

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \Psi}{\partial x^2} = i\hbar \frac{\partial \Psi}{\partial t} \quad F_{\text{net}} = 0$$

$$\Psi(x, t) = A e^{i(kx - \omega t)} \quad \frac{\hbar^2 k^2}{2m} = \hbar \omega$$

$$\hat{p} = A [\cos(kx - \omega t) + i \sin(kx - \omega t)] \frac{\hbar^2 k^2}{2m} = E$$

plane wave solution

prob. of finding particle at (x, t)

$$|\Psi|^2 = \Psi^* \Psi = (A^* e^{-i(kx - \omega t)}) A e^{i(kx - \omega t)} \\ = A^* A = |A|^2 = \text{constant}$$

equally likely to be found anywhere
perfect wave, no localization

Total probability = 1

$$\int_{-\infty}^{\infty} |\Psi|^2 dx = 1 \quad \text{solve this for } A.$$

if $|\Psi|^2 = \text{constant}$ & range $-\infty$ to ∞
then Ψ is unnormalizable & doesn't
describe a real object

so $A e^{i(kx - \omega t)}$ is not a real solution by
itself

BUT Schrodinger eq. is linear

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \Psi}{\partial x^2} = i\hbar \frac{\partial \Psi}{\partial t}$$

if Ψ_1 & Ψ_2 are solutions

then $\Psi_1 + \Psi_2$ is also a solution

Solutions to Sch eq are

linear combinations of $A_k e^{i(kx - \omega t)}$
w/ different values of k

And some of these combos are normalizable.

Uncertainty
 $x = 5m \pm 0.01m$

standard deviation
 $\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{N}}$
 Δx
 $5m \pm 0.01m$
 $x \pm \Delta x$

plane wave
 $\Delta x = +\infty$ location is completely unknown
 $\Delta p = \Delta(\hbar k) = 0$ momentum is perfectly known

Δx smaller
 $\Delta p \neq 0$ some uncertainty in λ

Δx is very small
 Δp is very uncertain

More certain x is,
 less certain $\lambda \rightarrow k \rightarrow p$ are

$\Delta x \Delta p \geq \frac{\hbar}{2}$ Heisenberg uncertainty principle

" \geq " depends on shape of $\psi(x, t)$

Neither Δx or $\Delta p = 0$
 so you cannot know exact location
 or exact momentum of an object.

Does an object even have an exact location? Some say yes, some no.

e.g. electron in an atom
 $\Delta x = 10^{-10}m$ (diameter of atom)

$\Delta p \geq \frac{\hbar}{2\Delta x} = 5 \times 10^{-25} \text{ kg m/s}$
 $\Delta v \geq \frac{\Delta p}{m} > 5.8 \times 10^5 \text{ m/s}$

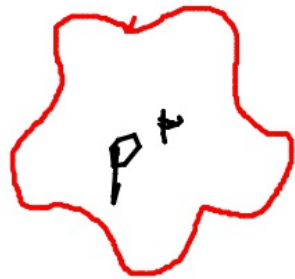
at that speed, electron
 can travel 1\AA (Δx) in $2 \times 10^{-14} \text{ s}$.

Electron could be anywhere in there
 - electrons are waves inside atoms.

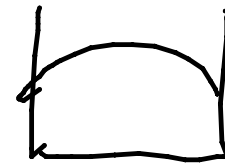
$p^+ e^-$
 e^- should slow down
 (accelerating charge gives off energy)
 and crash into p^+ if
 it's a particle

p^+

Electron forms a standing wave around the nucleus



And there is a minimum standing wave size



so electron can't

~~crash~~ get too close to p^+

Electron is not accelerating -
not orbiting nucleus -

so no radiation is given off \rightarrow stable atom.