

4) I throw a ball into the air at 5 m/s (straight up)

How long until it reaches the top of its flight?

$$\Delta y =$$

$$v_{iy} = +5\text{ m/s}$$

$$v_{fy} = 0\text{ m/s}$$

$$a_y = -9.8\text{ m/s}^2$$

$$\Delta t = \text{NEED}$$

$$v_f = v_i + a \Delta t$$

$$\Delta t = \frac{v_f - v_i}{a}$$

$$= \frac{0 - 5}{-9.8} = 0.51\text{ s}$$

0 top
+y ↑

5 m/s

Initial: right after ball leaves my hand

Final: top of its flight

• How long does it take to hit your hand again?

$$\Delta y =$$

$$v_{iy} = 0\text{ m/s}$$

$$v_{fy} =$$

$$a_y = -9.8\text{ m/s}^2$$

$$\Delta t = \text{NEED}$$

initial: top of its flight
final: right before it hits my hand

Can't solve this yet, but I could go back & get Δy

Instead,

Initial: when ball leaves my hand

$$\Delta y = 0\text{ m} \leftarrow \text{back where it started}$$

$$v_{iy} = +5\text{ m/s}$$

$$v_{fy} =$$

$$a_y = -9.8\text{ m/s}^2$$

$$\Delta t = \text{NEED}$$

$$\Delta y = v_i \Delta t + \frac{1}{2} a (\Delta t)^2$$

$$0 = 5 \Delta t - 4.9 (\Delta t)^2$$

$$= \Delta t [5 - 4.9 \Delta t]$$

$$\Rightarrow \Delta t = 0, \frac{5}{4.9} = 1.02\text{ s}$$

5/s ↑
5/s ↓

same time up as down

What is v_{fy} ?

$$v_{fy}^2 = v_{iy}^2 + 2a\Delta y$$

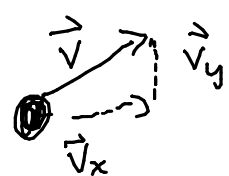
$$v_{fy}^2 = 25$$

$$v_{fy} = \pm 5\text{ m/s}$$

$$v_{fy} = -5\text{ m/s}$$

speed is same coming down as going up

Two-Dimensional Motion w/ Constant Acceleration

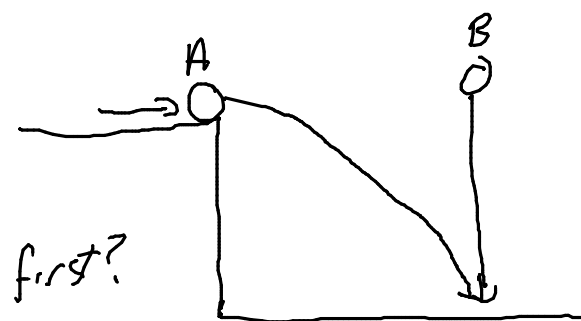


Δx
 v_{ix}
 v_{fx}
 a_x
 Δy
 v_{iy}
 v_{fy}
 a_y

- 9 unknowns
- 4 independent equations
- need 5 of these values

Dimensions are independent

e.g.



When A leaves the table, B is dropped

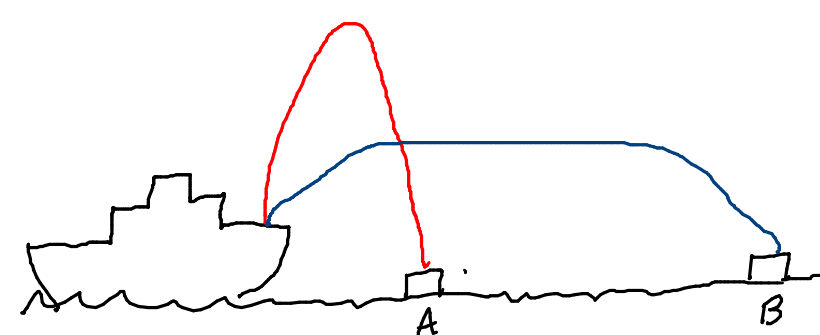
Which hits the ground first?

- A) A B) B
 C) Both at same time

Looking at vertical components

Δy is same for both
 $v_{iy} = 0$ is same for both (but A has additional x component)
 $a = 9.81$ for both.

so you can solve for Δt

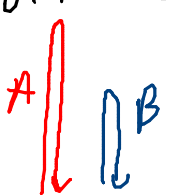


Cannon balls are not necessarily launched with same speed

Which target is hit first?

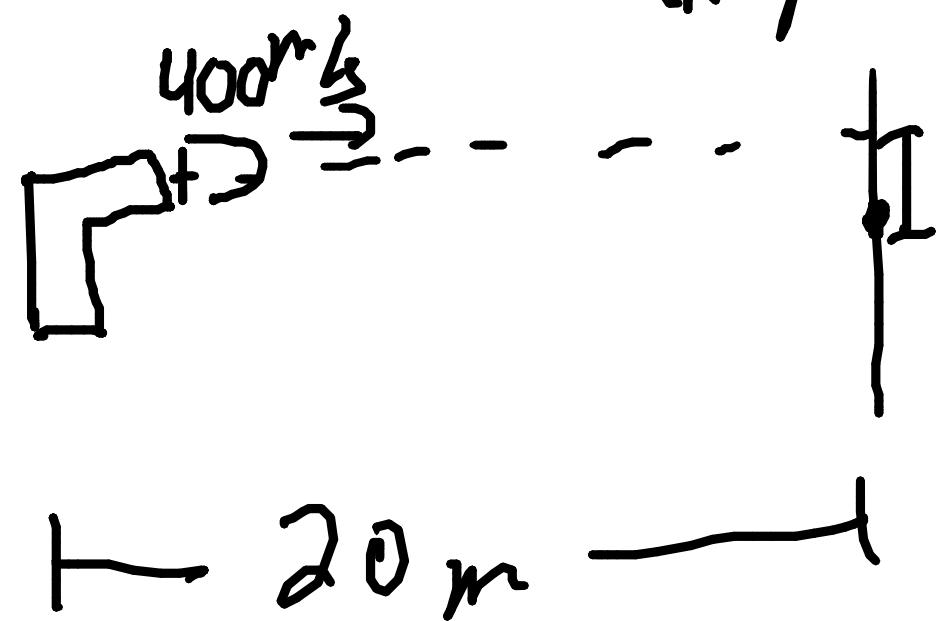
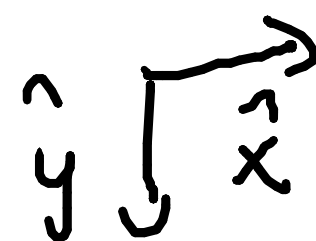
- A) A B) B C) Both the same

Look at vertical motion alone



Fire a bullet horizontally at 400 m/s at target
20 m away. How far below horizontal does bullet drop?

$$\begin{aligned}\Delta x &= 20\text{ m} & \Delta y &= \text{NEED} \\ v_{ix} &= 400\text{ m/s} & v_{iy} &= 0\text{ m/s} \\ v_{fx} & & v_{fy} & \\ a_x &= 0 & a_y &= 9.8\text{ m/s}^2\end{aligned}$$



$$\Delta t =$$

Can't solve y right away, (only 2 given)
So solve x column for Δt first.