

SEM in R with *lavaan*

Sabbir Ahmed Hemo

June 19, 2020

Loading libraries

```
library(tidyverse)
library(knitr)
library(lavaan)
library(lavaanPlot)
library(psych)
library(DiagrammeR)
library(DiagrammeRsvg)
library(rsvg)
```

Reading data from CSV

```
df <- read_csv("Reading_Header.csv", na = '999999') # specifying missing values while reading data

df <- df %>%
  mutate(across(.cols = c(starts_with('INT'), starts_with('FAM')), .fns = ~as.character(.x))) # categorizing data

glimpse(df)

## Rows: 537
## Columns: 15
## $ SUBJECT <dbl> 2, 2, 2, 3, 3, 3, 4, 4, 4, 5, 5, 5, 6, 6, 6, 7, 7, 7, 8, 8,...
## $ TEXT <chr> "Netz", "Wind", "Spek", "Netz", "Wind", "Spek", "Netz", "Wi...
## $ OSPAN <dbl> 0.7523810, 0.7523810, 0.7523810, 0.7979497, 0.7979497, 0.79...
## $ SSPAN <dbl> 0.6907937, 0.6907937, 0.6907937, 0.4099440, 0.4099440, 0.40...
## $ COM1 <dbl> 3, 1, 3, 2, 0, 2, 3, 2, 3, 3, 2, 2, 3, 3, 2, 3, 2, 3, 2, 2,...
## $ COM2 <dbl> 3, 1, 2, 2, 0, 2, 2, 1, 2, 3, 1, 1, 3, 3, 3, 3, 2, 2, 1, 0,...
## $ COM3 <dbl> 3, 2, 2, 2, 3, 1, 3, 1, 3, 3, 1, 1, 3, 1, 3, 3, 1, 3, 2, 2,...
## $ INT1 <chr> "3", "1", "1", "2", "1", "2", "2", "2", "2", "2", "3", "1", "1",...
## $ INT2 <chr> "3", "1", "1", "2", "1", "1", "2", "1", "1", "3", "1", "0",...
## $ INT3 <chr> "3", "0", "1", "2", "1", "1", "2", "1", "1", "3", "1", "1",...
## $ FAM1 <chr> "1", "3", "0", "2", "1", "2", "0", "1", "1", "2", "1", "0",...
## $ FAM2 <chr> "2", "2", "0", "3", "0", "1", "1", "2", "2", "3", "1", "1",...
```

```
## $ FAM3    <chr> "1", "2", "0", "2", "1", "1", "1", "1", "1", "3", "1", "1",...
## $ VOL     <dbl> 0.00, 0.25, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00,...
## $ INV     <dbl> 0.2500000, 0.2500000, 0.2500000, 0.6000000, 0.8000000, 0.50...
```

```
summary(df)
```

```
##      SUBJECT          TEXT          OSPAN          SSPAN
##  Min.   : 2.0   Length:537   Min.   :0.02451   Min.   :0.06803
## 1st Qu.: 50.0   Class :character   1st Qu.:0.60915   1st Qu.:0.45971
## Median : 97.0   Mode  :character   Median :0.74893   Median :0.57576
## Mean   :100.6                      Mean   :0.70170   Mean   :0.56546
## 3rd Qu.:144.0                      3rd Qu.:0.84944   3rd Qu.:0.68214
## Max.   :337.0                      Max.   :1.00000   Max.   :1.00000
##                                     NA's   :3
##      COM1          COM2          COM3          INT1
##  Min.   :0.000   Min.   :0.000   Min.   :0.000   Length:537
## 1st Qu.:1.000   1st Qu.:1.000   1st Qu.:1.000   Class :character
## Median :2.000   Median :2.000   Median :2.000   Mode  :character
## Mean   :1.818   Mean   :1.611   Mean   :1.855
## 3rd Qu.:2.000   3rd Qu.:2.000   3rd Qu.:3.000
## Max.   :3.000   Max.   :3.000   Max.   :3.000
##
##      INT2          INT3          FAM1          FAM2
##  Length:537   Length:537   Length:537   Length:537
## Class :character   Class :character   Class :character   Class :character
## Mode  :character   Mode  :character   Mode  :character   Mode  :character
##
##
##
##      FAM3          VOL          INV
##  Length:537   Min.   :0.0000   Min.   :0.000
## Class :character   1st Qu.:0.0000   1st Qu.:0.000
## Mode  :character   Median :0.0000   Median :0.250
##                                     Mean   :0.1316   Mean   :0.265
##                                     3rd Qu.:0.2500   3rd Qu.:0.400
##                                     Max.   :1.0000   Max.   :1.000
##                                     NA's   :9       NA's   :9
```

