Computer Project

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Roll number: 24

 $"Writing\ code\ a\ computer\ can\ understand\ is\ science.\ Writing\ code$ other programmers can understand is an art." — Jason Gorman

— Ken Thompson

Problem 1 An *n* digit integer $(a_1 a_2 \dots a_n)$, where each digit $a_i \in \{0, 1, \dots, 9\}$, is said to have *unique digits* if no digits are repeated, i.e., there is no i, j such that $a_i = a_j$ $(i \neq j)$.

Verify whether an inputted number has unique digits.

Solution

```
public class Unique {
          public static void main (String[] args) {
2
                 try {
                        long number = Long.parseLong(args[0]);
                        if (isUnique(number)) {
                               System.out.println("Unique Number!");
                        } else {
                               System.out.println("Not a Unique Number!");
                 } catch (NumberFormatException e) {
                        System.out.println("Enter an integer as the first argument!");
                 } catch (IndexOutOfBoundsException e) {
                        System.out.println("Enter 1 argument (integer)!");
                 }
14
          }
          public static boolean isUnique (long number) {
                 int[] count = new int[10];
                 for (long n = Math.abs(number); n > 0; n \neq 10) {
19
                        int digit = (int) n % 10;
                        count[digit]++;
21
                        if (count[digit] > 1){
                               return false;
                        }
                 }
                 return true;
          }
27
   }
```

"Elegance is not a dispensable luxury but a factor that decides between success and failure."

— Edsger W. Dijkstra

Problem 2 A partition of a positive integer n is defined as a collection of other positive integers such that their sum is equal to n. Thus, if (a_1, a_2, \ldots, a_k) is a partition of n,

$$n = a_1 + a_2 + \dots + a_k \qquad (a_i \in \mathbb{Z}^+)$$

Display every unique partition of an inputted number.

Solution

```
public class Partition {
          public static void main (String[] args) {
                 try {
                         int target = Integer.parseInt(args[0]);
                        if (target < 1) {</pre>
                                throw new NumberFormatException();
                         }
                        partition(target);
                 } catch (NumberFormatException e) {
                         System.out.println("Enter a natural number as the first
11
                             argument!");
                 } catch (IndexOutOfBoundsException e) {
                         System.out.println("Enter 1 argument (natural number)!");
                 }
14
          public static void partition (int target) {
                 partition(target, target, "");
          }
18
          public static void partition (int target, int previousTerm, String suffix) {
19
                 if (target == 0)
                         System.out.println(suffix);
21
                 for (int i = 1; i <= target && i <= previousTerm; i++)</pre>
                         partition(target - i, i, suffix + " " + i);
23
          }
24
25
```

— Leonardo da Vinci

Problem 3 A Caesar cipher is a type of monoalphabetic substitution cipher in which each letter in the plaintext is replaced by a letter some fixed number of positions down the alphabet. The positions are circular, i.e., after reaching Z, the position wraps around to A. For example, following is some encrypted text, using a right shift of 5.

Plain: ABCDEFGHIJKLMNOPQRSTUVWXYZ Cipher: FGHIJKLMNOPQRSTUVWXYZABCDE

Thus, after mapping the alphabet according to the scheme $A \mapsto 0, B \mapsto 1, \dots, Z \mapsto$ 23, we can define an encryption function E_n , in which a letter x is shifted rightwards by n as follows.

$$E_n(x) = (x+n) \mod 26$$

The corresponding decryption function D_n is simply

$$D_n(x) = (x - n) \mod 26$$

Implement a simple version of a *Caesar cipher*, encrypting capitalized plaintext by shifting it by a given value. Interpret positive shifts as rightwards, negative as leftwards.

