SEM in R with lavaan

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Loading libraries

```
library(tidyverse)
library(knitr)
library(lavaan)
library(lavaanPlot)
library(psych)
```

Reading data from CSV

```
df <- read_csv("Reading_Header.csv") # reading data

df <- df %>%
    #mutate(across(.cols = c(starts_with('INT'), starts_with('FAM')), .fns = ~as.character(.x))) %>% # re
    mutate(across(.cols = where(is.numeric), .fns = ~ifelse(.x == 999999, NA, .x))) %>% # recoding missi
    mutate(across(.cols = where(is.character), .fns = ~ifelse(.x %in% '999999', NA, .x))) # recoding mi

glimpse(df)

## Rows: 537
```

```
## Columns: 15
## $ SUBJECT <dbl> 2, 2, 2, 3, 3, 3, 4, 4, 4, 5, 5, 5, 6, 6, 6, 7, 7, 7, 8, 8,...
## $ TEXT
             <chr> "Netz", "Wind", "Spek", "Netz", "Wind", "Spek", "Netz", "Wi...
## $ OSPAN
             <dbl> 0.7523810, 0.7523810, 0.7523810, 0.7979497, 0.7979497, 0.79...
## $ SSPAN
             <dbl> 0.6907937, 0.6907937, 0.6907937, 0.4099440, 0.4099440, 0.40...
## $ COM1
             <dbl> 3, 1, 3, 2, 0, 2, 3, 2, 3, 3, 2, 2, 3, 3, 2, 3, 2, 3, 2, 2, ...
## $ COM2
             <dbl> 3, 1, 2, 2, 0, 2, 2, 1, 2, 3, 1, 1, 3, 3, 3, 3, 2, 2, 1, 0,...
## $ COM3
             <dbl> 3, 2, 2, 2, 3, 1, 3, 1, 3, 3, 1, 1, 3, 1, 3, 3, 1, 3, 2, 2,...
## $ INT1
             <dbl> 3, 1, 1, 2, 1, 2, 2, 2, 2, 3, 1, 1, 2, 2, 0, 3, 2, 2, 3, 0,...
## $ INT2
             <dbl> 3, 1, 1, 2, 1, 1, 2, 1, 1, 3, 1, 0, 1, 1, 0, 3, 1, 1, 2, 0,...
## $ INT3
             <dbl> 3, 0, 1, 2, 1, 1, 2, 1, 1, 3, 1, 1, 1, 1, 0, 3, 1, 1, 3, 0,...
## $ FAM1
             <dbl> 1, 3, 0, 2, 1, 2, 0, 1, 1, 2, 1, 0, 1, 1, 1, 3, 1, 1, 0, 0,...
## $ FAM2
             <dbl> 2, 2, 0, 3, 0, 1, 1, 2, 2, 3, 1, 1, 2, 2, 2, 3, 2, 1, 0, 0,...
## $ FAM3
             <dbl> 1, 2, 0, 2, 1, 1, 1, 1, 1, 3, 1, 1, 1, 2, 1, 3, 1, 1, 0, 0,...
## $ VOL
             <dbl> 0.00, 0.25, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00,...
## $ INV
             <dbl> 0.2500000, 0.2500000, 0.2500000, 0.6000000, 0.8000000, 0.50...
```

summary(df)

```
##
      SUBJECT
                       TEXT
                                          OSPAN
                                                            SSPAN
                   Length:537
                                             :0.02451 Min.
##
   Min. : 2.0
                                      Min.
                                                               :0.06803
   1st Qu.: 50.0
                   Class : character
                                      1st Qu.:0.60915
                                                       1st Qu.:0.45971
                   Mode :character
   Median: 97.0
                                      Median :0.74893
                                                       Median : 0.57576
##
   Mean :100.6
                                             :0.70170
                                                       Mean
                                                               :0.56546
##
                                      Mean
##
   3rd Qu.:144.0
                                      3rd Qu.:0.84944
                                                        3rd Qu.:0.68214
##
   Max. :337.0
                                      Max.
                                             :1.00000
                                                       Max.
