

Assignment 3

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QUESTION 1

a) We can use list to store the number of retailers, warehouse capacity and retailer's demand and dictionary to store transportation cost between supply and demand.

c) Let X_{ij} be the amount supplied from location i to location j

Constraints:

$$\text{Min (Z)} = \sum C_{ij}X_{ij}$$

Minimize Z (cost) where Z=

$$2X_{11} + 4X_{12} + 5X_{13} + 2X_{14} + X_{15} + 3X_{21} + X_{22} + 3X_{23} + 2X_{24} + 3X_{25}$$

Supply Constraints:

$$X_{11} + X_{12} + X_{13} + X_{14} + X_{15} \leq 2000$$

$$X_{21} + X_{22} + X_{23} + X_{24} + X_{25} \leq 3000$$

Demand Constraints:

$$X_{11} + X_{21} = 500$$

$$X_{12} + X_{22} = 800$$

$$X_{13} + X_{23} = 1800$$

$$X_{14} + X_{24} = 300$$

$$X_{15} + X_{25} = 700$$

Non-Negativity Constraints:

$$X_{1j} \geq 0$$

$$X_{2j} \geq 0$$

QUESTION 2:

Let X_{ij} be the amount supplied from location i to location j and C_{ij} be the transportation cost of supplying one unit of product from location i to location j

$$\text{Min (Z)} = \sum C_{ij}X_{ij}$$

$$\text{Min(Z)} = 9X_{11} + 14X_{12} + 12X_{13} + 17X_{14} + 11X_{21} + 10X_{22} + 6X_{23} + 10X_{24} + 12X_{31} + 8X_{32} + 15X_{33} + 7X_{34}$$

Supply Constraints:

$$X_{11} + X_{12} + X_{13} + X_{14} \leq 200$$

$$X_{21} + X_{22} + X_{24} \leq 200$$

$$X_{31} + X_{32} + X_{33} + X_{34} \leq 200$$

Demand Constraints:

$$X_{11} + X_{21} + X_{31} = 130$$

$$X_{12} + X_{22} + X_{32} = 170$$

$$X_{13} + X_{23} + X_{33} = 100$$

$$X_{14} + X_{24} + X_{34} = 150$$

Where $X_{ij} \geq 0$

QUESTION 3:

Let X_{ij} be the amount supplied from location i to location j and C_{ij} be the transportation cost of supplying one unit of product from location i to location j

Step 2:

$$\text{Min (Z)} = \sum C_{ij}X_{ij}$$

$$\text{Min(Z)} = 16X_{14} + 21X_{15} + 18X_{24} + 16X_{25} + 22X_{34} + 25X_{35} + 23X_{46} + 15X_{47} + 29X_{48} + 20X_{56} + 17X_{57} + 24X_{58}$$

Supply Constraints:

$$X_{14} + X_{15} = 72$$

$$X_{24} + X_{25} = 105$$

$$X_{34} + X_{35} = 83$$

Transshipment Constraints:

$$X_{14} + X_{24} + X_{34} = X_{46} + X_{47} + X_{48}$$

$$X_{15} + X_{25} + X_{35} = X_{56} + X_{57} + X_{58}$$

Demand Constraints:

$$X_{46} + X_{56} \leq 90$$

$$X_{47} + X_{57} \leq 80$$

Where $X_{ij} \geq 0$

QUESTION 4:

c. Let X_{ij} be the selection of caterers to the events and for simplicity I belongs to $\{A,B,C,D,E,F,G\}$ and J belongs to $\{1,2,3,4,5,6\}$

Minimize $Z =$

$$\begin{aligned}
 &12.6X_{A1} + 10.3X_{A2} + 14.0X_{A3} + 19.5X_{A4} + 25.0X_{A5} + 30.0X_{A6} + \\
 &14.5X_{B1} + 13.0X_{B2} + 16.5X_{B3} + 17.0X_{B4} + 22.5X_{B5} + 32.0X_{B6} + \\
 &13.0X_{C1} + 14.0X_{C2} + 17.6X_{C3} + 21.5X_{C4} + 23.0X_{C5} + 35.0X_{C6} + \\
 &11.5X_{D1} + 12.6X_{D2} + 13.0X_{D3} + 18.7X_{D4} + 26.2X_{D5} + 33.5X_{D6} + \\
 &10.8X_{E1} + 11.9X_{E2} + 12.9X_{E3} + 17.5X_{E4} + 21.9X_{E5} + 28.5X_{E6} + \\
 &13.5X_{F1} + 13.5X_{F2} + 15.5X_{F3} + 22.3X_{F4} + 24.5X_{F5} + 36.0X_{F6} + \\
 &12.5X_{G1} + 14.3X_{G2} + 16.0X_{G3} + 22.0X_{G4} + 26.7X_{G5} + 34.0X_{G6}
 \end{aligned}$$

Subject to:

Constraints:

Supply Constraint

$$X_{A1} + X_{A2} + X_{A3} + X_{A4} + X_{A5} + X_{A6} \leq 1$$

$$X_{B1} + X_{B2} + X_{B3} + X_{B4} + X_{B5} + X_{B6} \leq 2$$

$$X_{C1} + X_{C2} + X_{C3} + X_{C4} + X_{C5} + X_{C6} \leq 2$$

$$X_{D1} + X_{D2} + X_{D3} + X_{D4} + X_{D5} + X_{D6} \leq 1$$

$$X_{E1} + X_{E2} + X_{E3} + X_{E4} + X_{E5} + X_{E6} \leq 1$$

$$X_{F1} + X_{F2} + X_{F3} + X_{F4} + X_{F5} + X_{F6} \leq 1$$

$$X_{G1} + X_{G2} + X_{G3} + X_{G4} + X_{G5} + X_{G6} \leq 2$$

Demand Constraint

$$X_{A1} + X_{B1} + X_{C1} + X_{D1} + X_{E1} + X_{F1} + X_{G1} = 1$$

$$X_{A2} + X_{B2} + X_{C2} + X_{D2} + X_{E2} + X_{F2} + X_{G2} = 1$$

$$X_{A3} + X_{B3} + X_{C3} + X_{D3} + X_{E3} + X_{F3} + X_{G3} = 1$$

$$X_{A4} + X_{B4} + X_{C4} + X_{D4} + X_{E4} + X_{F4} + X_{G4} = 1$$

$$X_{A5} + X_{B5} + X_{C5} + X_{D5} + X_{E5} + X_{F5} + X_{G5} = 1$$

$$X_{A6} + X_{B6} + X_{C6} + X_{D6} + X_{E6} + X_{F6} + X_{G6} = 1$$

Where $X_{ij} \geq 0$

