation of pure CO to other molecules

Fig. 3 shows the steady-state fluxes of pure gases at feed pressure and temperature under dead end condition. The permeance

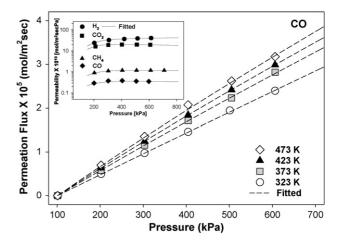


Fig. 3. Permeation flux of pure CO on a MTES templating silica/ $\alpha$ -alumina composite membrane at 323–473 K and referenced permeabilities of  $H_2$ ,  $CO_2$ ,  $CH_4$  and CO pure gases at 473 K: dead end (stage cut = 1) and sweeping gas (flow rate =  $0.68 \times 10^{-6} \, \text{m}^3 \, \text{s}^{-1}$ ) condition.

and permselectivity of single gas in the templating membrane were discussed in the previous study in terms of pore and membrane structure, molecular size and adsorption affinity [2]. In this study, the CO results in the membrane were compared to the characteristics of the other single gases. The permeation fluxes of CO were linearly proportional to feed pressure, which is similar to the permeation flux of  $H_2$  on the MTES membrane.  $CO_2$  and  $CH_4$  both have strong adsorption affinities on the membrane and favorable permeation flux curvatures [2]. Therefore, CO is presumed to be a weak adsorbate. In addition, the increase in permeate flux of CO with rising temperature is similar to the results with  $H_2$  and  $CH_4$  and different from the results with  $CO_2$  [2]. Therefore, the diffusional mechanism of CO in the membrane is presumed to be similar to that of  $H_2$  and  $CH_4$ .

Using steady-state permeation flux (Eq. (2)) in Fig. 3 and transient permeation flux (Eq. (1)) in Figs. 1 and 2, the single gas transport parameters, such as Maxwell–Stefan diffusivity (Eq. (6)), Langmuir parameter and saturated amount of adsorption (Eq. (10)), were estimated with the gPROMS estimation tool. As shown in Figs. 1–3, the simulated results for the PR and DP steps agreed well with the experimental results, including the steady-state and transient permeation behaviors. The obtained values and permeabilities of each gas are presented in Table 1.

Table 1 and Fig. 3 demonstrate that the permeance of  $H_2$  and  $CO_2$  was higher than the others. Increased permeance of  $H_2$  was ascribed to its small molecular size and the increased permeance of  $CO_2$  was ascribed to its high surface diffusion [2]. However, the permeance of CO on the MTES membrane was much lower ( $CO \approx 4.79 - 6.46 \times 10^{-11}$  mol m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>) than that of the other molecules. It is noteworthy that the diffusivity of  $CH_4$  is slightly lower than that of CO (Table 1), even though the permeance of  $CH_4$  is far higher than that of CO. This may be due to differences in molecular structure between  $CH_4$  and

CO. While CO has a linear structure, CH<sub>4</sub> has a tetrahedral molecular structure which might adversely affect diffusion due to steric hindrance. On the contrary, the contribution of surface diffusion to permeance is higher for CH<sub>4</sub> than for CO, owing to the stronger adsorption affinity of CH<sub>4</sub>.

# 4.3. Transient permeation and separation of $H_2/CO$ binary system

The permeation flux and separation factor of the  $H_2/CO$  (50:50, vol.%) binary mixture were measured as functions of pressure and temperature. Fig. 4a shows the transient permeation curves of the  $H_2/CO$  mixture at 373 K and 600 kPa at the PR step.  $H_2$  molecules started to permeate the membrane within 10 s; however, only minor permeation of CO was observed after 50 s. The permeation flux of  $H_2$  reached plateau (steady state) at about 150 s while that of CO reached plateau at about 250 s.