                                                               :1.00000
##
                                                        NA's
                                                               :3
##
        COM1
                        COM2
                                        COM3
                                                        INT1
##
   Min.
          :0.000
                   Min.
                          :0.000
                                   Min.
                                         :0.000
                                                   Min.
                                                         :0.000
                   1st Qu.:1.000
                                                   1st Qu.:1.000
   1st Qu.:1.000
                                   1st Qu.:1.000
   Median :2.000
                   Median :2.000
                                   Median :2.000
                                                   Median :2.000
##
##
   Mean :1.818
                   Mean :1.611
                                   Mean :1.855
                                                   Mean :1.702
   3rd Qu.:2.000
                   3rd Qu.:2.000
                                   3rd Qu.:3.000
##
                                                   3rd Qu.:2.000
   Max. :3.000
                   Max. :3.000
                                   Max. :3.000
                                                   Max.
                                                         :3.000
##
##
        INT2
                        INT3
                                        FAM1
                                                       FAM2
                                                                       FAM3
##
   Min.
         :0.000
                   Min.
                          :0.000
                                   Min.
                                         :0.000
                                                   Min.
                                                         :0.000
                                                                  Min.
                                                                        :0.0
   1st Qu.:1.000
                   1st Qu.:1.000
                                   1st Qu.:1.000
                                                   1st Qu.:1.000
                                                                   1st Qu.:1.0
##
##
   Median :2.000
                   Median :1.000
                                   Median :1.000
                                                   Median :2.000
                                                                  Median:1.0
                                   Mean
##
   Mean :1.549
                   Mean :1.428
                                         :1.281
                                                   Mean :1.533
                                                                  Mean :1.3
   3rd Qu.:2.000
                   3rd Qu.:2.000
                                   3rd Qu.:2.000
                                                   3rd Qu.:2.000
                                                                   3rd Qu.:2.0
##
   Max. :3.000
                   Max. :3.000
                                   Max. :3.000
                                                   Max. :3.000
                                                                  Max. :3.0
##
        VOL
##
                         INV
          :0.0000
   Min.
                    Min. :0.000
##
   1st Qu.:0.0000
                    1st Qu.:0.000
## Median :0.0000
                    Median :0.250
## Mean :0.1316
                    Mean :0.265
## 3rd Qu.:0.2500
                    3rd Qu.:0.400
## Max. :1.0000
                    Max.
                           :1.000
   NA's
          :9
                    NA's
                           :9
```

Code for producing Table-1

```
corr.lv.model <- '
# latent variable definitions

lat_COM =~ COM1 + COM2 + COM3
lat_INT =~ INT1 + INT2 + INT3
lat_FAM =~ FAM1 + FAM2 + FAM3
lat_WMC =~ OSPAN + SSPAN

# covariances

VOL ~~ INV
lat_INT ~~ lat_WMC</pre>
```

```
lat_INT ~~ lat_FAM
lat_INT ~~ lat_COM
lat_COM ~~ lat_FAM
lat_COM ~~ lat_WMC
lat_FAM ~~ lat_WMC
fit.lv.model <- cfa(model = corr.lv.model, data = df, cluster = 'SUBJECT') # Confirmatory factor model
summary(fit.lv.model, standardized=TRUE) # In covariance table std.lv includes the correlation
## lavaan 0.6-6 ended normally after 81 iterations
##
##
     Estimator
                                                        ML
##
     Optimization method
                                                    NLMINB
##
     Number of free parameters
                                                        44
##
##
                                                      Used
                                                                  Total
##
     Number of observations
                                                       525
                                                                    537
     Number of clusters [SUBJECT]
                                                       178
##
##
## Model Test User Model:
##
                                                   Standard
                                                                 Robust
##
     Test Statistic
                                                    276.379
                                                                 254.434
##
     Degrees of freedom
                                                          60
                                                                      60
##
     P-value (Chi-square)
                                                      0.000
                                                                   0.000
                                                                   1.086
##
     Scaling correction factor
##
          Yuan-Bentler correction (Mplus variant)
##
## Parameter Estimates:
##
##
     Standard errors
