

In 2D or 3D,

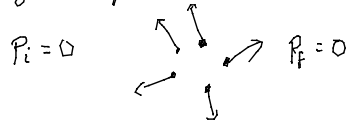
$$\Delta \vec{p} = \vec{p}_f - \vec{p}_i$$

if no net external force on system

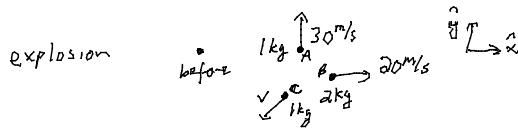
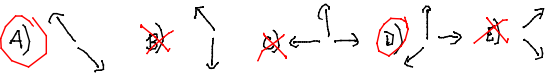
$$\vec{p}_f = \vec{p}_i$$

$$\vec{p}_{fx} = \vec{p}_{ix} \quad \vec{p}_{fy} = \vec{p}_{iy} \quad \vec{p}_{fz} = \vec{p}_{iz}$$

e.g. Explosions → an internal force



A bomb at rest explodes into 2 or 3 fragments.  
Which of these might show the path of those fragments? (Could be multiple.)



What is speed of C?

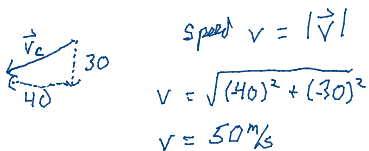
- A) 20 m/s   B) 30 m/s   C) 40 m/s   D) 50 m/s  
E) 60 m/s   F) 100 m/s

$$\vec{p}_A = 30 \frac{\text{kg} \cdot \text{m}}{\text{s}} \hat{y} \quad \vec{p}_B = 40 \frac{\text{kg} \cdot \text{m}}{\text{s}} \hat{x}$$

$$0 = \vec{p}_A + \vec{p}_B + \vec{p}_C = 30 \hat{y} + 40 \hat{x} + \vec{p}_C$$

$$-30 \hat{y} - 40 \hat{x} \frac{\text{kg} \cdot \text{m}}{\text{s}} = \vec{p}_C$$

$$\vec{v}_C = \frac{\vec{p}_C}{m} = \frac{-30 \hat{y} - 40 \hat{x} \frac{\text{kg} \cdot \text{m}}{\text{s}}}{1 \text{ kg}} = -30 \hat{y} - 40 \hat{x} \frac{\text{m}}{\text{s}}$$



$$\text{speed } v = |\vec{v}|$$

$$v = \sqrt{(40)^2 + (-30)^2}$$

$$v = 50 \text{ m/s}$$