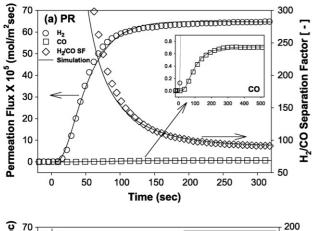
The experiments using single gases showed that the permeation flux of  $H_2$  reached steady state within 30 s [2] while that of CO took over 500 s to reach steady state. However, comparison of Fig. 4a to Figs. 1 and 2 reveals that the permeation flux rate of CO in the  $H_2$ /CO mixture increased while that of  $H_2$  decreased.  $H_2$  permeation was inhibited by CO molecules that had become stagnated after being adsorbed into membrane pores. In contrast, CO permeation was enhanced by  $H_2$  permeation. Similar phenomena were also observed in other  $H_2$  binary systems [1].

Fig. 4b demonstrates that the simulated results for the CO transient curve at the DP step agreed well with experimental data in spite of using estimated parameters from PR step transient curve. On the contrary, the transient permeation behavior of H<sub>2</sub> at the DP step differed significantly from the result at the PR step. This resulted in a large deviation between simulated and experimental results in permeation flux and separation fac-

Table 1	
Permeance, diffusivity, saturated amount of adsorption and Langmuir parameter of H <sub>2</sub> , CH <sub>4</sub> , CO, and CO <sub>2</sub> on MTES membrane	

	Permeance $(\text{mol m}^{-2} \text{ s}^{-1} \text{ Pa}^{-1})$	$D_1^S (m^2 s^{-1})$	$q_{\rm sat}~({ m mol}~{ m g}^{-1})$	b (Pa <sup>-1</sup> )
$\overline{H_2}$				
323 K	$2.89 \times 10^{-9}$	$8.50 \times 10^{-11}$ a	$9.60 \times 10^{-3}$ a	$2.30 \times 10^{-7a}$
373 K	$4.79 \times 10^{-9}$	$1.97 \times 10^{-10}$ a	$8.05 \times 10^{-3}$ a	$1.96 \times 10^{-7}$ a
423 K	$6.11 \times 10^{-9}$	$2.60 \times 10^{-10a}$	$7.92 \times 10^{-3}$ a	$1.94 \times 10^{-7}$ a
473 K	$6.62 \times 10^{-9}$	$2.81 \times 10^{-10a}$	$7.90 \times 10^{-3}$ a	$1.93 \times 10^{-7}$ a
CH <sub>4</sub>				
323 K	$1.20 \times 10^{-10}$	$1.27 \times 10^{-12a}$	$1.60 \times 10^{-3}$ a	$6.10 \times 10^{-6a}$
373 K	$1.29 \times 10^{-10}$	$1.88 \times 10^{-12a}$	$1.43 \times 10^{-3}$ a	$4.90 \times 10^{-6a}$
423 K	$1.39 \times 10^{-10}$	$2.60 \times 10^{-12}$ a	$1.30 \times 10^{-3}$ a	$4.05 \times 10^{-6a}$
473 K	$1.45 \times 10^{-10}$	$2.95 \times 10^{-12a}$	$1.28 \times 10^{-3}$ a	$3.90 \times 10^{-6a}$
CO				
323 K	$4.79 \times 10^{-11}$	$1.46 \times 10^{-12a}$	$4.20 \times 10^{-4}$ a	$1.10 \times 10^{-6}$
373 K	$5.58 \times 10^{-11}$	$3.50 \times 10^{-12a}$	$4.15 \times 10^{-4}$ a	$1.08 \times 10^{-6}$
423 K	$5.97 \times 10^{-11}$	$5.10 \times 10^{-12a}$	$4.05 \times 10^{-4}$ a	$1.00 \times 10^{-6}$
473 K	$6.46 \times 10^{-11}$	$7.70 \times 10^{-12a}$	$3.90 \times 10^{-4}$ a	$8.20 \times 10^{-7}$
$CO_2$				
323 K	$3.05 \times 10^{-9}$	$1.69 \times 10^{-11}$ a	$5.12 \times 10^{-3}$ a	$6.11 \times 10^{-6a}$
373 K	$2.46 \times 10^{-9}$	$3.10 \times 10^{-11}$ a	$2.60 \times 10^{-3}$ a	$4.00 \times 10^{-6a}$
423 K	$2.00 \times 10^{-9}$	$3.60 \times 10^{-11}$ a	$1.94 \times 10^{-3}$ a	$3.45 \times 10^{-6a}$
473 K	$1.50 \times 10^{-9}$	$4.21 \times 10^{-11}$ a	$1.37 \times 10^{-3}$ a	$3.11 \times 10^{-6a}$

<sup>&</sup>lt;sup>a</sup> Referred from Moon et al. [2].



