# Computer Project

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Roll number: 24

 $"Writing\ code\ a\ computer\ can\ understand\ is\ science.\ Writing\ code$ other programmers can understand is an art." — Jason Gorman "I am rarely happier than when spending an entire day programming my computer to perform automatically a task that would otherwise take me a good ten seconds to do by hand."

— Douglas Adams

**Problem 1** An *n* digit integer  $(a_1 a_2 \dots a_n)$ , where each digit  $a_i \in \{0, 1, \dots, 9\}$ , is said to have *unique digits* if no digits are repeated, i.e., there is no i, j such that  $a_i = a_j$   $(i \neq j)$ .

Verify whether an inputted number has unique digits.

**Solution** The problem involves simply counting the number of occurrences of each digit in the given number and checking whether any of them exceed 1.

# main (number:Integer)

- 1. Initialize an integer array digits of length 10, indexed with integers from [0] to [9] with all elements set to 0.
- 2. If number exceeds 0, proceed. Otherwise, jump to (3).
  - (a) Store the last digit<sup>1</sup> of number in a temporary variable d.
  - (b) Increment the integer at the d index of digits.
  - (c) If digits[d] exceeds 1, the number does not have unique digits. Display a suitable message, and exit.
  - (d) Discard the last digit of number by performing an integer division by 10 and storing the result back in number.
  - (e) Jump to (2).
- 3. The number has *unique digits*. Display a suitable message.
- 4. Exit

<sup>&</sup>lt;sup>1</sup>The last digit of an integer n is simply  $n \mod 10$ 

```
public class Unique {
          public static void main (String[] args) {
                 try {
                        /* Parse the first command line argument as the number
                           to check for unique digits */
                        long number = Long.parseLong(args[0]);
                        if (isUnique(number)) {
                               System.out.println("Unique Number!");
                        } else {
                               System.out.println("Not a Unique Number!");
                 } catch (NumberFormatException | IndexOutOfBoundsException e) {
12
                        /* Handle missing or incorrectly formatted arguments */
                        System.out.println("Enter 1 argument (number[integer])!");
                 }
          }
          public static boolean isUnique (long number) {
18
                 /* Keep track of the number of occurrences of each digit */
                 int[] count = new int[10];
20
                 for (long n = Math.abs(number); n > 0; n /= 10) {
                        /* Extract the last digit of the number */
                        int digit = (int) n % 10;
                        count[digit]++;
                        if (count[digit] > 1){
25
                               return false;
26
27
                 }
29
                 return true;
30
          }
31
   }
```

Unique::main(String[])			
long	number	The inputted number	
Unique::isUnique(long)			
long	number	The number to check for uniqueness	
int[]	count	The number of occurrences of each digit	
long	n	Counter, temporarily stores the value of number	
int	digit	The last digit in n	

"Elegance is not a dispensable luxury but a factor that decides between success and failure."

— Edsger W. Dijkstra

**Problem 2** A partition of a positive integer n is defined as a collection of other positive integers such that their sum is equal to n. Thus, if  $(a_1, a_2, \ldots, a_k)$  is a partition of n,

$$n = a_1 + a_2 + \dots + a_k \qquad (a_i \in \mathbb{Z}^+)$$

Display every unique partition of an inputted number.

**Solution** This problem can be solved elegantly using  $recursion^2$ . Note that when partitioning a number n, we can calculate the partitions of (n-1) and append 1 to each solution. Similarly, we can append 2 to partitions of (n-2), 3 to partitions of (n-3), and so on. By continuing in this fashion, all cases will be reduced to the single base  $case^3$  of finding the partitions of 0, of which there are trivially none. [citation needed]

There is a slight flaw in this algorithm — partitions are often repeated. This can be overcome by imposing the restriction that each new term has to be of a lesser magnitude than the previous. In this way, repeated partitions will be automatically discarded.

```
main (target:Integer)
```

- 1. Call partition(target, target, "").
- 2. Exit

partition (target:Integer, previousTerm:Integer, suffix:String)

- 1. If target is 0, display suffix and return.
- 2. Initialize a counter i to 1.
- 3. If i is less than or equal to both the target and previousTerm, proceed. Otherwise, jump to (4).
  - (a) Call partition(target i, i, suffix + " " + i).
  - (b) Increment i by 1.
  - (c) Jump to (3).
- 4. Return

<sup>&</sup>lt;sup>2</sup>Recursion occurs when a thing is defined in terms of itself or of its type.

<sup>&</sup>lt;sup>3</sup>A base case is a case for which the answer is known and can be expressed without recursion.

```
public class Partition {
          public static void main (String[] args) {
3
                 try {
                        /* Parse the first command line argument as the target sum */
                        int target = Integer.parseInt(args[0]);
                        if (target < 1) {</pre>
                                throw new NumberFormatException();
                        }
                        partition(target);
                 } catch (NumberFormatException | IndexOutOfBoundsException e) {
                        /* Handle missing or incorrectly formatted arguments */
12
                        System.out.println("Enter 1 argument (number[natural
                            number])!");
                 }
14
          }
          /* Wrapper method for displaying partitions of a number */
17
          public static void partition (int target) {
                 partition(target, target, "");
19
          }
          /* Display the partitions of the target */
          public static void partition (int target, int previousTerm, String suffix) {
                 /* Base case : '0' has no partitions */
24
                 if (target == 0)
25
                        System.out.println(suffix);
26
                 /* Recursively solve for partitions by diminishing the target,
                    adding that difference to the solution, and partitioning the
28
                    remaining sum */
29
                 for (int i = 1; i <= target && i <= previousTerm; i++)</pre>
30
                        partition(target - i, i, suffix + " " + i);
31
          }
32
33 }
```

Partition::main(String[])			
int	target	The inputted number	
Partition::partition(int)			
int	target	The number to be partitioned	
Partition::partition(int, int, String)			
int	target	The number to be partitioned	
int	previousTerm	The previous term in the partition sequence	
String	suffix	Terms in the sequence calculated so far	
int	i	Counter variable, stores the next term in the se-	
		quence	

### — Leonardo da Vinci

**Problem 3** A Caesar cipher is a type of monoalphabetic substitution cipher in which each letter in the plaintext is replaced by a letter some fixed number of positions down the alphabet. The positions are circular, i.e., after reaching Z, the position wraps around to A. For example, following is some encrypted text, using a right shift of 5.

Plain: ABCDEFGHIJKLMNOPQRSTUVWXYZ Cipher: FGHIJKLMNOPQRSTUVWXYZABCDE

Thus, after mapping the alphabet according to the scheme  $A \mapsto 0, B \mapsto 1, \dots, Z \mapsto$  23, we can define an encryption function  $E_n$ , in which a letter x is shifted rightwards by n as follows.

$$E_n(x) = (x+n) \mod 26$$

The corresponding decryption function  $D_n$  is simply

$$D_n(x) = (x - n) \mod 26$$

Implement a simple version of a *Caesar cipher*, encrypting capitalized plaintext by shifting it by a given value. Interpret positive shifts as rightwards, negative as leftwards.

**Solution** This problem can be solved simply by exploiting the fact that Unicode characters are already arranged in order, with successive alphabets encoded by consecutive numbers. In addition, the encryption function can be defined exactly as given in the question — characters can be converted to their corresponding codes, manipulated by addition of the shift, and converted back into alphabetic form.

# main (shift:Integer, plainText:String)

- 1. Normalize plainText to uppercase.
- 2. Normalize shift by replacing it with shift mod 26.
- 3. Initialize an empty String cipherText.
- 4. Initialize a counter i to 0.
- 5. If i is less than the length of plainText, proceed. Otherwise, jump to (6).
  - (a) Store the character in plainText at position i in a variable plain.
  - (b) Initialize an empty character crypt.
  - (c) If plain is not an alphabet, assign plain to crypt and jump to (5g).
  - (d) Convert plain into a number, such that A is mapped to 0, B to 1 and so on. Store this in a temporary variable n.

