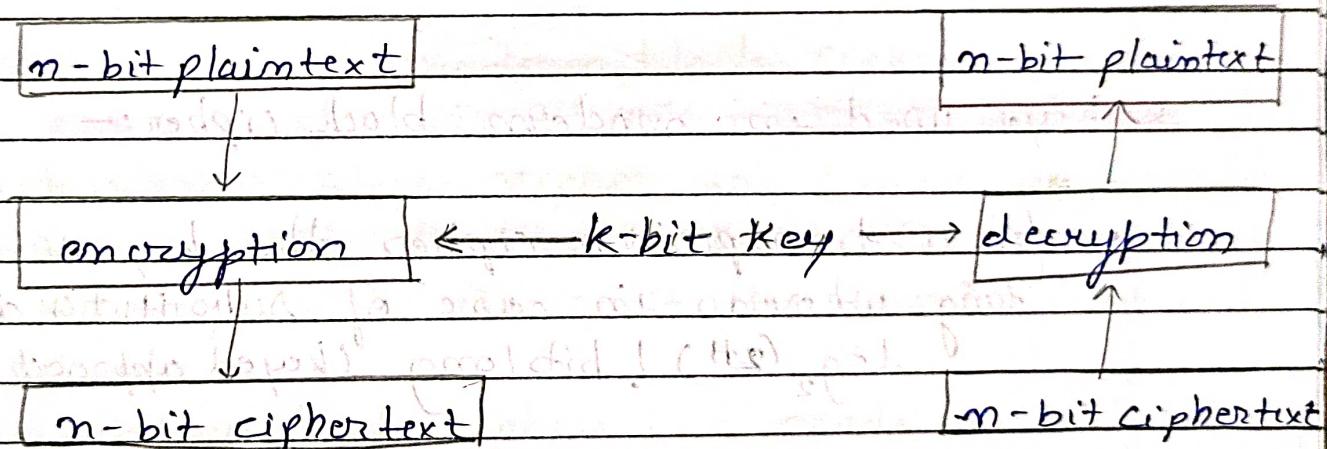


UNIT-2

* Modern block ciphers

- traditional ciphers methods are character oriented whereas modern ciphers methods are bit oriented where the bits are manage in blocks.
- following figure shows a modern block cipher where the plaintext is divided into n -bit blocks and if required padding bits are added to the last block.
- the value of n can be 64, 128, 256 or 512 bits.

fig 5.1 A modern block cipher.



Q - how many padding bits must be added to a message of 100 characters if 8 bit ASCII is used for encoding and block size should be 64 bit.

→ Since $M = 100$ characters and we are using 8 bit the size of message is $= 100 \times 8 = 800$ bits.

Now, we have to convert 800 bits into 64 bit blocks.

no. of blocks $\Rightarrow 12 \Rightarrow 64$ bit blocks

no. of padding bits $\Rightarrow 32 + 32$ i.e. total number of blocks required is $12 + 1 = 13$ bits

a - A modern block cipher is design as a substitution cipher or transposition cipher justify your answer
 → Refer for example Chap 5

→ In block cipher we have to do both substitution and transposition

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→ In block cipher we have to do both substitution and transposition

* keys used in modern block cipher:-

$$n = 128, 64, 256 \text{ or } 512 \text{ bit}$$

for a transposition cipher the key is $\log n!$ bit long whereas in case of substitution cipher is $\log_2(2^n)!$ bit long (keyed approach)

key

- substitution and transposition cipher with keyless cipher

- keyless ciphers are categorized into two parts
 keyless transposition cipher and keyless substitution cipher.

- In keyless transposition cipher there is a fixed key size that consist of permutation cipher and is represented as a table when

called as permutation cipher

(a) (b) (c)

(d)

implemented in software.

- keyless transposition cipher are also called as P-box - diffusion box or P-box - permutation box.
(reorder of the bits)

* keyless substitution cipher:-

- In these method a fixed key of a predetermined size defining mapping from the input to the output is design.

mapping is define either in the form of a table or a mathematical equation.

- keyless substitution cipher is known as S-box {substitution box}
(mapping of the bits)

* components of modern block cipher:-

(generally the key can be chosen as prime no.)

- modern blocks ciphers are keyed substitution ciphers in which the key allows partial mapping from the possible inputs to the possible outputs.

- modern blocks ciphers are made a combination of transposition units {P-box, D-box} and substitution unit {S-box}

- \rightarrow diffusion, confusion

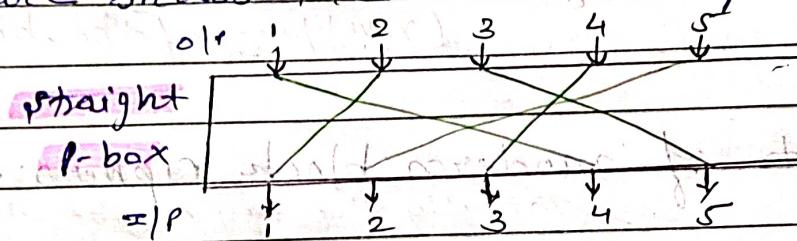
P-Boxes

An $n \times n$ p-box (permutation box) is one of three types:-

- straight p-box
- compression p-box
- expansion p-box

(a) straight p-box:-

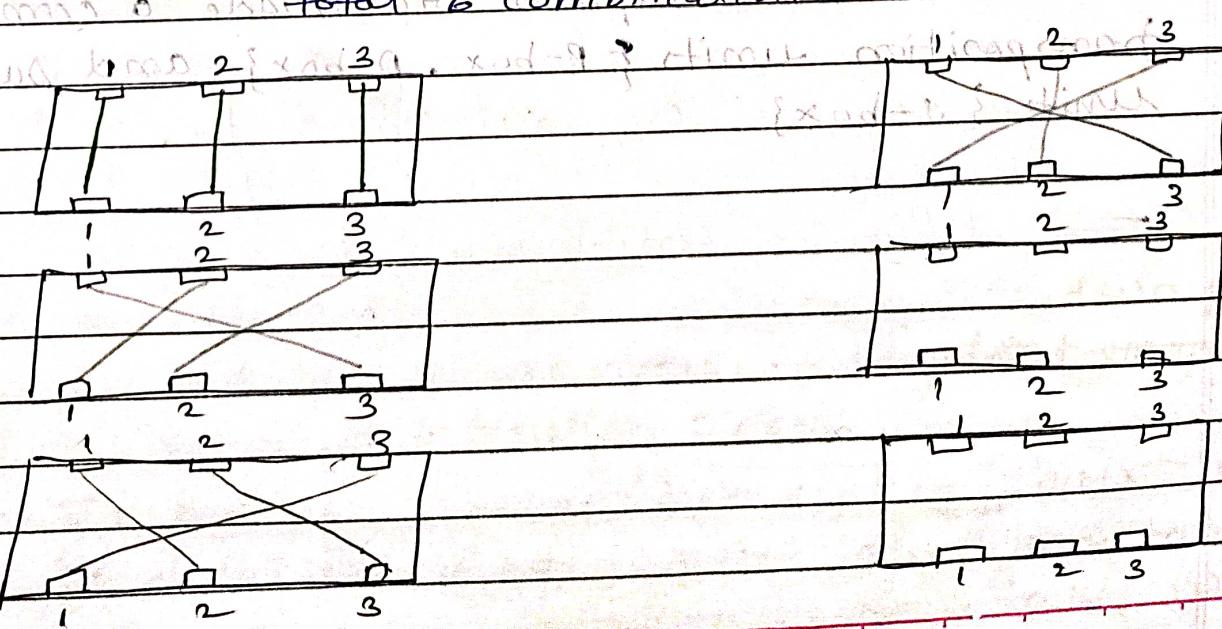
In straight p-box it has 'm' inputs and 'n' outputs. Their one-to-one mapping is possible, following figure shows the above concepts:-



Q- Show all the possible mapping for 3×3 Pox :-

$$\rightarrow m! = 3! = 3 \times 2 \times 1 = 6$$

so there are 6 combinations must be their



- P-boxes are keyless where the mapping is already predetermined. The mapping can be either prewired (hardware) or either tabular (software).
- following shows the examples where the entries in the table are the input and the position of the entries are the output:-

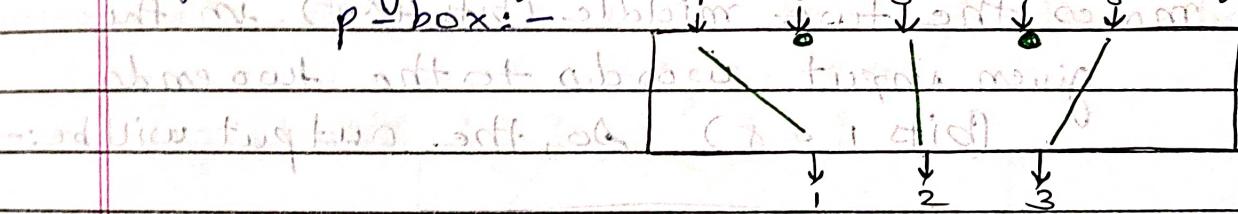
* from the given table the total blocks is 64
or the size of p-box is 64

(b) compression p-box :-

- In compression p-box it has 'm' inputs and 'n' outputs where $m < n$ that is some of the inputs are blocked and do not reach the output



- following figure shows an example of compression p-box:-



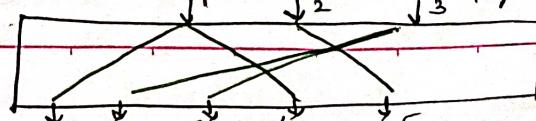
- compression p-box are used when we need to permute the bit and at the same time decrease the number of bits for the next stage.

(c) expansion p-box:-

- An expansion p-box has 'm' inputs & 'n' outputs where $m > n$.

- Thus, some of the outputs are connected to more than one inputs.

- following figures shows the expansion p-box:-



expansion P-box are used when we need to permute the bits and at the same time increase the number of bits for the next stage.

Ques-1) Design an 8×8 permutation table for a 'P' box that moves the two middle bits (bits 4 & 5) in the given input words to the two ends (bits 1 & 8) in the output word. relative position of the other bit should not be changed

→ 8×8 permutation table for a 'P' box as $m = n = 8$ than it is straight P box.