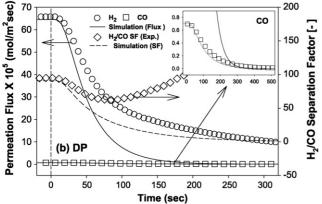


Fig. 4. Transient permeation flux in  $H_2/CO$  binary mixture (50/50, vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 323 K and 500 kPa: (a) PR (pressurization) step and (b) DP (depressurization) step. Sweeping gas flow rate (=0.85  $\times\,10^{-6}\,m^3s^{-1})$  and stage cut (=0.60) were maintained constantly.

tor. As shown in Fig. 4b, the permeation flux of  $H_2$  decreased drastically at the beginning of the DP step. However, the tailing phenomenon was observed after  $100 \, s$  because  $H_2$  molecules with small kinetic diameter and low adsorption affinity (Table 1) remain in the pore under near atmospheric condition.

Fig. 5 shows temperature dependencies of transient permeation flux and separation factor of  $H_2/CO$  mixture (50/50, vol.%) and Table 2 shows the permeance and diffusivity estimated from experimental data on the MTES membrane at various temperatures and fixed pressure (500 kPa). As shown in Fig. 5 and Table 2, permeance and diffusivity of CO in the  $H_2/CO$  binary system were increased with temperature. In addition, both the permeation flux and rate to reach steady state increased with temperature. This is because both  $H_2$  and CO are weak-adsorptive

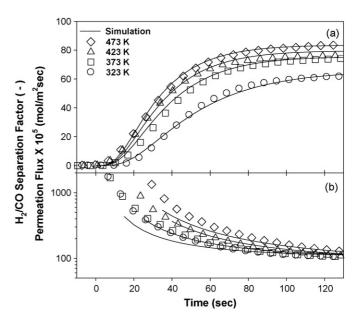


Fig. 5. Temperature dependencies of transient permeation flux of  $H_2/CO$  binary mixture (50/50, vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 500 kPa: (a)  $H_2/CO$  binary mixture permeation fluxes and (b)  $H_2/CO$  separation factor. Sweeping gas flow rate (=0.85 × 10<sup>-6</sup> m<sup>3</sup> s<sup>-1</sup>) and stage cut (=0.60) were maintained constantly.

molecules and their molecular movements are activated with temperature. The shape of the transient permeation flux curve of CO changed was significantly when the temperature was raised from 323 to 373 K, which was similar to the results with pure CO in Fig. 2a. Unlike transient permeation flux behaviors, the  $H_2/CO$  separation factors (flux ratio between  $H_2$  and CO) were not significantly affected by temperature, except for at the initial onset of the experiment (Fig. 5b).

# 4.4. Steady-state permeation and separation of $H_2/CO$ binary system

Fig. 6 shows the steady-state permeation flux curve and separation factor of the  $H_2/CO$  mixture in the range of 323–473 K. The steady-state permeation flux of  $H_2/CO$  mixture was almost linearly proportional to feed pressure. The average permeance and separation factor were  $1.53-2.04 \times 10^{-9}$  mol m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup> and 92.99–110.40, respectively.