- (e) Add shift to n, calculate its least residue modulo 26<sup>4</sup>, and store the result in n.
- (f) Convert n back into a character and store the result in crypt.
- (g) Append crypt to cipherText.
- (h) Increment i by 1 and jump to (5).
- 6. Display cipherText.
- 7. Exit

```
public class CaesarShift {
          public static void main (String[] args) {
2
                 try {
                        /* Parse the first command line argument as the shift */
                        int shift = Integer.parseInt(args[0]) % 26;
                        /* Parse the second command line argument as the text to
                            encrypt */
                        String plaintext = args[1].toUpperCase();
                        String ciphertext = "";
                        for (int i = 0; i < plaintext.length(); i++) {</pre>
                                char plain = plaintext.charAt(i);
                                char crypt = ' ';
                                if ('A' <= plain && plain <= 'Z') {</pre>
                                       /* Only shift letters of the alphabet */
                                       crypt = numToChar(charToNum(plain) + shift);
14
                                } else {
                                       /* Keep special characters intact */
                                       crypt = plain;
                                /* Append the encrypted character to the cipherText */
                                ciphertext += crypt;
20
21
                        System.out.println(ciphertext);
                 } catch (NumberFormatException | IndexOutOfBoundsException e) {
                         /* Handle missing or incorrectly formatted arguments */
24
                        System.out.println("Enter 2 arguments (shift[integer],
                            plaintext[text])!");
                 }
26
          }
27
          /* Map letters to numbers */
          public static int charToNum (char letter) {
30
```

<sup>&</sup>lt;sup>4</sup>The set of integers  $K = \{0, 1, 2, \dots, n-1\}$  is called the least residue system modulo n. The number k such that  $k \in K$  and  $a \equiv k \pmod{n}$  is called the least residue of a modulo n.

```
return Character.toUpperCase(letter) - 'A';

/* Map numbers to letters */

public static char numToChar (int number) {
    return (char) ('A' + Math.floorMod(number, 26));
}
```

<pre>CaesarShift::main(String[])</pre>			
int	shift	The inputted 'shift'	
String	plainText	The text to encrypt	
String	cipherText	The encrypted text	
int	i	Counter variable, stores the position in plainText	
char	plain	The character to encrypt	
char	crypt	The encrypted form of plain	
	CaesarShift::charToNum(char)		
char	letter	The character to convert to an integer	
CaesarShift::numToChar(int)			
int	number	The number to convert to a character	

"There are 2 hard problems in computer science: cache invalidation, naming things, and off-by-1 errors."

— Leon Bambrick

**Problem 4** A *palindrome* is a sequence of characters which reads the same backwards as well as forwards. For example, madam, racecar and kayak are words which are palindromes. Similarly, the sentence "A man, a plan, a canal -- Panama!" is also a palindrome.

Analyze a sentence of input and display all *words* which are palindromes. If the entire *sentence* is also a palindrome, display it as well.

(A word is an unbroken sequence of characters, separated from other words by whitespace. Ignore single letter words such as I and a. Ignore punctuation, numeric digits, whitespace and case while analyzing the entire sentence.)

**Solution** The main challenge here is intelligently dividing a *sentence* into its component *words*. Verifying whether a sequence of characters is a palindrome is fairly simple — extracting those characters from a string of alphabets, numbers, punctuation and whitespace is not.

The main idea behind isolating words from sentences is to define two *markers* — a start to keep track of the boundary between whitespace and letters, and an end to mark the boundary between letters and whitespace. In this way, the markers can inch their way along the sentence, isolating words in the process. Managing the order of condition checking and incrementing of counters does require some careful manoeuvring in order to avoid any *off-by-1 errors*<sup>5</sup> — any of which would inevitably result in incorrect, hence undesirable output. [citation needed]

### main ()

- 1. Accept a string as input, store it in a variable sentence.
- 2. Call checkWords (sentence) and checkSentence (sentence). Store the returned values in booleans.
  - (a) If either of them is true, set a boolean foundPalindrome to true, otherwise set it to false.
- 3. Display a suitable message if foundPalindrome is false.
- 4. Exit

 $<sup>^{5}</sup>$ An off-by-one error often occurs in computer programming when an iterative loop iterates one time too many or too few.

# checkWords (sentence:String)

- 1. Initialize a boolean foundPalindrome to false.
- 2. Initialize two integer counters: start to -1, end to 0.
- 3. If end is less than the length of sentence, proceed. Otherwise, jump to (4).
  - (a) Increment start as long as the character at the [start + 1] position in sentence is whitespace.
  - (b) Assign end to start.
  - (c) Increment end as long as it does not exceed the length of sentence and the character at the [end] position in sentence is not whitespace.
  - (d) Assign the string of characters between start and end from sentence (inclusive, exclusive) to a variable word.
  - (e) Call isPalindrome(word). If word is a palindrome:
    - i. Set foundPalindrome to true.
    - ii. Display word.
  - (f) Assign end 1 to start.
  - (g) Jump to (3)
- 4. Return foundPalindrome

# checkSentence (sentence:String)

- 1. Call isPalindrome(sentence). If sentence is a palindrome:
  - (a) Display word.
  - (b) Return true.
- 2. Return false.

### isPalindrome (text:String)

- 1. Normalize text by converting it into uppercase and removing all non-alphabetic characters.
- 2. Let the length of text be labeled temporarily as t.
- 3. Initialize two integer counters: i to 0, j to 1 1.
- 4. If i is less than j, proceed. Otherwise, jump to (5).
  - (a) If the characters at positions i and j in text are not equal, return false.
  - (b) Increment i by 1.
  - (c) Decrement j by 1.
  - (d) Jump to (4)
- 5. Return true only if text is longer than one character. Otherwise, return false.

```
import java.util.Scanner;
   public class Palindrome {
3
          public static void main (String[] args) {
                 System.out.print("Enter your sentence : ");
                 String sentence = (new Scanner(System.in)).nextLine().trim();
                 /* Keep track of whether palindromes have been found */
                 boolean foundPalindrome = false;
                 System.out.println("Palindromes : ");
                 foundPalindrome |= checkWords(sentence);
                 foundPalindrome |= checkSentence(sentence);
11
                 if (!foundPalindrome) {
12
                        System.out.println("(No palindromes found!)");
                 }
          }
          /* Slice a sentence into words and check each individually */
          public static boolean checkWords (String sentence) {
18
                 boolean foundPalindrome = false;
                 int start = -1;
20
                 int end = 0;
                 while (end < sentence.length()) {</pre>
                        while (Character.isWhitespace(sentence.charAt(++start)));
                        end = start;
24
                        while (end < sentence.length() &&
25
                             !Character.isWhitespace(sentence.charAt(end++)));
                        String word = sentence.substring(start, end).trim();
26
                        if (isPalindrome(word)) {
                                foundPalindrome = true;
28
20
                                System.out.println(getAlphabets(word));
30
                        start = end - 1;
                 return foundPalindrome;
          }
34
          /* Check the sentence as a whole */
36
          public static boolean checkSentence (String sentence) {
                 if (isPalindrome(sentence)) {
                        System.out.println("The sentence '" + sentence + "' is a
39
                            palindrome.");
                        return true;
40
                 }
41
                 return false;
42
```

```
}
43
44
          /* Check whether a piece of text is identical forward as well as backwards */
45
          public static boolean isPalindrome (String text) {
46
                 String rawText = getAlphabets(text).toUpperCase();
                 for (int i = 0, j = rawText.length() - 1; i < j; i++, j--) {
48
                         if (rawText.charAt(i) != rawText.charAt(j)) {
49
                                return false;
50
                        }
                 }
52
                 /* Make sure that the text is not just one letter */
                 return (rawText.length() > 1);
          }
56
          /* Strip a piece of text of all characters except alphabetic ones */
          public static String getAlphabets (String text) {
                 String rawText = "";
59
                 for (int i = 0; i < text.length(); i++) {</pre>
60
                        if (Character.isAlphabetic(text.charAt(i))) {
61
                                rawText += text.charAt(i);
63
64
                  }
                 return rawText;
65
          }
67
```