Code for producing Table-1

Results can be found in Covariances table

```
corr.lv.model <- '
# latent variable definitions

lat_COM =~ COM1 + COM2 + COM3
lat_INT =~ INT1 + INT2 + INT3
lat_FAM =~ FAM1 + FAM2 + FAM3
lat_WMC =~ OSPAN + SSPAN
```

```

# covariances

VOL ~~ INV
lat_INT ~~ lat_WMC
lat_INT ~~ lat_FAM
lat_INT ~~ lat_COM
lat_COM ~~ lat_FAM
lat_COM ~~ lat_WMC
lat_FAM ~~ lat_WMC

'

fit.lv.model <- cfa(model = corr.lv.model, data = df, cluster = 'SUBJECT', ordered = paste0(rep(c("INT"

summary(fit.lv.model, standardized=TRUE) # In covariance table std.lv includes the correlation

## lavaan 0.6-6 ended normally after 86 iterations
##
##      Estimator                      DWLS
##      Optimization method          NLMINB
##      Number of free parameters      50
##
##                               Used      Total
##      Number of observations          525      537
##      Number of clusters [SUBJECT]     178
##
## Model Test User Model:
##                               Standard      Robust
##      Test Statistic                570.553    556.927
##      Degrees of freedom              60         60
##      P-value (Chi-square)            0.000      0.000
##      Scaling correction factor        1.073
##      Shift parameter                 25.050
##      simple second-order correction
##
## Parameter Estimates:
##
##      Standard errors                Robust.sem
##      Information                    Expected
##      Information saturated (h1) model Unstructured
##
## Latent Variables:
##      Estimate  Std.Err  z-value  P(>|z|)  Std.lv  Std.all
##      lat_COM =~
##      COM1      1.000
##      COM2      1.411    0.211    6.671    0.000    0.645    0.682
##      COM3      1.312    0.215    6.102    0.000    0.600    0.626
##      lat_INT =~