- As given : $\boxed{1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8}$

- moves the two middle bits (bits 4 & 5) in the given input words to the two ends (bits 1 & 8) so, the output will be :-

~~1 2 3 4 5 6 7 8~~

~~4 1 2 3 6 7 8 5~~

Qn-19] A message has 2000 characters. If it is supposed to be encrypted using a block cipher of 64 bits, find the size of the padding and the number of blocks. Given:-

→ message = 2000 characters. 8 bits ASCII

encrypted using block cipher = 64 bits. $2000 \times 8 = 16000$

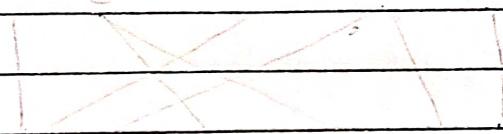
the size of padding bits are = $16000 \div 64$

$\frac{2}{64} \boxed{16000}$

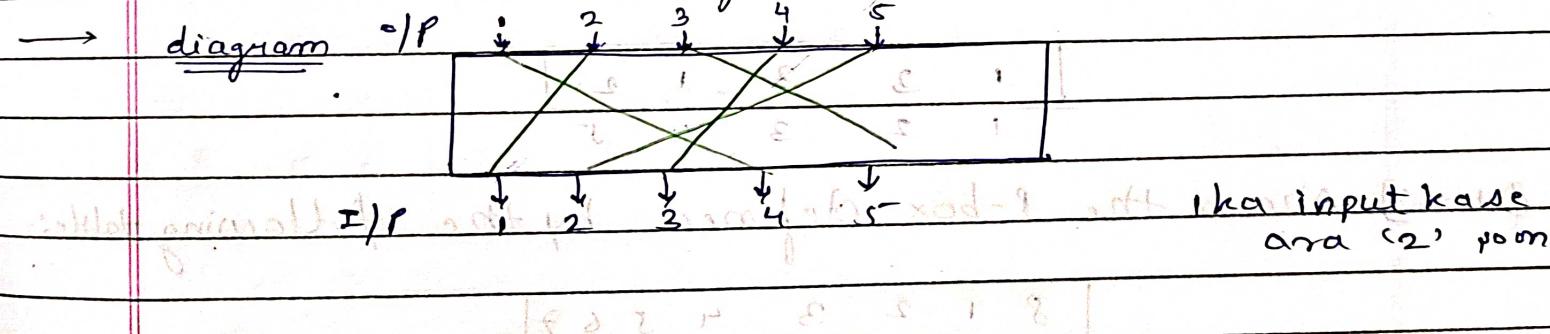
no. of blocks are = 250

→ no. of 64 bits containing with 250 blocks

→ 250 blocks in total



Qn-20] Show the permutation table for the straight P-box in figure 5.4



2	5	4	1	3
---	---	---	---	---

2 small arrows
3 - 1 award 3 blocks 5 blocks

o/p → 1 2 3 4 5

2nd row 3rd row 4th row 5th row

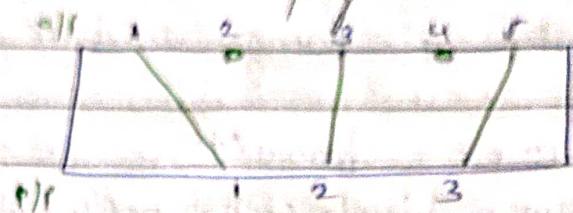
1st row 2nd row 3rd row 4th row 5th row

1st row 2nd row 3rd row 4th row 5th row

1st row 2nd row 3rd row 4th row 5th row

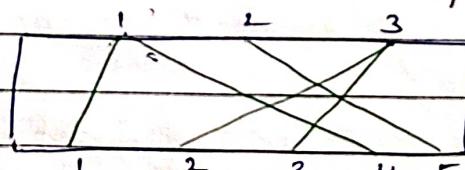
1st row 2nd row 3rd row 4th row 5th row

Ques-18) Show the permutation table for the expansion P-box in figure 5.4:-



O/P →	1 3 5
	1 2 3

Ques-22) Show the permutation table for the expansion P-box in figure 5.4:-

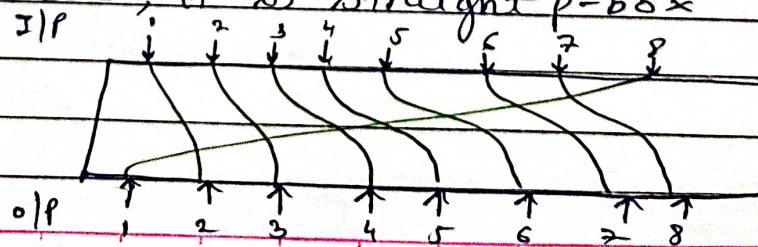


1 3 3 1 2
1 2 3 4 5

Ques-23) Show the P-box defined by the following table:-

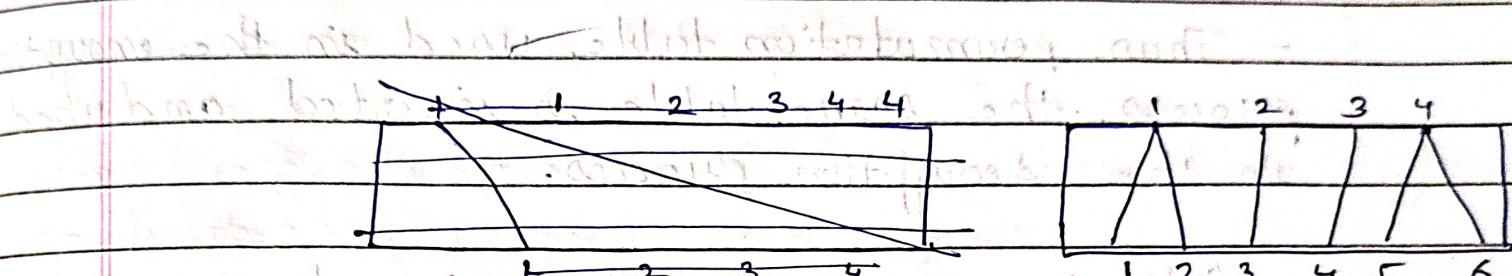
8 1 2 3 4 5 6 7
8 1 2 3 4 5 6 7

→ the above table shows 1-8 same range
hence, it is straight P-box



Ques-24] Determine whether the p-box with the following permutation table is a straight P-box, a compression P-box, or an expansion P-box.

→ As the number of inputs and output is 4, hence, it is an expansion P-box.



Ques-25]

Given the P-box $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (a) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (b) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (c) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (d) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (e) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (f) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (g) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (h) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (i) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (j) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (k) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (l) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

state → diff tool (m) $\{[1 \leq x \leq 2, 0 \leq y \leq 3], [1 \leq x \leq 2, 0 \leq y \leq 3]\}$

* Invertibility :-

- from the three types of p-boxes, a straight p-box is invertible because the number inputs and outputs are mapped 1:1.
- Thus, permutation table used in the encryption process, the same table is inverted and used in the decryption process.
- following example shows inventing a given straight p-box permutation table :-

Ques

i) original table	<table border="1"> <tr><td>6</td><td>3</td><td>4</td><td>5</td><td>2</td><td>1</td></tr> <tr><td>6</td><td>3</td><td>4</td><td>5</td><td>2</td><td>1</td></tr> </table>	6	3	4	5	2	1	6	3	4	5	2	1	ii) Add indices
6	3	4	5	2	1									
6	3	4	5	2	1									
iii) swap content & indices	<table border="1"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr><td>6</td><td>3</td><td>4</td><td>5</td><td>2</td><td>1</td></tr> </table>	1	2	3	4	5	6	6	3	4	5	2	1	iv) Post the table
1	2	3	4	5	6									
6	3	4	5	2	1									

pg:- 157 of 252 figs.7

Ques - A straight P-box is invertible, but compression and expansion p-box are not. Why? Justify or explain with the example.

* Substitution Box or S-Box:-

Substitution Box or S-Box can have different number of input and output.

- S-box can be keyed or keyless but modern block cipher normally uses keyless where the mapping is pre-determined.

- S-box is an ' $m \times n$ ' substitution unit where m and n are not same. $m \times n \Rightarrow \neq$

standard S-boxes are represent using matrices for the given mathematical equations.

- S-boxes are classified as linear S-box and non-linear S-box.

- linear versus non-linear S-boxes :- In an S-box with ' m ' inputs and ' m ' outputs, we call the inputs x_0, x_1, \dots, x_m and the outputs y_1, \dots, y_m . the relationship between the inputs and the outputs can be represented as a set of equations. $y_1 = f_1(x_1, x_2, \dots, x_m)$

$$y_2 = f_2(x_1, x_2, \dots, x_m)$$

$$y_m = f_m(x_1, x_2, \dots, x_m)$$

- In a linear S-box, the above relations can be expressed as:-

$$y_1 = a_{1,1}x_1 \oplus a_{1,2}x_2 \oplus \dots \oplus a_{1,n}x_n$$

$$y_2 = a_{2,1}x_1 \oplus a_{2,2}x_2 \oplus \dots \oplus a_{2,n}x_n$$

$$y_m = a_{m,1}x_1 \oplus a_{m,2}x_2 \oplus \dots \oplus a_{m,n}x_n$$

- In a non-linear S-box we cannot have the above relations for every output. The terms in non-linear S-box will be represented as -

$$x_1 \cdot x_2, x_3 \cdot x_5 \text{ etc}$$

Ques - for the given equations $y_1 = x_1 \oplus x_2 \oplus x_3$, $y_2 = x_1$. find whether the S-box is linear or non-linear. Represent the relationship using matrices.

Given:- $y_1 = x_1 \oplus x_2 \oplus x_3$, $y_2 = x_1$

From:- the above given equations show that it is a linear equation. S-box.

Given:- $y_1 = a_{1,1}x_1 \oplus a_{1,2}x_2 \oplus a_{1,3}x_3$

$$y_2 = a_{2,1}x_1 \oplus a_{2,2}x_2 \oplus a_{2,3}x_3$$

x_1	x_2	x_3	y_1	y_2
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	1
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Ques- In an s-box with three inputs and two outputs, we have the equations as, $y_1 = x_1 \cdot x_2$ $y_2 = x_1 + x_2 \cdot x_3$ identify the type of the s-box.

Given:- $y_1 = x_1 \cdot x_2$ $y_2 = x_1 + x_2 \cdot x_3$

Soln:- the above equation is a non-linear s-box as the it is non-linear because there is no relationship between the i/p and o/p hence, the matrix can't be drawn.

Ques- S-box may or maynot be invertible justify your answer.

* for an invertible s-box the number of input bits should be equal with the number of output bits following shows an example.

* I/O relation of 2×2 s-box is shown in the following table :-

left most	0	1	→ right most
top	01	11	
bottom	10	00	

* show the inverse s-box table:

- As the no. of input bits = output bits hence the inverse can be taken out.

Soln:- for the above table the left most bit of the given input defines the row and the remaining rightmost bits define the column.

The above table can be represented as:-

I/P \Rightarrow	00	01	10	11
-------------------	----	----	----	----

I/P \Rightarrow	00	01	11	10	00
-------------------	----	----	----	----	----

Add	1	3	2	0
	0	1	2	3

Swap	0	1	2	3
	1	3	2	0

Sort	0	1	2	3
	3	0	2	1

O/P: - 3 0 2 1

11 00 10 01

I/P: - 0 0 0 0 1 1 0 1 1 1

0 1 1 1 1 0 1 0 0 1

We have to find invertible S-box.

0	11	00	\Rightarrow	Invertible S-box
1	10	01		

Ques: find the invertible 3×3 S-box for the given values of add indices, sum and index.

00	01	10	11	00	01	10	11
0	011	101	111	100	010	110	001
1	000	010	001	110	100	000	010

$$\rightarrow I/P: \Rightarrow 0 0 0 | 0 0 0 | 0 0 0 | 0 1 0 | 0 1 1 | 0 1 0 0 | 1 0 1 | 1 1 0 | 1 1 1$$

$$O/P: \Rightarrow 1 0 1 | 1 1 0 | 1 0 1 | 0 1 1 | 0 0 1 | 1 0 0 | 0 0 0 | 0 1 0 | 0 0 1 | 1 1 0$$

Add indices and sum of 3rd row = 5 & 2nd row = 4 & 1st row = 2 & 4

3	5	7	4	0	2	1	6
0	1	2	3	4	5	6	7

0	1	2	3	4	5	6	7
3	5	7	4	0	2	1	6

4	6	5	0	3	1	7
0	1	2	3	4	5	6

100 110 101 000 011 001 111 010

8 2 4 0 1 5 7 6

0 5 3 6 4 2 1 7

O/P 100 110 101 000 011 001 111 010

I/P 000 001 010 011 100 101 110 111

	00	01	10	11
0	100	110	101	000
1	011	001	111	010

\Rightarrow Invertible S-box

000-	00	01	10	11	000-	
0	110	001	010	011		
1	100	111	101	000		

000-	0	1	
0	00	10	
1	11	01	

Ques - write the short note third component (Ex-or operation)

2) other component :- { x-or operation, complement, Inverse, circular shift (L & R), swap, ^{Page No.} SPLIT & COMBINE }

Ques - 15] (a) Show the result of 3-bit circular left shift on word $(10011011)_2$

(b) Show the result of 3-bit circular shift on the word resulting from part a.

