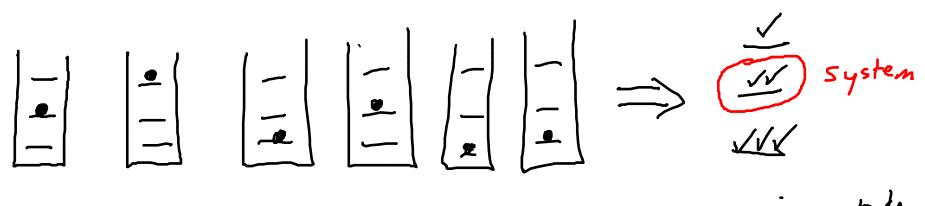


Identical Particles



Consider all particles in one energy microstate to be the "system"

Porticles enter of leave system by changing energy.

by shoring energy with other particles.

Define occupancy n of state = H particles in that state

Let & be the energy of our chosen microstate

Let p be the "chemical potential" of the reservoir
Let p be the "chemical potential" of the reservoir
Let p be particles not in system

u << & then u is "small" low density -> non-interacting particles Non-interacting particles How many particles are in State E? <n>= Probability
of being × N -BE for entire set of particles S = #1 5, M=-KT JMZ = - KT 3N [NMZ, - (NMN-N)] = -kT[lnZ, -lnN] M=-KTh = → Z,= Ne-B/ $\langle n \rangle = \frac{N e^{-\beta \epsilon}}{Z_1} = \frac{N e^{-\beta \epsilon}}{N e^{-\beta \mu}} = e^{-\beta (\epsilon - \mu)}$ $\bar{n} = \langle n \rangle = \frac{1}{\rho^{\beta(E-\mu)}}$ when $\mu \ll E$.

Using Gibbe Statistics.

"states": # of particles n in the system
(i.e. the microstate &)

$$\mathcal{J} = \sum_{s} e^{-\beta(E_{s} - \mu N_{s})} \qquad N_{s} = n \quad E_{s} = n \varepsilon$$

$$= \sum_{n=0}^{-\beta(n\xi-\mu n)} = \sum_{n=0}^{-n\beta(\xi-\mu)}$$

Bosons
$$Z = \sum_{n=0}^{N} e^{-n\beta(E-\mu)}$$

Let
$$\chi = \beta(\varepsilon - \mu)$$

Bosons:
$$Z_{g} = \sum_{n=0}^{\infty} e^{-nx} = \frac{1}{1-e^{-x}}$$

Fermions:
$$Z_F = \sum_{n=0}^{1} e^{-nx} = 1 + e^{-x}$$

Average occupancy

$$\bar{n} = \frac{1}{2} \sum_{n} n e^{-nx} = \frac{1}{2} \sum_{n} \left(-\frac{1}{2x} e^{-nx} \right)$$

Fermions

$$Z_F = 1.7e^{-x}$$

$$\frac{\partial Z}{\partial x} = -e^{-x}$$

$$\overline{n} = -\frac{1}{2} \frac{\partial \overline{x}}{\partial x} = -\frac{e^{-x}}{1 + e^{-x}} = \frac{1}{e^{x} + 1}$$

If
$$E = \mu$$
, $\bar{n} = \frac{1}{2}$

high 1



Bosons

$$\frac{\partial Z}{\partial x} = -(1 - e^{-x})^{-2}(-(e^{-x}))$$

$$= -\frac{e^{-x}}{(1 - e^{-x})^2} = -e^{-x}Z^2$$

$$\bar{n} = -\frac{1}{Z} \frac{\partial Z}{\partial x} = +\frac{1}{Z}(xe^{-x}Z^{\frac{1}{2}})$$

$$= \frac{e^{-x}}{1 - e^{-x}} e^{x} = \frac{1}{e^{x} - 1}$$

$$\bar{n} = e^{\frac{1}{RE-N} - 1} \quad \text{Bose-Einstein distribution}$$

$$\mathcal{E}_{x}\mu$$
 $\chi \text{ small}$
 $e^{x}-1$
 $\chi = \frac{1}{1+x-1} = \frac{1}{x} \text{ huge.}$

M is determined by
$$\sum_{s} \bar{n}_{s} = N$$
energy \bar{n}_{s}
microstate