```

```

##      INT1          1.000          0.923      0.923
##      INT2          0.986      0.018      54.433      0.000      0.910      0.910
##      INT3          0.944      0.017      54.917      0.000      0.871      0.871
##      lat_FAM =~
##      FAM1          1.000          0.893      0.893
##      FAM2          0.966      0.021      45.380      0.000      0.863      0.863
##      FAM3          1.032      0.023      45.470      0.000      0.922      0.922
##      lat_WMC =~
##      OSPAN          1.000          0.130      0.654
##      SSPAN          0.995      0.267      3.720      0.000      0.130      0.756
##
## Covariances:
##      Estimate      Std.Err      z-value      P(>|z|)      Std.lv      Std.all
##      VOL ~~
##      INV          -0.008      0.003      -2.836      0.005      -0.008      -0.145
##      lat_INT ~~
##      lat_WMC          0.005      0.007      0.702      0.482      0.039      0.039
##      lat_FAM          0.440      0.031      14.017      0.000      0.534      0.534
##      lat_COM ~~
##      lat_INT          0.196      0.035      5.636      0.000      0.465      0.465
##      lat_FAM          0.111      0.028      3.969      0.000      0.271      0.271
##      lat_WMC          0.020      0.006      3.523      0.000      0.334      0.334
##      lat_FAM ~~
##      lat_WMC          0.007      0.007      1.077      0.281      0.064      0.064
##
## Intercepts:
##      Estimate      Std.Err      z-value      P(>|z|)      Std.lv      Std.all
##      .COM1          1.832      0.042      44.133      0.000      1.832      2.031
##      .COM2          1.619      0.041      39.017      0.000      1.619      1.712
##      .COM3          1.867      0.045      41.479      0.000      1.867      1.947
##      .INT1          0.000          0.000      0.000      0.000      0.000      0.000
##      .INT2          0.000          0.000      0.000      0.000      0.000      0.000
##      .INT3          0.000          0.000      0.000      0.000      0.000      0.000
##      .FAM1          0.000          0.000      0.000      0.000      0.000      0.000
##      .FAM2          0.000          0.000      0.000      0.000      0.000      0.000
##      .FAM3          0.000          0.000      0.000      0.000      0.000      0.000
##      .OSPAN          0.707      0.012      59.905      0.000      0.707      3.545
##      .SSPAN          0.568      0.008      74.341      0.000      0.568      3.311
##      VOL          0.130      0.018      7.357      0.000      0.130      0.572
##      INV          0.264      0.012      21.320      0.000      0.264      1.091
##      lat_COM          0.000          0.000      0.000      0.000      0.000      0.000
##      lat_INT          0.000          0.000      0.000      0.000      0.000      0.000
##      lat_FAM          0.000          0.000      0.000      0.000      0.000      0.000
##      lat_WMC          0.000          0.000      0.000      0.000      0.000      0.000
##
## Thresholds:
##      Estimate      Std.Err      z-value      P(>|z|)      Std.lv      Std.all
##      INT1|t1          -1.234      0.073      -16.916      0.000      -1.234      -1.234
##      INT1|t2          -0.278      0.056      -5.008      0.000      -0.278      -0.278
##      INT1|t3          0.788      0.061      12.839      0.000      0.788      0.788
##      INT2|t1          -1.102      0.069      -16.035      0.000      -1.102      -1.102
##      INT2|t2          -0.065      0.055      -1.177      0.239      -0.065      -0.065
##      INT2|t3          0.956      0.065      14.733      0.000      0.956      0.956
##      INT3|t1          -0.949      0.065      -14.657      0.000      -0.949      -0.949