(c) compare the result of part b with the original word in part a.

→ (a) Soln:- find :- result of 3-bit circular leftshift
given :- $\begin{pmatrix} b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\ 1 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \end{pmatrix}_2$

$$\begin{array}{cccccccc} b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\ | & 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 \end{array}$$

(b) Soln:- find :- result of 3 bit circular rightshift
given:- 11011001

$$\begin{array}{cccccccc} b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\ | & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \end{array}$$

(c) Soln:- compare the result of part b & part a.

$$\begin{array}{cccccccc} b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\ | & 1 & 0 & 1 & 1 & 0 & 0 & 1 \\ a \Rightarrow & 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ b \Rightarrow & 1 & 0 & 0 & 1 & 1 & 0 & 1 \end{array}$$

- Ques 16] a) Swap the word $(10011011)_2$
 b) Swap the word resulting from part a
 c) Compare the result of part a and part b to
 show that swapping is a self-invertible
 operation.

(a) Soln:— $(10011011)_2$ is converted to

Third column (MSB) = 11011011
 Second column (middle) = 00000000
 First column (LSB) = 11111111

Third column (MSB) = 11011011
 Second column (middle) = 00000000
 First column (LSB) = 11111111

Putting & doing in binary addition = 10011011

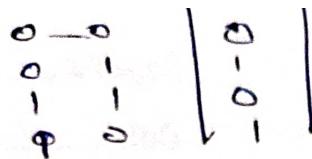
add 10011011 add 10011011 add 10011011

10011011 10011011 10011011 10011011

10011011 10011011 10011011 10011011

Page No. _____

Date 1/1



All-17) find the result of the following operations:-

(a) $(01001101) \oplus (01001101) \Rightarrow 00000000$

(b) $(01001101) \oplus (10110010) \Rightarrow 11111111$

(c) $(01001101) \oplus (00000000) \Rightarrow 01001101$

(d) $(01001101) \oplus (11110111) \Rightarrow 10110010$

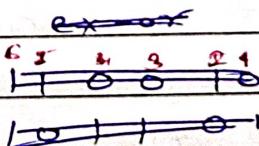
(Qn) A 6×2 S-box is ~~exor~~ the odd number bits to get the left bit of the output. similarly perform ex-or operation on the even number bits to get the right bit of the output. perform the mentioned on the following input string.

→ 110010 → 101101

Given:- 6×2 S-box

- find:-
- odd number bits to get the left bit of o/p.
 - even number bits to get the right bit of o/p.

- odd number bits

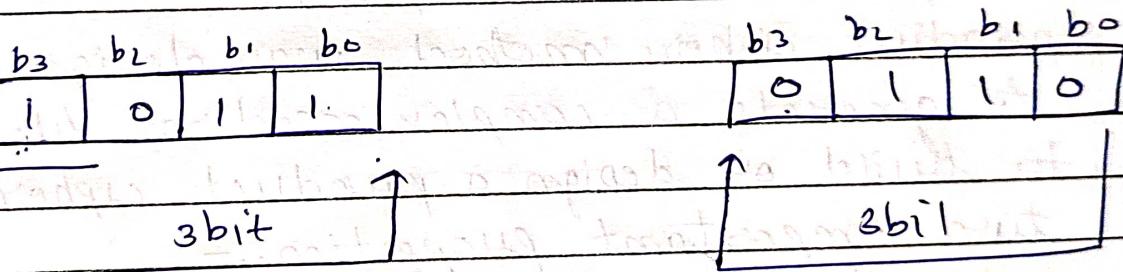


	6	5	4	3	2	1	
1	1	1	0	0	-1	0	
0							

Ques- The left most bit of a 4×3 s-box is one if the other three bits is zero then the other three bits are rotated to right one bit similarly if the left most bits is one then the three other bits are rotated to the left one bit, perform the above and generate the output for the given inputs.

1) 1011

2) 0110



0	1	1	1	0	1	1	0	0
---	---	---	---	---	---	---	---	---

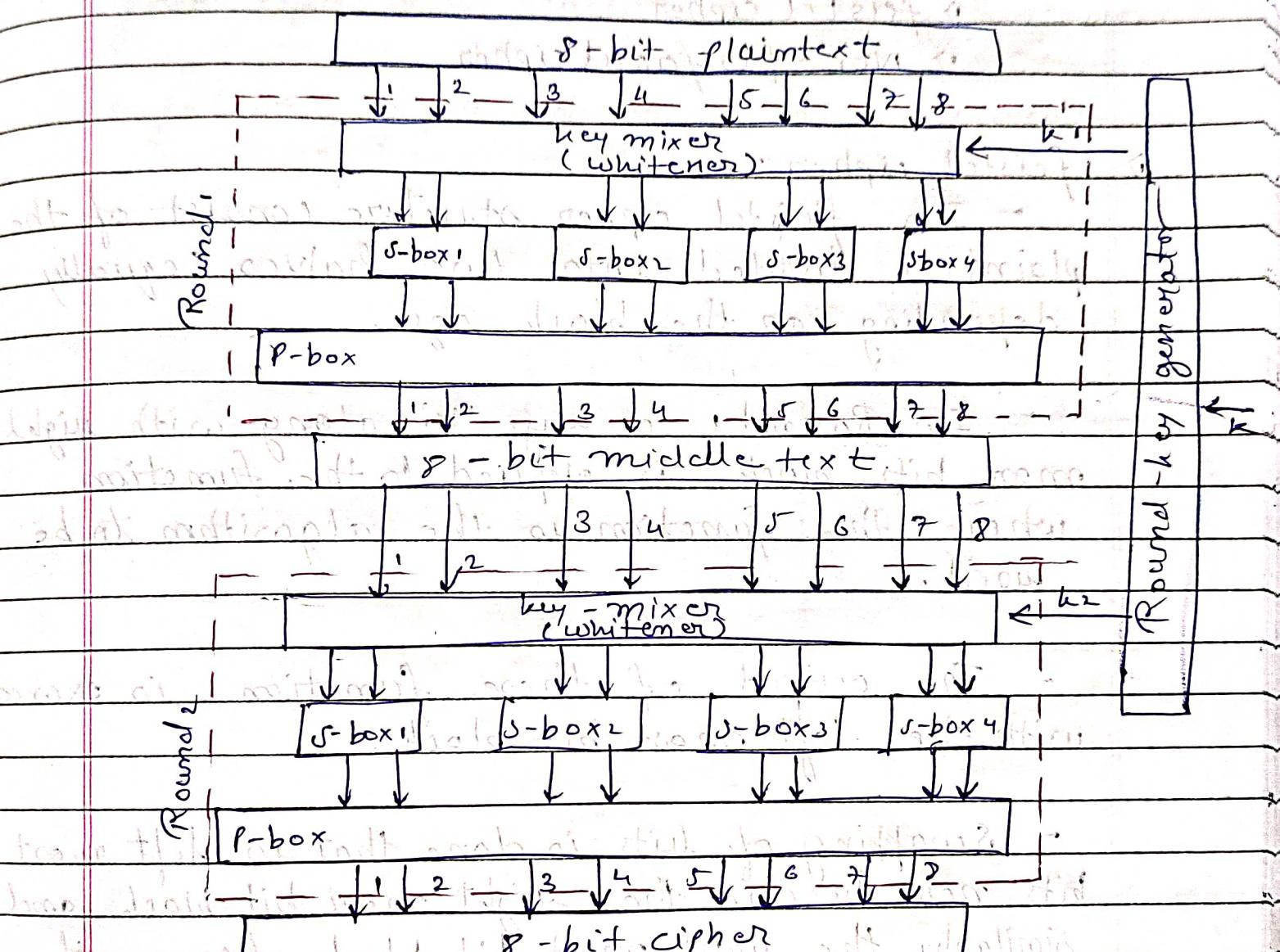
Q1 - Write short note on product cipher.

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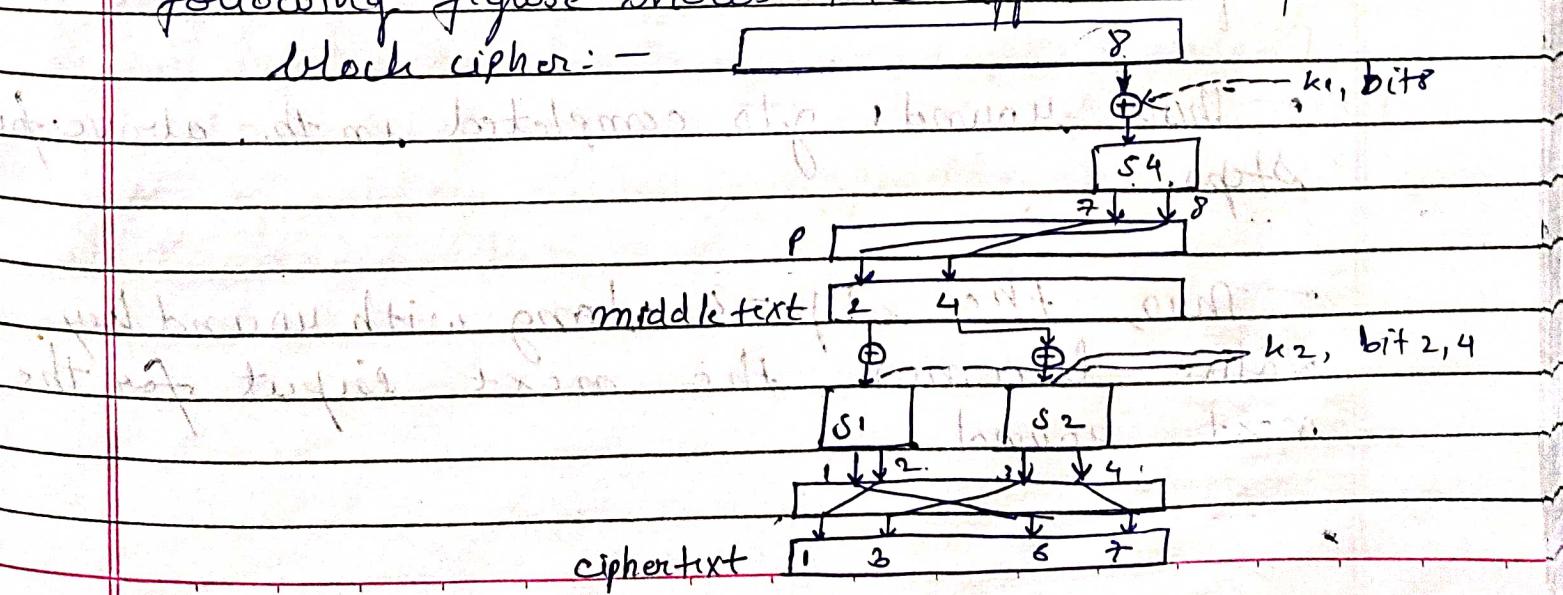
Date / /

- * Product cipher :- → modern block cipher → was introduced by Shannon
- Substitution
- Transposition
- other components
- * properties:-
 - Diffusion — hides the relationship between CT and PT
 - Confusion — confuse the relationship between key and CT
- Product cipher is the combination of substitution, transposition, other components.
- Product cipher method was designed by Shannon to generate a complex modern block cipher.
- To build or design a product cipher, Shannon uses two important properties:-
 - Diffusion:- that hides the relationship between the CT and PT
 - Confusion:- these properties confuse the attacker to find the key and CT.
- Product cipher consists of 3 steps blocks.
- Following figure shows
- Confusion and diffusion properties are applied number of time or iterated number of times that each iteration known as rounds.

