I've been talking about 4(x). I could also talk about 4(p) instead. eq. What is the probability that a particle - has a momentum between -1 & 1. eg. What is probability that a particle has a position between -181. $P = \int_{-1}^{1} |\psi(x)|^2 dx$ $P = \int_{-1}^{1} |\Psi(p)|^2 dp$ $\psi(x) = \langle x | \psi \rangle$ $\psi(p) = \langle p|\psi \rangle = \int_{-\infty}^{\infty} \psi_p(x) \psi(x) dx$ I need Ψ_p in terms of χ . $\psi(p) = \sqrt{2\pi i} \int_{-\infty}^{\infty} e^{-ipx/k} \psi(x) dx$ $\psi(p) = \sqrt{2\pi i} e^{ipx/k}$ $p \psi(x) c p \psi(x)$ $\int |\psi_{p}|^{2} dx = 1$

Chapter 4! QM in three dimensions (Spherical coordinates) it = + H P $\frac{1}{2m} \frac{d^2}{dx^2} + V$ 3D, $H = -\frac{k^2}{\lambda m} \nabla^2 + \sqrt{\frac{k^2}{2m}}$ $\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$ 11/2 de 7 1 normalization If $\psi(r)$ are energy eigenstates, 1.e. $HY_n(r) : E_nY_n(r)$ then any $\Psi(\vec{r},t) = \sum_{n} c_n \Psi_n(\vec{r}) e^{-iEnt/t}$

assuming H is time-impendent

```
x=rcosp sino
  y= rsing sing
    3 = 1 cos 0
              \nabla^2 = \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left( \sin \theta \frac{\partial}{\partial \theta} \right) + \frac{1}{r^2 \sin \theta} \left( \frac{\partial^2}{\partial \theta^2} \right)
                  Laptacian in spherical coordinates
      Energy eigenstates satisfy H4=E4
        To solve, use separation of variables
                           \Psi(r,\theta,\phi) c \Re(r)\Theta(\theta)\Phi(\phi)
                   \overline{\bigoplus}^{"} = -m^2 \overline{\bigoplus}
                                -> D=Ae + Be-imp
Let m be + on -
           Because $+211 (>> $
                    \Phi(\phi+2\pi)=\Phi(\phi)
                    \Phi(\phi+2\pi)=e^{im\phi}e^{im2\pi}=e^{im\phi}
                                                      m must be an integer
\frac{1}{\Theta} \left[ \sin \theta \frac{\partial}{\partial \theta} \left( \sin \theta \frac{\partial \Theta}{\partial \theta} \right) + l(l+1) \sin^2 \theta \right] = m^2
                (O) = A P/ (cos O)
         Associated Legendre function
P_{e}(x) = (1-x^{2})^{|m|/2} \left(\frac{d}{dx}\right)^{|m|} P_{e}(x)
      Legendre polynomial
P_{2}(x) = 2^{\frac{1}{2}} \left( \frac{d}{dx} \right)^{2} (x^{2}-1)^{2}
         P_{\ell}(x) blows up in the -1 \le x \le 1 range unless \ell \ge 0.
    P_{\ell}^{m}(x) = \frac{1}{2^{\ell}\ell!} \left(1-x^{2}\right)^{lm/2} \left(\frac{d}{dx}\right)^{\ell+lml} \left(x^{2}-1\right)^{\ell}
            I can only take all derivatives of (x2-1)
              before I get zero, and so
                                    l+1m1 < 21
                                      1ml≤l
     m: -l, -l+1, +l+2, ..., l-1, l
\bigvee_{\ell}^{m}(\emptyset,\phi) = A e^{im\phi} P_{\ell}^{m}(\cos\theta) = \Theta(0) \overline{\Phi}(\phi)
     A = \sqrt{\frac{2l+1}{4\pi}} \frac{(l-|m|)!}{(l+|m|)!} \times \begin{cases} (-1)^m & m \ge 0 \\ 1 & m \le 0 \end{cases}
   Spherical harmonic functions
             Solo Ye Ver send do do = See, Smm.

Hey are of thogonal.
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