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 $\begin{array}{cccccccc} H & H & H & H & H & H & H & H \\ T & T & T & T & T & T & T & T \end{array}$   
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2. a) 2 fair coins.

8 coins total.

$\frac{2}{8} \rightarrow \frac{1}{4}$  chance of fair coin.

b) There is a  $\frac{1}{2}$  chance the coin comes up heads.

c)  $P(F|R)$  - fair and TTH - P

$P(UTR)$  - unfair tails favored & TTH

$P(UH|R)$  - unfair heads favored & TTH

$P(F)$  - fair die chosen

$P(UT)$  - unfair tails favored die chosen

$P(UH)$  - unfair heads favored die chosen

$P(R)$  - roll was TTH

$$\begin{aligned} P(R) &= P(R|F) \cdot P(F) + P(R|UT) \cdot P(UT) + P(R|UH) \cdot P(UH) \\ &= (.25 \cdot .25) + (.140625 \cdot .375) + (.046875 \cdot .375) \\ &= .1328125 \end{aligned}$$

$$P(F|R) = P(R|F) \cdot \frac{P(F)}{P(R)} = .25 \cdot \frac{(.14)}{.1328125} = .471$$

The probability that the coin was fair given the flips TTH is .471.

d)  $P(H)$  - probability of heads

$P(F)$  - probability of fair

$$P(H) = \frac{1}{2}$$

$$P(H|F) = \frac{1}{2}$$

Since  $P(H)$  and  $P(H|F)$  are equal, the events are independent.