following figure shows the product cipher of 2 rounds



following figure shows the diffusion & confusion in a block cipher:-



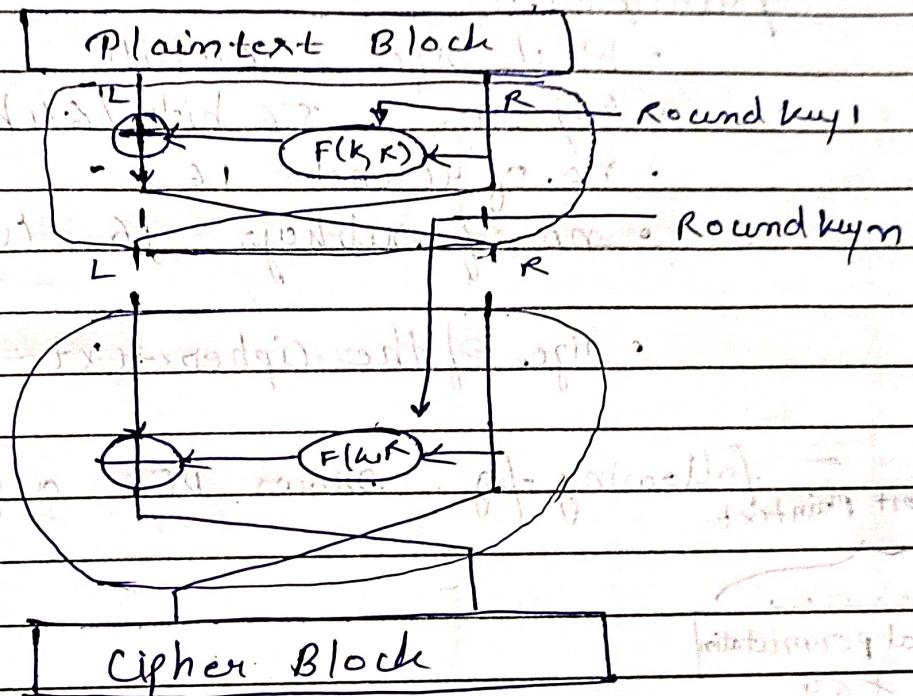
- * classes of p classes of p-product cipher :-
- p-product cipher are divided into two classes
 - feistel cipher
 - Non - feistel cipher

⇒ feistel cipher :-

- In feistel cipher structure consist of the plaintext divided into two halves equally depending on the block size.
- In Round 1, a key k_1 along with eight most bits block is applied to the function where the function is the algorithm to be used.
- The output of these function is exored with the left most bit block.
- Swapping of bits is done that is left most bits now become the eight most bit block and similarly the eight most bit block becomes the left most bit block.
- Thus, Round 1 gets completed in the above four steps.
- Thus, the step - 4 along with round key value becomes the next input for the next round.

* Thus, after the number of rounds completed depending on the type of algorithm we get the final cipher text block.

- following figure shows the above process:-



* Block cipher design principles are based on the following:

- 1) Block Size :- length of PT = CT [as per the algo]
- 2) Key Size :- master keysize = [as per the algo]
- 3) total number of rounds :- conversion from PT \rightarrow CT
- 4) No. of subkeys count :- as per the algo
- 5) Round function definition :

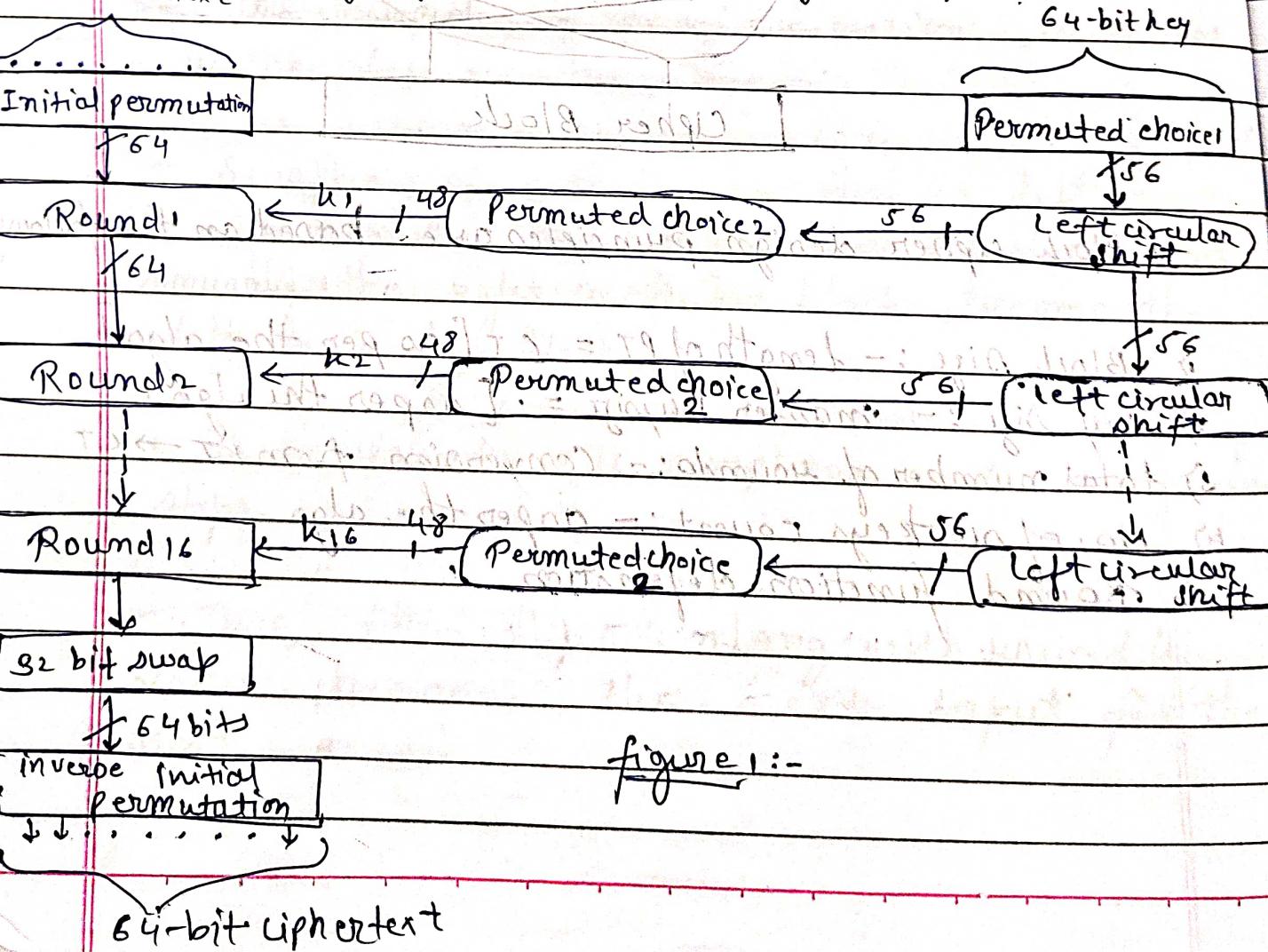
* DES Algorithm :- (Data encryption Standard algo)

→ DES algorithm is based on the concept of feistel structures.

→ Thus, DES algorithm is based on the following principles:-

- block size = 64 bits
- key size = 56 bits / 64 bits
- no. of round = 16
- no. of subkeys = 16 (where each subkey size = 48 bits)
- size of the cipher text = 64 bits.

→ following fig. shows DES algorithm process:-



following fig. shows DES single round function process

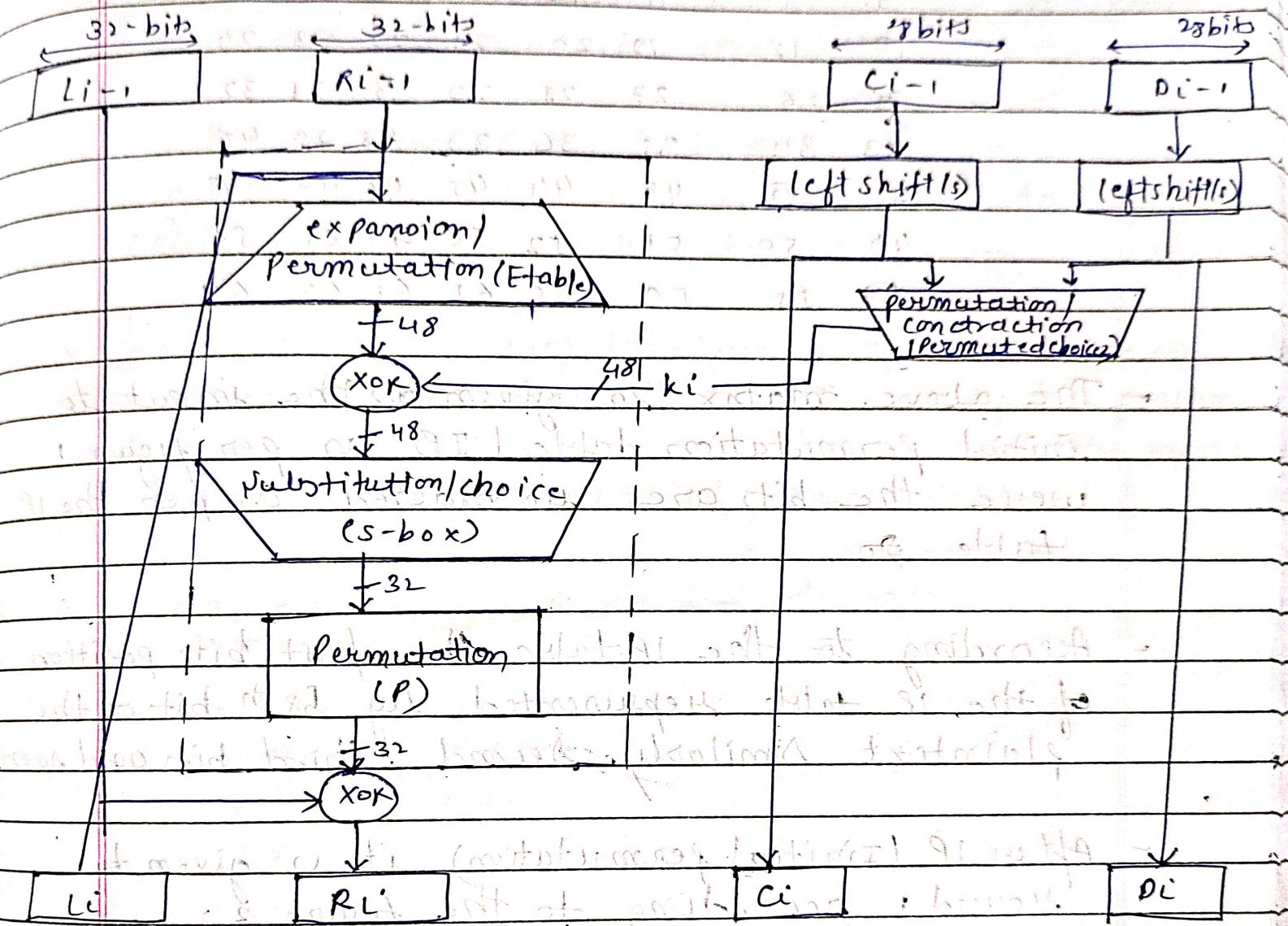


figure 2:-

* DES encryption process: - mainly 5 steps -
 1) Initial state of plain text
 2) Substitution of plain text
 3) Permutation of plain text
 4) XOR of plain text with key
 5) Substitution of cipher text

[Type 1] consider the 64 bit plaintext as an input because in DES algorithm the block size = 64 bit.
 the 64 bit plaintext is represented as 8×8 matrix as shown below:

- 64-bit PT as 8×8 matrix form

*	1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16	
17	18	19	20	21	22	23	24	
25	26	27	28	29	30	31	32	
33	34	35	36	37	38	39	40	
41	42	43	44	45	46	47	48	
49	50	51	52	53	54	55	56	
57	58	59	60	61	62	63	64	

- The above matrix is given as the input to initial permutation table (IP) as per figure 1 where the bits are re-ordered as per the IP table. \rightarrow $(\times 64 \rightarrow 56)$
- According to the IP-table the first bit position of the IP table represented by 58th bit of the plaintext. Similarly Second ; third bits and so on.
- After IP (Initial permutation) it is given to round 1 according to the figure 2.
- Thus, the plaintext is now divided into two equal halves each of 32 bit block size.
- Now, the right half 32 bit is given to the expansion permutation table where the bits are expanded from $32 \rightarrow 48$ bits.