Due to increased mobility of the molecules in the MTES membrane pores, the permeation flux of  $H_2/CO$  mixture increased with temperature (Fig. 6a). The separation factor of  $H_2/CO$  mixture increased with temperature at a fixed pressure,

Table 2 The permeance and Maxwell–Stefan diffusivity of  $H_2/CO$  mixture

	Permeance (mol m <sup>-2</sup> s <sup>-1</sup> Pa <sup>-1</sup> )		$D_1^{S}$ (m <sup>2</sup> s <sup>-1</sup> )		
	H <sub>2</sub> /CO	$H_2$	CO	$\overline{ ext{H}_2}$	СО
323 K	$1.53 \times 10^{-9}$	$1.51 \times 10^{-9}$	$1.63 \times 10^{-11}$	$2.70 \times 10^{-11}$	$4.60 \times 10^{-12}$
373 K	$1.83 \times 10^{-9}$	$1.81 \times 10^{-9}$	$1.73 \times 10^{-11}$	$3.75 \times 10^{-11}$	$8.20 \times 10^{-12}$
423 K	$1.98 \times 10^{-9}$	$1.96 \times 10^{-9}$	$1.85 \times 10^{-11}$	$4.08 \times 10^{-11}$	$1.16 \times 10^{-11}$
473 K	$2.04 \times 10^{-9}$	$2.02 \times 10^{-9}$	$1.83 \times 10^{-11}$	$4.40 \times 10^{-11}$	$1.60 \times 10^{-11}$

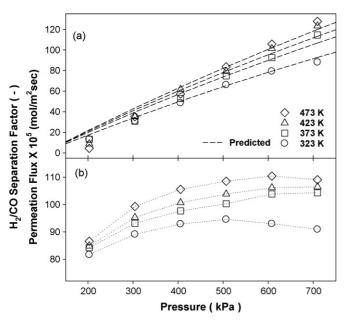


Fig. 6. Steady-state permeation of  $H_2/CO$  binary mixture (50/50, vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 323–473 K: (a)  $H_2/CO$  binary mixture permeation fluxes and (b)  $H_2/CO$  separation factor. Sweeping gas flow rate (=0.85 ×  $10^{-6}$  m<sup>3</sup> s<sup>-1</sup>) and stage cut (=0.60), were maintained constantly.

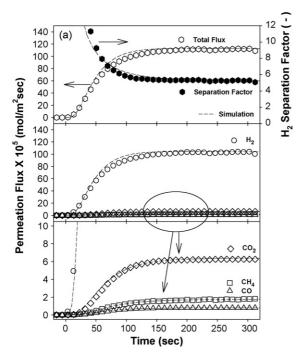
and also increased slightly with pressure at a fixed temperature (Fig. 6b). Fig. 3 indicates that the permeation flux of pure CO increased almost linearly with pressure; however the increasing ratio of CO permeation flux was much smaller than that of  $H_2$  [2]. As a result, the  $H_2$ /CO separation factor did not increase linearly with pressure. Except for 323 K, the separation factor at

Table 3 The permselectivities and separation factors of  $H_2/CH_4$ ,  $H_2/CO$ ,  $H_2/CO_2$  binary mixtures (50/50, vol.%) at 600 kPa and 323–473 K temperature range

	H <sub>2</sub> /CH <sub>4</sub> <sup>a</sup>	H <sub>2</sub> /CO	$H_2/CO_2^a$	
Permselectivity				
323 K	24.01	61.39	0.99	
373 K	36.58	86.97	2.08	
423 K	43.24	103.60	3.28	
473 K	44.18	103.59	4.48	
Separation factor				
323 K	10.49	92.99	1.68	
373 K	16.17	104.83	3.00	
423 K	18.64	106.16	4.36	
473 K	20.74	110.40	6.45	

a Referred from Moon et al. [1].

each temperature was converged between 100 and 110 with an increase in pressure. Since CO molecules are weakly adsorbed on the pore wall compared to the other adsorptive molecules, such as CO<sub>2</sub> and CH<sub>4</sub>, H<sub>2</sub> permeation is less disturbed by CO. Therefore, in the H<sub>2</sub>/CO system, higher separation factors could be expected than those in the H<sub>2</sub>/CO<sub>2</sub> and H<sub>2</sub>/CH<sub>4</sub> systems [1]. As shown in Table 3, the permselectivity calculated from single gas permeation was different from the separation factor obtained from binary separation. However, since the permeation mechanisms of H<sub>2</sub> and CO are dominated by molecular sieving rather than surface diffusion, especially at higher temperature, the permselectivity became similar to the separation factor. In addition, the separation factor increased relative to temperature in all the binary systems.