Solution

```
public class CaesarShift {
          public static void main (String[] args) {
                  try {
                         int shift = Integer.parseInt(args[0]) % 26;
                         String plaintext = args[1].toUpperCase();
                         String ciphertext = "";
                         for (int i = 0; i < plaintext.length(); i++) {</pre>
                                char plain = plaintext.charAt(i);
                                char crypt = ' ';
                                if ('A' <= plain && plain <= 'Z') {</pre>
                                       crypt = numToChar(charToNum(plain) + shift);
                                } else {
                                       crypt = plain;
13
14
                                ciphertext += crypt;
```

```
16
                        System.out.println(ciphertext);
17
                 } catch (NumberFormatException e) {
18
                        System.out.println("Enter an integer as the first argument!");
19
                 } catch (IndexOutOfBoundsException e) {
                        System.out.println("Enter 2 arguments (shift, plaintext)!");
21
                 }
          }
          public static int charToNum (char letter) {
25
                 return Character.toUpperCase(letter) - 'A';
          }
27
          public static char numToChar (int number) {
                 return (char) ('A' + Math.floorMod(number, 26));
          }
31
   }
```

"There are 2 hard problems in computer science: cache invalidation, naming things, and off-by-1 errors."

— Leon Bambrick

Problem 4 A *palindrome* is a sequence of characters which reads the same backwards as well as forwards. For example, madam, racecar and kayak are words which are palindromes. Similarly, the sentence "A man, a plan, a canal -- Panama!" is also a plaindrome.

Analyze a sentence of input and display all *words* which are palindromes. If the entire *sentence* is also a palindrome, display it as well.

(A word is an unbroken sequence of characters, separated from other words by whitespace. Ignore single letter words such as I and a. Ignore punctuation, numeric digits, whitespace and case while analyzing the entire sentence.)

Solution

```
import java.util.Scanner;
2
   public class Palindrome {
          public static void main (String[] args) {
                 System.out.print("Enter your sentence : ");
                 String sentence = (new Scanner(System.in)).nextLine().trim();
                 boolean foundPalindrome = false;
                 System.out.println("Palindromes : ");
                 foundPalindrome |= checkWords(sentence);
                 foundPalindrome |= checkSentence(sentence);
                 if (!foundPalindrome) {
                        System.out.println("(No palindromes found!)");
                 }
          }
          public static boolean checkWords (String sentence) {
                 boolean foundPalindrome = true;
17
                 int start = -1;
18
                 int end = 0;
19
                 while (end < sentence.length()) {</pre>
                        while (Character.isWhitespace(sentence.charAt(++start)));
                        end = start;
```

```
while (end < sentence.length() &&
23
                             !Character.isWhitespace(sentence.charAt(end++)));
                         String word = sentence.substring(start, end).trim();
24
                         if (isPalindrome(word)) {
                                foundPalindrome = true;
                                System.out.println(getAlphabets(word));
                         start = end - 1;
                  }
                 return foundPalindrome;
31
          }
          public static boolean checkSentence (String sentence) {
                  if (isPalindrome(sentence)) {
35
                         System.out.println(sentence);
36
                         return true;
                  }
                 return false;
39
          }
40
          public static boolean isPalindrome (String text) {
42
43
                 String rawText = getAlphabets(text).toUpperCase();
                  for (int i = 0, j = rawText.length() - 1; i < j; i++, j--) {
44
                         if (rawText.charAt(i) != rawText.charAt(j)) {
                                return false;
46
47
                 }
48
                 return (rawText.length() > 1);
50
          public static String getAlphabets (String text) {
                 String rawText = "";
53
                 for (int i = 0; i < text.length(); i++) {</pre>
54
                         if (Character.isAlphabetic(text.charAt(i))) {
55
                                rawText += text.charAt(i);
                  }
58
                 return rawText;
59
          }
60
   }
61
```

"I am rarely happier than when spending an entire day programming my computer to perform automatically a task that would otherwise take me a good ten seconds to do by hand."

— Douglas Adams

Problem 5 The *Sieve of Eratosthenes* is a simple, ancient algorithm for finding all prime numbers up to any given limit. It does so by iteratively marking as composite the multiples of each prime, starting with the first prime number, 2.

Implement the *Sieve of Eratosthenes* to display primes upto a given limit, as well as the number of primes calculated.

