

Physics 3410 Homework #7

4 problems

Due by March 21

▷ 1.

For the following four partial derivatives, write an equivalent derivative or ratio of thermodynamic variables. One of them is a Maxwell relation, one is a reciprocal Maxwell relation, and one involves the Gibbs-Duhem relation.

$$(a) \left(\frac{\partial \mu}{\partial P} \right)_T \quad (b) \left(\frac{\partial \mu}{\partial P} \right)_{N,S} \quad (c) \left(\frac{\partial N}{\partial V} \right)_{F,T} \quad (d) \left(\frac{\partial N}{\partial V} \right)_{P,T}$$

▷ 2.

Given one mole of diamond vs one mole of graphite,

	G	S	V
1 mol Graphite	0 J	5.74 J/K	5.30 cm ³
1 mol Diamond	2900 J	2.38 J/K	3.42 cm ³

(Assume S and V are constant over the temperatures and pressures we're considering, which is a reasonable approximation.)

(a) At room temperature 300 K, at what pressure does diamond become more stable?

(b) At standard pressure 10⁵ Pa, at what temperature does diamond become more stable?

▷ 3.

The fictional compound *hillonium* has two different solid phases, miranite and kevinite. At standard temperature and pressure,

- 1 mole of miranite has $G = 0$ J, entropy $S = 3$ J/K, and volume $V = 4$ cm³
- 1 mole of kevinite has $G = 500$ J, entropy $S = 5$ J/K, and volume $V = 3$ cm³

(a) Which is more stable at room temperature? That is, which one is more common?

(b) At what temperature does the other compound become stable?

▷ 4.

Use the Clausius-Clapeyron relation to find the slope of the liquid-gas phase transition line at the natural boiling point of water (i.e. $P = 10^5$ Pa, $T = 373$ K). Assume that the water vapor is an ideal gas, and that the water has mass density $\rho = 958$ kg/m³. (You'll also need that each molecule of water has mass $m = 3 \times 10^{-26}$ kg.)