- thus, the output of the expansion permutation table (EPTable) is need to be exord with the output of permuted choice 2 table for these we have to generate the subkey.
- As the key size = 64bit but the cipher key size for DES algorithm is 56 bit key thus, we need to apply permuted choice 1 table to reduce from 64 bit to 56 bit.
- here, parity bit drop technique is applied where we need to discard 8 bits that is the parity bits positions from the given 64 bit key and then permute the rest of the bit using permuted choice 1 table.
- thus, the bit positions — discards.
- 8^{th} bit = parity bits
- 16^{th} bit = —
- 24^{th} bit = —
- 32^{th} bit = —
- 40^{th} bit = —
- 48^{th} bit = —
- 56^{th} bit = —
- * 57^{th} bit of the key is the first position as a output.
- according to the figure two 56bit are divided into two equal halves each of 28bit.
- Thus, each 28bit is given as input to Ls (left circular shift). thus, number of bit to be shifted depends on the round number. refer the table where for

However, the number of bits to be shifted is equal to 11. Refer the table for more details.

- The output of LCS is given to permuted choice table where reordering of bits are performed and the bits are reduced from 56 to 48 bits.
 - The discarded bits are (9, 18, 22, 25, 35, 38, 43, 54); these is also called as contraction & reduction method.
- The output of permuted choice 2 table is with ex-orred with expansion permutation table (properties is closure)
- The 48 bit output of ex-orred result to be applied to s-boxes. Here, the bits are reduced from 48 to 32 bit

$$\text{row} \leftarrow 00 - 0 \quad 10 = 2^{\text{nd}} \text{ row}$$

$$01 - 1 \quad 0011 = 3^{\text{rd}} \text{ column}$$

$$10 - 2 \quad \therefore 1000 \quad \text{1st row}$$

$$11 - 3 \quad \text{1111}$$

$$\text{column} \rightarrow 00000000 \quad 8 \times 9 = 32$$

$$0001 = 1 \quad S_1 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$1111 = 15 \quad 8 \times 6 = 48 \text{ bits}$$

$$S_1 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$S_8 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$S_8 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$S_8 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$S_8 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

$$S_8 \rightarrow [1 \quad 0 \quad 0 \quad 11 \quad 0]$$

- So the 6th bit input 100110 is reduced to 1000 that is equal to 4 bit thus the process is repeated for total 8 s-box tables to get 32-bit output.
- Now, the output of s-box that is 32 bit is given to the permutation function P where the bits are again rearranged according to the following table.
- The output of p-function of 32 bit is Ex-or with left (32 bit) most bit and stored in right most bit.
- Similarly the right half will be stored with left half and these will be act as a input for the next round along with the key values.
- The process is repeated for 16 number of rounds. After the 16th round 32 swap is their and is applied to inverse initial permutation table denoted as $I(p^{-1})$ (refer the table from the slide)
- Thus finally, the 64bit or output of IP inverse is generated as cipher text.

Q1 - Write the explanation for single round permutation
 Q2 - What are the bit digest in permuted choice two
 Q3 - 6bit to 4bit (using s-box)

Ques - The input to s-box1 is 100011 what is output

1 0 0 0 1 1 11
row = 11 = 3 column = 00011
unit colm

- it is called as s-box rule.

- write the s-box rule. find row and column of the input

pg 167 Table 6.10 - S-box8

Ques - if the given input is 100000 what is the output

row = 10 = 2 column = 00000

Ques - i) Answer the following que about s-box in DES:-

a) Show the result of passing 11011 through s-box3

→ row = 11 = 3 column = 10111 = 11, (row) + 1 = 10
③

b) Show the result of passing 001100 through s-box4

→ row = 00 = 0 column = 01100

c) show the result of passing 000000 through s-box2

→ row = 00 = 0 column = 000000

d) show the result of passing 11111 through s-box2

→ ⑥ row = 11 = 3 column = 11111

* Blow fish algorithm:-

- blow fish is a symmetric key algorithm (same key is used to perform encry & decry) therefore
- the size of the plain text is 64 bit
- it uses the concept of feistel structure
- it has variable key size as compare to DES(56bit)
(32bit to 448bit)
- blow fish was developed by Bruce Schneier in 1993
- total number of rounds = 16 to convert P.T to C.T
- it is alternative to DES algorithm method.
- blow fish algorithm is divided into four parts :-
 1. Generation of sub keys.
 2. Data encryption/decryption process.

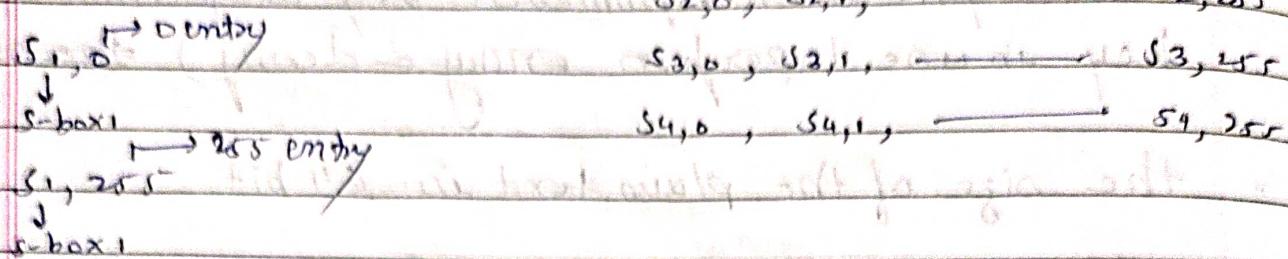
* Generation of sub keys:-

- As the key size is variable that is of the size
 $448 \Rightarrow 14$ 32 bit to 448 bit which is divided into 14 sub
 keys i.e k_1, k_2, \dots, k_{14} each of 32 bit
 size

- blow fish introduces the concept of p-array and s-boxes.

- thus, there are total 18 p-arrays numbered from P_1 to P_{18} or P_0 to P_{17} followed by 4 s-boxes of size 8×32

- each s-box has total 256 entries (0 to 255) which is defined as $s_{1,0}, s_{1,1}, \dots, s_{1,255}$



- each s-box has 8-bit input and 32-bit output

thus in 8-bit input $i^{th}, 7^{th}, 6^{th} \Rightarrow$ represents the rows, where as the remaining bit $(2, 3, 4, 5, \epsilon)$ \Rightarrow represents the columns.

thus, the interaction of row and column determines the value of s-box.

* initialize the p-array value first followed by initializing four s-boxes with a fixed string where the values are the bits (representing) the fractional part of the pi (π) value in hexadecimal form.

Generating following shows some initial values of subkeys:-

$$P[1] = 243f6a88$$

$$P[2] = 85a308d3$$

$$P[18] = 21e638c4$$

$$S[4, 255] = 8ac87236$$

Perform bit wise ex-or operation between the P-array and key values assuming the key value as 448 bits.

$$k = \frac{448}{32} = 14$$

$k_1 - k_{14}$

$P_1 - P_{18}$

$$P_1 = P_1 \text{ } x\text{-or } k_1 \quad (1)$$

$$P_2 = P_2 \text{ } x\text{-or } k_2 \quad (2)$$

$$P_3 = P_3 \text{ } x\text{-or } k_3 \quad (3)$$

$$P_4 = P_4 \text{ } x\text{-or } k_4 \quad (4)$$

$$P_5 = P_5 \text{ } x\text{-or } k_5 \quad (5)$$

$$P_6 = P_6 \text{ } x\text{-or } k_6 \quad (6)$$

$$P_7 = P_7 \text{ } x\text{-or } k_7 \quad (7)$$

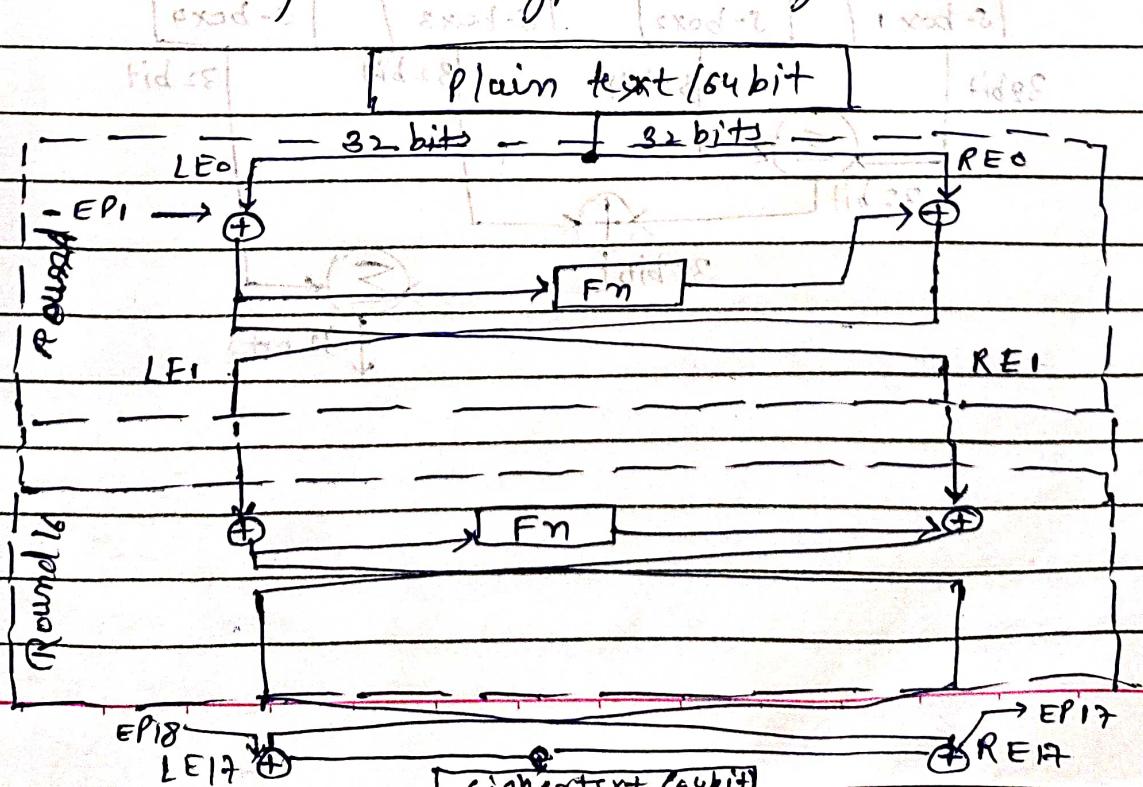
$$P_8 = P_8 \text{ } x\text{-or } k_8 \quad (8)$$

Reuse of sub

$k_1 \leftrightarrow k_4$

* Blowfish encryption process

In these process a 64-bit plaintext is divided into two equal half and with the use of P-box and S-boxes in the function F following shows the blowfish encryption diagram.