                                             Robust.cluster
##
     Information
                                                   Observed
     Observed information based on
                                                    Hessian
##
##
## Latent Variables:
                      Estimate Std.Err z-value P(>|z|)
                                                             Std.lv Std.all
##
##
     lat_COM =~
       COM1
##
                         1.000
                                                               0.525
                                                                        0.582
       COM2
##
                         1.193
                                   0.134
                                            8.919
                                                     0.000
                                                               0.626
                                                                        0.662
##
       COM3
                         1.059
                                   0.138
                                                     0.000
                                                                        0.580
                                            7.692
                                                               0.556
##
     lat_INT =~
##
       INT1
                         1.000
                                                               0.811
                                                                        0.879
##
       INT2
                         0.988
                                   0.038
                                           25.796
                                                     0.000
                                                               0.801
                                                                        0.866
##
       INT3
                         0.922
                                   0.042
                                           22.153
                                                     0.000
                                                               0.747
                                                                        0.830
##
     lat_FAM =~
##
       FAM1
                         1.000
                                                               0.827
                                                                        0.856
```

##	FAM2	0.907	0.042	21.394	0.000	0.749	0.799
##	FAM3	0.957	0.035	27.384	0.000	0.791	0.880
##	<pre>lat_WMC =~</pre>						
##	OSPAN	1.000				0.112	0.561
##	SSPAN	1.350	0.535	2.525	0.012	0.151	0.881
##							
##	Covariances:						
##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
##	VOL ~~						
##	INV	-0.008	0.002	-3.542	0.000	-0.008	-0.145
##	<pre>lat_INT ~~</pre>						
##	lat_WMC	0.001	0.006	0.139	0.890	0.009	0.009
##	lat_FAM	0.335	0.035	9.651	0.000	0.500	0.500
##	lat_COM ~~						
##	lat_INT	0.196	0.027	7.289	0.000	0.460	0.460
##	lat_FAM	0.112	0.025	4.521	0.000	0.258	0.258
##	<pre>lat_WMC</pre>	0.018	0.007	2.499	0.012	0.310	0.310
##	<pre>lat_FAM ~~</pre>						
##	<pre>lat_WMC</pre>	0.005	0.005	0.989	0.323	0.052	0.052
##							
##	Intercepts:						
##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
##	.COM1	1.832	0.045	41.168	0.000	1.832	2.031
##	.COM2	1.619	0.041	39.131	0.000	1.619	1.712
##	.COM3	1.867	0.046	40.384	0.000	1.867	1.947
##	.INT1	1.716	0.038	45.582	0.000	1.716	1.861
##	.INT2	1.560	0.035	44.073	0.000	1.560	1.686
##	.INT3	1.438	0.036	39.514	0.000	1.438	1.598
##	.FAM1	1.286	0.039	32.607	0.000	1.286	1.332
##	.FAM2	1.543	0.045	34.079	0.000	1.543	1.644
##	.FAM3	1.301	0.042	31.227	0.000	1.301	1.447
##	.OSPAN	0.707	0.015	47.508	0.000	0.707	3.545
##	.SSPAN	0.568	0.013	44.104	0.000	0.568	3.311
##	VOL	0.130	0.011	12.013	0.000	0.130	0.572
##	INV	0.264	0.012	21.624	0.000	0.264	1.091
##	lat_COM	0.000				0.000	0.000
##	lat_INT	0.000				0.000	0.000
##	lat_FAM	0.000				0.000	0.000
##	${\tt lat_WMC}$	0.000				0.000	0.000
##							
##	Variances:						
##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
##	.COM1	0.538	0.046	11.632	0.000	0.538	0.662
##	.COM2	0.503	0.054	9.399	0.000	0.503	0.562
##	.COM3	0.610	0.054	11.286	0.000	0.610	0.664
##	.INT1	0.194	0.025	7.684	0.000	0.194	0.228
##	.INT2	0.214	0.033	6.585	0.000	0.214	0.250
##	.INT3	0.252	0.031	8.036	0.000	0.252	0.311
##	.FAM1	0.248	0.025	9.925	0.000	0.248	0.267
##	.FAM2	0.319	0.036	8.806	0.000	0.319	0.362
##	.FAM3	0.182	0.028	6.394	0.000	0.182	0.225
##	.OSPAN	0.027	0.006	4.843	0.000	0.027	0.685
##	.SSPAN	0.007	0.008	0.806	0.420	0.007	0.224
##	VOL	0.052	0.006	8.949	0.000	0.052	1.000

```
##
       INV
                         0.058
                                  0.005
                                          12.514
                                                    0.000
                                                              0.058
                                                                       1.000
##
                         0.275
                                  0.048
                                          5.796
                                                    0.000
                                                              1.000
                                                                       1.000
       lat COM
                                                    0.000
                                                              1.000
##
       lat INT
                         0.657
                                  0.045
                                          14.643
                                                                       1.000
##
       lat_FAM
                         0.683
                                  0.045
                                          15.063
                                                    0.000
                                                              1.000
                                                                       1.000
##
       lat_WMC