```

```
##      INT3|t2          0.002    0.055    0.044    0.965    0.002    0.002
##      INT3|t3          1.224    0.073   16.859    0.000    1.224    1.224
##      FAM1|t1         -0.694    0.060  -11.602    0.000   -0.694   -0.694
##      FAM1|t2          0.229    0.055    4.139    0.000    0.229    0.229
##      FAM1|t3          1.175    0.071   16.557    0.000    1.175    1.175
##      FAM2|t1         -0.994    0.066  -15.108    0.000   -0.994   -0.994
##      FAM2|t2         -0.117    0.055   -2.136    0.033   -0.117   -0.117
##      FAM2|t3          1.010    0.066   15.256    0.000    1.010    1.010
##      FAM3|t1         -0.821    0.062  -13.243    0.000   -0.821   -0.821
##      FAM3|t2          0.219    0.055    3.965    0.000    0.219    0.219
##      FAM3|t3          1.321    0.076   17.335    0.000    1.321    1.321
```

```
##
## Variances:
##      Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .COM1      0.605   0.052   11.555   0.000   0.605   0.743
##      .COM2      0.478   0.063    7.575   0.000   0.478   0.535
##      .COM3      0.559   0.061    9.174   0.000   0.559   0.608
##      .INT1      0.149                0.149   0.149
##      .INT2      0.172                0.172   0.172
##      .INT3      0.242                0.242   0.242
##      .FAM1      0.202                0.202   0.202
##      .FAM2      0.256                0.256   0.256
##      .FAM3      0.149                0.149   0.149
##      .OSPAN     0.023   0.005    4.942   0.000   0.023   0.572
##      .SSPAN     0.013   0.004    2.847   0.004   0.013   0.428
##      VOL        0.052   0.003   16.357   0.000   0.052   1.000
##      INV        0.058   0.004   15.341   0.000   0.058   1.000
##      lat_COM     0.209   0.049    4.298   0.000   1.000   1.000
##      lat_INT     0.851   0.019   44.197   0.000   1.000   1.000
##      lat_FAM     0.798   0.024   33.406   0.000   1.000   1.000
##      lat_WMC     0.017   0.005    3.441   0.001   1.000   1.000
```

```
##
## Scales y*:
##      Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      INT1      1.000                1.000   1.000
##      INT2      1.000                1.000   1.000
##      INT3      1.000                1.000   1.000
##      FAM1      1.000                1.000   1.000
##      FAM2      1.000                1.000   1.000
##      FAM3      1.000                1.000   1.000
```

```
# Estimating Cronbach's alpha for Latent variable
```

```
alpha(df %>% select(starts_with("COM"))) # Estimate for Comprehension
```

```
##
## Reliability analysis
## Call: alpha(x = df %>% select(starts_with("COM")))
##
##      raw_alpha std.alpha G6(smc) average_r S/N ase mean sd median_r
##      0.64      0.64      0.54      0.37 1.7 0.027 1.8 0.71      0.36
##
## lower alpha upper      95% confidence boundaries
## 0.58 0.64 0.69
```

```
##
## Reliability if an item is dropped:
##      raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## COM1      0.53      0.53   0.36      0.36 1.1   0.040   NA  0.36
## COM2      0.50      0.50   0.34      0.34 1.0   0.043   NA  0.34
## COM3      0.58      0.58   0.41      0.41 1.4   0.036   NA  0.41
##
## Item statistics
##      n raw.r std.r r.cor r.drop mean  sd
## COM1 537  0.75  0.76  0.57  0.45  1.8 0.91
## COM2 537  0.78  0.77  0.59  0.47  1.6 0.94
## COM3 537  0.75  0.74  0.52  0.42  1.9 0.96
##
## Non missing response frequency for each item
##      0    1    2    3 miss
## COM1 0.09 0.25 0.42 0.25    0
## COM2 0.13 0.33 0.35 0.20    0
## COM3 0.10 0.25 0.35 0.30    0
```

```
alpha(df %>% select(starts_with("INT")) %>% mutate_all(as.numeric)) # Estimate for Interest
```

```
##
## Reliability analysis
## Call: alpha(x = df %>% select(starts_with("INT")) %>% mutate_all(as.numeric))
##
##      raw_alpha std.alpha G6(smc) average_r S/N      ase mean  sd median_r
##          0.9      0.9      0.85      0.74 8.6 0.0078  1.6 0.84      0.74
##
## lower alpha upper      95% confidence boundaries
## 0.88 0.9 0.91
##
## Reliability if an item is dropped:
##      raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## INT1      0.84      0.84   0.72      0.72 5.2   0.014   NA  0.72
## INT2      0.85      0.85   0.74      0.74 5.7   0.013   NA  0.74
## INT3      0.87      0.87   0.76      0.76 6.4   0.012   NA  0.76
##
## Item statistics
##      n raw.r std.r r.cor r.drop mean  sd
## INT1 537  0.92  0.92  0.86  0.81  1.7 0.93
## INT2 537  0.91  0.91  0.84  0.80  1.5 0.93
## INT3 537  0.90  0.90  0.82  0.78  1.4 0.90
##
## Non missing response frequency for each item
##      0    1    2    3 miss
## INT1 0.11 0.28 0.39 0.21    0
## INT2 0.14 0.34 0.36 0.17    0
## INT3 0.18 0.33 0.39 0.11    0
```

```
alpha(df %>% select(starts_with("FAM")) %>% mutate_all(as.numeric)) # Estimate for Familiarity
```

```
##
## Reliability analysis
```

```
## Call: alpha(x = df %>% select(starts_with("FAM"))) %>% mutate_all(as.numeric))
##
##   raw_alpha std.alpha G6(smc) average_r S/N   ase mean   sd median_r
##     0.88     0.88     0.84     0.71 7.5 0.0089 1.4 0.84     0.69
##
##   lower alpha upper      95% confidence boundaries
## 0.86 0.88 0.9
##
## Reliability if an item is dropped:
##   raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## FAM1     0.82     0.82     0.69     0.69 4.6   0.016   NA 0.69
## FAM2     0.87     0.87     0.77     0.77 6.6   0.011   NA 0.77
## FAM3     0.81     0.81     0.68     0.68 4.3   0.016   NA 0.68
##
## Item statistics
##      n raw.r std.r r.cor r.drop mean   sd
## FAM1 537 0.91 0.91 0.84 0.78 1.3 0.96
## FAM2 537 0.88 0.88 0.77 0.73 1.5 0.94
## FAM3 537 0.91 0.91 0.85 0.80 1.3 0.90
##
## Non missing response frequency for each item
##      0    1    2    3 miss
## FAM1 0.25 0.34 0.29 0.12    0
## FAM2 0.16 0.29 0.39 0.15    0
## FAM3 0.21 0.38 0.32 0.09    0
```

```
alpha(df %>% select(ends_with("PAN"))) # Estimate for WMC
```

```
##
## Reliability analysis
## Call: alpha(x = df %>% select(ends_with("PAN")))
##
##   raw_alpha std.alpha G6(smc) average_r S/N   ase mean   sd median_r
##     0.66     0.67     0.5     0.5    2 0.029 0.63 0.16     0.5
##
##   lower alpha upper      95% confidence boundaries
## 0.61 0.66 0.72
##
## Reliability if an item is dropped:
##   raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## OSPAN     0.50     0.5     0.25     0.5  NA     NA 0.50 0.5
## SSPAN     0.25     0.5     NA     NA  NA     NA 0.25 0.5
##
## Item statistics
##      n raw.r std.r r.cor r.drop mean   sd
## OSPAN 537 0.89 0.87 0.61 0.5 0.70 0.20
## SSPAN 534 0.84 0.87 0.61 0.5 0.57 0.17
```