- divide the given r_r of 64 bit into two equal half L & R of 32 bit each.

Algorithm: then the :-

$$L_i = L \oplus P_i \quad R_i = R$$

Function (L_d)

$$R_i = \text{fun}(L_i) \oplus P_i$$

swap (L_i, R_i)

unswap (L_i, R_i)

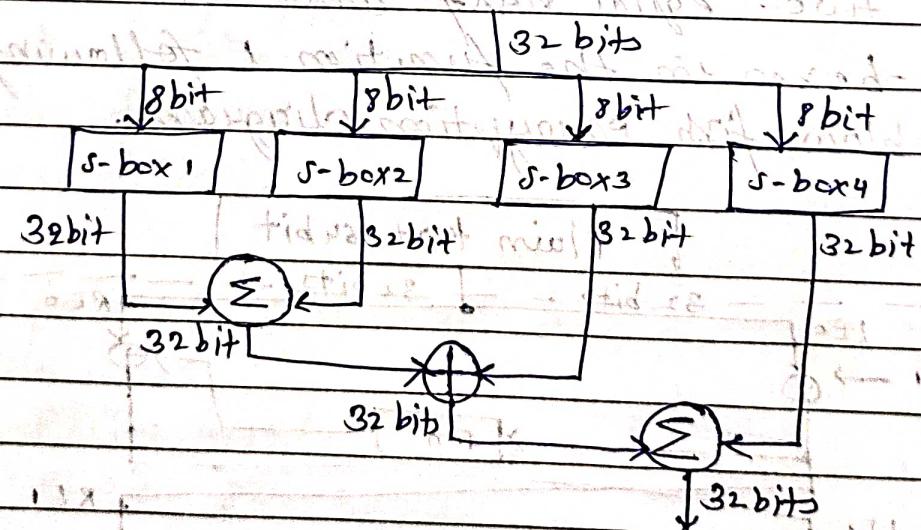
then,

$$L = L \oplus P_{18}$$

$$R = R \oplus P_{17}$$

we get ciphertext.

- the function F in the above figure is as follows:



The function f in fig A is as follows as shown in fig (B).

- ① Divide the 32 bit left block into four 8 bit subblocks i.e 8 bit s blocks named as $f[a, b, c, d]$

- ② Compute

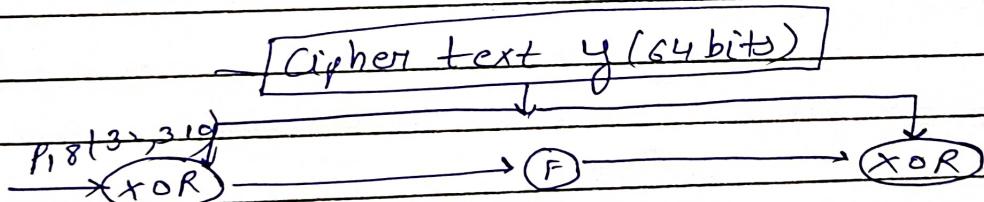
$$f[a, b, c, d] = ((s_1, a + s_2, b) \text{ XOR } s_3, c) + s_4, d.$$

$$\text{let } a = 10, b = 95, c = 37, d = 191$$

$$\text{Then } f[a, b, c, d] = ((s_1, 10 + s_2, 95) \text{ XOR } s_3, 32 + s_4, 191)$$

following fig shows the blowfish decryption process.

Actual
Phase
is pose
Chp-3
and
edition



Page No. _____

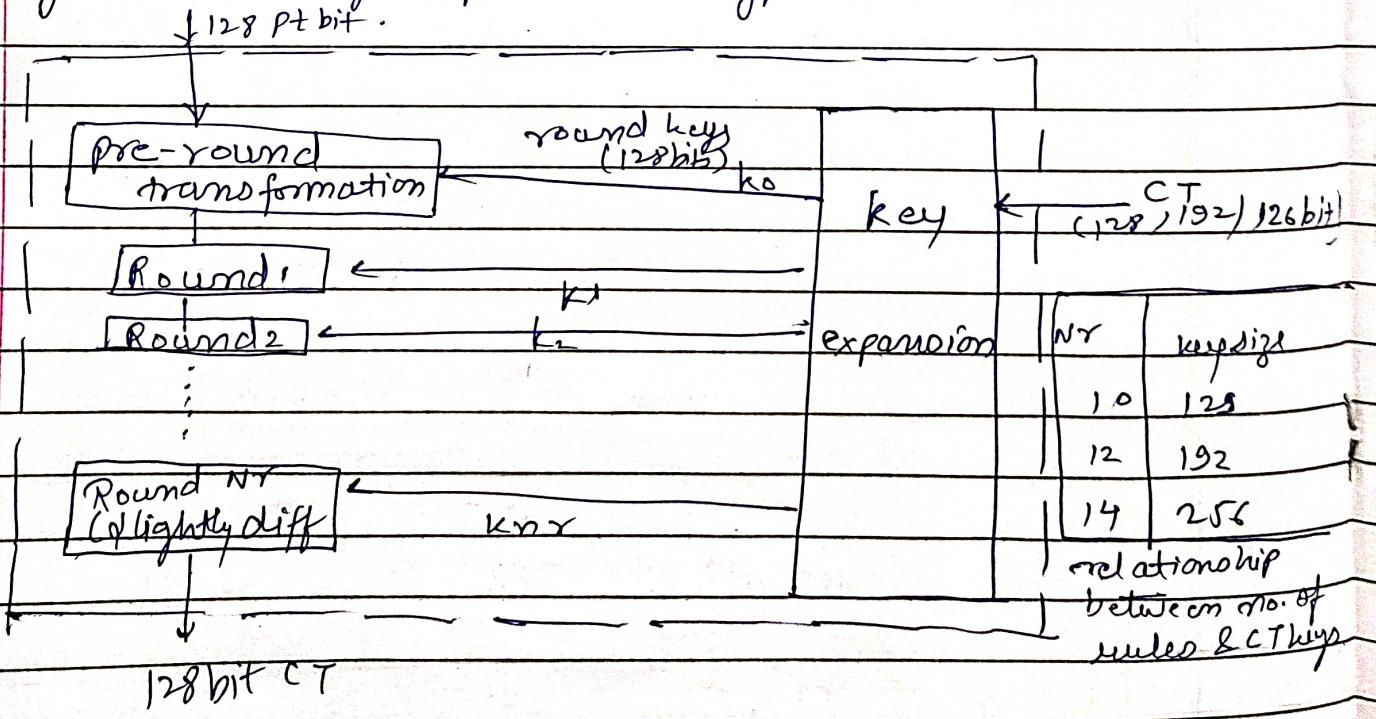
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Q Justify how to generate the sub-key values using blowfish encryption algo.

* AES Algorithm (Advance encryption cipher)

- symmetric key block cipher method.
- developed as various institute of standards & technology (NIST) in dec 2021

* General design of AES encryption cipher:-



* The no. of round keys generated by the key expansion algorithm is always one more than the no. of round keys.

In other words, we have no. of round keys = $n+1$
we refer keys, $k_0, k_1, k_2, \dots, k_n$

• Data units used in AES:-

There are 5 data units - bit, byte, word, block, state

① Byte

$$\boxed{\text{Byte}} \rightarrow [b_0 \ b_1 \ b_2 \ b_3 \ b_4 \ b_5 \ b_6 \ b_7] \rightarrow \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \\ b_6 \\ b_7 \\ b \end{bmatrix}$$

② word

$$\boxed{\text{word}} \xrightarrow[w]{} [B_0 \ B_1 \ B_2 \ B_3] \rightarrow \begin{bmatrix} B_0 \\ B_1 \\ B_2 \\ B_3 \\ w \end{bmatrix}$$

③ block

$$\boxed{b_0 \ b_1 \ b_2 \ b_3 \ b_4 \ b_5}$$

④ State

$$S \rightarrow : \begin{array}{|c|c|c|c|c|} \hline & s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ \hline s_1,0 & s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ \hline s_2,0 & s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ \hline s_3,0 & s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \\ \hline \end{array}$$

∴ each value of given matrix is 1 byte.

$$16 \times 8 = 128 \text{ bytes}$$

each column represent word.

Ques-1) for the given PT = "AES" uses a matrix convert into a state matrix.

→ As the given PT = 4 character

i.e. $14 \times 8 = 112$ bit but we need to make it 128.

Now,

To insert 2 bogus character i.e. 2

Then it would be written as,

PT = "AES uses a matrix" → (Hexadecimal)

Convert character into the int values

A	E	S	U	S	E	S	A	M	A	T	R	I	X	Z	Z
00	04	18	20	18	04	18	00	12	00	19	17	08	23	25	25

↓ int into hexadecimal

Block :-	00	04	12	14	12	04	12	00	0C	00	13	11	08	17	13	13
----------	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----

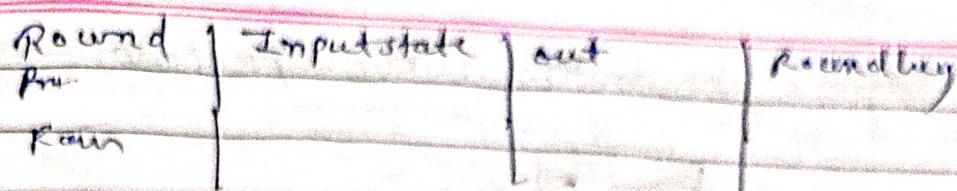
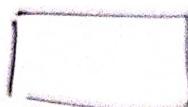
$$\text{state} = \begin{pmatrix} B_0 & B_4 & B_8 & B_{12} \\ B_1 & B_5 & B_9 & B_{13} \\ B_2 & B_6 & B_{10} & B_{14} \\ B_3 & B_7 & B_{11} & B_{15} \end{pmatrix} = \begin{pmatrix} 00 & 12 & 0C & 08 \\ 04 & D4 & 00 & 17 \\ 12 & 12 & 13 & 19 \\ 14 & 00 & 11 & 19 \end{pmatrix}$$

Ques-2) PT = "THIS IS AN EXERCISE" convert into state

→ convert given character into values:

T	H	I	S	I	S	A	N	E	X	E	R	C	I	S	E
19	07	18	18	18	0	13	04	23	04	17	02	08	18	04	1

Block :-	13	07	08	12	08	12	00	04	17	04	11	02	08	12	04	1
----------	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	---



* AES round structure :-

Round = state matrix

- 4×4 matrix
- bytes
- columns
- top to bottom.

* 4 types of transformation

- substitution → subtypes
- permutation → shift row
- mix input → mix columns
- Add round key ~~+ key values~~ → Add Round key
In these we will perform XOR operation.

