

NLP Numericals-3

Q1. Convert the following CFG grammar into CNF form

$S \rightarrow A | cB | c$

$A \rightarrow Bc | b$

$B \rightarrow cAA | \epsilon$

CNF

$V \rightarrow V_1 V_2$

$V \rightarrow T$

Step 1 - Remove Null Production

$S \rightarrow A | cB | c$

$A \rightarrow Bc | b | c$

$B \rightarrow cAA$

Step 2 Remove Unit Production

$S \rightarrow Bc | b | c | cB$

$A \rightarrow Bc | b | c$

$B \rightarrow cAA$

Step 3

Adding $X \rightarrow AA$ $Y \rightarrow c$

$S \rightarrow BY | b | c | YB$

$A \rightarrow BY | b | c$

$B \rightarrow YX$

$X \rightarrow AA$

$Y \rightarrow c$

Q2 Construct a parse tree for the following sentence using CFG rules: "The man read this book"

Rules:

S → NP VP

S → VP

NP → Det Nom

Nom → Noun

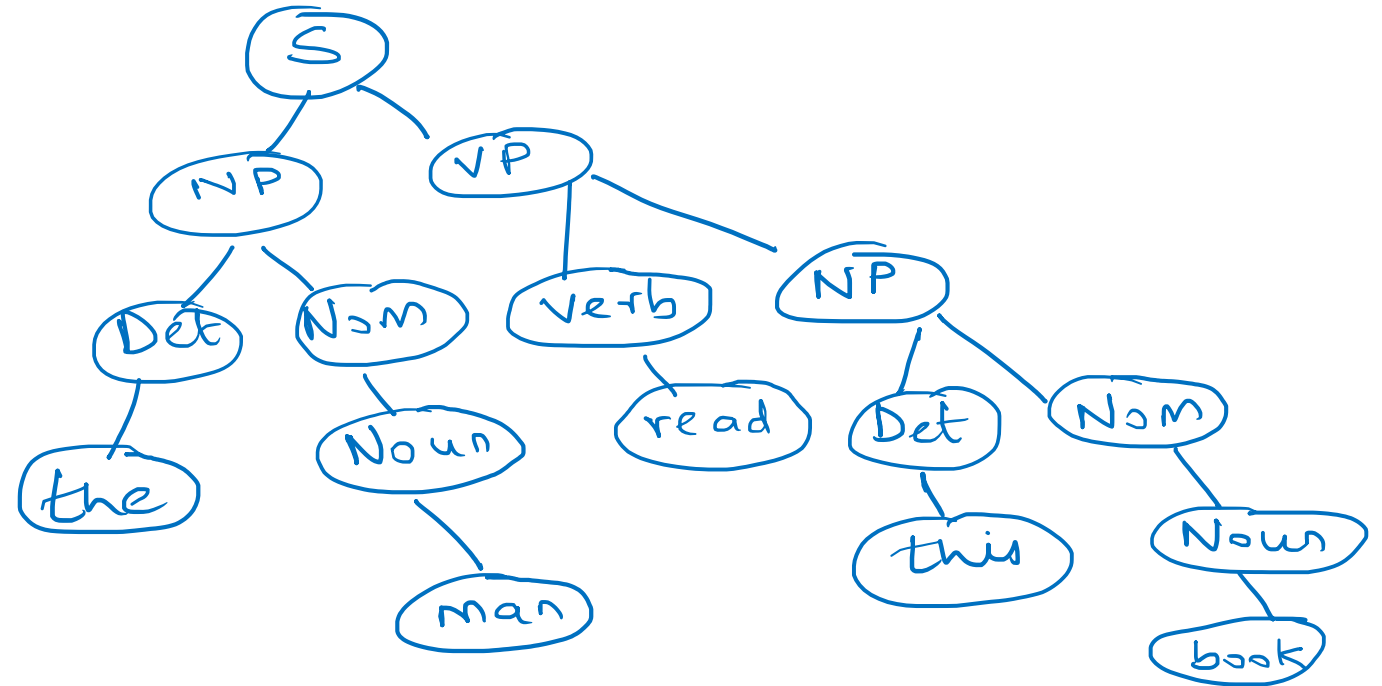
VP → verb NP

Verb → read

Det → the, this

Noun → book, man

Verb → book, read



Q3.Using the CKY algorithm find the possible parse tree for the following statement:” **A pilot likes flying planes**” using the following rules