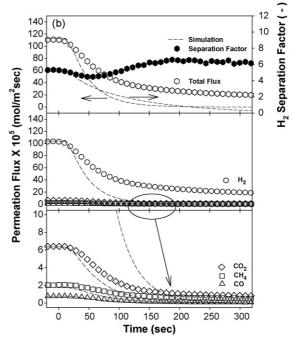


Fig. 7. Transient permeation flux and separation factor of  $H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26, vol.%) at (a) PR step and (b) DP step on a MTES templating silica/ $\alpha$ -alumina composite membrane at 373 K and 600 kPa: top) total flux and  $H_2$  separation factor, middle and bottom) transient permeation of each gases. Sweeping gas flow rate (=0.85 × 10<sup>-6</sup> m<sup>3</sup>s<sup>-1</sup>) and stage cut (=0.60) were maintained constantly.

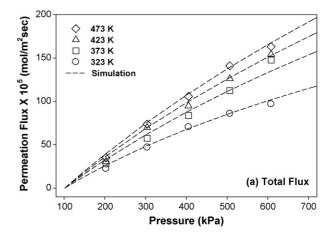
# 4.5. Transient permeation and separation of quaternary mixture

Fig. 7 shows the transient permeation and separation factor curves for the  $\rm H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26, vol.%) at 373 K and 600 kPa (500 kPa pressure drop). The composition of quaternary mixture used in this study was similar to the actual gas mixture produced using a hydrogen reformer on natural gas.

Fig. 7a demonstrates that, during the PR step, transient permeation of H<sub>2</sub> molecules started within 10 s while permeation of other components was observed after 10-20 s. Initially, little permeation was observed due to the competitive adsorption and pore filling that occurred in the silica layer of the membrane. After a certain period of time, CO<sub>2</sub>, CH<sub>4</sub> and CO began to permeate the membrane in sequence. Unlike the adsorptive molecules through the zeolite- or CMS-type membrane [1,2], the roll-up phenomenon was not observed in the transient permeation profiles in spite of the weak adsorption of H<sub>2</sub> and strong adsorption of CO<sub>2</sub> or CH<sub>4</sub> in the membrane pores. As the adsorption process proceeded, the vacant sites in the pore were mainly occupied by CO<sub>2</sub>. This is because of the strong adsorption affinity and high partial pressure of CO<sub>2</sub> in the feed. Therefore, the surface concentration of CO and CH<sub>4</sub> with lower diffusivity and H<sub>2</sub> with weak adsorption affinity could not be intensified to show the roll-up. Furthermore, Fig. 7a showed that CO could be removed most effectively from the feed gas in the MTES membrane due to the higher adsorption affinity and hindrance effect of CO<sub>2</sub> and  $CH_4$ .

Fig. 7b shows the transient permeation flux of  $H_2$  quaternary mixture at the DP step. The sequence to reach the completely desorbed (regenerated) state of each component is the same as the results at the PR step in Fig. 8a. In this study, both diffusivity difference and competitive adsorption between molecules work as a driving force of permeation and separation. As shown in Fig. 7a, the transient simulated results at the PR step were well fitted to the experimental data. However, in the case of the DP step, some deviations in the transient curves of  $H_2$  and  $CO_2$  were observed between the simulated results and experimental data in Fig. 7b when the parameters obtained at the PR step were applied. This implies that the mechanism at the PR step is different from that at the DP step.

