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CSCI 3104, Algorithms Requiz Standard 6, Version A

Profs. Chen & Grochow Spring 2020, CU-Boulder

Instructions: This quiz is open book and open note. You may post clarification questions to Piazza, with the understanding that you may not receive an answer in time and posting does count towards your time limit (30 min for 1x, 37.5 min for 1.5x, 45 min for 2x). Questions posted to Piazza must be posted as **PRIVATE QUESTIONS.** Other use of the internet, including searching for answers or posting to sites like Chegg, is strictly prohibited and will count as violations of the academic honor code. Such violations are, at a minimum, grounds to receive a 0. Proofs should be written in complete sentences. Show and justify all work to receive full credit.

Standard 6. Using the pluq-in/unroll/substitution method, solve the following recurrence relation.

$$T(n) = \begin{cases} 11 & : n < 3, \\ 5T(n-3) + 13 & : n \ge 3. \end{cases}$$
 (1)

T(n) = ST(n-3) + 13
= S(5T(n-6)+13)+13
= 52T(n-6)+(1+5)13
$= s^{2}(sT(n-9)+13)+(1+s)(3)$
$= 5^3 T (n-9) + (1+5+5^2) 13$
, b.1:
() +(n) = 5 + T(n-3k) + 13 = 5
Solve for 12:
n-3k 43 (base (ase)
n-3k c3 (base (asc) +3k +3k
$\frac{1}{100} + \frac{1}{100} + \frac{1}{100} = \frac{1}{100} + \frac{1}{100} = \frac{1}{100} + \frac{1}{100} = \frac{1}$
-3 -3 3
Plug back-in: p-1. Est is a geometric scries,
Plug back-ini del 120 13 a geometric scres,
Plug back-in: 4-1. [25] 13 a geometric scree, 120 T(n) = 5 (n-3)/3 + 13 &
250 1-5
Plug back in to recovence.
T(=)= 9 +13.1-5
$T(x) = \frac{5}{5} \frac{(n-3)/3}{+13 \cdot \frac{1-5}{1-5}}$ $= \frac{5}{5} \frac{(n-3)/3}{-13 \cdot (1-5)^{1/3}}$
$= \Theta(5^{(n-3)/3}) $ simplify $\Theta(5^{n/3})$
$= \underbrace{\Theta\left(5^{(n-3)/3}\right)}_{= \underbrace{\Theta\left(5^{(n-3)/3}\right)}} \text{ simplify} \underbrace{\Theta\left(5^{n/3}\right)}_{= \underbrace{\Theta\left(5^{(n-3)/3}\right)}}$
1 0 0 7