Solution

```
public class SieveOfEratosthenes {
          private final int upperLimit;
          private boolean[] primes;
          public SieveOfEratosthenes (int upperLimit) {
                  this.upperLimit = upperLimit;
                  this.initPrimes();
          }
          public boolean[] getPrimes () {
                  return primes;
11
13
          public void initPrimes () {
                  this.primes = new boolean[upperLimit];
                  primes[0] = false;
                  primes[1] = false;
17
                  for (int i = 2; i < upperLimit; i++)</pre>
18
                         primes[i] = true;
19
          }
20
21
          public void sievePrimes () {
                  int prime = 2;
                  while ((prime * prime) < upperLimit) {</pre>
24
                         int multiple = prime * prime;
25
                         while (multiple < upperLimit) {</pre>
26
                                primes[multiple] = false;
```

```
multiple += prime;
28
                         }
29
                         while (!primes[++prime]);
30
                 }
31
          }
32
   }
33
   public class Primes {
          public static void main (String[] args) {
                  try {
                         int upperLimit = Integer.parseInt(args[0]);
                         if (upperLimit < 2)</pre>
                                throw new NumberFormatException();
                         SieveOfEratosthenes sieve = new
                             SieveOfEratosthenes(upperLimit);
                         sieve.sievePrimes();
                         showPrimes(sieve.getPrimes());
                  } catch (NumberFormatException | ArrayIndexOutOfBoundsException e) {
                         System.out.println("Enter an integer (>1) as the first
11
                             argument!");
                         System.out.println("(Primes will be dislayed up to, not
12
                             including this integer)");
                 }
13
          }
          public static void showPrimes (boolean[] primes) {
                  int primeCount = 0;
                  int maxLength = Integer.toString(primes.length).length();
                  for (int i = 0; i < primes.length; i++) {</pre>
19
                         if (primes[i]) {
                                System.out.printf("%" + maxLength + "d ", i);
                                primeCount++;
                         }
23
                  System.out.println("\nTotal number of primes : " + primeCount);
25
          }
26
   }
27
```

— Ted Nelson

Problem 6 Design a simple interface for an examiner which can format and display marks scored by a group of students in a particular examination. Calculate the percentage scored by each candidate and display the list of students and percentages in an ASCII bar chart, arranged alphabetically.

Solution

```
public class Marksheet {
          public static final int SCREEN_WIDTH = 100;
          private final double maxMarks;
          private final int numberOfStudents;
          private int lastStudent;
          private String[] names;
          private double[] marks;
          public Marksheet (double maxMarks, int numberOfStudents) {
                 this.maxMarks = maxMarks;
                 this.numberOfStudents = numberOfStudents;
11
                 this.names = new String[numberOfStudents];
                 this.marks = new double[numberOfStudents];
                 this.lastStudent = -1;
          }
          public boolean addMarks (String name, double score) {
                 try {
                        names[++lastStudent] = name;
19
                        marks[lastStudent] = score;
20
                        return true;
                 } catch (IndexOutOfBoundsException e) {
                        return false;
                 }
          }
26
          public void displayChart () {
                 System.out.println(Marksheet.multiplyString("-",
                     Marksheet.SCREEN_WIDTH));
                 for (int i = 0; i <= lastStudent; i++) {</pre>
29
                        double fraction = marks[i] / maxMarks;
30
```

```
String name = (names[i].length() < 16)</pre>
                                        ? names[i]
                                        : (names[i].substring(0,13) + "...");
33
                         int points = (int) (fraction * (SCREEN_WIDTH - 34));
34
                         String bar = multiplyString("*", points)
                                 + multiplyString(" ", SCREEN_WIDTH - 34 - points);
36
                         System.out.printf("| %16s | %s | %6.2f %% |%n"
                                                       , name
                                                        bar
                                                       , fraction * 100);
40
                  }
41
                  System.out.println(Marksheet.multiplyString("-",
42
                      Marksheet.SCREEN_WIDTH));
          }
43
44
          public void displayMaxScorers () {
                  String maxScorers = "";
46
                  double maxScore = getMaxScore();
47
                  for (int i = 0; i <= lastStudent; i++) {</pre>
48
                         if (marks[i] == maxScore) {
                                 maxScorers += ", " + names[i];
                  }
                  System.out.println(maxScorers.substring(1)
                                        + " scored the highest ("
54
                                        + maxScore + "/"
                                        + maxMarks + ")");
56
          }
58
          public void sortByName () {
59
                  for (int right = lastStudent; right > 0; right--)
                         for (int i = 1; i <= right; i++)</pre>
61
                                 if (names[i-1].compareToIgnoreCase(names[i]) > 0)
62
                                        swapRecords(i, i - 1);
63
          }
66
          public double getMaxScore () {
                  double max = Integer.MIN_VALUE;
                  for (int i = 0; i <= lastStudent; i++) {</pre>
                         max = Math.max(max, marks[i]);
                  }
71
                  return max;
          }
73
          private void swapRecords (int x, int y) {
```

```
String tempName = names[x];
76
                 double tempMark = marks[x];
77
                 names[x] = names[y];
78
                 marks[x] = marks[y];
                 names[y] = tempName;
                 marks[y] = tempMark;
81
          }
          public static String multiplyString (String s, int n) {
                 String out = "";
85
                 while (n --> 0)
                         out += s;
87
                 return out;
          }
89
   }
   import java.util.Scanner;
   import java.util.InputMismatchException;
   public class ScoreRecorder {
          public static void main (String[] args) {
                 Scanner inp = new Scanner(System.in);
6
                 double maxMarks = 0.0;
                 int numberOfStudents = 0;
                 try {
                         System.out.print("Enter the maximum marks alotted for each
10
                             student : ");
                         maxMarks = inp.nextDouble();
                         System.out.print("Enter the total number of students : ");
                         numberOfStudents = inp.nextInt();
13
                         if (maxMarks <= 0) {</pre>
14
                                System.out.println("Maximum marks must be positive!");
                                System.exit(0);
16
                         }
17
                         if (numberOfStudents <= 0) {</pre>
                                System.out.println("Number of students must be
19
                                    positive!");
                                System.exit(0);
21
22
                         Marksheet sheet = new Marksheet(maxMarks, numberOfStudents);
                         System.out.println("Enter " + numberOfStudents + " students'
23
                             names and marks : ");
                         for (int i = 0; i < numberOfStudents; i++) {</pre>
                                String name = "";
25
                                while (!inp.hasNextDouble()) {
26
```

