

$$\uparrow + \leftarrow = \nwarrow$$

A) \nearrow C) \searrow
 B) \nwarrow D) \swarrow



$$\downarrow - \rightarrow =$$

$$\downarrow + (-\rightarrow)$$

$$\downarrow + \leftarrow =$$

D \swarrow



$$\leftarrow + \downarrow =$$

Sum = \swarrow

A) \nwarrow B) \nearrow
 C) \swarrow D) \searrow



$$\leftarrow + \downarrow =$$

Sum \swarrow

$$\vec{A} = \rightarrow \quad 2\vec{A} = \overrightarrow{\quad\quad\quad}$$

$$\vec{A} - \vec{A} \rightleftharpoons$$

$\vec{0}$ zero vector
 arrow with no length
 vector with no magnitude

Changes

Δx "change in x "

does not mean $\Delta \times x$

DO NOT DO

THIS:

$$\frac{\Delta x}{\Delta t}$$

NO!

e.g. m : money in a bank account

$m_i = \$40$ at start of month

$m_f = \$10$ at end of month

$$\frac{10}{40} = \frac{1}{4}$$

$\Delta m =$ A) $+\$50$ B) $+\$30$ C) $-\$30$ D) $-\$50$

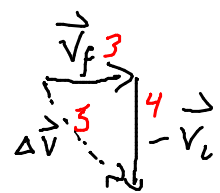
$$\Delta m = m_f - m_i$$

e.g. $\vec{v}_i = 4 \text{ m/s}$ $\vec{v}_f = 3 \text{ m/s}$ What is $\Delta \vec{v}$?

Direction: A) \nwarrow B) \nearrow C) \swarrow D) \searrow F)?

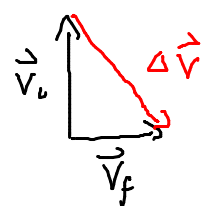
Magnitude: A) 1 m/s B) 5 m/s C) 7 m/s F)?

$$\Delta \vec{v} = \vec{v}_f - \vec{v}_i$$

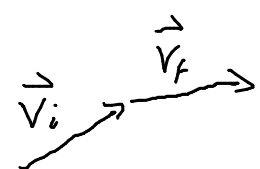


$$|\Delta \vec{v}| \neq |\vec{v}_f| - |\vec{v}_i|$$

$$\vec{v}_i + \Delta \vec{v} = \vec{v}_f$$



$\Delta \vec{v}$: vector to add to \vec{v}_i to get \vec{v}_f



$$\Delta \vec{v} =$$

A) \rightarrow

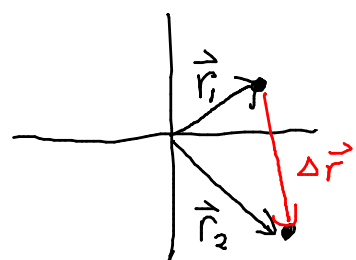
B) \downarrow

C) \leftarrow

D) \uparrow



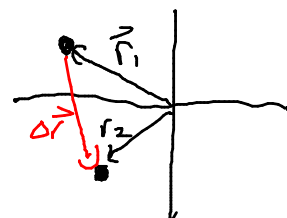
Position & Displacement



\vec{r} : position vector
for that point

$$\Delta \vec{r} = \vec{r}_2 - \vec{r}_1$$

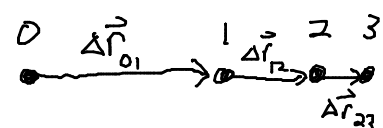
displacement



position vectors depend
on your choice of origin
& are arbitrary

displacement is not

Displacement can show up in physics equations
but position (almost) never will.



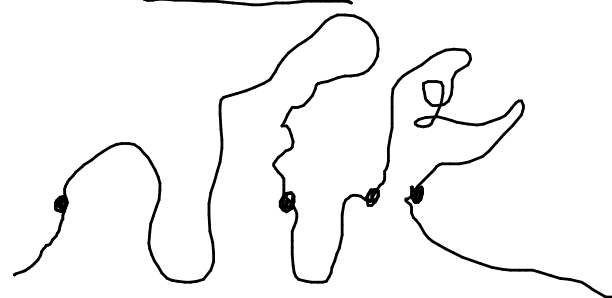
proportional

$$\vec{v} \propto \Delta \vec{r}$$

if Δt is large (1 hour, e.g.)
then \vec{v} is small

$$\vec{v} \propto \frac{1}{\Delta t}$$

$$\rightarrow \boxed{\vec{v} = \frac{\Delta \vec{r}}{\Delta t}} \quad \text{or} \quad \Delta \vec{r} = \vec{v} \Delta t$$



actual
velocity $\vec{v} = \frac{d\vec{r}}{dt}$ when $\Delta t \rightarrow 0$
(derivative $\frac{d\vec{r}}{dt}$)

when Δt isn't tiny

$\frac{\Delta \vec{r}}{\Delta t}$ "average velocity"