                         0.013
                                  0.006
                                           2.196
                                                    0.028
                                                              1.000
                                                                       1.000
# Estimating Cronbach's alpha for Latent variable
alpha(df %>% select(starts_with("COM"))) # Estimate for Comprehension
##
## Reliability analysis
## Call: alpha(x = df %>% select(starts_with("COM")))
##
    raw_alpha std.alpha G6(smc) average_r S/N
##
                                                 ase mean
                                                            sd median_r
##
         0.64
                   0.64
                           0.54
                                     0.37 1.7 0.027 1.8 0.71
                                                                   0.36
##
##
   lower alpha upper
                          95% confidence boundaries
## 0.58 0.64 0.69
##
##
   Reliability if an item is dropped:
        raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
##
                                         0.36 1.1
## COM1
            0.53
                       0.53
                               0.36
                                                     0.040
                                                              NA 0.36
## COM2
             0.50
                       0.50
                               0.34
                                         0.34 1.0
                                                     0.043
                                                              NA 0.34
## COM3
                               0.41
                                         0.41 1.4
             0.58
                       0.58
                                                     0.036
                                                              NA 0.41
##
##
   Item statistics
         n raw.r std.r r.cor r.drop mean
## COM1 537 0.75 0.76 0.57
                                0.45 1.8 0.91
## COM2 537 0.78 0.77 0.59
                                0.47 1.6 0.94
## COM3 537 0.75 0.74 0.52
                                0.42 1.9 0.96
## Non missing response frequency for each item
           0
              1
                     2
                          3 miss
## COM1 0.09 0.25 0.42 0.25
## COM2 0.13 0.33 0.35 0.20
                               0
## COM3 0.10 0.25 0.35 0.30
                               0
alpha(df %>% select(starts_with("INT")) %>% mutate_all(as.numeric)) # Estimate for Interest
##
## Reliability analysis
## Call: alpha(x = df %>% select(starts_with("INT")) %>% mutate_all(as.numeric))
##
##
    raw_alpha std.alpha G6(smc) average_r S/N
                                                  ase mean
                                                              sd median_r
##
          0.9
                    0.9
                           0.85
                                     0.74 8.6 0.0078 1.6 0.84
##
                          95% confidence boundaries
   lower alpha upper
## 0.88 0.9 0.91
##
  Reliability if an item is dropped:
       raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
            0.84
                       0.84
                                         0.72 5.2
## INT1
                               0.72
                                                     0.014
                                                               NA 0.72
```

```
NA 0.74
## INT2
            0.85
                      0.85
                              0.74
                                      0.74 5.7
                                                    0.013
## TNT3
            0.87
                      0.87
                              0.76
                                       0.76 6.4
                                                    0.012
                                                            NA 0.76
##
## Item statistics
         n raw.r std.r r.cor r.drop mean
## INT1 537 0.92 0.92 0.86
                             0.81 1.7 0.93
## INT2 537 0.91 0.91 0.84 0.80 1.5 0.93
## INT3 537 0.90 0.90 0.82 0.78 1.4 0.90
## Non missing response frequency for each item
          0
             1
                    2
                         3 miss
## INT1 0.11 0.28 0.39 0.21
                              0
## INT2 0.14 0.34 0.36 0.17
## INT3 0.18 0.33 0.39 0.11
alpha(df %>% select(starts_with("FAM")) %>% mutate_all(as.numeric)) # Estimate for Familarity
##
## Reliability analysis
## Call: alpha(x = df %>% select(starts_with("FAM")) %>% mutate_all(as.numeric))
##
    raw_alpha std.alpha G6(smc) average_r S/N
##
                                                 ase mean
                                                           sd median r
                                    0.71 7.5 0.0089 1.4 0.84
##
        0.88
                  0.88
                          0.84
                                                                 0.69
##
## lower alpha upper
                         95% confidence boundaries
## 0.86 0.88 0.9
##
## Reliability if an item is dropped:
##
       raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## FAM1
            0.82
                      0.82
                              0.69
                                        0.69 4.6
                                                    0.016
                                                            NA 0.69
## FAM2
            0.87
                      0.87
                              0.77
                                        0.77 6.6
                                                    0.011
                                                            NA 0.77
## FAM3
            0.81
                      0.81
                              0.68
                                        0.68 4.3
                                                    0.016
                                                            NA 0.68