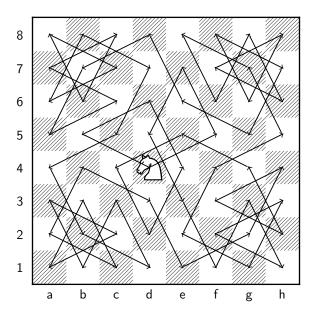
```
name += inp.next() + " ";
27
                                }
28
                                double marks = inp.nextDouble();
29
                                if (marks <= 0 || marks > maxMarks) {
30
                                       System.out.println("Marks must be within 0.0 and
                                           " + maxMarks + "!");
                                       System.exit(0);
32
                                }
33
                                sheet.addMarks(name.trim(), marks);
35
                         sheet.sortByName();
                        sheet.displayChart();
                         sheet.displayMaxScorers();
                 } catch (InputMismatchException e) {
39
                        System.out.println("Invalid Input!");
40
                        System.exit(0);
41
                 }
42
          }
43
44 }
```

"My project is 90% done. I hope the second half goes as well."

— Scott W. Ambler

Problem 7 A *Knight's Tour* is a sequence of moves of a knight on a chessboard such that the *knight* visits every square only once. If the knight ends on a square that is one knight's move from the beginning square, the tour is *closed* forming a closed loop, otherwise it is *open*.

There are many ways of constructing such paths on an empty board. On an 8×8 board, there are no less than 26,534,728,821,064 directed closed tours. Below is one of them.

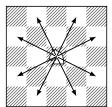


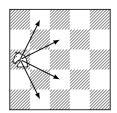
Construct a *Knight's Tour* (open or closed) on an $n \times n$ board, starting from a given square.

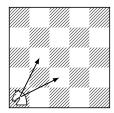
(Mark each square with the move number on which the knight landed on it. Mark the starting square 1.)

 $^{^{1}}$ Two tours along the same path that travel in opposite directions are counted separately, as are rotations and reflections.

Solution A knight on a chessboard can move to a square that is two squares away horizontally and one square vertically, or two squares vertically and one square horizontally.