Palindrome::main(String[])			
String	sentence	Stores the text to check for palindromes	
boolean	foundPalindrome	Stores whether palindromes have been found	
	Palindrome::checkWords(String)		
String	sentence	Stores the sentence to divide into words	
boolean	foundPalindrome	Stores whether palindromes have been found	
int	start	Counter variable, stores the index of the start of a	
		word	
int	end	Counter variable, stores the index of the end of a	
		word	
String	word	Stores words in sentence, extracted between start	
		and end	
	Palindrome::checkSentence(String)		
String	sentence	Stores the sentence to divide into words	
	Palindrome::isPalindrome(String)		
String	text	Stores the text to check	
String	rawText	Stores only alphabets from text	
int	i	Counter variable, stores the current index in text	
Palindrome::getAlphabets(String)			
String	text	Stores the text to extract alphabets from	
String	rawText	Stores only alphabets from text	
int	i	Counter variable, stores the current index in text	

"In programming the hard part isn't solving problems, but deciding what problems to solve."

— Paul Graham

**Problem 5** A *prime number* (or a *prime*) is a natural number greater than 1 that has no positive divisors other than 1 and itself.

Display all primes up to a given limit, along with their number.

**Solution** This problem can be tackled in a multitude of ways. [citation needed] We could define a function for checking the primality of a given number, then iterate through all numbers in the required range. A common way of checking for primality is *trial division*. It consists of testing whether the number n is a multiple of any integer between 2 and  $\sqrt{n}$ . Although this works well enough for small numbers, repeating this consecutively for very large inputs is tedious and inefficient. Since the problem consists of identifying primes in a range, and not individually, we can make use of more efficient methods.

The Sieve of Eratosthenes is a simple, ancient algorithm for finding all prime numbers up to any given limit. It does so by iteratively marking as composite the multiples of each prime, starting with the first prime number, 2. As a result, when a prime p is found, none of its multiples will be tested further for primality — they are eliminated early on. In comparison,  $trial\ division$  has worse theoretical complexity than that of the Sieve of Eratosthenes in generating ranges of primes. When testing each prime, the optimal trial division algorithm uses all prime numbers not exceeding its square root, whereas the Sieve of Eratosthenes produces each composite only from its prime factors.

### main (upperLimit:Integer)

- 1. Create a new SieveOfEratosthenes, pass it upperLimit and assign it to sieve.
- 2. Call sieve->sievePrimes().
- 3. Display the indices which correspond to true in the boolean array sieve->primes.
- 4. Exit

### SieveOfEratosthenes (upperLimit:Integer)

- Initialize a boolean array primes, indexed with integers from [0] to [upperLimit 1], with all elements set to true.
- 2. Set primes [0] and primes [1] to true.
- 3. **Define** the function SieveOfEratosthenes::sievePrimes() and return the resultant object.

### SieveOfEratosthenes::sievePrimes ()

- 1. Initialize an integer variable prime to 2.
- 2. If prime is less than the square root of upperLimit, proceed. Otherwise, return.
  - (a) Initialize an integer variable multiple to the square of prime.
  - (b) If multiple is less than upperLimit, proceed. Otherwise, jump to (2c).
    - i. Set primes [multiple] to false.
    - ii. Increment multiple by prime.
    - iii. Jump to (2b)
  - (c) Increment prime until primes [prime] is true.
  - (d) Jump to (2).
- 3. Return

```
public class SieveOfEratosthenes {
          private final int upperLimit;
          private boolean[] primes;
          /* Initialize the list of numbers using an uper limit */
          public SieveOfEratosthenes (int upperLimit) {
                 this.upperLimit = upperLimit;
                 this.initPrimes();
          }
          public boolean[] getPrimes () {
11
                 return primes;
12
          }
          /* Initialize all value to 'prime' by default */
          public void initPrimes () {
                 this.primes = new boolean[upperLimit];
                 /* Mark known values as 'not prime' */
18
                 primes[0] = false;
19
                 primes[1] = false;
20
                 for (int i = 2; i < upperLimit; i++)</pre>
                        primes[i] = true;
          }
24
          /* Iteratively sieve the numbers to leave primes behind */
          public void sievePrimes () {
27
                 /* Start with the first prime */
                 int prime = 2;
28
```

```
while ((prime * prime) < upperLimit) {</pre>
                         /* Start with the first multiple not crossed off */
30
                         int multiple = prime * prime;
31
                        while (multiple < upperLimit) {</pre>
32
                                /* Cross multiples of a prime off the list */
                                primes[multiple] = false;
34
                                multiple += prime;
36
                         /* Skip forward to the next prime */
                        while (!primes[++prime]);
38
                 }
          }
40
   }
   public class Primes {
          public static void main (String[] args) {
                 try {
                         /* Parse the first command line argument as the upper limit
                           on primes to calculate */
                         int upperLimit = Integer.parseInt(args[0]);
                         if (upperLimit < 2) {</pre>
                                throw new NumberFormatException();
                         SieveOfEratosthenes sieve = new
                             SieveOfEratosthenes(upperLimit);
                         sieve.sievePrimes();
11
                         showPrimes(sieve.getPrimes());
                 } catch (NumberFormatException | IndexOutOfBoundsException e) {
                         /* Handle missing or incorrectly formatted arguments */
14
                         System.out.println("Enter 1 argument (limit[integer, >1])!");
                         System.out.println("(Primes will be dislayed up to, not
                             including 'limit')");
                  }
17
18
          /* Display all primes calculated */
20
          public static void showPrimes (boolean[] primes) {
21
                  int primeCount = 0;
                  /* Format all number to the same width */
                  int maxLength = Integer.toString(primes.length).length();
24
                 for (int i = 0; i < primes.length; i++) {</pre>
                         /* If 'i' is prime, primes[i] will be marked 'true' */
26
                         if (primes[i]) {
                                System.out.printf("%" + maxLength + "d ", i);
28
                                primeCount++;
```

SieveOfEratosthenes			
int	upperLimit	The number of integers to sieve	
boolean[]	primes	Primes, with contents indicating the primality of the	
		index	
	SieveOfEratosthenes::initPrimes()		
int	i	Counter variable	
	SieveOfEratosthenes::sievePrimes()		
int	prime	Counter variable, stores current primes found	
int	multiple	Counter variable, stores the multiples of prime	
Primes::main(String[])			
int	upperLimit	The highest integer to check for primality (exclusive)	
SieveOf	sieve	An object capable of sieving primes	
Eratosthenes			
	Primes::showPrimes(boolean[])		
boolean[]	primes	Primes, with contents indicating the primality of the	
		index	
int	primeCount	The number of primes found	
int	maxLength	The length of the longest number to display	
int	i	Counter variable, stores the current integer to check	
		for primality	

— Ted Nelson

**Problem 6** Design a simple interface for an examiner which can format and display marks scored by a group of students in a particular examination. Calculate the percentage scored by each candidate and display the list of students and percentages in an ASCII bar chart, arranged alphabetically.

**Solution** This problem calls for a fairly straightforward flow of logic. The main goal is to present the user with a simple way of providing input, along with nicely formatted output.

