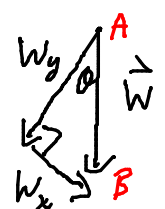


$$\vec{N} + \vec{S} + \vec{W} = 0$$

static equilibrium
(not moving)

$$\vec{N} = N \hat{y} \quad \vec{S} = -S \hat{x}$$



$$\vec{W} = mg(+\sin\theta \hat{x} - \cos\theta \hat{y})$$

which is θ ?

$$N \hat{y} - S \hat{x} + mg \sin\theta \hat{x} - mg \cos\theta \hat{y} = 0$$

$$(-S + mg \sin\theta) \hat{x} + (N - mg \cos\theta) \hat{y} = 0$$

$$\downarrow$$

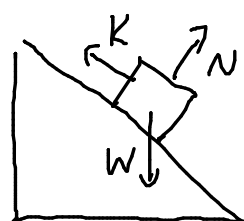
$$-S + mg \sin\theta = 0$$

$$\downarrow$$

$$N - mg \cos\theta = 0$$

$$S = mg \sin\theta$$

$$N = mg \cos\theta$$



$$K = mg \sin\theta \quad N = mg \cos\theta$$

but only if velocity is
constant

because $\vec{K} + \vec{N} + \vec{W} = m\vec{a}$

Kinetic friction does not adjust to balance other forces.

Therefore $K = mg \sin\theta$ is only true for one value of θ .

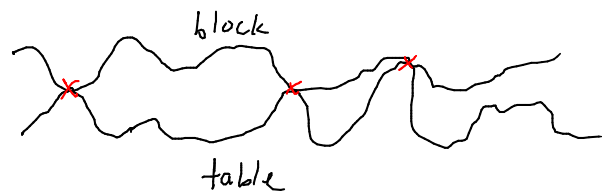
If θ is bigger, $mg \sin\theta$ "wins"
and block ~~accelerates~~ speeds up.

If θ is smaller, K "wins"
and block slows down.

How

How does friction work?

Microscopic scale



at these contact points, atoms of block & table will stick together

(if two completely flat surfaces they would cold-weld together)

As you slide block against table, these bonds form & break repeatedly
→ kinetic friction

If block sits on table, bonds have time to get stronger
→ static friction

Our model of friction gives us an average picture

$$|\vec{K}| = \mu_k |\vec{N}| \quad \leftarrow \text{normal force between surfaces}$$

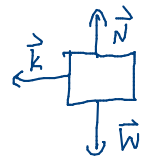
μ_k : coefficient of kinetic friction
unitless
 $\mu_k = \frac{|\vec{K}|}{|\vec{N}|}$

μ_k depends on type of surfaces

e.g. $\mu_k = 0.2$ wood against wood

$\mu_k = 0.8$ rubber against concrete

e.g. $m = 1 \text{ kg}$
 10 N
 $\mu_k = 0.5$
 $\Rightarrow v$
What is block's acceleration?
 $\vec{a} = \frac{\vec{F}_{\text{net}}}{m}$



This points
A) ← B) ↑ C) → D) ↓ E) other

$$\vec{N} + \vec{W} = 0 \rightarrow N = W = 10 \text{ N}$$

$$\vec{F}_{\text{net}} = \vec{K} = \leftarrow$$

$$K = \mu_k N$$

$$K = (0.5)(10 \text{ N}) = 5 \text{ N}$$

$$a = \frac{F_{\text{net}}}{m} = \frac{5 \text{ N}}{1 \text{ kg}} = 5 \text{ m/s}^2$$

Static Friction

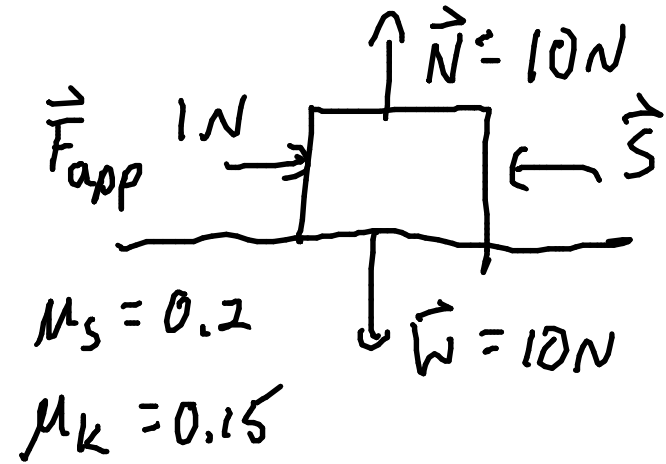
is adjustable unlike \vec{K}
but it's breakable

$$|\vec{S}| \leq \mu_s |\vec{N}|$$

μ_s : coefficient of static friction
usually $\mu_s \geq \mu_k$

e.g. egg on Teflon $\mu_s = 0.04$ wood on wood
 $\mu_s = 0.25 - 0.3$

boots on rock $\mu_s = 1.2$ $\mu_k = 0.2$



What is $|\vec{S}|$?

A) $0.2N$

B) $1N$

C) $1.5N$

D) $2N$

E) $10N$

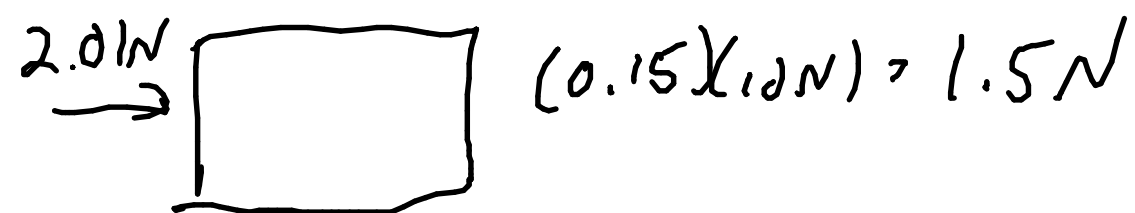
S will balance out
other forces

so long as $S \leq \mu_s N$

$$\mu_s N = (0.2)(10N) = 2N$$

$$1N \leq 2N \text{ so OK!}$$

if $F_{app} = 2.01N$ then static friction breaks
& kinetic friction takes over



$$F_{net} = 0.51N$$

sudden increase in F_{net}
and acceleration