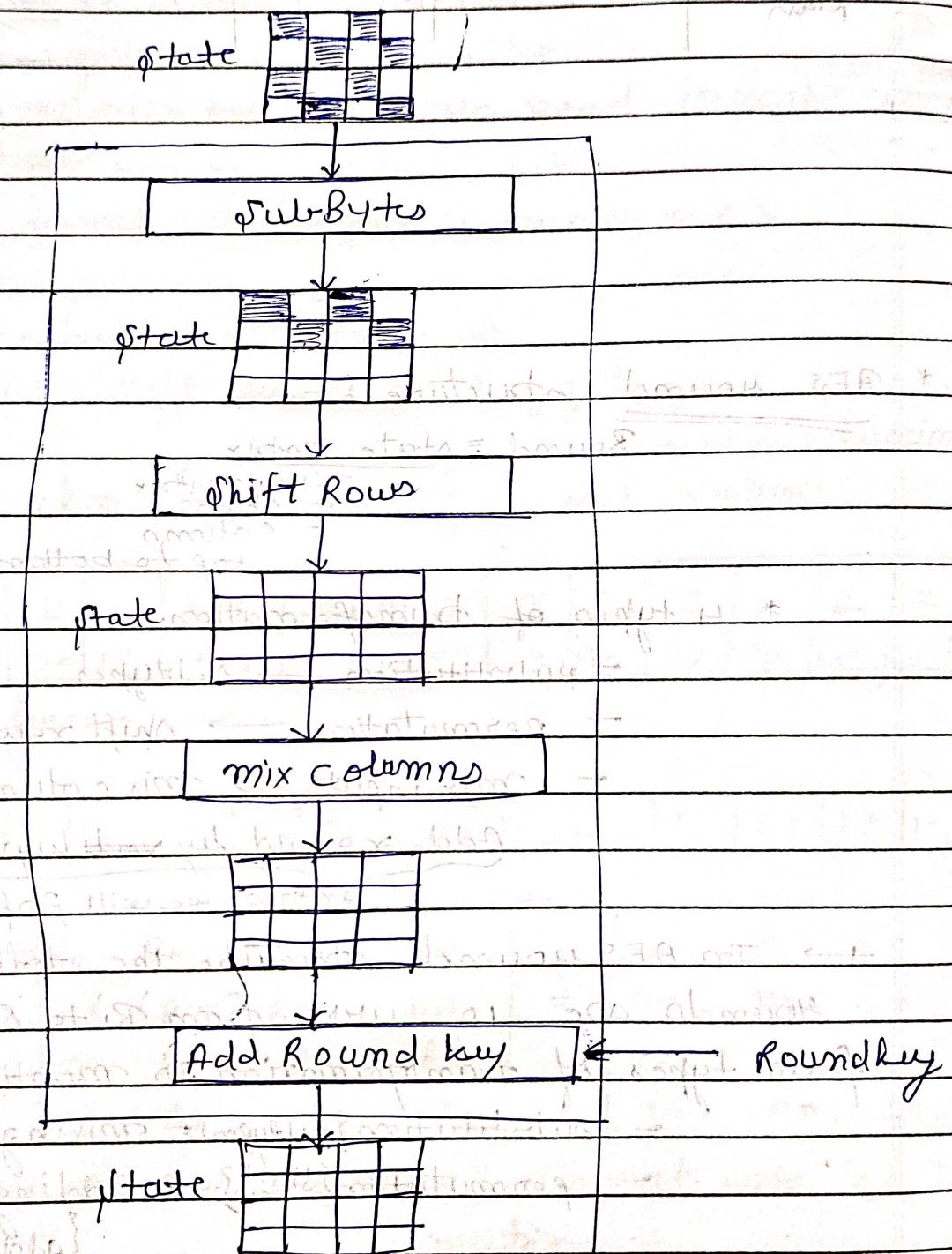
→ In AES round structure the total number of rounds are 10 were from 'R₀' to 'R₉', AES uses four types of transformation as mentioned below:-

- substitution {subtypes} + mixing {mix column meth}
- permutation {shift} - adding round key values.
{add round key}

- the input to each round is a state matrix and the output is given to each and every transformation as shown in figure below:-

- the last round i.e R₁₀ performs the following transformation:- Substitution {subtypes}.
- permutation {shift row?}
- adding round key values {add round key}

→ following figure shows the above process:-



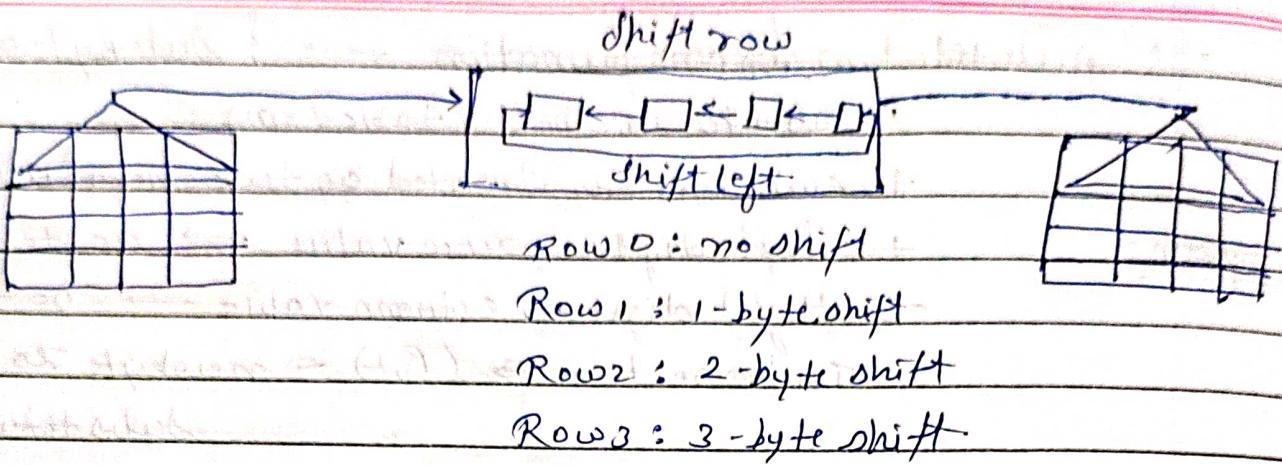
- Substitution Transformation → { Sub-Byte method }
- + subBytes method (+table form)
 - + each byte is treated as two hexadecimal digits
 - + left digit = row value → 00 to FF(15)
 - + right digit = column value → 00 to FF(15)
 - + Intersection $\Rightarrow (R, C) = \text{new byte to be substituted}$
 - + Size of AES S-Box - 16×16

o convert the given state matrix using subBytes transformation

state	00 77 12 0C 08
	04 04 04 00 23
	12 00 12 03 13 19
	14 02 00 2A 11 019

63 E C9 77 FE 18 07
F2 77 00 63 E2 26 C7
C9 E2 05 73 30 D4 17
FA E2 E2 82 77 D4 17

- Permutation transformation method → { shift row method }
- + In these method permutation is done at the byte level.
 - + shifting is done to the left
 - + number of shifts depend on the word number value of the state matrix.
 - + following figure shows the shift row method:-



Q- Perform shift rows transformation for the given state matrix.

	63	C9	FE	30	State
	F2	03	F2	63	
	C9	C9	51	70	
	CF	A	63	82	

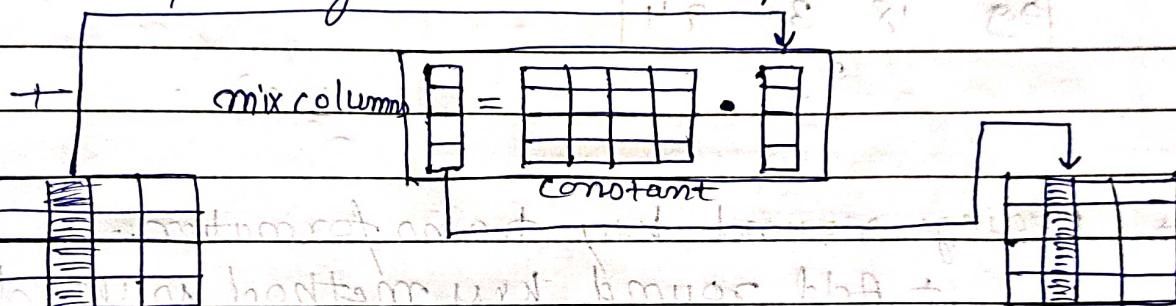
→	63	C9	FE	30	
	F2	63	26	F2	
	7D	D4	FE	C9	
	D4	FA	63	82	

* write rules in paper if marks would be deducted

Rounds	Input State	Output State	Round Key
--------	-------------	--------------	-----------

* Mixing Column transformation method:-

- + mix column method is operated at the column level
- + matrix multiplication is done with a constant square matrix as shown below.
- + thus, this method combines or multiplies each byte with a different constant value and generates the output state matrix.
- + following shows the above process:-



$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \xleftarrow{\text{Inverse}} \begin{bmatrix} 0E & 0B & 0D & 09 \\ 09 & 0E & 0B & 0D \\ 0D & 09 & 0E & 0B \\ 0B & 0D & 09 & 0E \end{bmatrix}$$

Q- perform mix column transformation for the given state matrix:

$$\begin{bmatrix} 63 & C9 & FE & 30 \\ F2 & 63 & 26 & F2 \\ 7D & 19 & C9 & C9 \\ D4 & FA & 63 & 82 \end{bmatrix}$$

E	62 C9 FE 30	x	02 08 01 01
F2	63 26 F2	x	01 02 03 01
70	D4 C9 AC	x	01 01 02 03
D4	FA 63 82	x	03 01 01 02

addition of round key with state matrix

60	02 27 26	with a difference of 1
CF	92 91 0D	difference of 13
0C	0C F4 D6	with a difference of 10
99	18 30 74	with a difference of 16

Ex-Or operation

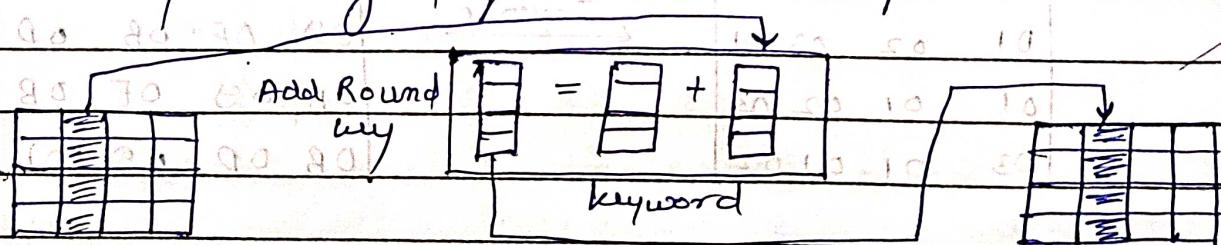
* Adding round key transformation:-

+ Add round key method is used.

+ Ex-or operation is performed between

input state matrix column with the given keyword values.

The following figure shows the process:



Ques - perform add round key transformation for given matrices.