##
## Item statistics
         n raw.r std.r r.cor r.drop mean
## FAM1 537 0.91 0.91 0.84
                              0.78 1.3 0.96
## FAM2 537 0.88 0.88 0.77
                               0.73 1.5 0.94
## FAM3 537 0.91 0.91 0.85
                             0.80 1.3 0.90
## Non missing response frequency for each item
          0
              1
                    2
                         3 miss
## FAM1 0.25 0.34 0.29 0.12
## FAM2 0.16 0.29 0.39 0.15
## FAM3 0.21 0.38 0.32 0.09
                              0
alpha(df %>% select(ends_with("PAN"))) # Estimate for WMC
##
## Reliability analysis
## Call: alpha(x = df %>% select(ends_with("PAN")))
##
##
   raw_alpha std.alpha G6(smc) average_r S/N ase mean sd median_r
##
        0.66
                  0.67
                                     0.5
                                         2 0.029 0.63 0.16
                           0.5
```

```
##
## lower alpha upper
                       95% confidence boundaries
## 0.61 0.66 0.72
##
## Reliability if an item is dropped:
        raw_alpha std.alpha G6(smc) average_r S/N alpha se var.r med.r
## OSPAN
             0.50
                       0.5
                              0.25
                                         0.5 NA
                                                 NA 0.50
## SSPAN
                                         NA NA
             0.25
                       0.5
                                NA
                                                      NA 0.25
                                                                0.5
##
## Item statistics
          n raw.r std.r r.cor r.drop mean
## OSPAN 537 0.89 0.87 0.61 0.5 0.70 0.20
## SSPAN 534 0.84 0.87 0.61
                                0.5 0.57 0.17
```

Code for producing Table-2

##

```
myModel <- readLines("model.lav")</pre>
cat(myModel, fill = TRUE)
                                    lat_COM =~ COM1 + COM2 + COM3
## # latent variable definitions
## lat_INT =~ INT1 + INT2 + INT3 lat_FAM =~ FAM1 + FAM2 + FAM3
## lat_WMC =~ OSPAN + SSPAN
                               # regressions
## lat_COM ~ lat_WMC + lat_INT + lat_FAM + VOL + INV
## VOL ~ lat_WMC + lat_INT + lat_FAM INV ~ lat_WMC + lat_INT + lat_FAM
## # mediators # variances and covariances VOL ~~ INV lat INT ~~ lat WMC
## lat_FAM ~~ lat_WMC lat_INT ~~ lat_FAM
fit <- sem(model = myModel, data = df, cluster = 'SUBJECT')</pre>
summary(fit, standardized=TRUE)
## lavaan 0.6-6 ended normally after 111 iterations
##
##
     Estimator
                                                        ML
                                                    NLMINB
##
     Optimization method
##
     Number of free parameters
                                                        52
##
##
                                                                 Total
                                                      Used
     Number of observations
##
                                                       525
                                                                   537
##
     Number of clusters [SUBJECT]
                                                       178
##
## Model Test User Model:
                                                                 Robust
##
                                                   Standard
##
    Test Statistic
                                                     99.488
                                                                 94.087
##
    Degrees of freedom
                                                         52
                                                                     52
##
    P-value (Chi-square)
                                                      0.000
                                                                  0.000
##
    Scaling correction factor
                                                                  1.057
##
          Yuan-Bentler correction (Mplus variant)
```

## ##	Parameter Estimate	s:							
##	Standard errors			Robus	t.cluster				
##	Information			100000	Observed				
##	Observed informa	tion based	on		Hessian				
##									
##	Latent Variables:								
##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all		
##	lat_COM =~								
##	COM1	1.000				0.526	0.583		
##	COM2	1.154	0.119	9.730	0.000	0.607	0.642		
##	COM3	1.090	0.136	8.026	0.000	0.573	0.598		
##	<pre>lat_INT =~</pre>								
##	INT1	1.000				0.815	0.884		
##	INT2	0.977	0.038			0.796	0.861		
##	INT3	0.916	0.041	22.330	0.000	0.747	0.830		
##	<pre>lat_FAM =~</pre>								
##	FAM1	1.000				0.827	0.857		
##	FAM2	0.906	0.042		0.000	0.749	0.798		
##	FAM3	0.956	0.035	27.328	0.000	0.791	0.880		
##	lat_WMC =~	1 000				0 110	0 500		
##	OSPAN	1.000 1.359	0 570	0 275	0.010	0.112 0.152	0.560		
## ##	SSPAN	1.359	0.572	2.375	0.018	0.152	0.884		
	Regressions:								
##	negressions.	Estimate	Std Frr	z-value	P(> -)	Std.lv	Std.all		
##	lat_COM ~	LBUIMGUC	Dua.LII	Z varuc	1 (> 2)	bua.iv	Dua.aii		
##	lat_WMC	1.140	0.347	3.284	0.001	0.242	0.242		
##	lat_INT	0.188	0.046	4.097	0.000	0.291	0.291		
##	lat_FAM	0.012	0.039	0.300	0.765	0.018	0.018		
##	VOL	-0.643	0.138		0.000	-1.222	-0.279		
##	INV	-0.538	0.129	-4.175	0.000	-1.023	-0.247		
##	VOL ~								
##	<pre>lat_WMC</pre>	-0.279	0.159	-1.756	0.079	-0.031	-0.136		
##	<pre>lat_INT</pre>	-0.091	0.016	-5.679	0.000	-0.075	-0.326		
##	lat_FAM	0.008	0.014	0.555	0.579	0.006	0.028		
##	INV ~								
##	lat_WMC	-0.225	0.122	-1.846	0.065	-0.025	-0.104		
##	lat_INT	-0.082	0.016	-5.047	0.000				
##	lat_FAM	-0.009	0.015	-0.572	0.567	-0.007	-0.030		
##	a .								
	Covariances:	Eatimoto	C+d Enn	luo	D(> -)	C+4 1	C+4 -11		
## ##	.VOL ~~	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all		
##	.INV	-0.014	0.002	-5.619	0.000	-0.014	-0.280		
##	lat_INT ~~	0.014	0.002	0.013	0.000	0.014	0.200		
##	lat_WMC	0.001	0.006	0.157	0.875	0.010	0.010		
##	lat_FAM ~~	0.002	0.000	0.10.	0.0.0	0.020	0.020		
##	lat_WMC	0.005	0.005	0.975	0.330	0.052	0.052		
##	lat_INT ~~								
##	lat_FAM	0.336	0.035	9.668	0.000	0.499	0.499		
##									
##	Intercepts:								
##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all		