Similar to the phenomenon observed with the  $H_2/CO$  binary mixture, the permeation flux of  $H_2$  at the beginning of the DP step decreased drastically. Since  $H_2$  permeation is mainly affected by pore diffusion or molecular sieving rather than by surface diffusion, the diminished pressure drop at the DP step was not a significant driving force for  $H_2$  permeation. In addition, because surface diffusion is the dominant transport mechanism of  $CO_2$  on the MTES membrane, concentration gradient is more important than pressure difference for driving membrane transport. Therefore, the permeation flux of these molecules decreased drastically over time. Moreover, the tailing phenomenon in the quaternary mixture was observed after 100 s, which was the same as the result with the  $H_2/CO$  binary mixture in Fig. 4. At the DP step,  $H_2$  with low adsorption affinity remained in the pore and the permeation was disturbed by the other gases when the pres-



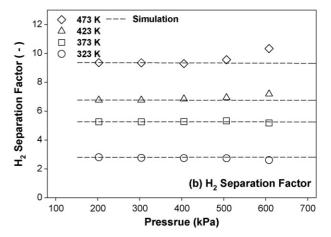


Fig. 8. Steady-state permeation of  $H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26 vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 323–473 K: (a) permeation flux and (b)  $H_2$  separation factor. Sweeping gas flow rate (=0.85  $\times$  10<sup>-6</sup> m<sup>3</sup> s<sup>-1</sup>) and stage cut (=0.60) were maintained constantly.

sure approached atmospheric conditions., particularly by  $CO_2$  and partially  $CH_4$ . However, it is noted that the permeation flux of CO reaches to zero concentration without any tailing at the DP step. Therefore, it is confirmed that CO molecules are very weakly adsorbed in the membrane pore at the PR step as mentioned above.

# 4.6. Steady-state permeation and separation of $H_2/CH_4/CO/CO_2$ quaternary mixture

Fig. 8 shows the steady-state permeation and separation factor of  $H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26, vol.%) through the MTES membrane. The permeation flux of the quaternary mixture became almost linearly proportional to feed pressure with an increase in temperature, whereas the separation factor variation was comparatively small with feed pressure. The separation factor could be improved by increasing temperature at the pressure range tested. The permeance of the quaternary mixture on the MTES membrane is  $2.07-3.37 \times 10^{-9} \, \text{mol m}^{-2} \, \text{s}^{-1} \, \text{Pa}^{-1}$  and the separation factor of  $H_2/(CH_4 + CO + CO_2)$  is 2.61-10.33 (Table 4).

Table 4
Permeance and separation factor of quaternary mixture (H<sub>2</sub>/CH<sub>4</sub>/CO/CO<sub>2</sub>: 69/3/2/26, vol.%)

	Permeance ( $\operatorname{mol} \operatorname{m}^{-2} \operatorname{s}^{-1} \operatorname{Pa}^{-1}$ )	Permselectivity	Separation factor
323 K	$2.07 \times 10^{-9}$	1.12	2.61
373 K	$2.84 \times 10^{-9}$	2.30	5.18
423 K	$3.10 \times 10^{-9}$	3.61	7.18
473 K	$3.37 \times 10^{-9}$	5.19	10.33

In the quaternary mixture, the feed stream was mainly composed of H<sub>2</sub> and CO<sub>2</sub>. In addition, as shown in Table 1, single gas permeabilities of CH<sub>4</sub> and CO on MTES membranes are far lower than those of H<sub>2</sub> and CO<sub>2</sub>. The permselectivity and separation factor of the H<sub>2</sub>/CO<sub>2</sub> mixture are far lower than those of the other binary mixtures due to the strong adsorption affinity and fast surface diffusion of CO<sub>2</sub> [1]. In addition, CH<sub>4</sub> and CO played relatively minor roles in the quaternary mixture permeation/separation behaviors owing to their weak adsorption affinity and slow diffusion. Therefore, the permeation behavior of the quaternary mixture was similar to that of the H<sub>2</sub>/CO<sub>2</sub> mixture. Moreover, as shown in Table 4, the separation factor at each temperature was approximately two-fold higher than the permselectivity. This implies that molecular interactions contribute to the permeation and separation of the quaternary mixture on the METS membrane.