47 40 A3 4C	53 57	AC 19 28 57
87 D4 70 9F	⊕ 05	77 FA D1 5C
94 E4 3A 82	A1	66 DC 09 00
ED A5 A6 BC		F3 21 41 6A

DB	59	8B	1B
40	2E	A1	C3
F2	38	13	D2
1E	84	D7	D6

$$\begin{array}{l} \rightarrow A5 \oplus 21 \\ 10100101 \oplus 00100001 \\ 10000100 = 84 \\ \rightarrow 3A \oplus 29 \\ 00111010 \oplus 00101001 \\ 00010011 \end{array}$$

13

 $\rightarrow 47 \oplus AC$

$$\begin{array}{l} 4 \times 16^1 + 7 \times 16^0 \oplus 10 \times 16^1 + 12 \times 16^0 \\ 64 + 7 \oplus 160 + 12 \end{array}$$

$$071 \oplus 172$$

$$\begin{array}{r} 128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \\ \cancel{0} \quad \cancel{1} \quad \cancel{1} \quad \cancel{0} \quad \cancel{0} \quad \cancel{1} \quad \cancel{0} \quad \cancel{0} \\ \cancel{0} \quad \cancel{1} \quad \cancel{1} \quad \cancel{0} \quad \cancel{1} \quad \cancel{0} \quad \cancel{1} \quad \cancel{0} \\ \hline \cancel{1} \quad \cancel{1} \quad \cancel{0} \quad \cancel{0} \quad \cancel{1} \quad \cancel{0} \quad \cancel{0} \quad \cancel{0} \end{array}$$

 $\rightarrow 47 \oplus AC$

$$01000111 \oplus 10101100$$

$$\underline{11101011} = 219 = DB$$

FB

 $\rightarrow E4 \oplus DC$

$$11100100 \oplus 11011100$$

$$00111000 = 38$$

$$\begin{array}{r} 01000111 \\ 10101100 \\ \hline 11101011 \end{array}$$

 $\rightarrow 40 \oplus 19$

$$01000000 \oplus 00011001$$

59

 $\rightarrow D4 \oplus FA$

$$11010100 \oplus 11111000$$

$$00101110$$

2E

 $\rightarrow A3 \oplus 28$

$$10100011 \oplus 00101000$$

10100001

A1

8B

 $\rightarrow 9F \oplus 5C$

$$10011111 \oplus 01011100$$

$$11000011$$

 $\rightarrow 4C \oplus 57$

$$01001100 \oplus 01010111$$

C3

00011011

 $\rightarrow 94 \oplus 66$

1B

$$10010100 \oplus 01100110$$

 $\rightarrow 37 \oplus 77$

$$00110111 \oplus 01110111$$

$$11110D10$$

$$01000000$$

F2

40

 $\rightarrow ED \oplus F3$

$$\begin{array}{r} 11101101 \oplus 11110011 \\ 00011110 \Rightarrow 1E \end{array}$$

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Date / /

$$- 42 \oplus 00$$

$$0100,0010, \oplus 0000\ 0000$$

$$0100,0010$$

$$10010100 \oplus 8121100$$

$$11031000$$

$$- A6 \oplus 41$$

$$1010,0110 \oplus 0100\ 0001$$

$$001111100111$$

$$- D7$$

$$- BC \oplus 6A$$

$$10111100 \oplus 0110\ 1010$$

$$11010110$$

$$D6$$

$$- AD \oplus 10$$

$$- 001111 \oplus 0010\ 1011$$

$$0011110000$$

$$- A8 \oplus 0000$$

$$00011000 \oplus 00000000$$

$$- 0010,0000$$

$$- 10001011 \oplus 00001110$$

$$100000101$$

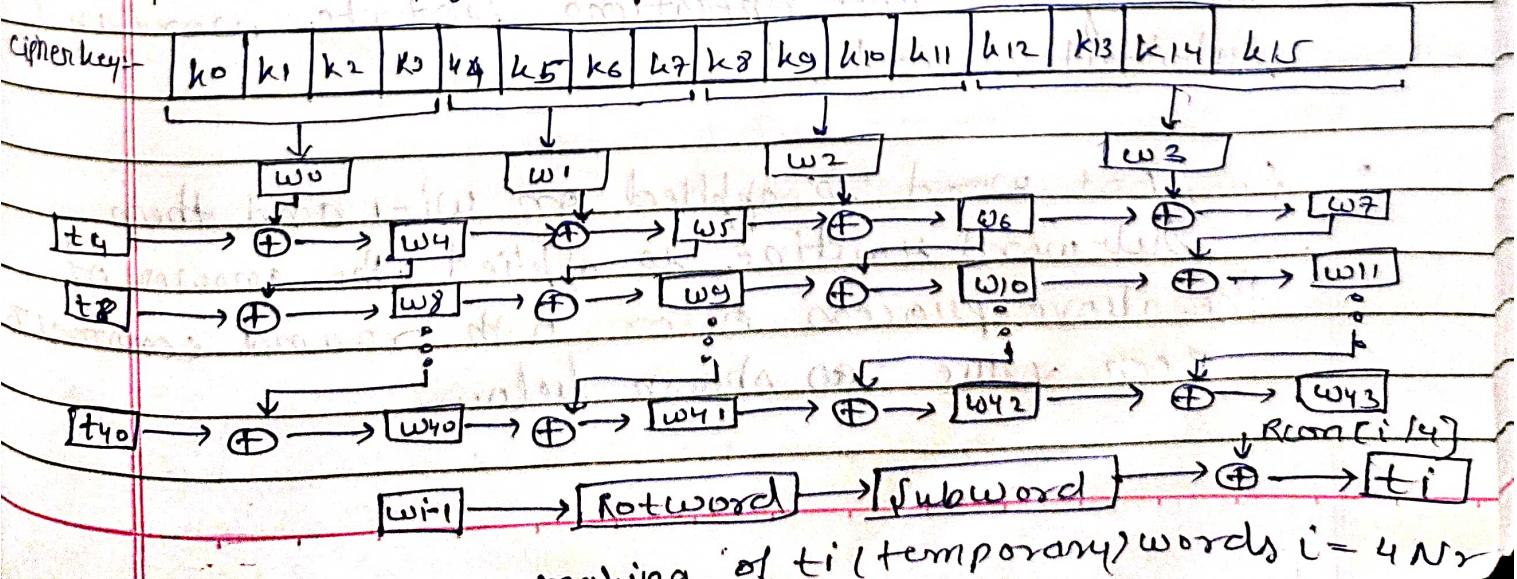
$$- 1A$$

$$00010100 \oplus 00000000$$

~~Q3 * AES key expansion process :- (128 bits)~~

- In AES key expansion process it generates $(Nr+1)$ round keys of size 128 bit each
- from the given 128 bit cipherkey, it is used during ~~perround~~ transformation stage.
- Thus, the remaining round keys are generated from the given 128 bit cipherkey
- Round keys are generated word by word where word = 4 bits thus, the expansion process creates $4 \times (Nr+1)$ words
- Thus, the words are called as $w_0, w_1, w_2, \dots, w_{4(Nr+1)}$
- 128 bit — 44 words — R_{10} ($w_0 - w_{43}$)
- 192 bit — 52 words — R_{12} ($w_0 - w_{51}$)
- 256 bit — 60 words — R_{14} ($w_0 - w_{59}$)

- following figure shows the key expansion process for 128 AES:-



From the above diagram the process is as follows:

- The given cipher key is of 16 bits i.e. 1 (128 bits) represents as k_0 to k_{15} in binary.
- The four words are created from the given cipher key where each word consists of 4 bits.
- Therefore, $w_0 = k_0 \oplus k_3$; $w_1 = k_4 \oplus k_7$, $w_2 = k_8 \oplus k_{11}$
 $w_3 = k_{12} \oplus k_{15}$.
- The remaining words from w_4 to w_{43} are generated as follows: (w_i for $i=4 \text{ to } 43$)

(a) if $(i \bmod 4) \neq 0$, $w_i = w_{i-1} \oplus w_{i-4}$

(b) if $(i \bmod 4) = 0$, $w_i = t \oplus w_{i-4}$

here, t is a temporary word where,

$t = \text{subword} - (\text{rot word } (w_{i-1})) \oplus R(\text{con}_i)$

where, t is a temporary word that stores the result of the two operations rotate word and substitute word.

- So, rot word is applied on w_{i-1} and then sub word routine is applied the answer of the above process ex-or with round constant R con value as shown below.

Rcon Constants

Round	Constant K(rcon)	Round	Constant (K(rcon))
1	(01 00 00 00)16	6	(20 00 00 00)16
2	(02 00 00 00)16	7	(40 00 00 00)16
3	(04 00 00 00)16	8	(80 00 00 00)16
4	(08 00 00 00)16	9	(1B 00 00 00)16
5	(10 00 00 00)16	10	(36 00 00 00)16

- (Rcon values) on the round constant values can be calculated using GF(28) and using irreducible polynomial ($x^8 + x^4 + x^3 + x + 1$).
{(refer pg. 236) of forzen E-book for process}

- following shows the pseudocode for 128 bit AES:-

KeyExpansion ([key₀ to key₁₅], [w₀ to w₄₃])

```
{
    for(i=0 to 3)
        wi ← key4i + key4i+1 + key4i+2 + key4i+3
    for(i=4 to 43)
    {
        if (i mod 4 ≠ 0) wi ← wi - 1 + wi - 4
        else
        {
            t ← subWord(RotWord(wi-1) ⊕ Rconi/4)
            wi ← t ⊕ wi - 4
        }
    }
}
```

• (i mod 4 ≠ 0) because it is a temporary word

• (i mod 4 = 0) because it is a constant word

• (RotWord) is a rotation

• (subWord) is a substitution

• (Rcon_{i/4}) is a constant

Q - Alice and Bob agreed upon a 128 bit cipher bit as given as :-

$w_0 \quad w_1 \quad w_2 \quad w_3 \quad w_4 \quad w_5 \quad w_6 \quad w_7 \quad w_8 \quad w_9 \quad w_{10} \quad w_{11} \quad w_{12} \quad w_{13} \quad w_{14} \quad w_{15}$
 24 75 A2 B3 34 75 56 88 31 E2 12 00 13 AA 54 87 16

Calculate the keys for each round for AES 128 bit version.

round	value of t	first word in the round	second word in the round	third word in round	fourth word in the round
pre-round (R0)	$w_0 = 24, 75, A2, B3$	$w_1 = 34, 75, 56, 88$	$w_2 = 31, E2, 12, 00$	$w_3 = 13, AA, 54, 87$	
R1	$A020177D$	$w_04 = 8955B5CE$	$w_05 = BD20E346$	$w_06 = 8C(C2F1)E$	$w_07 = 9F6675A9$
R2	$w_08 =$	$w_09 =$	$w_{10} =$	$w_{11} =$	

Round 1 (Substitution, Permutation, Substitution, Permutation)

(S-box + Rcon)

Substitution → S-box → P-box → Substitution

Round 1

$w_04 =$ In pseudocode.
 $w_04 =$ if (numb 4 ≠ 0) → half
 else : → numA → 00.

Substitution → subword (Rotword (w_{i-1}) ⊕ Rcon)
 Rotword (13AA5487)

subword (13AA5487) = AA548713
 AA548713 → Rcon.

Rotword (AA548713) ⊕ Rcon
 AC20177d ⊕ Rcon
 AC20177d ⊕ 01000000

$A(201770) \oplus 0110000000$

$$\begin{array}{r} 10101100 \\ 00000001 \\ 10101100 \\ \hline 00100000 \\ 00100000 \\ \hline 00010111 \end{array}$$

$A(201770)$

$$\begin{array}{r} 0111100 \\ 00000000 \\ \hline 01111000 \end{array}$$

$t \leftarrow A(201770)$

$w_4 \leftarrow t + w_0$

$w_4 \leftarrow A(201770) \oplus 2A75A2B3$

$w_4 \leftarrow 8955B5CE$

$w_{05} = i = 5$

$w_5 \leftarrow w_4 \oplus w_1$

$8955B5CE \oplus 34755688$

$w_5 \leftarrow BD20E346$

$w_{06} = i = 6$

$w_6 \leftarrow w_5 \oplus w_2$

$w_6 \leftarrow BD20E346 \oplus 31E21200$

$w_6 \leftarrow 8C C2F1278$

$w_{07} = i = 7$

$w_7 \leftarrow w_6 \oplus w_3$

$w_7 \leftarrow 8CC2F148 \oplus 13AA5487$

$w_7 \leftarrow 9F66A5C1$

* Round 2

$w_8 = \text{In pseudocode.}$

$i=8 \text{ if } (4 \bmod 4 \neq 0) - \text{false}$

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$t \leftarrow \text{subword}(\text{Rotword}(w_{i-1})) \oplus R(\alpha_i)_4$

$t \leftarrow \text{subword}(\text{Rotword}(GF66AS(i_1))) \oplus R(\alpha_1)_2$

$t \leftarrow \text{subword}(66AS(i_1)GF) \oplus R(\alpha_2)_2$

$t \leftarrow \text{subword}(330678DB) \oplus R(\alpha_2)_2$

$t \leftarrow 330678DB \oplus 02000000$

$t \leftarrow 0FF000000$

0CF000000 → 00000000