The mobility of a knight can make varies greatly with its position on the board — near the centre, it can jump to one of 8 squares while when in a corner, it can jump to only 2. On the other hand, the number of possible sequences of squares a knight can traverse grows extremely quickly. Although it may seem that a simple brute force search can quickly find one of trillions of solutions, there are approximately 4×10^{51} different paths to consider on an 8×8 board. For even larger boards, iterating through every possible path is clearly impractical. [citation needed]

This problem calls for implementing a $backtracking^2$ algorithm, coupled with some $heuristic^3$ to speed up the search. One such heuristic is Warnsdorf's Rule.

The knight is moved so that it always proceeds to the square from which the knight will have the *fewest* onward moves.

This allows us to define a ranking alorithm for each possible path — the positions which result in the smallest number of further moves, or is furthest away from the board's centre will be investigated first. In case of a tie, we can either proceed without making any changes to the already existing positions, or introduce a random element. This has the effect of producing different results on successive executions, giving a variety of solutions.

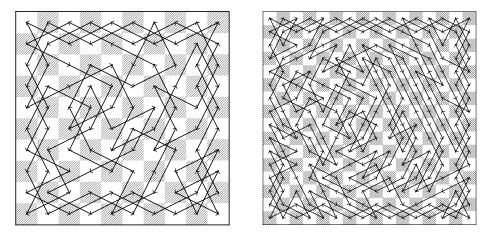
One drawback of resolving ties randomly is that an early "wrong" choice in the position tree can force the calculation of every resulting path without reaching a solution, effectively reducing the algorithm to a brute force search. This is especially problematic

²Backtracking is a general algorithm for finding some or all solutions to some computational problems that incrementally builds candidates to the solutions, and abandons each partial candidate ("backtracks") as soon as it determines that the candidate cannot possibly be completed to a valid solution.

³A heuristic technique is any approach to problem solving that employs a practical method not guaranteed to be optimal or perfect, but sufficient for the immediate goals. Where finding an optimal solution is impossible or impractical, heuristic methods can be used to speed up the process of finding a satisfactory solution.

for large boards, where it may take hours to backtrack and reach a solution. Thus, the "randomness factor" should be adjusted according to the board size.

A high randomness can be useful for searching specifically for *closed tours*, as a randomness of 0 simply produces the same solution every time (which may or may not be closed). Below are some tours generated by the program.