# main (upperLimit:Integer)

- 1. Input the maximum marks allotted for the examination as a floating point. Store it as maxMarks.
- 2. Input the total number of students whose marks are to be recorded as an integer. Store it as numberOfStudents.
- 3. Create a new Marksheet, pass it maxMarks, numberOfStudents and assign it to sheet.
- 4. Initialize an integer counter i to 0;
- 5. If i is less than numberOfStudents, proceed. Otherwise, jump to (6).
  - (a) Input a student's name as a string. Store it as name.
  - (b) Input the student's marks as a floating point. Store it as marks.
  - (c) Call sheet->addMarks(name, marks).
  - (d) Jump to (5).
- 6. Call sheet->sortByName().
- 7. Call sheet->displayChart().
- 8. Call sheet->sortMaxScorers().
- 9. Exit

# Marksheet (maxMarks:FloatingPoint, numberOfStudents:Integer)

- 1. Initialize a string array names, indexed with integers from [0] to [numberOfStudents 1]
- 2. Initialize a floating point array marks, indexed with integers from [0] to [numberOfStudents 1].
- 3. Initialize an integer counter lastStudent to -1.
- 4. **Define** the functions:

- (a) Marksheet::addMarks(name, score)
- (b) Marksheet::sortByName()
- (c) Marksheet::displayChart()
- (d) Marksheet::displayMaxScorers()
- 5. **Return** the resultant object.

# Marksheet::addMarks (name:String, score:FloatingPoint)

- 1. Increment lastStudent by 1.
- 2. Set the names [lastStudent] to name.
- 3. Set the marks[lastStudent] to score.
- 4. Return

# Marksheet::sortByName ()

- 1. Assign lastStudent to right.
- 2. If right exceeds 0, proceed. Otherwise, return.
  - (a) Initialize an integer counter i to 1.
  - (b) If i is less than or equal to right, proceed. Otherwise, jump to (2c).
    - i. If names [i-1] comes lexicographically after names [i]:
      - A. Swap the elements at names [i-1] and names [i].
      - B. Swap the elements at marks[i-1] and marks[i].
    - ii. Jump to (2b).
  - (c) Jump to (2).

### Marksheet::displayChart ()

- 1. For every string name in names:
  - (a) Calculate the length of the bar in the chart as a fraction of the screen width. Store the calculated number of characters to display as points.
  - (b) Display name, a string of suitable characters for the bar of length points, along with the percentage scored.
- 2. Return

### Marksheet::displayMaxScorers ()

- 1. Calculate the maximum floating point in marks and store it as maxScore.
- 2. For every integer i between 0 and numberOfStudents (inclusive, exclusive) such that marks[i] is equal to the maxScore, display names[i].
- 3. Return

```
public class Marksheet {
          public static final int SCREEN_WIDTH = 100;
          private final double maxMarks;
          private final int numberOfStudents;
          private int lastStudent;
          private String[] names;
          private double[] marks;
          /* Initialize some final data */
          public Marksheet (double maxMarks, int numberOfStudents) {
                 this.maxMarks = maxMarks;
11
                 this.numberOfStudents = numberOfStudents;
12
                 this.names = new String[numberOfStudents];
                 this.marks = new double[numberOfStudents];
                 this.lastStudent = -1;
          }
          /* Add names and marks to the stack */
18
          public boolean addMarks (String name, double score) {
                 try {
20
                        names[++lastStudent] = name;
                        marks[lastStudent] = score;
                        return true;
                 } catch (IndexOutOfBoundsException e) {
24
                        return false;
                 }
26
          }
27
          /* Display the names and percentages in a bar chart */
29
30
          public void displayChart () {
                 System.out.println(Marksheet.multiplyString("-",
31
                     Marksheet.SCREEN_WIDTH));
                 for (int i = 0; i <= lastStudent; i++) {</pre>
                        /* Calculate the fraction of marks earned */
33
                        double fraction = marks[i] / maxMarks;
34
                        String name = (names[i].length() < 16)</pre>
                                       ? names[i]
36
                                       : (names[i].substring(0,13) + "...");
                        int points = (int) (fraction * (SCREEN_WIDTH - 34));
                        /* Generate and pad the bar to display */
                        String bar = multiplyString("*", points)
40
                                + multiplyString(" ", SCREEN_WIDTH - 34 - points);
41
                        System.out.printf("| %16s | %s | %6.2f %% |%n"
42
                                                     , name
43
```

```
, bar
44
                                                      , fraction * 100);
45
46
                 System.out.println(Marksheet.multiplyString("-",
47
                     Marksheet.SCREEN_WIDTH));
48
49
          /* Display the name of students with the highest score */
          public void displayMaxScorers () {
                 String maxScorers = "";
                 double maxScore = getMaxScore();
                 for (int i = 0; i <= lastStudent; i++) {</pre>
                         if (marks[i] == maxScore) {
                                maxScorers += ", " + names[i];
56
                         }
                 }
                 System.out.println(maxScorers.substring(1)
                                       + " scored the highest ("
60
                                       + maxScore + "/"
61
                                       + maxMarks + ")");
          }
          /* Sort the names and associated marks lexicographically */
          public void sortByName () {
                 for (int right = lastStudent; right > 0; right--)
                         for (int i = 1; i <= right; i++)</pre>
                                if (names[i-1].compareToIgnoreCase(names[i]) > 0)
                                       swapRecords(i, i - 1);
          }
          /* Get the value of the highest score */
          public double getMaxScore () {
75
76
                 double max = Integer.MIN_VALUE;
                 for (int i = 0; i <= lastStudent; i++) {</pre>
                         max = Math.max(max, marks[i]);
                 }
                 return max;
80
          }
82
          /* Utility function to swap student records */
          private void swapRecords (int x, int y) {
84
                 String tempName = names[x];
                 double tempMark = marks[x];
86
                 names[x] = names[y];
                 marks[x] = marks[y];
```

```
names[y] = tempName;
                  marks[y] = tempMark;
90
           }
91
92
           /* Utility funtion for repeating strings */
           public static String multiplyString (String s, int n) {
94
                   String out = "";
                   while (n \longrightarrow 0)
96
                          out += s;
                  return out;
98
           }
    }
100
    import java.util.Scanner;
    import java.util.InputMismatchException;
    public class ScoreRecorder {
           public static void main (String[] args) {
 5
                   /* Create an object capable of maning input */
                   Scanner inp = new Scanner(System.in);
                  double maxMarks = 0.0;
                  int numberOfStudents = 0;
                  try {
                          System.out.print("Enter the maximum marks allotted for each
                              student : ");
                          maxMarks = inp.nextDouble();
12
                          System.out.print("Enter the total number of students : ");
13
                          numberOfStudents = inp.nextInt();
                          /* Check for any erraneous data */
                          if (maxMarks <= 0) {</pre>
                                 System.out.println("Maximum marks must be positive!");
                                 System.exit(0);
19
                          if (numberOfStudents <= 0) {</pre>
20
                                 System.out.println("Number of students must be
21
                                     positive!");
                                 System.exit(0);
22
                          }
23
                          /* Create an object capable of recording scoresheets */
24
                          Marksheet sheet = new Marksheet(maxMarks, numberOfStudents);
25
                          System.out.println("Enter " + numberOfStudents + " students'
26
                              names and marks : ");
                          /* Accept student data */
                          for (int i = 0; i < numberOfStudents; i++) {</pre>
28
                                 String name = "";
29
```

```
while (!inp.hasNextDouble()) {
30
                                       name += inp.next() + " ";
31
                                }
32
                                double marks = inp.nextDouble();
33
                                if (marks <= 0 || marks > maxMarks) {
                                       System.out.println("Marks must be within 0.0 and
35
                                           " + maxMarks + "!");
                                       System.exit(0);
36
                                }
                                sheet.addMarks(name.trim(), marks);
38
                         }
                         /* Sort and display */
40
                         sheet.sortByName();
41
                         sheet.displayChart();
42
                         sheet.displayMaxScorers();
43
                 } catch (InputMismatchException e) {
                         /st Handle missing or incorrectly formatted arguments st/
45
                         System.out.println("Invalid Input!");
46
                         System.exit(0);
47
                 }
48
          }
49
   }
50
```