Fig. 9 shows the steady-state permeation of each component ((a) H<sub>2</sub>, (b) CH<sub>4</sub>, (c) CO, and (d) CO<sub>2</sub> in H<sub>2</sub>/CH<sub>4</sub>/CO/CO<sub>2</sub> quaternary mixture (69/3/2/26, vol.%)) at 473K on the MTES membrane. In the quaternary mixture, H<sub>2</sub> was found to have almost linear permeation flux relative to increasing feed pressure. On the contrary, CO<sub>2</sub> permeation flux exhibited a favorable curvature. The permeation fluxes of CH<sub>4</sub> and CO were linear with respect to changes in pressure; however, the CH<sub>4</sub> and CO

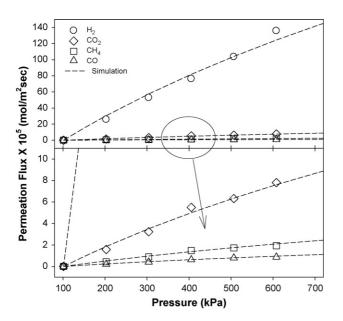


Fig. 9. Steady-state permeation of each component in  $H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26, vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 373 K: Sweeping gas flow rate (=0.85  $\times$  10<sup>-6</sup> m<sup>3</sup> s<sup>-1</sup>) and stage cut (=0.60), were maintained constantly.

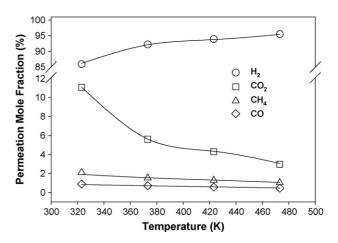


Fig. 10. Temperature dependency of permeation mole fraction of  $H_2/CH_4/CO/CO_2$  quaternary mixture (69/3/2/26, vol.%) on a MTES templating silica/ $\alpha$ -alumina composite membrane at 500 kPa and 323–473 K. Sweeping gas flow rate (=0.85  $\times$  10 $^{-6}$  m³s $^{-1}$ ) and stage cut (=0.60) were maintained constantly.

permeation fluxes varied only slightly compared to those of  $H_2$  and  $CO_2$ .

Fig. 10 shows the temperature dependency of permeation mole fraction of  $H_2/CH_4/CO/CO_2$  mixture. At low temperature, due to the fast surface diffusion and strong adsorption of  $CO_2$ , the permeation of  $H_2$  was significantly hindered by the preoccupied  $CO_2$  in the pore wall of the membrane. Therefore, the low  $H_2$  selectivity was observed in Fig. 8 and the permeation mole fraction of  $CO_2$  was relatively high in Fig. 10. On the contrary, at high temperature, owing to activation of  $H_2$  molecules and unfavorable adsorptive condition of  $CO_2$  in the membrane pores, the permeation flux of  $H_2$  steeply increased whereas that of  $CO_2$  decreased, as mentioned for single gas permeation.

The temperature dependencies of CO and  $CH_4$  in the quaternary mixture are smaller than  $H_2$  and  $CO_2$ . In addition,  $CO_2$  with high partial pressure in the membrane pore leads to hindrance effect for these molecules, even at high temperature. As a result, although the permeation flux of pure CO and  $CH_4$  was increased with temperature, the permeated mole fraction of both molecules in the mixture was slightly decreased, as shown in Fig. 10.

### 5. Conclusions

Since permeance of pure CO on the MTES membrane is very low (CO  $\approx 4.79 - 6.46 \times 10^{-11} \ \text{mol m}^{-2} \ \text{s}^{-1} \ \text{Pa}^{-1}$ ), a high separation factor (92.99–110.40) and permeance (1.53–2.04  $\times$  10<sup>-9</sup> mol m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>) could be obtained from the H<sub>2</sub>/CO binary mixture. The MTES membrane has good potential for application in CO clean-up processes for the fuel cell systems and for use in hydrogen stations. In this study, we were able to develop a membrane process suitable for separating H<sub>2</sub> from CO and other reformate gases (CO<sub>2</sub> or CH<sub>4</sub>) that showed a molecular sieving effect.

