Choose c items from a collection of Nitems If order matters, "permutation" (e.g. pres-both, vice-president, secretary) (4.9. · put all items in a line, & take first c of them N! ways to line things up can rearrange the rabble any way without changing result, so N' overcoults by a forctor of (N-c)! = N! Permutation If order desnit matter, you can rearrange the rabble and the chosen ones, so N! overcounts by (N-c)! and c! N-c) c! Combination (Which? P C) At in denom? 1 3 N choose $c':\begin{pmatrix} N \\ C \end{pmatrix} \equiv \frac{N!}{c!(N-c)!}$ binomial coefficient. $(x+y)^{3} = (x+y)(x+y) (x+y)$ $= \binom{3}{3}x^{3} + \binom{3}{2}x^{2}y + \binom{3}{1}xy^{2} + \binom{3}{0}y^{3}$ $(x+y)^{n} = \sum_{i=0}^{n} \binom{n}{i} x^{i} y^{n-i}$ choose 2 objects out of 5 $\binom{5}{2} = \frac{5!}{2! \ 3!} = \frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{(2 \cdot 1)(3 \cdot 2 \cdot)} = \frac{20}{2} = 10$ AP CD

AC CE

AD DE $\binom{0}{N} = \frac{N!}{N!} = \frac{1}{N!}$ $\binom{N}{N}$: 1 $\begin{pmatrix} N \\ \underline{A} \end{pmatrix} = \frac{N!}{1!(N-1)!} = N$ $\begin{pmatrix} c \\ N \end{pmatrix} = \begin{pmatrix} N - c \\ N \end{pmatrix}$

Very Large Numbers if N>>1, N is "large" N+12N 1023+521023 2N \$ N if N>> 1, then N!, N", 2", etc VLN X LN $10^{10^{23}} \times 10^{23} = 10^{10^{23} + 23} \approx 10^{10^{23}}$ NN! ZN! eg. N2"22" In (VLN) - LN so logarithms are handy when works with VLNs. VLN - In NN = NlmN R Shan = Nhaz ELN In N! = NIN N - N Stirling's approximation ln(10!); ln(3628000); 15.10 L.g. N=10 10la 10-10: 13.0 148 enos. for N=100, Stirling's approximation has a 0.8% error e.g. how many ways can I rearrange 50 red bolls 2 50 blue balls?

 $\Omega = \frac{100!}{60! \, \text{col}} =$ ln - 2 = ln 100! - ln 50! - ln 50!

≈ (100 ln 100 - 100) - (50 ln 50 - 50) - (50 l 50 - 50) = (100 m 100 - 50 lm 50 - 50 lm 50) + (-100 + 50 + 50) = 100 ln 100 - 100 ln 50

alub = luba ln = 100 ln 50 = 100 ln 2

1 ≈ 2100

NI = Ne Vain & (Ne).