Marksheet		
int	SCREEN_WIDTH	Number of characters to use in the display width
double	maxMarks	The maximum marks allotted for the examination
int	numberOf	The number of students whose marks are to be
	Students	recorded
int	lastStudent	The index number of the last student added to the
		marksheet
String[]	names	The names of the students
double[]	marks	The marks of the students
	Marksheet:	:addMarks(String, double)
String	name	The name of the student to be added
double	score	The marks of the student to be added
Marksheet::displayChart()		
int	i	Counter variable
double	fraction	The fraction on marks scored over the maximum
		marks

String	name	Temporarily stores a formatted version of a student's		
		name		
int	points	The number of characters to display in the bar chart		
String	bar	The bar in the chart, along with whitespace padding		
	Marksh	eet::displayMaxScorers()		
String	maxScorers	The list of highest scoring students		
double	maxScore	The highest score		
int	i	Counter variable		
	Marksheet::sortByName()			
int	right	Counter variable		
int	i	Counter variable		
	Marksheet::getMaxScore()			
double	max	The maximum score in marks		
int	i	Counter variable		
	Markshe	et::swapRecords(int, int)		
int	x, y	The indices of the records to swap		
String	tempName	Temporary storage of a name		
double	tempMark	Temporary storage of a mark		
	Marksheet::multiplyString(String, int)			
String	S	The string to multiply		
int	n	The number of times to multiply s		
String	out	The string containing n copies of s		
	Scorel	Recorder::main(String[])		
Scanner	inp	The input managing object		
double	maxMarks	The maximum marks allotted for the examination		
int	numberOf	The number of students whose marks are to be		
	Students	recorded		
Marksheet	sheet	An object capable of managing student records		
int	i	Counter variable		
String	name	The name of the student to be added		
double	marks	The marks of the student to be added		

— L. Peter Deutsch

**Problem 7** The determinant of a square matrix  $A_{n,n}$  is defined recursively as follows.

$$det(A_{n,n}) = \begin{vmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & \cdots & a_{n,n} \end{vmatrix} = \sum_{j=1}^{n} (-1)^{i+j} a_{i,j} \cdot det(M_{i,j})$$

where  $M_{i,j}$  is defined as the minor of  $A_{n,n}$ , an  $(n-1) \times (n-1)$  matrix formed by removing the *i*th row and *j*th column from  $A_{n,n}$ .

The determinant of a  $(2 \times 2)$  matrix is simply given by

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

For example, the determinant of a  $(3\times3)$  matrix is given by the following expression.

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$
$$= aei + bfg + cdh - ceg - bdi - afh$$

Calculate the determinant of an inputted  $(n \times n)$  square matrix.

**Solution** This problem offers the opportunity to showcase the power of recursive functions. Here, the complex task of calculating the determinant of a large matrix can be subdivided into multiple smaller tasks. In fact, each of these tasks is precisely the same as the larger one — the only difference is the size of the matrices. Eventually, the problem reduces to finding the determinants of multiple  $(2 \times 2)$  matrices. The values thus obtained can be pieced together to form the final answer.

main ()

- 1. Input the size (number of rows/columns) of the square matrix. Store it as size.
- 2. Create a new SquareMatrix, pass it size, and assign it to matrix.
- 3. For each  $i \in \{1, 2, ..., size\}$ :

- (a) For each  $j \in \{1, 2, \dots, size\}$ :
  - i. Input an integer as n.
  - ii. Set the element at [i, j] of matrix to n.
- 4. Call matrix->getDeterminant() and display the returned value.
- 5. Exit

# Matrix (rows:Integer, columns:Integer)

- Initialize an integer array of integer arrays elements, indexed with integers from [1] to [rows], with each contained integer array indexed with integers from [1] to [columns].
- 2. **Return** the resultant object.

# SquareMatrix (size:Integer)

- 1. **Define** the functions:
  - (a) SquareMatrix::getDeterminant()
  - (b) SquareMatrix::getMinorMatrix(row, column)
- 2. Return a Matrix, with both rows and columns set to size.

# SquareMatrix::getDeterminant ()

- 1. If the size is 1, return the only element (elements[1, 1]).
- 2. If the size is 2, return (elements[1, 1] × elements[2, 2]) (elements[1, 2] × elements[2, 1]).
- 3. Initialize an integer variable determinant to 0.
- 4. For each  $i \in \{1, 2, ..., size\}$ :
  - (a) Call this->getMinorMatrix(i, i)->getDeterminant(). Store the result in d.
  - (b) Add  $((-1)^{i+1} \times matrix[1, i] \times d)$  to determinant.
- 5. Return determinant.

### SquareMatrix::getMinorMatrix (row:Integer, column:Integer)

- 1. Create a new SquareMatrix, pass it (size 1), and assign it to minor.
- 2. Copy all elements from this to minor, except for those at position [row, \*] or [\*, column].
- 3. Return minor.

```
public class Matrix {
          protected final int rows;
          protected final int columns;
          protected int[][] elements;
          /* Initialize a matrix of a given order */
          public Matrix (int rows, int columns) {
                 this.rows = rows;
                 this.columns = columns;
                 this.elements = new int[rows][columns];
          }
11
12
          public int getRows () {
                 return this.rows;
          public int getColumns () {
                 return this.columns;
18
          }
20
          /* Set elements in the matrix using natural indices */
          public void setElementAt (int element, int row, int column) {
                 if (row < 1 || row > rows || column < 1 || column > columns)
                        return;
                 elements[row-1][column-1] = element;
          }
26
27
          /* Get elements from the matrix using natural indices */
          public int getElementAt (int row, int column) {
29
                 if (row < 1 || row > rows || column < 1 || column > columns)
30
                        return Integer.MIN_VALUE;
31
                 return elements[row-1][column-1];
          }
33
   }
34
   public class SquareMatrix extends Matrix {
          protected int size;
          /* Initialize the matrix with the same number of rows and columns */
          public SquareMatrix (int size) {
                 super(size, size);
                 this.size = size;
          }
```

```
public int getSize () {
                 return this.size;
11
13
          /* Recursively calculate the determinant of the matrix */
          public int getDeterminant () {
                  /* Base cases */
                 if (this.size == 1)
                         return getElementAt(1, 1);
                  if (this.size == 2)
19
                         return (getElementAt(1, 1) * getElementAt(2, 2))
                                - (getElementAt(1, 2) * getElementAt(2, 1));
21
                  int determinant = 0;
                  /* Accumulate the determinants of minors with alternating signs */
23
                 for (int i = 1; i <= size; i++)
                         determinant += ((int) Math.pow(-1, 1+i))
                                       * getElementAt(1, i)
26
                                       * getMinorMatrix(1, i).getDeterminant();
27
                 return determinant;
28
          }
          /* Get the minor matrix by removing a row and a column */
          public SquareMatrix getMinorMatrix (int row, int column) {
32
                  /* Check bounds */
                  if (row < 1 || row > size || column < 1 || column > size)
34
                         return null;
                  if (this.size <= 1)</pre>
36
                         return new SquareMatrix(0);
                  SquareMatrix minor = new SquareMatrix(this.size - 1);
38
                  for (int i = 1, p = 1; p < size; i++, p++) {
                         /* Skip 'row' */
40
                         if (i == row)
41
                                i++;
42
43
                         for (int j = 1, q = 1; q < size; j++, q++) {
                                /* Skip 'column' */
44
                                if (j == column)
45
46
                                       j++;
                                /* Copy values into the new matrix */
47
                                minor.setElementAt(this.getElementAt(i, j), p, q);
                         }
49
                  }
                 return minor;
51
          }
52
   }
53
```

```
import java.util.Scanner;
   public class Determinant {
          public static void main (String[] args) {
                  /* Create an object for managing input */
                  Scanner inp = new Scanner(System.in);
6
                  try {
                         System.out.print("Enter the size of the (size X size) square
                             matrix : ");
                         int size = inp.nextInt();
9
                         /* Create a sqare matrix which has suitable methods for
                             calculation */
                         SquareMatrix matrix = new SquareMatrix(size);
                         System.out.println("Enter " + (size * size) + " integers : ");
12
                         for (int i = 1; i <= size; i++)</pre>
13
                                for (int j = 1; j <= size; j++)</pre>
                                       matrix.setElementAt(inp.nextInt(), i, j);
                         System.out.println("\nThe determinant is : " +
16
                             matrix.getDeterminant());
                  } catch (Exception e) {
17
                         /* Handle missing or incorrectly formatted arguments */
18
19
                         System.out.println("Invalid Input!");
                  }
20
          }
          /* Display the matrix in a neat format */
23
          public static void showMatrix (Matrix m) {
24
                  for (int i = 1; i <= m.getRows(); i++) {</pre>
                         for (int j = 1; j <= m.getColumns(); j++) {</pre>
26
                                System.out.printf("%4d ", m.getElementAt(i, j));
2.8
29
                         System.out.println();
                  }
30
          }
31
32 }
```