The tendency of the path to remain close to the edges of the board is clearly evident.

```
public class TourSolver {
          private final int size;
          private Position[] path;
          private int numberOfMoves;
          private int[][] board;
          private int[][] degreesOfFreedom;
          private Position initPosition;
          private double tieBreakRandomness;
          private static final int[][] KNIGHT_MOVES = {
                  \{-1, -2\}, \{-1, 2\}, \{1, -2\}, \{1, 2\},
                  \{-2, -1\}, \{-2, 1\}, \{2, -1\}, \{2, 1\}
          };
          public TourSolver (int size, Position initPosition, double randomness) {
                  this.size = size;
16
                 this.initPosition = initPosition;
                 this.tieBreakRandomness = randomness / 2.0;
                 this.path = new Position[size * size];
                 this.numberOfMoves = 0;
20
                 this.initBoard();
21
```

```
this.initDegreesOfFreedom();
          }
23
24
          public void resetSolution () {
                  this.path = new Position[size * size];
                  this.numberOfMoves = 0;
                  this.initBoard();
          }
          private void initBoard () {
31
                  board = new int[size][size];
                  for (int i = 0; i < size; i++)</pre>
33
                         for (int j = 0; j < size; j++)
                                 board[i][j] = 0;
35
          }
36
          private void initDegreesOfFreedom () {
                  degreesOfFreedom = new int[size][size];
39
                  for (int i = 0; i < size; i++)</pre>
40
                         for (int j = 0; j < size; j++)
                                 degreesOfFreedom[i][j] = getPossibleMovesCount(new
42
                                     Position(i, j));
          }
43
          public boolean addMove (Position p) {
45
                  if (numberOfMoves < (size * size)) {</pre>
46
                         path[numberOfMoves++] = p;
47
                         board[p.getX()][p.getY()] = numberOfMoves;
                         return true;
49
                  }
                  return false;
          }
53
          public boolean removeMove () {
54
                  if (numberOfMoves > 0) {
                         Position p = path[numberOfMoves - 1];
                         board[p.getX()][p.getY()] = 0;
57
                         path[--numberOfMoves] = null;
                         return true;
                  }
                  return false;
          }
62
          public int[][] getBoard () {
64
                  return board;
          }
66
```

```
67
           public Position[] getSolution () {
68
                   if (size < 5)
69
                          return null;
70
                   addMove(initPosition);
                   if(solve(initPosition))
                          return path;
                  return null;
           }
76
           public boolean solve (Position p) {
                   if (numberOfMoves == (size * size))
                          return true;
                  Position[] possibleMoves = getPossibleMoves(p);
80
                   if (possibleMoves[0] == null)
81
                          return false;
                   sortMoves(possibleMoves);
83
                   for (Position move : possibleMoves) {
84
                          if (move != null) {
85
                                 addMove(move);
                                 if (solve(move))
87
                                         return true;
                                 removeMove();
89
                          }
                   }
91
                  return false;
92
           }
93
           public void sortMoves (Position[] moves) {
95
                   int count = 0;
                  for (Position p : moves)
                          if (p != null)
98
                                 count++;
99
                   for (int right = count; right > 0; right--)
100
                          for (int i = 1; i < right; i++)</pre>
                                 if (compareMoves(moves[i-1], moves[i]) > 0)
                                         swapMoves(i-1, i, moves);
103
           }
104
           public int compareMoves (Position a, Position b) {
106
                   int aCount = getPossibleMovesCount(a);
107
                   int bCount = getPossibleMovesCount(b);
108
                   if (aCount != bCount)
                          return aCount - bCount;
110
                   int aFree = degreesOfFreedom[a.getX()][a.getY()];
111
                   int bFree = degreesOfFreedom[b.getX()][b.getY()];
112
```

```
if (aFree != bFree)
113
                          return aFree - bFree;
114
                  return (Math.random() < tieBreakRandomness)? 1 : -1;</pre>
115
           }
116
           private static void swapMoves (int x, int y, Position[] moves) {
118
                  Position t = moves[x];
119
                  moves[x] = moves[y];
120
                  moves[y] = t;
           }
122
           public Position[] getPossibleMoves (Position start) {
124
                  Position[] possibleMoves = new Position[KNIGHT_MOVES.length];
                  int i = 0;
126
                  for (int[] move : KNIGHT MOVES) {
127
                          int x = start.getX() + move[0];
                          int y = start.getY() + move[1];
129
                          if (isWithinBoard(x, y) && board[x][y] == 0) {
130
                                 possibleMoves[i++] = new Position(x, y);
131
133
134
                  return possibleMoves;
           }
           public int getPossibleMovesCount (Position start) {
137
                  int i = 0;
                  for (Position p : getPossibleMoves(start))
139
                          if (p != null)
                                 i++;
141
                  return i;
           }
143
           public boolean isWithinBoard (int x, int y) {
145
                  return (x >= 0 && x < size && y >= 0 && y < size);
146
           }
147
148
    public class Position {
           private final int x;
 3
           private final int y;
           public Position (int x, int y) {
                  this.x = x;
                  this.y = y;
           }
```

```
public Position (String s) {
10
                  int x = 0;
11
                  int i = 0;
12
                  while (i < s.length() && Character.isAlphabetic(s.charAt(i))) {</pre>
                         x = (x * 26) + Character.toLowerCase(s.charAt(i)) - 'a' + 1;
14
                         i++;
                  }
16
                  int y = Integer.parseInt(s.substring(i));
                  this.x = x - 1;
18