```
##
      .COM1
                          2.058
                                    0.063
                                            32.769
                                                       0.000
                                                                 2.058
                                                                          2.281
##
      .COM2
                          1.880
                                    0.067
                                                       0.000
                                                                          1.987
                                            27.855
                                                                 1.880
##
      .COM3
                          2.113
                                    0.068
                                            30.988
                                                       0.000
                                                                 2.113
                                                                          2.203
##
      .INT1
                          1.716
                                    0.038
                                            45.582
                                                       0.000
                                                                 1.716
                                                                          1.861
##
      .INT2
                          1.560
                                    0.035
                                            44.073
                                                       0.000
                                                                 1.560
                                                                          1.686
##
      .INT3
                                    0.036
                                                       0.000
                          1.438
                                            39.514
                                                                 1.438
                                                                          1.598
##
                                    0.039
                                            32.607
                                                       0.000
      .FAM1
                          1.286
                                                                 1.286
                                                                          1.332
##
      .FAM2
                          1.543
                                    0.045
                                            34.080
                                                       0.000
                                                                 1.543
                                                                          1.644
##
      .FAM3
                          1.301
                                    0.042
                                            31.227
                                                       0.000
                                                                 1.301
                                                                          1.447
##
                                    0.015
      .OSPAN
                          0.707
                                            47.508
                                                       0.000
                                                                 0.707
                                                                          3.545
##
      .SSPAN
                          0.568
                                    0.013
                                            44.104
                                                       0.000
                                                                 0.568
                                                                          3.311
##
      .VOL
                                    0.011
                                            12.013
                                                       0.000
                                                                          0.572
                          0.130
                                                                 0.130
##
      .INV
                          0.264
                                    0.012
                                            21.624
                                                       0.000
                                                                 0.264
                                                                          1.091
##
      .lat_COM
                          0.000
                                                                 0.000
                                                                          0.000
##
                          0.000
                                                                 0.000
                                                                          0.000
       lat_INT
##
       lat_FAM
                          0.000
                                                                 0.000
                                                                          0.000
##
       lat_WMC
                          0.000
                                                                 0.000
                                                                          0.000
##
## Variances:
##
                       Estimate Std.Err z-value P(>|z|)
                                                               Std.lv Std.all
##
      .COM1
                          0.537
                                    0.045
                                            11.960
                                                       0.000
                                                                0.537
                                                                          0.660