Matrix			
int	rows	Number of rows in the matrix	
int	columns	Number of columns in the matrix	
int[][]	elements	The array of integer arrays, storing the elements of	
		the matrix	
		SquareMatrix	
int	size	Number of both rows and columns in the matrix	
SquareMatrix::getDeterminant()			
int	determinant	The determinant of the SquareMatrix	
int	i	Counter variable	
SquareMatrix::getMinorMatrix(int, int)			
int	row	The row to remove from the matrix	
int	column	The column to remove from the matrix	
SquareMatrix	minor	The matrix obtained by removing row and column	
int	i, j	Counter variables	
Determinant::main(String[])			
Scanner	inp	The input managing object	
int	size	Number of both rows and columns in the matrix	
SquareMatrix	matrix	The matrix whose determinant is to be calculated	
int	i, j	Counter variables	
Determinant::showMatrix(Matrix)			
Matrix	m	The matrix to display	
int	i, j	Counter variables	

"My project is 90% done. I hope the second half goes as well."

— Scott W. Ambler

**Problem 8** A *Knight's Tour* is a sequence of moves of a knight on a chessboard such that the *knight* visits every square only once. If the knight ends on a square that is one knight's move from the beginning square, the tour is *closed* forming a closed loop, otherwise it is *open*.

There are many ways of constructing such paths on an empty board. On an  $8 \times 8$  board, there are no less than 26,534,728,821,064 directed closed tours. Below is one of them.



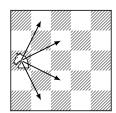
Construct a *Knight's Tour* (open or closed) on an  $n \times n$  board, starting from a given square.

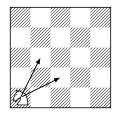
(Mark each square with the move number on which the knight landed on it. Mark the starting square 1.)

 $<sup>^6</sup>$ Two tours along the same path that travel in opposite directions are counted separately, as are rotations and reflections.

**Solution** A knight on a chessboard can move to a square that is two squares away horizontally and one square vertically, or two squares vertically and one square horizontally.







The mobility of a knight can make varies greatly with its position on the board — near the centre, it can jump to one of 8 squares while when in a corner, it can jump to only 2. On the other hand, the number of possible sequences of squares a knight can traverse grows extremely quickly. Although it may seem that a simple brute force search can quickly find one of trillions of solutions, there are approximately  $4 \times 10^{51}$  different paths to consider on an  $8 \times 8$  board. For even larger boards, iterating through every possible path is clearly impractical. [citation needed]

This problem calls for implementing a  $backtracking^7$  algorithm, coupled with some  $heuristic^8$  to speed up the search. One such heuristic is Warnsdorf's Rule.

position The knight is moved so that it always proceeds to the square from which the knight will have the *fewest* onward moves.

This allows us to define a ranking algorithm for each possible path — the positions which result in the smallest number of further moves, or is furthest away from the board's centre will be investigated first. In case of a tie, we can either proceed without making any changes to the already existing positions, or introduce a random element. This has the effect of producing different results on successive executions, giving a variety of solutions.

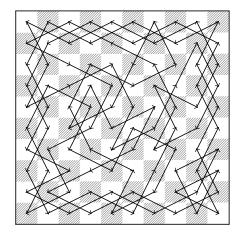
One drawback of resolving ties randomly is that an early "wrong" choice in the position tree can force the calculation of every resulting path without reaching a solution, effectively reducing the algorithm to a brute force search. This is especially problematic

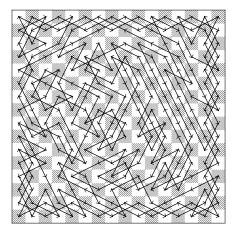
<sup>&</sup>lt;sup>7</sup>Backtracking is a general algorithm for finding some or all solutions to some computational problems that incrementally builds candidates to the solutions, and abandons each partial candidate ("backtracks") as soon as it determines that the candidate cannot possibly be completed to a valid solution.

<sup>&</sup>lt;sup>8</sup>A heuristic technique is any approach to problem solving that employs a practical method not guaranteed to be optimal or perfect, but sufficient for the immediate goals. Where finding an optimal solution is impossible or impractical, heuristic methods can be used to speed up the process of finding a satisfactory solution.

for large boards, where it may take hours to backtrack and reach a solution. Thus, the "randomness factor" should be adjusted according to the board size.

A high randomness can be useful for searching specifically for *closed tours*, as a randomness of 0 simply produces the same solution every time (which may or may not be closed). Below are some tours generated by the program.





The tendency of the path to remain close to the edges of the board, where the mobility of the knight is restricted, is clearly evident.

main (boardSize:Integer, initSquare:Position, randomness:FloatingPoint)

- 1. Create a new TourSolver, pass it boardSize, initSquare, randomness, and assign it to t.
- 2. Call t->getSolution(). Store the returned move stack as solution.
- 3. Display the board obtained by calling t->getBoard() along with the moves in solution.
- 4. Exit

TourSolver (size:Integer, initSquare:Position, randomness:FloatingPoint)

- 1. Initialize an integer arrays of integer arrays indexed with integers from [1] to [size], simulating a chessboard. Store it as board, which records the move numbers on which the knight lands on it.
- 2. Initialize a Position stack path, along with methods to add and remove Position's from it.
- 3. Set an integer counter numberOfMoves to 0, as part of the path stack.
- 4. **Define** the functions:
  - (a) TourSolver::solve(p)

- (b) TourSolver::getPossibleMoves(p)
- 5. **Return** the resultant object.

### TourSolver::solve (p:Position)

- 1. If the path stack is full, return true, indicating that the tour has been solved.
- 2. Call this->getPossibleMoves(p). Store the returned list of possible legal moves as moves.
- 3. Sort moves, ranking each possible position according to Warnsdorf's Rule.
- 4. For every move in the list moves:
  - (a) Push move onto the path stack and board.
  - (b) If the call this->solve(move) returns true, return true. Otherwise, pop move from the path stack and board (backtrack).
- 5. If the list moves has been exhausted, **return false**, indicating that there are no solutions from the position p for that particular move stack.