Code for producing Table-2 and Tbale-3

In the regression table Std.all includes the estimates in Table-2 and Std.lv includes estimate for Table-3. I am not clear why the sign is opposite with respect to the sign in the paper in Table-3.

```
myModel <- readLines("model.lav")
```

```
cat(myModel, fill = TRUE)
```

```
## # latent variable definitions lat_COM =~ COM1 + COM2 + COM3
## lat_INT =~ INT1 + INT2 + INT3 lat_FAM =~ FAM1 + FAM2 + FAM3
## lat_WMC =~ OSPAN + SSPAN # regressions
## lat_COM ~ a * lat_WMC + b * lat_INT + c * lat_FAM + VOL + INV
## VOL ~ d * lat_WMC + e * lat_INT + f * lat_FAM
## INV ~ g * lat_WMC + h * lat_INT + i * lat_FAM # variances and covariances
## VOL ~~ INV lat_INT ~~ lat_WMC lat_FAM ~~ lat_WMC lat_INT ~~ lat_FAM
```

```
fit <- sem(model = myModel, data = df, cluster = 'SUBJECT', ordered = paste0(rep(c("INT", "FAM"), each = 3), "1"),
summary(fit, standardized=TRUE)
```

```
## lavaan 0.6-6 ended normally after 102 iterations
```

```
##
## Estimator DWLS
## Optimization method NLMINB
## Number of free parameters 58
##
## Used Total
## Number of observations 525 537
## Number of clusters [SUBJECT] 178
##
```

```
## Model Test User Model:
```

```
## Standard Robust
## Test Statistic 59.776 127.152
## Degrees of freedom 52 52
## P-value (Chi-square) 0.214 0.000
## Scaling correction factor 0.523
## Shift parameter 12.880
## simple second-order correction
##
```

```
## Parameter Estimates:
```

```
## Standard errors Robust.sem
## Information Expected
## Information saturated (h1) model Unstructured
##
```

```
## Latent Variables:
```