##
      .COM2
                          0.527
                                    0.051
                                            10.395
                                                       0.000
                                                                 0.527
                                                                          0.588
##
      .COM3
                          0.591
                                    0.052
                                            11.283
                                                       0.000
                                                                          0.643
                                                                0.591
##
      .INT1
                          0.186
                                    0.025
                                             7.465
                                                       0.000
                                                                          0.219
                                                                 0.186
##
                                             6.958
      .INT2
                          0.222
                                    0.032
                                                       0.000
                                                                0.222
                                                                          0.259
##
      .INT3
                          0.252
                                    0.031
                                             8.205
                                                       0.000
                                                                 0.252
                                                                          0.312
##
      .FAM1
                          0.247
                                    0.025
                                             9.894
                                                       0.000
                                                                 0.247
                                                                          0.265
##
      .FAM2
                          0.319
                                    0.036
                                             8.824
                                                       0.000
                                                                 0.319
                                                                          0.363
##
      .FAM3
                          0.183
                                    0.028
                                             6.421
                                                       0.000
                                                                          0.226
                                                                 0.183
##
                                    0.006
      .OSPAN
                          0.027
                                             4.577
                                                       0.000
                                                                 0.027
                                                                          0.687
##
      .SSPAN
                          0.006
                                    0.009
                                             0.742
                                                       0.458
                                                                 0.006
                                                                          0.219
##
      .VOL
                          0.046
                                    0.005
                                             8.873
                                                       0.000
                                                                 0.046
                                                                          0.883
##
                                    0.005
      .INV
                          0.053
                                            11.472
                                                       0.000
                                                                 0.053
                                                                          0.903
##
                          0.167
                                    0.035
                                             4.820
                                                       0.000
      .lat_COM
                                                                 0.603
                                                                          0.603
##
       lat_INT
                          0.665
                                    0.045
                                            14.787
                                                       0.000
                                                                 1.000
                                                                          1.000
##
       lat_FAM
                          0.684
                                    0.045
                                                       0.000
                                                                 1.000
                                                                          1.000
                                            15.054
##
       lat_WMC
                          0.012
                                    0.006
                                             2.102
                                                       0.036
                                                                 1.000
                                                                          1.000
```

Code for producing Figure-2

```
tmp<-capture.output(rsvg_png(charToRaw(export_svg(grph)),'SEM.png'))
cat('![Structural equation model with estimated standardized coefficients.](stnds.qa.png){#fig:SEM}\n\n</pre>
```

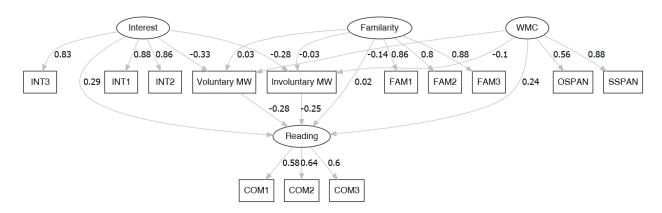


Figure 1: Structural equation model with estimated standardized coefficients.

