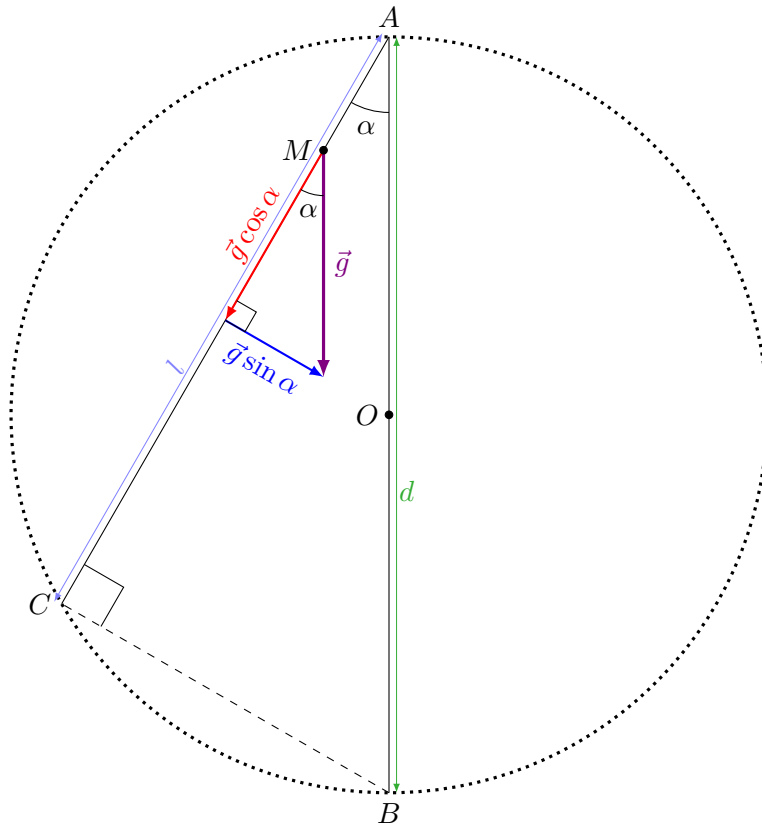


Sliding down Chords of a Circle

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Points A, B, C lie on a circle. A particle at rest at point A falls under the influence of gravity along AC , reaching point C in time t . The line segment AC is inclined from AB , a vertical diameter, by an angle α . The following figure illustrates the given problem.



Note that $\triangle ABC$ is right-angled at C . Therefore, we have :

$$\begin{aligned} l &= d \cos \alpha \\ a_l &= -g \cos \alpha \end{aligned}$$

Where a_l is the net acceleration of the particle along AC . The equations of uniformly accelerated motion along a straight line along AC give :

$$\begin{aligned} -l &= v_0 t + \frac{1}{2} a_l t^2, \\ -d \cos \alpha &= -\frac{1}{2} g \cos \alpha t^2, \end{aligned}$$

$$t = \sqrt{\frac{2d}{g}}$$

Clearly, the time taken to reach C from A along a straight line is independent of the angle α made with the vertical. Thus, time taken for a particle to slide from the highest point of a circle down to any other point on the circumference via a chord is a constant.