$$|\Psi\rangle \rightarrow \int S_x$$

two ostputs

- 1) analyzer mill report a value (one of its eigenvalues)
- a) particle will change to a different state (one of 19s eigenvectors)

States are represented by normalized kets.

if  $\binom{1}{2}$  is an eigenvector of A

then  $\binom{2}{4}$  is as well  $\binom{-i}{-2i}$  etc.

$$\binom{1}{3}\binom{9}{4}=\binom{9}{6}$$
  $\implies$  Let  $a^{e}$ 

$$\binom{1}{3}\binom{1}{4}\binom{1}{c} = \lambda\binom{1}{c}$$

$$\begin{pmatrix}
1+2c \\
3+4c
\end{pmatrix} = \begin{pmatrix}
\lambda \\
\lambda c
\end{pmatrix} \longrightarrow$$

$$1+2c = \lambda c$$

$$3+4c = \lambda c$$

$$A = \sqrt{A^{2}} - \langle A \rangle^{2}$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\langle A \rangle = \langle \Psi | A | A | \Psi \rangle$$

$$\Delta S_{z} = \sqrt{\langle S_{z}^{2} \rangle} - \langle S_{z} \rangle^{2}$$

$$= \sqrt{\frac{t^{2}}{4} - 0} = \frac{t}{2}$$

$$S_{z} = 0 \pm \frac{t}{2}$$

```
Uncertainty Principle: Suppose thro operators A&B
measuring some state 14>
    (\Delta A)^2 = \langle (A - \langle A \rangle)^2 \rangle
             = \langle \Psi | (A - \langle A \rangle) (A - \langle A \rangle) | \Psi \rangle
              = <f1f> if 1f> = A-<A>) 14>
                                                         (A Hormitian)
   Ditto: 19> = (B-<B>) 14>
               (DB)2= < 519>
Couchy-Schwarz Inequality: \langle f|f\rangle\langle g|g\rangle \geq |\langle f|g\rangle|^2

(\Delta A)^2 (\Delta B)^2
  If Generally, if \bar{z} is a complex number  \frac{1}{2!} \left( (3-4i) - (3+4i) \right) 
 |z|^2 = (Re z)^2 + (Im z)^2 \ge (Im z)^2 
 \frac{1}{2!} (-8i) = -4 
                                   \left|\frac{1}{z}\right|^{2} \geq \left[\frac{1}{2i}\left(2-z^{*}\right)\right]^{2}
  (\Delta A)^{2} (\Delta B)^{2} = \left[\frac{1}{2\pi} \left(\langle f | g \rangle - \langle g | f \rangle\right)\right]^{2}
 <f19>= <41 (A-<A>) (B-(B) 14>
           = <41 ABI4> - <A> <41814>-<B> <4414)+42B>
           = < 4 | ABIY > - < A > & B >
            = <AB> - <A><B>
  <91f> = <BA> -<A><B>
   <f19>-<91f> = <AB>-<BA>
                           = < AB-BA> = < [A,B] >
       (\Delta A)^{2} (\Delta B)^{2} \geq (\frac{1}{2i})^{2} [A,B]^{2}
          DA DB = 2: ([A,B]) Uncertainty
principle
69. 9 14>29>
                                 [5x,54]
          ΔSx ΔSy ≥ \(\frac{1}{2i}\) \(\text{it S}_2\)
           Sx Sy ≥ to <Sz>
          ý 14> = 15> <Sz> = ±

∴ △Sx △Sy ≥ ±

4
                    in particular, netter ASX or ASY = 6.
y 14>= 10>
                             <53> = 0
                        DSx DSy ≥ 0.
```