                  this.y = y - 1;
          }
20
          public int getX () {
22
                  return x;
23
          }
24
25
          public int getY () {
26
                  return y;
27
          }
29
          public boolean equals (Position p) {
                  return (p != null)
                         && (this.getX() == p.getX()) && (this.getY() == p.getY());
33
          @Override
35
          public String toString () {
                  return xToString(this.x) + (this.y + 1);
37
          }
          public static String xToString (int n) {
40
                  int x = n + 1;
41
                  String letters = "";
42
                  while (x > 0) {
43
                         letters = (char) ('a' + (--x % 26)) + letters;
44
                         x /= 26;
45
                  }
46
47
                  return letters;
          }
48
   }
49
   public class KnightTour {
          public static void main (String[] args) {
                  try {
```

```
int boardSize = Integer.parseInt(args[0]);
                         if (boardSize <= 0)</pre>
5
                                throw new NumberFormatException();
                        String initSquare = (args.length > 1)? args[1] : "a1";
                         double randomness = (args.length > 2)?
                             Double.parseDouble(args[2])
                                                          : Math.pow(0.8, boardSize) * 2;
                        TourSolver t = new TourSolver(boardSize, new
                            Position(initSquare), randomness);
                         Position[] solution = t.getSolution();
11
12
                         if (solution != null) {
                                showBoard(t.getBoard());
                                showMoves(solution);
                                if (isClosed(solution))
                                       System.out.println("\nThe tour is Closed!");
                         } else {
                                System.out.println("No Knight's Tours found!");
19
                 } catch (Exception e) {
20
                         System.out.print("Enter an integer (> 1) as the first
                             argument, ");
                         System.out.println("and a well formed chessboard coordinate as
                            the second!");
                        System.out.println("
                                                                        (size,
23
                             startSquare * , randomness * )");
                         System.out.println();
24
                                                        -> Solve a Tour on a (size x
                        System.out.println("(size
25
                             size) board)");
                         System.out.println("(startSquare * -> A square in algebraic
26
                             chess notation of the form 'fr',");
                         System.out.println("
                                                           where f = the letter
27
                             representing the file(column)");
                                                           \quad \text{and} \quad
                         System.out.println("
                                                               r = the number
28
                             representing the rank(row).)");
                         System.out.println("(startSquare is set to 'a1' by default)");
20
                        System.out.println("(randomness * -> A number between O(no
30
                             randomness) and 1(even chances),");
                         System.out.println("
                                                           determining the randomness in
                             ranking positions of");
                         System.out.println("
                                                          the same weightage while
32
                             searching. A randomness of 0 will");
                         System.out.println("
                                                           produce the same tour every
                             time, for a specific size and");
                         System.out.println("
                                                           startSquare. Keep extremely
34
                             small values of randomness for");
                         System.out.println("
                                                          very large boards.)");
35
```

```
System.out.println("(randomness is set to 2 * (0.8)^boardSize
36
                             by default)");
                        System.out.println();
37
                         System.out.println("
                                                                                        <
38
                             * = optional arguments >");
                 }
39
          }
40
41
          public static void showBoard (int[][] board) {
                 String hLine = " " + multiplyString("+----", board.length) + "+";
43
                 System.out.println(hLine);
                 for (int column = board.length - 1; column >= 0; column--) {
45
                         System.out.printf(" %2d ", column + 1);
46
                         for (int row = 0; row < board.length; row++) {</pre>
47
                                System.out.printf("| %3d ", board[row][column]);
48
                         }
                        System.out.printf("|%n%s%n", hLine);
50
                  }
                  System.out.print(" ");
                  for (int i = 0; i < board.length; i++) {</pre>
                        System.out.printf(" %2s ", Position.xToString(i));
54
                  System.out.println();
56
          }
58
          public static void showMoves (Position[] moves) {
                  System.out.print("\nMoves : ");
                 String movesOut = "";
                 for (int i = 1; i < moves.length; i++) {</pre>
62
                        movesOut += (moves[i-1] + "-" + moves[i] + ", ");
                 System.out.println(movesOut.substring(0, movesOut.length() - 2));
          }
66
67
          public static String multiplyString (String s, int n) {
                  String result = "";
                  while (n --> 0)
                        result += s;
                 return result;
          }
73
          public static boolean isClosed (Position[] path) {
                  int l = path.length - 1;
                 int dX = Math.abs(path[0].getX() - path[1].getX());
                 int dY = Math.abs(path[0].getY() - path[1].getY());
                 return (dX == 1 && dY == 2) || (dX == 2 && dY == 1);
```