Permeance of the quaternary mixture ( $H_2/CH_4/CO/CO_2$ ) on MTES membrane is  $2.07-3.37 \times 10^{-9} \, \text{mol m}^{-2} \, \text{s}^{-1} \, \text{Pa}^{-1}$  and the separation factor of  $H_2/(CO+CH_4+CO_2)$  is 6–24. When the feed pressure was increased, the permeation flux and the

H<sub>2</sub> separation factor increased slightly. Increased temperature caused the permeation flux of H<sub>2</sub> to increase and that of CO<sub>2</sub> to decrease drastically. At low temperature the permeation of H<sub>2</sub> was significantly hindered and low H<sub>2</sub> selectivity was obtained. This was due to the strong surface diffusion effect of CO<sub>2</sub>. On the contrary, the permeation and selectivity of H<sub>2</sub> were increased with temperature because of activation of H2 molecules and unfavorable conditions for CO<sub>2</sub> adsorption. However, because CO and CH<sub>4</sub> showed weak adsorption affinity and slow diffusion on the MTES membrane, their permeation fluxes decreased with an increase in temperature, which was the opposite of what was observed during single gas permeation. Moreover, compared to the other impurities, CO was most successfully removed from the H<sub>2</sub> mixture.

The MTES membrane showed great potential for hydrogen separation from reforming gas with high selectivity and high permeance. Silica membranes are expected to be used for separating hydrogen in reforming environment at high temperatures.

# Acknowledgment

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### Nomenclature

#### Roman letters

 $q_i$ 

 $q_i^{\rm sat}$ 

 $r_{\rm P}$ 

 $(\text{mol } g^{-1})$ 

pore radius (m)

parameter in the Langmuir isotherm model ( $Pa^{-1}$ )  $b_i$ parameter of species i in the Langmuir isotherm  $b_{0,i}$ model at zero loading ( $Pa^{-1}$ ) Poiseuille structural parameters of species i (m<sup>2</sup>)  $D_{:}^{\mathrm{Kn}}$ Knudsen diffusivity of species i (m<sup>2</sup> s<sup>-1</sup>)  $\mathbf{\mathfrak{D}}_{0,i}$ Maxwell-Stefan surface diffusivity at infinite temperature ( $m^2 s^{-1}$ ) Maxwell–Stefan surface diffusivity (m<sup>2</sup> s<sup>-1</sup>)  $\mathbf{D}_i$ activation energy  $(J \text{ mol}^{-1})$  $E_{\rm a}$ heat of adsorption  $(J \text{ mol}^{-1})$  $\Delta H_{\rm ads}$ temperature dependant parameter for saturated  $k_1$ adsorption capacity (mol/g) temperature dependant parameter for saturated  $k_2$ adsorption capacity molecular weight of species  $i \pmod{g^{-1}}$  $M_i$ molar flux of species  $i \pmod{m^{-2} s^{-1}}$ molar flux of pore diffusion of species i  $(\text{mol m}^{-2} \, \text{s}^{-1})$ molar flux of surface diffusion of species i  $(\text{mol m}^{-2} \text{ s}^{-1})$  $N_i^{\text{tot}}$ total molar flux of species of  $i \pmod{m^{-2} s^{-1}}$  $P_i$ partial pressure of species i (Pa)

adsorbed species concentration within layer pores

saturated capacity of adsorbed species  $i \pmod{g^{-1}}$ 

gas constant, 8.314 ( $J \text{ mol}^{-1} \text{ K}^{-1}$ ) R t Tabsolute temperature (K) Greek letters porosity of membrane thermodynamic factor of species i,j $\Gamma_{ij}$ viscosity of species i (Pas)  $\eta_i$ chemical potential of species I (J mol<sup>-1</sup>)  $\mu_i$ fractional surface occupancy of species i  $\theta_i$ membrane density (g m $^{-3}$ ) ρ τ tortuosity factor Subscripts/superscripts i, j, 1, 2component i,j,1,2viscous flow vis Knudsen flow Kn total flow tot

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sat

saturated

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