	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
## lat_COM =~						
## COM1	1.000				0.465	0.515
## COM2	1.357	0.193	7.043	0.000	0.631	0.667
## COM3	1.307	0.205	6.373	0.000	0.607	0.633
## lat_INT =~						
## INT1	1.000				0.925	0.925
## INT2	0.981	0.018	54.248	0.000	0.908	0.908
## INT3	0.940	0.017	54.999	0.000	0.870	0.870


```

##   lat_FAM =~
##       FAM1           1.000                0.893    0.893
##       FAM2           0.968    0.022    44.710    0.000    0.864    0.864
##       FAM3           1.032    0.023    45.099    0.000    0.922    0.922
##   lat_WMC =~
##       OSPAN           1.000                0.131    0.656
##       SSPAN           0.989    0.240     4.122    0.000    0.129    0.754
##
## Regressions:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   lat_COM ~
##       lat_WMC (a)    0.895    0.252     3.552    0.000    0.252    0.252
##       lat_INT (b)    0.146    0.039     3.752    0.000    0.290    0.290
##       lat_FAM (c)    0.008    0.032     0.263    0.792    0.016    0.016
##       VOL      -0.559    0.130    -4.283    0.000   -1.203   -0.274
##       INV      -0.454    0.118    -3.840    0.000   -0.976   -0.236
##   VOL ~
##       lat_WMC (d)   -0.209    0.082    -2.537    0.011   -0.027   -0.120
##       lat_INT (e)   -0.081    0.010    -8.320    0.000   -0.075   -0.329
##       lat_FAM (f)    0.008    0.010     0.758    0.448    0.007    0.031
##   INV ~
##       lat_WMC (g)   -0.249    0.093    -2.687    0.007   -0.033   -0.134
##       lat_INT (h)   -0.073    0.013    -5.417    0.000   -0.068   -0.280
##       lat_FAM (i)   -0.006    0.014    -0.397    0.691   -0.005   -0.021
##
## Covariances:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .VOL ~~
##       .INV      -0.014    0.003    -4.941    0.000   -0.014   -0.286
##   lat_INT ~~
##       lat_WMC      0.005    0.007     0.707    0.479    0.040    0.040
##   lat_FAM ~~
##       lat_WMC      0.007    0.007     1.079    0.281    0.064    0.064
##   lat_INT ~~
##       lat_FAM      0.441    0.031    14.020    0.000    0.534    0.534
##
## Intercepts:
##               Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##   .COM1          2.025    0.064    31.510    0.000    2.025    2.245
##   .COM2          1.880    0.073    25.758    0.000    1.880    1.988
##   .COM3          2.118    0.078    27.114    0.000    2.118    2.209
##   .INT1           0.000                0.000    0.000
##   .INT2           0.000                0.000    0.000
##   .INT3           0.000                0.000    0.000
##   .FAM1           0.000                0.000    0.000
##   .FAM2           0.000                0.000    0.000
##   .FAM3           0.000                0.000    0.000
##   .OSPAN          0.707    0.012    59.905    0.000    0.707    3.545
##   .SSPAN          0.568    0.008    74.341    0.000    0.568    3.311
##   .VOL            0.130    0.018     7.357    0.000    0.130    0.572
##   .INV            0.264    0.012    21.320    0.000    0.264    1.091
##   .lat_COM        0.000                0.000    0.000
##   lat_INT         0.000                0.000    0.000
##   lat_FAM         0.000                0.000    0.000

