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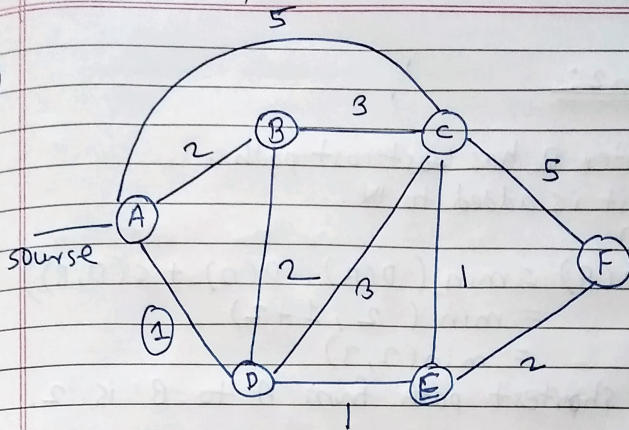
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→ Find link cost from nodes A to F using link state broadcast algorithm

⇒ $c(i, j)$ = link cost from node i to node j
 $D(v)$ = cost from source node to destination v that has least cost
 $P(v)$ = previous node (neighbor of v) along with least cost path from v
 N = total number of nodes available

Step 1 :

Source is A

A to B → 2

A to C → 5

A to D → 1

A to E → ∞

A to F → ∞

Step	N	$D(B), P(B)$	$D(C), P(C)$	$D(D), P(D)$	$D(E), P(E)$
1	A	2, A	5, A	1, A	∞
				$D(E), P(E)$	∞

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Vertex D has least cost path.

 \therefore it is added to N. $v = B, w = D$

$$\begin{aligned}
 \therefore D(B) &= \min(D(B), D(D) + c(D, B)) \\
 &= \min(2, 1+2) \\
 &= \min(2, 3)
 \end{aligned}$$

 \therefore shortest path from A to B is 2. $v = C, w = D$

$$\begin{aligned}
 D(C) &= \min(D(C), D(D) + c(D, C)) \\
 &= \min(5, 1+3) \\
 &= \min(5, 4)
 \end{aligned}$$

 \therefore shortest path from A to C is 4 $v = E, w = D$

$$\begin{aligned}
 D(E) &= \min(D(E), D(D) + c(D, E)) \\
 &= \min(\infty, 1+1) \\
 &= \min(\infty, 2)
 \end{aligned}$$

 \therefore shortest path from A to E is 2. $D(F)$ is ∞

step	N	$D(B), P(B)$	$D(C), P(C)$	$D(D), P(D)$	$D(E), P(E)$	$D(F), P(F)$
1	A	2, A	5, A	1, A	∞	∞
2	A, D	2, A	4, D		2, D	∞

Step 3:

Both E & B have least cost path is step 2.
Have to determine the least cost path of remaining vertices through E.

$$v=B, w=E$$

$$\begin{aligned} D(B) &= \min(D(B), D(E) + c(E, B)) \\ &= \min(2, 2 + \infty) \\ &= \min(2, \infty) \end{aligned}$$

Shortest path from A to B is 2.

$$v=C, w=E$$

$$\begin{aligned} D(C) &= \min(D(C), D(E) + c(E, C)) \\ &= \min(4, 2 + 1) \\ &= \min(4, 3) \end{aligned}$$

\therefore shortest path from A to C is 3

$$v=F, w=E$$

$$\begin{aligned} D(F) &= \min(D(F), D(E) + c(E, F)) \\ &= \min(\infty, 2 + 2) \\ &= \min(\infty, 4) \end{aligned}$$

shortest path from A to F is 4

Step	N	$D(B), p(B)$	$D(C), p(C)$	$D(D), p(D)$	$D(E), p(E)$	$D(F), p(F)$
1	A	2, A	5, A	1, A	∞	∞
2	AD	2, A	4, D		2, D	∞
3	ADE	2, A	3, E			4, E

Step 4:

B vertex has least cost path in step 3.

\therefore It is added in N.

Now, need to determine the least cost path of remaining vertices through B.

$$v = C, w = B$$

$$\begin{aligned} D(B) &= \min(D(C), D(B) + c(B, C)) \\ &= \min(3, 2 + 3) \\ &= \min(3, 5) \end{aligned}$$

\therefore shortest path from A to C is 3

$$v = F, w = B$$

$$\begin{aligned} D(B) &= \min(D(F), D(B) + c(B, F)) \\ &= \min(4, \infty) \\ &= \min(4, \infty) \end{aligned}$$

\therefore shortest path from A to F is 4.

Step	N	$D(B), P(B)$	$D(C), P(C)$	$D(D), P(D)$	$D(E), P(E)$	$D(F), P(F)$
1	A	2, A	5, A	1, A	∞	∞
2	AD	2, A	4, D		2, D	∞
3	ADE	2, A	3, E			4, E
4	ADEB		3, E			4, E

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Step 5:

C vertex has the least cost path in step 4.
 \therefore it is added to N.

Now, need to determine least cost path of remaining vertices through C.

$$V = F, w = C$$

$$\begin{aligned} D(B) &= \min(D(F), D(C) + c(C, F)) \\ &= \min(4, 3 + 5) \\ &= \min(4, 8) \end{aligned}$$

\therefore shortest path from A to F is 4.

step	N	$D(B), P(B)$	$D(C), P(C)$	$D(D), P(D)$	$D(E), P(E)$
5	ADEBC		3, E		4, E

Final table :-

step	N	$D(B), P(B)$	$D(C), P(C)$	$D(D), P(D)$	$D(E), P(E)$	$D(F), P(F)$
1	A	2, A	5, A	1, A	∞	∞
2	AD	2, A	4, D		2, D	∞
3	ADE	2, A	3, E			4, E
4	ADEB		3, E			4, E
5	ADEBC					4, E
6	ADEBCF					