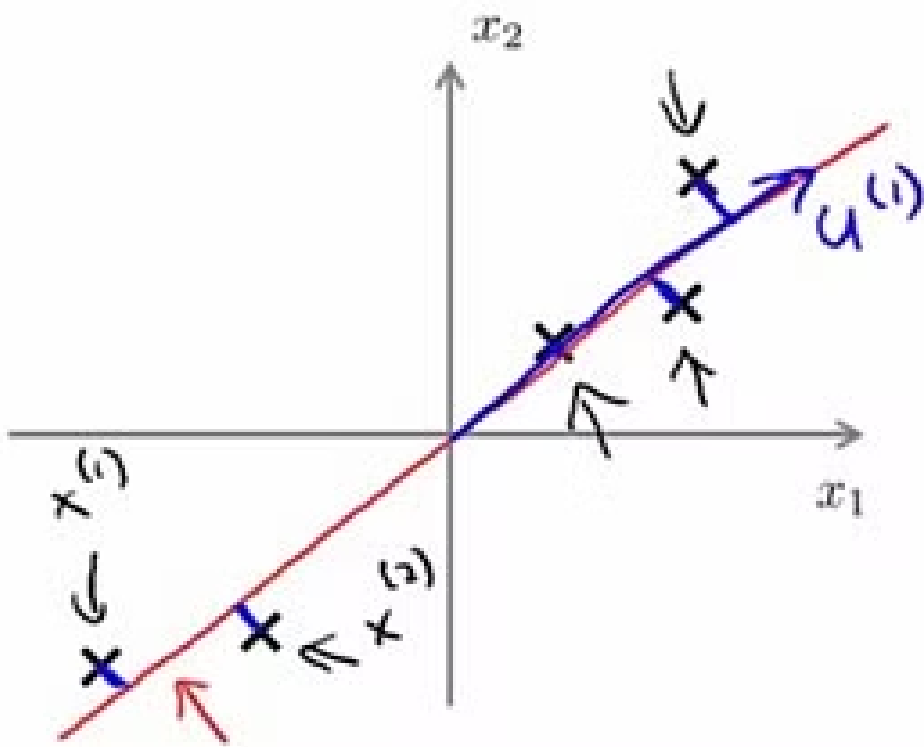


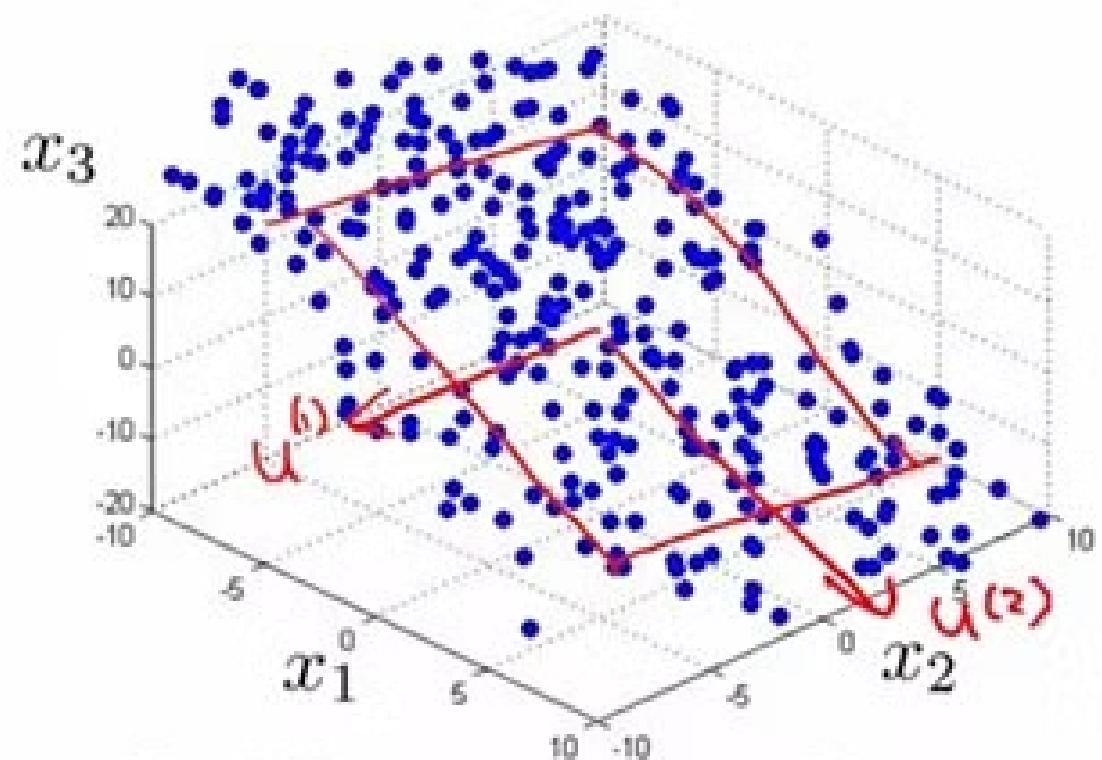
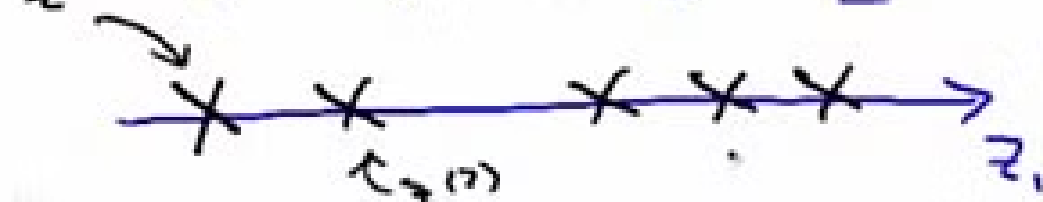
Principal Component Analysis (PCA)

01/04



Reduce data from 2D to 1D

$$x^{(i)} \in \mathbb{R}^2 \rightarrow z^{(i)} \in \mathbb{R}$$



Reduce data from 3D to 2D

- **PCA is a dimensionality reduction technique used in data analysis and machine learning.**
- **It helps uncover patterns and relationships in high-dimensional data.**
- **PCA transforms the data into a new set of variables called principal components.**

Step 1

Standardize the data:

- If features are measured on different scales, standardize them to have zero mean and unit variance.
- Ensures each feature contributes equally to PCA.

Step 2

Compute the covariance matrix:

- Calculate the covariance matrix of the standardized data.
- Represents the relationships between different features.

Step 3

Compute the eigenvectors and eigenvalues:

- **Eigenvectors represent directions of maximum variance.**
- **Eigenvalues indicate the amount of variance captured by each eigenvector.**

Step 4

Select the principal components:

- Sort eigenvalues in descending order.
- Choose the top-k eigenvectors (principal components) based on explained variance.

Step 5

Project the data onto the new feature space:

- **Multiply the standardized data by the selected eigenvectors.**
- **Obtain a new lower-dimensional representation of the data.**

Benefits of PCA:

- **Dimensionality reduction:** PCA reduces the number of features while preserving most of the information.
- **Data visualization:** PCA can visualize high-dimensional data in a lower-dimensional space.

Benefits of PCA:

- **Feature extraction: PCA identifies the most important features that contribute to the variance in the data.**
- **Noise reduction: PCA can eliminate noise by removing low-variance components.**

Applications of PCA:

- **Exploratory data analysis**
- **Pattern recognition**
- **Image and signal processing**
- **Machine learning feature selection**

*Thank
You*