

$E = U_0 e^{ikx}$
 $U_0 = 0$
 $x=0$
 $k = \frac{\sqrt{2mE}}{\hbar}$
 $k' = \frac{\sqrt{2m(E-U_0)}}{\hbar}$

$\psi_L(x) = A e^{ikx} + B e^{-ikx}$
 $\psi_R(x) = C e^{ik'x}$
 $\psi_L(0) = \psi_R(0)$
 $A + B = C$
 $Aik - Bik = C i k'$
 $\hookrightarrow B = \frac{k-k'}{k+k'} A$ $C = \frac{2k}{k+k'} A$

$|A e^{ikx}|^2 = |A|^2$ is proportional to
 # of particles per unit length

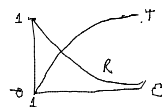
$\frac{\# \text{ particles}}{\text{time}} = \frac{\# \text{ particles}}{\text{distance}} \times \frac{\text{distance}}{\text{time}} = v \frac{\#}{\text{distance}}$
 $v = \frac{p}{m} = \frac{\hbar k}{m}$
 $\propto |A|^2 v \propto |A|^2 k$
 rate of incident particles

$R = \frac{\text{rate of reflected particles}}{\text{rate of incident particles}}$
 $= \frac{|B|^2 k}{|A|^2 k} = \left(\frac{k-k'}{k+k'} \right)^2$

$T = \frac{\text{rate transmitted}}{\text{rate incident}}$
 $= \frac{|C|^2 k'}{|A|^2 k} = \frac{4kk'}{(k+k')^2}$

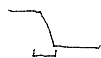
if $E = U_0$
 $k = \sqrt{U_0} \frac{\sqrt{2mE}}{\hbar}$ $k' = \sqrt{U_0} \frac{\sqrt{2m(E-U_0)}}{\hbar}$
 $R = \left(\frac{\sqrt{E} - \sqrt{E-1}}{\sqrt{E} + \sqrt{E-1}} \right)^2$ $T = \frac{4\sqrt{E}\sqrt{E-1}}{(\sqrt{E} + \sqrt{E-1})^2}$
 $R + T = 1$

if $E \gg 1$ $\sqrt{E-1} \ll 1$ $R \approx \left(\frac{\sqrt{E}}{\sqrt{E}} \right)^2 = 1$
 if $E \gg 1$ $R \approx 0$ $T \approx 1$



Would this work for a bowling ball? No

λ is an approximation



Change in U occurs over a distance d

if $d \ll \lambda$ of particles it looks vertical

for bowling ball, $\lambda \ll d$

so solution doesn't hold

for a realistic shelf