```

```

##      lat_WMC          0.000          0.000      0.000
##
## Thresholds:
##      Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      INT1|t1    -1.234   0.073  -16.916   0.000   -1.234   -1.234
##      INT1|t2    -0.278   0.056   -5.008   0.000   -0.278   -0.278
##      INT1|t3     0.788   0.061   12.839   0.000    0.788    0.788
##      INT2|t1    -1.102   0.069  -16.035   0.000   -1.102   -1.102
##      INT2|t2    -0.065   0.055   -1.177   0.239   -0.065   -0.065
##      INT2|t3     0.956   0.065   14.733   0.000    0.956    0.956
##      INT3|t1    -0.949   0.065  -14.657   0.000   -0.949   -0.949
##      INT3|t2     0.002   0.055    0.044   0.965    0.002    0.002
##      INT3|t3     1.224   0.073   16.859   0.000    1.224    1.224
##      FAM1|t1    -0.694   0.060  -11.602   0.000   -0.694   -0.694
##      FAM1|t2     0.229   0.055    4.139   0.000    0.229    0.229
##      FAM1|t3     1.175   0.071   16.557   0.000    1.175    1.175
##      FAM2|t1    -0.994   0.066  -15.108   0.000   -0.994   -0.994
##      FAM2|t2    -0.117   0.055   -2.136   0.033   -0.117   -0.117
##      FAM2|t3     1.010   0.066   15.256   0.000    1.010    1.010
##      FAM3|t1    -0.821   0.062  -13.243   0.000   -0.821   -0.821
##      FAM3|t2     0.219   0.055    3.965   0.000    0.219    0.219
##      FAM3|t3     1.321   0.076   17.335   0.000    1.321    1.321
##
## Variances:
##      Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      .COM1       0.598   0.050   11.860   0.000    0.598    0.735
##      .COM2       0.497   0.058    8.506   0.000    0.497    0.555
##      .COM3       0.551   0.058    9.443   0.000    0.551    0.599
##      .INT1       0.144           0.144    0.144
##      .INT2       0.176           0.176    0.176
##      .INT3       0.243           0.243    0.243
##      .FAM1       0.202           0.202    0.202
##      .FAM2       0.253           0.253    0.253
##      .FAM3       0.151           0.151    0.151
##      .OSPAN      0.023   0.004    5.469   0.000    0.023    0.570
##      .SSPAN      0.013   0.004    3.210   0.001    0.013    0.431
##      .VOL        0.046   0.003   16.545   0.000    0.046    0.884
##      .INV        0.052   0.003   15.540   0.000    0.052    0.894
##      .lat_COM     0.129   0.030    4.345   0.000    0.599    0.599
##      lat_INT      0.856   0.019   44.492   0.000    1.000    1.000
##      lat_FAM      0.798   0.024   33.133   0.000    1.000    1.000
##      lat_WMC      0.017   0.005    3.770   0.000    1.000    1.000
##
## Scales y*:
##      Estimate Std.Err z-value P(>|z|) Std.lv Std.all
##      INT1        1.000           1.000    1.000
##      INT2        1.000           1.000    1.000
##      INT3        1.000           1.000    1.000
##      FAM1        1.000           1.000    1.000
##      FAM2        1.000           1.000    1.000
##      FAM3        1.000           1.000    1.000

```

Code for producing Figure-2

```
labels = list(lat_INT = "Interest", lat_FAM = "Familiarity", lat_WMC = "WMC", lat_COM = "Reading", VOL =
grph <- lavaanPlot(model = fit, stand = TRUE,
  labels = labels, node_options = list(shape = "box", fontname = "Helvetica"),
  edge_options = list(color = "grey"), coef = TRUE)

tmp<-capture.output(rsvg_png(charToRaw(export_svg(grph))), 'SEM.png'))

cat('![Structural equation model with estimated standardized coefficients.](SEM.png){#fig:SEM}\n\n')
```