Code for producing Table-4

```
df %>% select(-SUBJECT, -TEXT) %>% lowerCor(digits = 2)
##
       OSPAN SSPAN COM1 COM2 COM3 INT1 INT2 INT3 FAM1 FAM2 FAM3
## OSPAN
       1.00
## SSPAN 0.50
             1.00
        0.11 0.21 1.00
## COM1
## COM2
        0.14 0.14 0.41
                       1.00
## COM3
        0.15 0.15 0.34 0.36
                             1.00
## INT1
        0.11 0.05 0.22 0.29
                             0.29
                                  1.00
## INT2
        0.08 -0.03 0.18 0.28
                             0.24
                                   0.76
                                        1.00
## INT3
        0.05 -0.05 0.18 0.26
                             0.27
                                   0.74
                                        0.72
                                             1.00
        0.01 0.00 0.05 0.13
## FAM1
                             0.10
                                   0.34
                                        0.37
                                             0.32
                                                  1.00
## FAM2
        0.11 0.07 0.11 0.21
                             0.20
                                   0.41
                                        0.48
                                             0.40
                                                   0.68 1.00
## FAM3
        0.03 0.06 0.11 0.17
                             0.15
                                   0.36
                                        0.40
                                             0.34
                                                  0.77
                                                        0.69 1.00
## VOL
       -0.13 -0.08 -0.15 -0.21 -0.22 -0.28 -0.21 -0.24 -0.17 -0.14 -0.13
## INV
##
      VOL
           INV
## VOL 1.00
## INV -0.15
           1.00
describe(df %>% select(-SUBJECT, -TEXT)) %>% rownames_to_column() %>% kable(digits = 2)
```

rowname	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew	kurtosis	se
OSPAN	1	537	0.70	0.20	0.75	0.73	0.16	0.02	1	0.98	-1.17	1.07	0.01
SSPAN	2	534	0.57	0.17	0.58	0.57	0.16	0.07	1	0.93	-0.28	0.05	0.01
COM1	3	537	1.82	0.91	2.00	1.88	1.48	0.00	3	3.00	-0.35	-0.67	0.04
COM2	4	537	1.61	0.94	2.00	1.64	1.48	0.00	3	3.00	-0.08	-0.91	0.04

rowname	vars	n	mean	sd	median	${\it trimmed}$	mad	min	max	range	skew	kurtosis	se
COM3	5	537	1.85	0.96	2.00	1.94	1.48	0.00	3	3.00	-0.38	-0.87	0.04
INT1	6	537	1.70	0.93	2.00	1.75	1.48	0.00	3	3.00	-0.23	-0.81	0.04
INT2	7	537	1.55	0.93	2.00	1.56	1.48	0.00	3	3.00	-0.05	-0.86	0.04
INT3	8	537	1.43	0.90	1.00	1.41	1.48	0.00	3	3.00	-0.07	-0.83	0.04
FAM1	9	537	1.28	0.96	1.00	1.23	1.48	0.00	3	3.00	0.20	-0.96	0.04
FAM2	10	537	1.53	0.94	2.00	1.54	1.48	0.00	3	3.00	-0.13	-0.88	0.04
FAM3	11	537	1.30	0.90	1.00	1.26	1.48	0.00	3	3.00	0.14	-0.80	0.04
VOL	12	528	0.13	0.23	0.00	0.08	0.00	0.00	1	1.00	2.10	4.40	0.01
INV	13	528	0.27	0.24	0.25	0.24	0.37	0.00	1	1.00	0.81	0.40	0.01