

Angular acceleration

$$\alpha = \frac{\Delta \omega}{\Delta t} \quad \text{rad/s}^2$$

~~$\omega = 0 - 60 \text{ mph}$
in 5 s
 60 m/hr/s~~

Compare

$$v = \frac{\Delta x}{\Delta t} \quad a = \frac{\Delta v}{\Delta t}$$

$$\omega = \frac{\Delta \theta}{\Delta t} \quad \alpha = \frac{\Delta \omega}{\Delta t}$$

instead of $\Delta x = v_i \Delta t + \frac{1}{2} a (\Delta t)^2$

we get $\Delta \theta = \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2$

$$\omega_f = \omega_i + \alpha \Delta t$$

$$\omega_f^2 = \omega_i^2 + 2\alpha \Delta \theta$$

etc

Speeding up: α & ω same sign.

Slowing down: α & ω opposite sign

eg. Wheel spins initially at $5 \frac{\text{rev}}{\text{s}}$ ccw.
slows to a halt in 10s. α ?

A) $\Delta \theta$:

B) $\omega_i = 5 \frac{\text{rev}}{\text{s}} \times \frac{2\pi \text{ rad}}{1 \text{ rev}} = 10\pi \frac{\text{rad}}{\text{s}}$

C) $\omega_f = 0$

D) $\alpha = \text{NEED}$

E) $\Delta t = 10\text{s}$



$$\omega_f = \omega_i + \alpha \Delta t$$

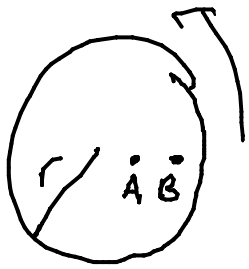
$$\frac{\omega_f - \omega_i}{\Delta t} = \alpha = \frac{0 - 10\pi \frac{\text{rad}}{\text{s}}}{10\text{s}} = -3.14 \frac{\text{rad}}{\text{s}^2}$$

How many times does it go around?

$$\Delta \theta = \frac{1}{2} (\omega_i + \omega_f) \Delta t$$

$$= \frac{1}{2} (10\pi + 0)(10\text{s}) = 50\pi \text{ rad}$$

$$50\pi \text{ rad} \times \frac{1 \text{ rev}}{2\pi \text{ rad}} = \boxed{25 \text{ rev}}$$



Which point has larger angular velocity?

A) A

B) B

C) Both same

All points on a rigid wheel have same angular velocity.

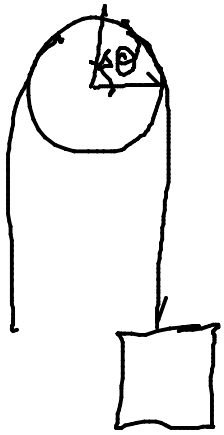
B has farther to go, in same amount of time, so its linear velocity is larger.

$$\text{distance} = r \Delta \theta \quad \leftarrow \text{radians}$$

$$\text{speed} = \frac{\text{distance}}{\text{time}} = r \frac{\Delta \theta}{\Delta t}$$

$$\boxed{v = r \omega} \quad \text{only for } \omega \text{ in rad/s,}$$

"faster" could mean "larger v "
or "larger ω "



point on pulley
moves through an
angle $\Delta\theta$
& move through a
distance $r\Delta\theta$

How far does block move then?

Block moves in sync with rope

Rope moves in sync with pulley

IF rope doesn't slip

radius of
↓ pulley

∴ rope & block move a distance $r\Delta\theta$

$$\frac{d}{\Delta t} = r \frac{\Delta\theta}{\Delta t}$$

speed of block = $r \times \omega$ of pulley

$$v = r\omega$$