# TourSolver::getPossibleMoves (p:Position)

- 1. Initialize a list of moves possible Moves.
- 2. For every possible square move a knight can jump to from p (on an empty board):
  - (a) If move is currently a legal move, without falling outside the board or on a previously traversed square, add it to possibleMoves.
- 3. Return possibleMoves

## Source Code

```
public class TourSolver {
          private final int size;
          private Position[] path;
          private int numberOfMoves;
          private int[][] board;
          private int[][] degreesOfFreedom;
          private Position initPosition;
          private double tieBreakRandomness;
          /* Store the list of possible changes in the 'x' and 'y' coordinates of
             a knight on an empty board */
11
          private static final int[][] KNIGHT_MOVES = {
12
                 \{-1, -2\}, \{-1, 2\}, \{1, -2\}, \{1, 2\},
                 \{-2, -1\}, \{-2, 1\}, \{2, -1\}, \{2, 1\}
          };
          /* Initialize the board and move stack */
          public TourSolver (int size, Position initPosition, double randomness) {
18
                 this.size = size;
                 this.initPosition = initPosition;
20
                  this.tieBreakRandomness = randomness / 2.0;
                 this.path = new Position[size * size];
                 this.numberOfMoves = 0;
                 this.initBoard();
                 this.initDegreesOfFreedom();
          }
26
27
          /* Reset the board */
          public void resetSolution () {
29
30
                 this.path = new Position[size * size];
                 this.numberOfMoves = 0;
31
                 this.initBoard();
          }
          /* Initialize a blank board */
35
          private void initBoard () {
                 board = new int[size][size];
37
                 for (int i = 0; i < size; i++)</pre>
                         for (int j = 0; j < size; j++)
                                board[i][j] = 0;
          }
41
42
          /* Calculate the mobility of a knight on each square */
43
          private void initDegreesOfFreedom () {
44
```

```
degreesOfFreedom = new int[size][size];
45
                 for (int i = 0; i < size; i++)</pre>
46
                         for (int j = 0; j < size; j++)
47
                                degreesOfFreedom[i][j] = getPossibleMovesCount(new
48
                                    Position(i, j));
          }
49
          /* Push a move onto the move stack, add it to the board */
          public boolean addMove (Position p) {
                  if (numberOfMoves < (size * size)) {</pre>
53
                         path[numberOfMoves++] = p;
                         board[p.getX()][p.getY()] = numberOfMoves;
                         return true;
                 }
                 return false;
          }
          /* Pop a move from the move stack, remove it from the board */
61
          public boolean removeMove () {
                  if (numberOfMoves > 0) {
                         Position p = path[numberOfMoves - 1];
64
                         /* Empty squares are marked '0' */
                         board[p.getX()][p.getY()] = 0;
66
                         path[--numberOfMoves] = null;
                         return true;
                 }
                 return false;
70
          }
72
          public int[][] getBoard () {
                 return board;
76
          /* Get the stack of moves comprising a knight's tour */
          public Position[] getSolution () {
                  if (size < 5)
                         return null;
80
                  addMove(initPosition);
81
                  if(solve(initPosition))
                         return path;
83
                 return null;
          }
85
          /* Recursively solve a tour from a given position */
87
          public boolean solve (Position p) {
                 /* If the move stack is full, the tour has been solved */
89
```

```
if (numberOfMoves == (size * size))
90
                          return true;
91
                   /* Get every legal move and rank them using Warnsdorf's Rule */
92
                  Position[] possibleMoves = getPossibleMoves(p);
93
                   if (possibleMoves[0] == null)
                          return false;
95
                   sortMoves(possibleMoves);
                  for (Position move : possibleMoves) {
97
                          if (move != null) {
                                 /* Try a move */
99
100
                                 addMove(move);
                                 if (solve(move))
                                        return true;
                                 /* Backtrack */
103
                                 removeMove();
104
                          }
                   }
106
                  return false;
107
           }
108
           /* Sort a list of positions using Warnsdorf's Rule */
           public void sortMoves (Position[] moves) {
111
                  int count = 0;
                  for (Position p : moves)
113
                          if (p != null)
114
                                 count++;
115
                  for (int right = count; right > 0; right--)
116
                          for (int i = 1; i < right; i++)</pre>
                                 if (compareMoves(moves[i-1], moves[i]) > 0)
118
                                        swapMoves(i-1, i, moves);
119
           }
120
121
           /* Compare 2 moves using Warnsdorf's Rule */
           public int compareMoves (Position a, Position b) {
123
                   /* Compare the mobilities of the knight */
                   int aCount = getPossibleMovesCount(a);
                  int bCount = getPossibleMovesCount(b);
126
                  if (aCount != bCount)
127
                          return aCount - bCount;
                   /* Compare the mobilities of the knight on an empty board */
129
                  int aFree = degreesOfFreedom[a.getX()][a.getY()];
130
                  int bFree = degreesOfFreedom[b.getX()][b.getY()];
131
                   if (aFree != bFree)
                          return aFree - bFree;
133
                   /* Resolve ties using a predecided element of randomness */
134
                  return (Math.random() < tieBreakRandomness)? 1 : -1;</pre>
```

```
}
136
           /* Utility function to swap moves in the list of possible moves */
138
           private static void swapMoves (int x, int y, Position[] moves) {
139
                  Position t = moves[x];
                  moves[x] = moves[y];
141
                  moves[y] = t;
142
           }
143
           /* Get the list of all possible, legal moves not touching a previously
145
              travelled square from a given position */
           public Position[] getPossibleMoves (Position start) {
147
                  Position[] possibleMoves = new Position[KNIGHT_MOVES.length];
148
                  int i = 0;
149
                  for (int[] move : KNIGHT MOVES) {
150
                          /* Generate a new */
                          int x = start.getX() + move[0];
                          int y = start.getY() + move[1];
153
                          /* Check the legality of that move */
154
                          if (isWithinBoard(x, y) && board[x][y] == 0) {
                                 possibleMoves[i++] = new Position(x, y);
156
157
                  }
158
                  return possibleMoves;
161
           /* Get the number of legal moves */
162
           public int getPossibleMovesCount (Position start) {
                  int i = 0;
164
                  for (Position p : getPossibleMoves(start))
165
                          if (p != null)
                                 i++;
167
                  return i;
168
           }
169
170
           /* Check whether a position lies within the board */
171
           public boolean isWithinBoard (int x, int y) {
172
                  return (x >= 0 && x < size && y >= 0 && y < size);
173
           }
174
175
    }
```

```
public class Position {
          private final int x;
          private final int y;
          /* Initialize using the coordinates on the board */
          public Position (int x, int y) {
                 this.x = x;
                  this.y = y;
          }
          /* Initialize using the position in algebraic notation */
          public Position (String s) {
12
                  int x = 0;
                 int i = 0;
14
                 while (i < s.length() && Character.isAlphabetic(s.charAt(i))) {</pre>
15
                         x = (x * 26) + Character.toLowerCase(s.charAt(i)) - 'a' + 1;
                         i++;
                  }
18
                 int y = Integer.parseInt(s.substring(i));
19
                 this.x = x - 1;
20
                 this.y = y - 1;
21
22
23
          public int getX () {
                 return x;
25
26
27
          public int getY () {
                 return y;
29
31
          public boolean equals (Position p) {
                 return (p != null)
33
                         && (this.getX() == p.getX()) && (this.getY() == p.getY());
34
          }
35
36
          @Override
37
          public String toString () {
38
                  return xToString(this.x) + (this.y + 1);
40
41
          /* Convert a file number to its algebraic notation form */
42
          public static String xToString (int n) {
                  int x = n + 1;
44
                 String letters = "";
45
                 while (x > 0) {
46
```

```
letters = (char) ('a' + (--x \% 26)) + letters;
47
                        x /= 26;
48
                 }
49
                 return letters;
50
          }
51
52
   }
   public class KnightTour {
          public static void main (String[] args) {
                 try {
                        /* Parse the first command line argument as the size of the
                        int boardSize = Integer.parseInt(args[0]);
                        if (boardSize <= 0)</pre>
6
                                throw new NumberFormatException();
                        /* Parse the second command line argument as the starting
                            square
                           of the knight, written in algebraic notation */
                        String initSquare = (args.length > 1)? args[1] : "a1";
                        /* Parse the third command line argument as the degree of
                           randomness to be used while resolving ties */
                        double randomness = (args.length > 2)?
13
                            Double.parseDouble(args[2])
                                                          : Math.pow(0.8, boardSize) * 2;
14
                        /* Create an object capable of solving knight's tours */
                        TourSolver t = new TourSolver(boardSize, new
                            Position(initSquare), randomness);
                        Position[] solution = t.getSolution();
                        if (solution != null) {
18
                                showBoard(t.getBoard());
                                showMoves(solution);
20
                                if (isClosed(solution))
                                       System.out.println("\nThe tour is Closed!");
                        } else {
                                System.out.println("No Knight's Tours found!");
24
                        }
                 } catch (Exception e) {
26
                        /* Handle missing or incorrectly formatted arguments */
27
                        System.out.print("Enter an integer (> 1) as the first
                            argument, ");
                        System.out.println("and a well formed chessboard coordinate as
29
                            the second!");
                        System.out.println("
                                                                        (size,
                            startSquare * , randomness * )");
                        System.out.println();
31
```

```
System.out.println("(size
                                                       -> Solve a Tour on a (size x
                            size) board)");
                        System.out.println("(startSquare * -> A square in algebraic
                            chess notation of the form 'fr',");
                        System.out.println("
                                                          where f = the letter
                            representing the file(column)");
                        System.out.println("
                                                          and r = the number
                            representing the rank(row).)");
                        System.out.println("(startSquare is set to 'a1' by default)");
36
                        System.out.println("(randomness * -> A number between O(no
37
                            randomness) and 1(even chances),");
                        System.out.println("
                                                          determining the randomness in
38
                            ranking positions of");
                        System.out.println("
                                                          the same weightage while
39
                            searching. A randomness of 0 will");
                        System.out.println("
40
                                                          produce the same tour every
                            time, for a specific size and");
                        System.out.println("
                                                          startSquare. Keep extremely
41
                            small values of randomness for");
                        System.out.println("
                                                          very large boards.)");
42
                        System.out.println("(randomness is set to 2 * (0.8)^boardSize
43
                            by default)");
                        System.out.println();
44
                                                                                       <
                        System.out.println("
45
                            * = optional arguments >");
                 }
46
          }
47
          /* Display the board, with each square marked with the move number on which
49
             the knight landed on it */
          public static void showBoard (int[][] board) {
                 String hLine = " " + multiplyString("+----", board.length) + "+";
                 System.out.println(hLine);
53
                 for (int column = board.length - 1; column >= 0; column--) {
54
                        System.out.printf(" %2d ", column + 1);
                        for (int row = 0; row < board.length; row++) {</pre>
                                System.out.printf("| %3d ", board[row][column]);
58
                        System.out.printf("|%n%s%n", hLine);
                 }
                 System.out.print(" ");
                 for (int i = 0; i < board.length; i++) {</pre>
                        System.out.printf(" %2s ", Position.xToString(i));
                 }
64
                 System.out.println();
          }
66
```

```
67
          /* Display the list of moves in the tour in algebraic notation */
68
          public static void showMoves (Position[] moves) {
69
                 System.out.print("\nMoves : ");
70
                 String movesOut = "";
                 for (int i = 1; i < moves.length; i++) {</pre>
                        movesOut += (moves[i-1] + "-" + moves[i] + ", ");
                 System.out.println(movesOut.substring(0, movesOut.length() - 2));
          }
76
          /* Utility function for repeating strings */
          public static String multiplyString (String s, int n) {
                 String result = "";
80
                 while (n --> 0)
81
                        result += s;
                 return result;
83
          }
84
85
          /* Check whether a tour is closed or not */
          public static boolean isClosed (Position[] path) {
87
                 int 1 = path.length - 1;
                 int dX = Math.abs(path[0].getX() - path[1].getX());
89
                 int dY = Math.abs(path[0].getY() - path[1].getY());
                 return (dX == 1 && dY == 2) || (dX == 2 && dY == 1);
91
          }
92
93 }
```