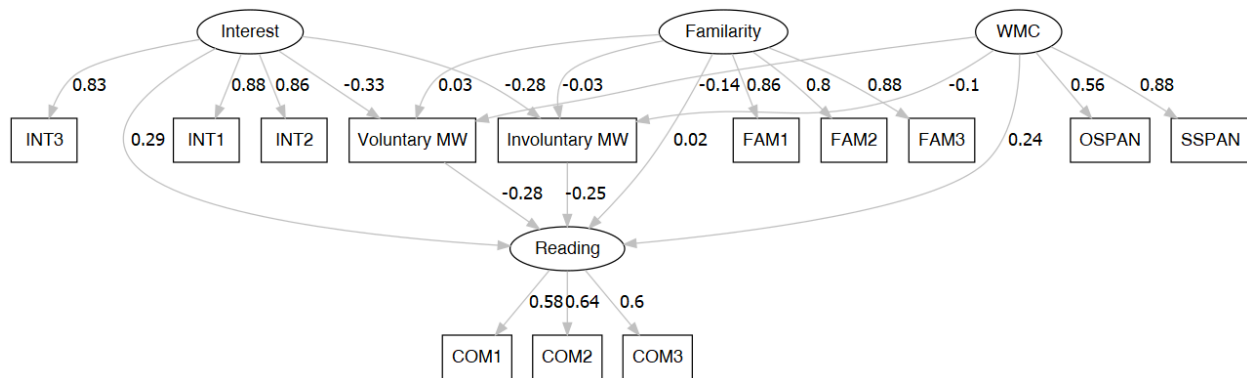


Figure 1: Structural equation model with estimated standardized coefficients.

Code for producing Table-4

```
df %>% select(-SUBJECT, -TEXT) %>% lowerCor(digits = 2)
```

```
##      OSPAN SSPAN COM1  COM2  COM3  INT1  INT2  INT3  FAM1  FAM2  FAM3
## OSPAN  1.00
## SSPAN  0.50  1.00
## COM1   0.11  0.21  1.00
## COM2   0.14  0.14  0.41  1.00
## COM3   0.15  0.15  0.34  0.36  1.00
## INT1   0.11  0.05  0.22  0.29  0.29  1.00
## INT2   0.08 -0.03  0.18  0.28  0.24  0.76  1.00
## INT3   0.05 -0.05  0.18  0.26  0.27  0.74  0.72  1.00
## FAM1   0.01  0.00  0.05  0.13  0.10  0.34  0.37  0.32  1.00
## FAM2   0.11  0.07  0.11  0.21  0.20  0.41  0.48  0.40  0.68  1.00
## FAM3   0.03  0.06  0.11  0.17  0.15  0.36  0.40  0.34  0.77  0.69  1.00
## VOL    -0.05 -0.13 -0.24 -0.21 -0.24 -0.30 -0.27 -0.25 -0.08 -0.17 -0.12
## INV    -0.13 -0.08 -0.15 -0.21 -0.22 -0.28 -0.21 -0.24 -0.17 -0.14 -0.13
##      VOL  INV
## VOL  1.00
## INV -0.15  1.00
```

```
describe(df %>% select(-SUBJECT, -TEXT)) %>% rownames_to_column() %>% kable(digits = 2)
```

rowname	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew	kurtosis	se
OSPAN	1	537	0.70	0.20	0.75	0.73	0.16	0.02	1	0.98	-1.17	1.07	0.01
SSPAN	2	534	0.57	0.17	0.58	0.57	0.16	0.07	1	0.93	-0.28	0.05	0.01
COM1	3	537	1.82	0.91	2.00	1.88	1.48	0.00	3	3.00	-0.35	-0.67	0.04
COM2	4	537	1.61	0.94	2.00	1.64	1.48	0.00	3	3.00	-0.08	-0.91	0.04
COM3	5	537	1.85	0.96	2.00	1.94	1.48	0.00	3	3.00	-0.38	-0.87	0.04
INT1	6	537	1.70	0.93	2.00	1.75	1.48	0.00	3	3.00	-0.23	-0.81	0.04
INT2	7	537	1.55	0.93	2.00	1.56	1.48	0.00	3	3.00	-0.05	-0.86	0.04
INT3	8	537	1.43	0.90	1.00	1.41	1.48	0.00	3	3.00	-0.07	-0.83	0.04
FAM1	9	537	1.28	0.96	1.00	1.23	1.48	0.00	3	3.00	0.20	-0.96	0.04
FAM2	10	537	1.53	0.94	2.00	1.54	1.48	0.00	3	3.00	-0.13	-0.88	0.04
FAM3	11	537	1.30	0.90	1.00	1.26	1.48	0.00	3	3.00	0.14	-0.80	0.04
VOL	12	528	0.13	0.23	0.00	0.08	0.00	0.00	1	1.00	2.10	4.40	0.01
INV	13	528	0.27	0.24	0.25	0.24	0.37	0.00	1	1.00	0.81	0.40	0.01