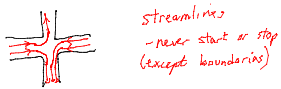
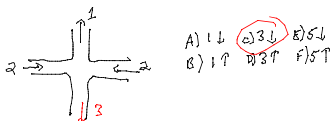
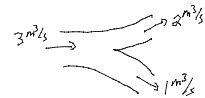
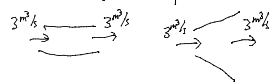


Flux: volume of fluid/s

phi Φ

flux in = flux out

when steady flow
and incompressible fluid (ρ constant)



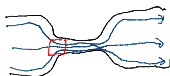
$$\Phi = A v$$

$$\frac{m^3}{s} = m^2 \frac{m}{s}$$

A: cross-sectional area
v: speed of water



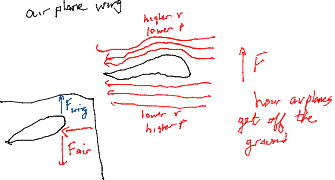
A: A gets smaller & Φ stays same
v gets bigger




Bernoulli's Principle
as speed increases, pressure decreases



air plane wing



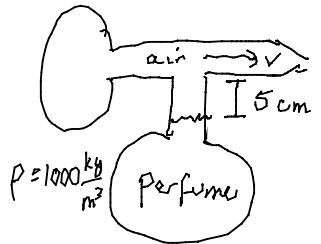

 artery
 blood
 obstruction
 can slow blood
 down, increase pressure

Bernoulli's Equation

$$P + \rho gh + \frac{1}{2} \rho v^2 = \text{constant}$$

if one term is constant
 and second term decreases
 then third term increases by same amount

- As v increases, P decreases
- As h decreases, P increases


 How fast must
 air go for perfume
 to reach it?

$\rho = 1000 \frac{\text{kg}}{\text{m}^3}$
 Perfume
 For perfume to rise,
 pressure of air has to
 drop by $\rho g (5\text{cm})$
 $= 490 \text{ Pa}$

for air pressure to drop by 490 Pa ,

$$490 \text{ Pa} = \frac{1}{2} \rho v^2$$

$$v^2 = \frac{2(490 \text{ Pa})}{(1.2 \text{ kg/m}^3)} \rightarrow v = 29 \text{ m/s}$$

• Viscosity

High viscosity - flows with difficulty

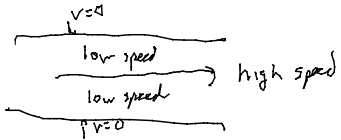
No viscosity - will flow through a pipe at constant speed forever

Viscous fluids need to be pushed or they will stop (friction)



$$\Delta P = 8 \pi \eta \frac{L V_{avg}}{A}$$

- η : viscosity coefficient
- L : length of pipe
- A : cross-sectional area
- V_{avg} : average speed



$$\text{Air } \eta = 1.8 \times 10^{-5} \text{ Pa} \cdot \text{s}$$

$$\begin{aligned} \text{Water } \eta &= 1.0 \times 10^{-3} \text{ Pa} \cdot \text{s} \text{ at } 20^\circ\text{C} \\ &= 0.7 \times 10^{-3} \text{ Pa} \cdot \text{s} \text{ at } 40^\circ\text{C} \end{aligned}$$

depends on temperature

$$\begin{aligned} \text{honey } 15^\circ\text{C} : \eta &= 600 \\ 40^\circ\text{C} : \eta &= 20 \end{aligned}$$