## Variable Description

TourSolver				
int	size	Number of files/ranks in the chessboard		
Position[]	path	Stack of moves which are part of the solved tour		
int	numberOfMoves	Counter variable, number of moves made in the		
		solved tour		
int[][]	board	An integer array of integer arrays, representing a		
		chessboard, with each square marked with the move		
		number at which the knight lands on it		
int[][]	degreesOf	An integer array of integer arrays, representing a		
	Freedom	chessboard, with each square marked with the num-		
		ber of possible knight moves from it (on an empty		
		board)		
Position	initPosition	The position on the board the knight starts from		
double	tieBreak	The degree to which a move in the path is randomly		
	Randomness	decided		
int[][]	KNIGHT_MOVES	List of legal changes in the $x$ and $y$ positions of a		
		knight		
TourSolver::initBoard()				
int	i, j	Counter variables		
TourSolver::initDegreesOfFreedom()				
int	i, j	Counter variables		
	TourSol	ver::addMove(Position)		
Position	p	The new position to add to the path stack		
TourSolver::removeMove()				
Position	p	The position popped from the path stack		
TourSolver::solve()				
Position[]	possible	List of possible moves that can be added to the path		
	Moves	stack		
Position	move	Current move to evaluate in the path		
TourSolver::sortMoves(Position[])				
Position[]	moves	List of moves to rank using Warnsdorf's heuristic		
int	count	Total number of moves in moves		
int	right	Counter variable		
int	i	Counter variable		

	TourSolver::compareMoves(Position, Position)				
Position	a, b	Positions/moves to compare using Warnsdorf's			
		heuristic			
int	aCount,	Respective number of possible legal moves for a and			
	bCount	b			
int	aFree,	Respective number of possible legal moves on an			
	bFree	empty board for a and b			
	TourSolver::swapMoves(int, int, Position[])				
int	x, y	The indices of the moves to swap			
Position[]	moves	Array of moves containing the moves to be swapped			
TourSolver::getPossibleMoves(Position)					
Position	start	Position from where possible moves are to be gener-			
		ated			
int	i	Counter variable			
int[]	move	Pair of legal changes in the $x$ and $y$ positions of a			
		knight			
int	х, у	New $x$ and $y$ positions of the knight			
TourSolver::getPossibleMovesCount(Position)					
Position	start	Position from where possible moves are to be gener-			
		ated			
Position	р	Possible position			
TourSolver::isWithinBoard(int, int)					
int	x, y	The $x$ and $y$ positions on the board to verify			
		Position			
int	x, y	The $x$ and $y$ coordinates on the board encoded by			
		the Position			
	Pos	ition::this(String)			
String	s	Chess position written in algebraic notation			
int	x, y	The $x$ and $y$ coordinates on the board			
int	i	Counter variable			
Position::xToString(int)					
int	n	File $(x \text{ position})$ to convert to algebraic notation			
String	letters	n expressed as a base 26 number, digits starting from			
		(a)			

int	Х	Counter variable, temporarily stores the file to con-			
		vert			
	<pre>KnightTour::main(String[])</pre>				
int	boardSize	Number of files/ranks in the chessboard			
String	initSquare	The position on the board the knight starts from			
		(algebraic notation)			
double	randomness	The degree to which a move in the path is randomly			
		decided			
TourSolver	t	An object capable of generating knight's tours			
Position[]	solution	The solved sequence of moves in the <i>knight's tour</i>			
<pre>KnightTour::showBoard(int[][])</pre>					
int[][]	board	An integer array of integer arrays, representing a			
		chessboard, with each square marked with the move			
		number at which the knight lands on it			
String	hline	Horizontal line drawn to represent board squares			
int	row, column,	Counter variables			
	i				
	KnightTour::showMoves(Position[])				
Position[]	moves	The sequence of moves to display			
int	i	Counter variable			
KnightTour::multiplyString(String, int)					
String	s	The string to multiply			
int	n	The number of times to multiply s			
String	out	The string containing n copies of s			
<pre>KnightTour::isClosed(Position[])</pre>					
Position[]	path	The solved sequence of moves in the <i>knight's tour</i>			
int	1	Index of last move in path			
int	dX, dY	Differences in $x$ and $y$ coordinates of the knight be-			
		tween the first and last moves			

This project was compiled with  $X_{\overline{1}} = X_{\overline{1}}$ .

All files involved in the making of this project can be found at https://github.com/sahasatvik/Computer-Project/tree/master/XI

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