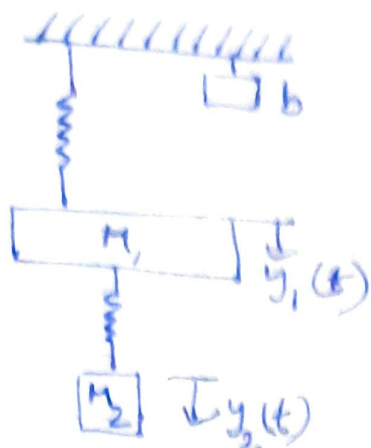


Question 1:



$$F(t) = \begin{bmatrix} F_1(t) \\ F_2(t) \end{bmatrix} = \begin{bmatrix} b \dot{y}_1 \\ -k_1 y_1 \end{bmatrix}$$

↑ k_{12}

F_{M_1}

F_{M_2}

Fig 1

Given, $M_1 = 100$, $k_1 = 50$, $b = 50$ M_2 & $k_2 = ?$

$$F_{M_1} = M_1 \frac{d^2 y_1}{dt^2}$$

$$b \dot{y}_1 = b \frac{dy_1}{dt}$$

$$k_1 y_1 = k_1 y_1$$

$$k_2 = k_{12} (y_1 - y_2)$$

$$F(t) = M_1 \frac{d^2 y_1}{dt^2} + b \frac{dy_1}{dt} + k_1 y_1 + k_{12} (y_1 - y_2)$$

Newton's 2nd Law of Motion on M_1

$$F_{M_2} = M_2 \frac{d^2 y_2}{dt^2}$$

①

$$F_{k_{12}} = k_{12} (y_2 - y_1)$$

Newton's 2nd law of Motion on M_2 ,

$$M_2 \frac{d^2 y_2}{dt^2} + k_{12} (y_2 - y_1) = 0$$

$$M_2 \frac{d^2 y_2}{dt^2} + k_{12} y_2 = k_{12} y_1 \quad \text{--- (2)}$$

$$\begin{bmatrix} M_1 s^2 + b s + k_1 + k_2 & -k_{12} \\ -k_{12} & M_2 s^2 + k_{12} \end{bmatrix} \begin{bmatrix} y_1(s) \\ y_2(s) \end{bmatrix} = \begin{bmatrix} F(s) \\ 0 \end{bmatrix}$$