

FLOATING POINT NUMBERS

- In some numbers, which have a fractional part, the position of the decimal point is not fixed as the number of bits before (or after) the decimal point may vary.
- Eg: 0010.01001, 0.0001101, -1001001.01** etc.
- As shown above, the position of the decimal point is not fixed, instead it **"floats"** in the number.
- For doubts contact Bharat Sir on 98204 08217
- Such numbers are called Floating Point Numbers.
- Floating Point Numbers are stored in a "Normalized" form.

NORMALIZATION OF A FLOATING POINT NUMBER

- Normalization is the process of shifting the point, left or right, so that there is only one non-zero digit to the left of the point. #Please refer Bharat Sir's Lecture Notes for this ...

<u>Floating Point Number</u>		<u>Normalized Number</u>
01010.01	→	$(-1)^0 \times 1.01001 \times 2^3$
11111.01	→	$(-1)^0 \times 1.111101 \times 2^4$
0.00101	→	$(-1)^0 \times 1.01 \times 2^{-3}$
-10.01	→	$(-1)^1 \times 1.001 \times 2^1$

- As seen above a Normalized Form of a number is:

$$(-1)^S \times 1.M \times 2^E$$

Where: S = Sign, M = Mantissa and E = Exponent.

- As Normalized numbers are of the 1.M format, the **"1"** is not actually stored, it is instead **assumed**. This saves the storage space by 1 bit for each number.
- Also the Exponent is stored in the biased form by adding an appropriate bias value to it so that -ve exponents can be easily represented.

Advantages of Normalization.

- Storing all numbers in a standard for makes **calculations easier** and **faster**.
- By **not storing** the **1** (of 1.M format) for a number, considerable **storage space** is **saved**.
- The **exponent** is **biased** so there is **no need** for **storing** its **sign bit** (as the biased exponent cannot be -ve).



SHORT REAL FORMAT / SINGLE PRECISION FORMAT / IEEE 754: 32 BIT FORMAT

S	Biased Exponent	Mantissa
(1)	(8) Bias value = 127	(23 bits)

- **32 bits** are used to store the **number**.
- **23 bits** are used for the **Mantissa**.
- **8 bits** are used for the Biased **Exponent**.
- **1 bit** used for the **Sign** of the number.
- The **Bias** value is $(127)_{10}$.
- The range is $\pm 1 \times 10^{-38}$ to $\pm 3 \times 10^{38}$ approximately.
- It is called as the **Single Precision Format** for Floating-Point Numbers.

LONG REAL FORMAT / DOUBLE PRECISION FORMAT / IEEE 754: 64 BIT FORMAT

S	Biased Exponent	Mantissa
(1)	(11) Bias value = 1023	(52 bits)

- **64 bits** are used to store the **number**.
- **52 bits** are used for the **Mantissa**.
- **11 bits** are used for the Biased **Exponent**.
- **1 bit** used for the **Sign** of the number.
- The **Bias** value is $(1023)_{10}$.
- The range is $\pm 10^{-308}$ to $\pm 10^{308}$ approximately.
- It is called as the **Double Precision Format** for Floating-Point Numbers.

Numericals on Floating Point Number Representation

1) Convert 2A3BH into Short Real and Temp Real formats {Exam question}

Short real:

Converting the number into binary we get:

0010 1010 0011 1011

Normalizing the number we get:

$$(-1)^0 \times 1.0101000111011 \times 2^{13}$$

Here S = 0; M = 0101000111011; True Exponent = 13.

Bias value for Short Real format is 127:

$$\begin{aligned} \text{Biased Exponent (BE)} &= \text{True Exponent} + \text{Bias} \\ &= 13 + 127 \\ &= 140. \end{aligned}$$

Converting the Biased exponent into binary we get:

Biased Exponent (BE) = (1000 1100)

Representing in the required format we get:

0	10001100	010100011101100...
S	Biased Exp	Mantissa
(1)	(8)	(23)

Converting the number into hexadecimal form we get:

4628EC00H ... 32 bits.

Temp real:

Bias value for Temp Real format is 16383:

$$\begin{aligned} \text{Biased Exponent (BE)} &= \text{True Exponent} + \text{Bias} \\ &= 13 + 16383 \\ &= 16396. \end{aligned}$$

Converting the Biased exponent into binary we get:

Biased Exponent (BE) = (100 0000 0000 1100)

Representing in the required format we get:

0	1000000000001100	1010100011101100...
S	Biased Exp	Mantissa
(1)	(15)	(64)

Converting the number into hexadecimal form we get:

400C A8EC 0000 0000 0000H ... 80 bits.



2) Convert $(12.125)_d$ into Temp Real format {Exam question}

Temp real:

Converting the number into binary we get:

1100.001 For doubts contact Bharat Sir on 98204 08217

Normalizing the number we get:

$$(-1)^0 \times 1.100001 \times 2^3$$

Here $S = 0$; $M = 100001$; True Exponent = 3.

Bias value for Temp Real format is 16383:

$$\begin{aligned} \text{Biased Exponent (BE)} &= \text{True Exponent} + \text{Bias} \\ &= 3 + 16383 \\ &= 16386. \end{aligned}$$

Converting the Biased exponent into binary we get:

Biased Exponent (BE) = (100 0000 0000 0010)

Representing in the required format we get:

0	1000000000000010	110000100000...
S	Biased Exp	Mantissa
(1)	(8)	(23)

Converting the number into hexadecimal form we get:

4002 C200 0000 0000 0000H ... 80 bits.