Fermi gas at T-O.  $\mathcal{E}_{F} = \frac{h^{2}}{8m} \left( \frac{3N}{\pi V} \right)^{2/3}$ Total energy, every of microslate  $\vec{n}$   $\vec{n} = n_x \hat{x} + n_y \hat{y} + n_z \hat{z}$   $U = 2 \int \int \int \mathcal{E}(\vec{n}) dn_x dn_y dn_z \qquad \mathcal{E}(\vec{n}) = \frac{h^2}{g_{mL^2}} |\vec{n}|^2$  $=2\int\int\int\frac{h^2}{8mL^2}n^2n^2\sin\theta\,dn\,d\theta\,d\phi$  $= \left(\int_{0}^{\pi/L} \int_{0}^{\pi/L} \sin\theta \, d\theta \, d\phi\right) \frac{L^{2}}{8\pi L^{2}} 2 \int_{0}^{R} n^{4} \, dn$   $= \int_{0}^{\pi/L} \int_{0}^{\pi/L} \sin\theta \, d\theta \, d\phi \int_{0}^{L^{2}} \left(\int_{0}^{R} \int_{0}^{R} n^{4} \, dn\right) dn$  $\frac{\pi}{2} 2 \sqrt{\frac{h^2}{8mL^2}} \left[ \frac{1}{5} n^5 \right]_0^R$ R3= 3 N  $U = \frac{h^2 \pi}{40 \text{ m } L^2} R^5$  $= \left(\frac{h^2}{8mL^2} R^2\right) \stackrel{\text{tf}}{\leq} R^3$ = CF = 3 N  $U = \frac{3}{5} N E_F$  (if all electrons were at surface then U would be  $N E_F$ ) For electrons in a metal,  $C_p \approx 1-2eV$   $kT = \frac{1}{40}eV$  at com temperature  $kT = \frac{1}{40}eV$ → KT << Ep > "low T"  $E_F \propto \left(\frac{1}{V}\right)^{2/3}$  so compressing a netal (Fermi gos) will increase  $E_F \approx U$ . -> positive work is required to compress

-> Fermi gas is fighting back -> pressure "degeneracy pressure" due to Poul, exclusion principle  $P = -\left(\frac{\partial U}{\partial V}\right)_{S,N} = -\frac{\partial}{\partial V}\left(\frac{3}{5}N\varepsilon_{E}\right) = -\frac{3}{5}N\frac{\partial}{\partial V}\left(\frac{L^{2}}{8m}\left(\frac{3N}{17}\right)^{\frac{3}{2}}V^{\frac{-3}{2}}\right)$ 3rd Low:  $S=0 @ T=0 = -\frac{3Nh^3}{5} \left(\frac{3N}{5}\right)^{\frac{1}{3}} \left(-\frac{2}{3} V^{-\frac{5}{3}}\right)$  $= + \frac{3}{3} \left( \frac{3Nh^{2}}{5} \left( \frac{3N}{8m} \left( \frac{3N}{11} \right)^{2/3} \right) \right) = 0$ P = 3 U Why atoms don't collapse lung solids are solid Why white dwarf stars aren't black holes if gravity too strong

T>0 but small IF u in normal gas, every particle would gain energy kt - in termigas, that won't work only e at surface can gain energy

H of e- that can gain

1s prop. to N & KT energy ( higher T -) bigger jumps -> H of e energy
per jump More particles of energy, empty stat it cart- $\Delta U \sim (NkT)(kT)$ it's blocked U=3NEF + AN(KT) AX Ex to get dimensions light  $= \frac{3}{5} N \varepsilon_{\rm F} + \frac{\pi}{4} \frac{1}{\varepsilon_{\rm F}} N(k\tau)^{2}$ heat capacity is linear unith temperature  $C_{\gamma} = \frac{\partial U}{\partial T} - \frac{\pi^2}{2} \frac{N}{\epsilon_F} k^2 T_{\alpha}$ actually seen in netals at low T at room T, Cv or T? T=O (3rd low) (phonons)