80 } 81 }

— L. Peter Deutsch

Problem 8 The determinant of a square matrix $A_{n,n}$ is defined recursively as follows.

$$det(A_{n,n}) = \begin{vmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & \cdots & a_{n,n} \end{vmatrix} = \sum_{j=1}^{n} (-1)^{i+j} a_{i,j} \cdot det(M_{i,j})$$

where $M_{i,j}$ is defined as the minor of $A_{n,n}$, an $(n-1) \times (n-1)$ matrix formed by removing the *i*th row and *j*th column from $A_{n,n}$.

The determinant of a (2×2) matrix is simply given by

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

For example, the determinant of a (3×3) matrix is given by the following expression.

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$
$$= aei + bfg + cdh - ceg - bdi - afh$$

Calculate the *determinant* of an inputted $(n \times n)$ square matrix.

Solution

```
public class Matrix {
    protected final int rows;
    protected final int columns;
    protected int[][] elements;

public Matrix (int rows, int columns) {
        this.rows = rows;
        this.columns = columns;
        this.elements = new int[rows][columns];
```

```
}
11
          public int getRows () {
                 return this.rows;
13
          public int getColumns () {
                 return this.columns;
          }
19
          public void setElementAt (int element, int row, int column) {
                  if (row < 1 || row > rows || column < 1 || column > columns)
21
                         return;
                  elements[row-1][column-1] = element;
23
          }
          public int getElementAt (int row, int column) {
26
                 if (row < 1 || row > rows || column < 1 || column > columns)
27
                         return Integer.MIN_VALUE;
28
                 return elements[row-1][column-1];
30
31
   }
32
   public class SquareMatrix extends Matrix {
          protected int size;
          public SquareMatrix (int size) {
                  super(size, size);
                 this.size = size;
          }
          public int getSize () {
                 return this.size;
10
          public int getDeterminant () {
                 if (this.size == 1)
13
                        return getElementAt(1, 1);
14
                 if (this.size == 2)
                         return (getElementAt(1, 1) * getElementAt(2, 2))
                                - (getElementAt(1, 2) * getElementAt(2, 1));
17
                 int determinant = 0;
                 for (int i = 1; i <= size; i++)</pre>
                         determinant += ((int) Math.pow(-1, 1+i)) * getElementAt(1, i)
20
                                                              * getMinorMatrix(1,
21
```

```
i).getDeterminant();
                 return determinant;
          }
23
24
          public SquareMatrix getMinorMatrix (int row, int column) {
                 if (row < 1 || row > size || column < 1 || column > size)
26
                         return null;
                 if (this.size <= 1)
                        return new SquareMatrix(0);
                 SquareMatrix minor = new SquareMatrix(this.size - 1);
30
                 for (int i = 1, p = 1; p < size; i++, p++) {
                         if (i == row)
32
                         for (int j = 1, q = 1; q < size; j++, q++) {
34
                                if (j == column)
35
                                       j++;
                                minor.setElementAt(this.getElementAt(i, j), p, q);
                         }
38
                 }
39
                 return minor;
40
41
42
   }
   import java.util.Scanner;
   public class Determinant {
          public static void main (String[] args) {
                 Scanner inp = new Scanner(System.in);
                 try {
6
                        System.out.print("Enter the size of the (size X size) square
                            matrix : ");
                         int size = inp.nextInt();
                        SquareMatrix matrix = new SquareMatrix(size);
                         System.out.println("Enter " + (size * size) + " integers : ");
                         for (int i = 1; i <= size; i++)</pre>
                                for (int j = 1; j <= size; j++)</pre>
                                       matrix.setElementAt(inp.nextInt(), i, j);
13
                         System.out.println("\nThe determinant is : " +
14
                            matrix.getDeterminant());
                 } catch (Exception e) {
                         System.out.println("Invalid Input!");
16
                 }
          }
19
          public static void showMatrix (Matrix m) {
```

```
for (int i = 1; i <= m.getRows(); i++) {
    for (int j = 1; j <= m.getColumns(); j++) {
        System.out.printf("%4d ", m.getElementAt(i, j));
}

System.out.println();
}

System.out.println();
}
</pre>
```