S->NP VP

VP->VBG NNS

VP->VBZ VP

NP->DT NN

NP->JJ NNS

DT->a

NN->pilot

VBZ->likes

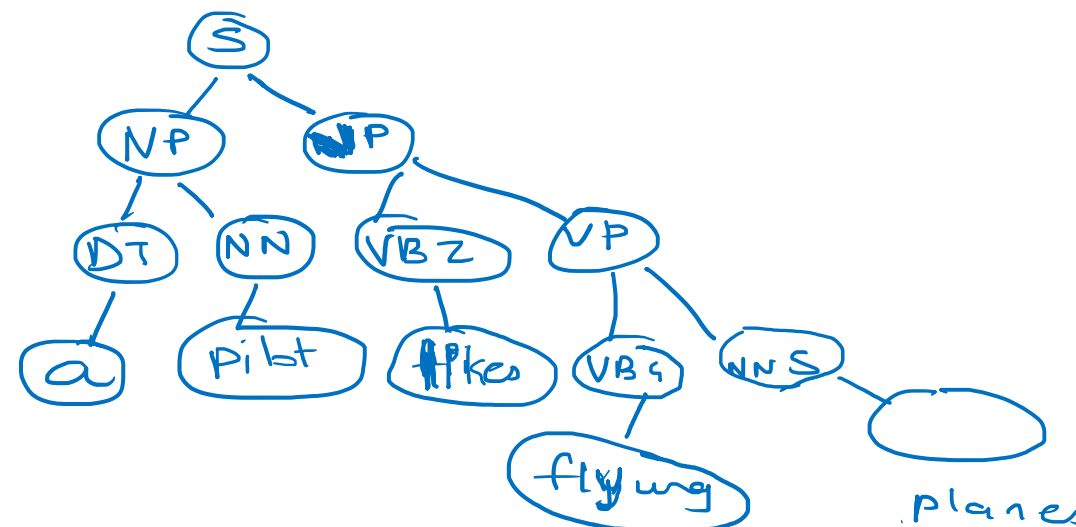
VBG->flying

JJ->>flying

NNS->planes

A	pilot	likes	flying	planes
DT α_{01}	NP α_{02}	— α_{03}	— α_{04}	S α_{05}
	NN α_{12}	— α_{13}	— α_{14}	— α_{15}
		VBZ α_{23}	= α_{24}	VP α_{25}
			VBG JJ α_{34}	VP NP α_{35}
				NNS α_{45}

$$\begin{aligned}\alpha_{02} &\rightarrow \alpha_{01} \alpha_{12} \\ \alpha_{13} &= \alpha_{12} \alpha_{23} \\ \alpha_{03} &= \alpha_{02} \alpha_{13} \\ \alpha_{24} &= \alpha_{23} \alpha_{34} \\ \alpha_{35} &= \alpha_{34} \alpha_{45} \\ \alpha_{25} &= \alpha_{23} \alpha_{35} \\ \alpha_{05} &= \alpha_{02} \alpha_{25}\end{aligned}$$



Q4. Find the probability of string **aaab** using the given PCFG

$S \rightarrow AB$ 0.5

$S \rightarrow BC$ 0.5

$A \rightarrow BA$ 0.3

$A \rightarrow a$ 0.7

$B \rightarrow CC$ 0.4

$B \rightarrow b$ 0.6

$C \rightarrow AB$ 0.2

$C \rightarrow a$ 0.8

① $S \rightarrow AB$ (0.5)

$S \rightarrow aB$ (0.7)

$S \rightarrow aCC$ (0.4)

$S \rightarrow aaC$ (0.8)

$S \rightarrow aaAB$ (0.2)

$S \rightarrow aaaB$ (0.7)

$S \rightarrow aaab$ (0.6)

$$P_1 = 0.5 \times 0.7 \times 0.4 \\ \times 0.8 \times 0.2 \times 0.7 \\ \times 0.6$$

$$P_1 = 0.009408$$

② $S \rightarrow BC$ (0.5)

$S \rightarrow C C C$ (0.4)

$S \rightarrow aCC$ (0.8)

$S \rightarrow aaC$ (0.8)

$S \rightarrow aaAB$ (0.2)

$S \rightarrow aaaB$ (0.7)

$S \rightarrow aaab$ (0.6)

$$P_2 = 0.5 \times 0.4 \times 0.8 \times 0.8 \\ \times 0.2 \times 0.7 \times 0.6$$

$$P_2 = 0.010752$$

$$\begin{aligned}
 \textcircled{1} \quad S &\rightarrow AB & (0.5) \\
 S &\rightarrow BAB & (0.3) \\
 S &\rightarrow CAB & (0.4) \\
 S &\rightarrow aCAB & (0.8) \\
 S &\rightarrow aaAB & (0.8) \\
 S &\rightarrow aaaaB & (0.7) \\
 S &\rightarrow aaaa b & (0.6)
 \end{aligned}$$

$$\begin{aligned}
 P_3 &= 0.5 \times 0.3 \times 0.4 \times 0.8 \\
 &\quad \times 0.8 \times 0.7 \times 0.6
 \end{aligned}$$

$$P_3 = 0.01612$$

$$\begin{aligned}
 P(aaab) &= P_1 + P_2 + P_3 \\
 &= 0.009408 + \\
 &\quad 0.01075 + \\
 &\quad 0.01612 \\
 &= \underline{\underline{0.0363}}
 \end{aligned}$$

Q5. Find the probability of the sentence: **astronomers saw stars with ears** using the given PCFG

S → NP VP 1.0

VP → V NP 0.7

VP → VP PP 0.3

PP → P NP 1.0

P → with 1.0

V → saw 1.0

NP → NP PP 0.4

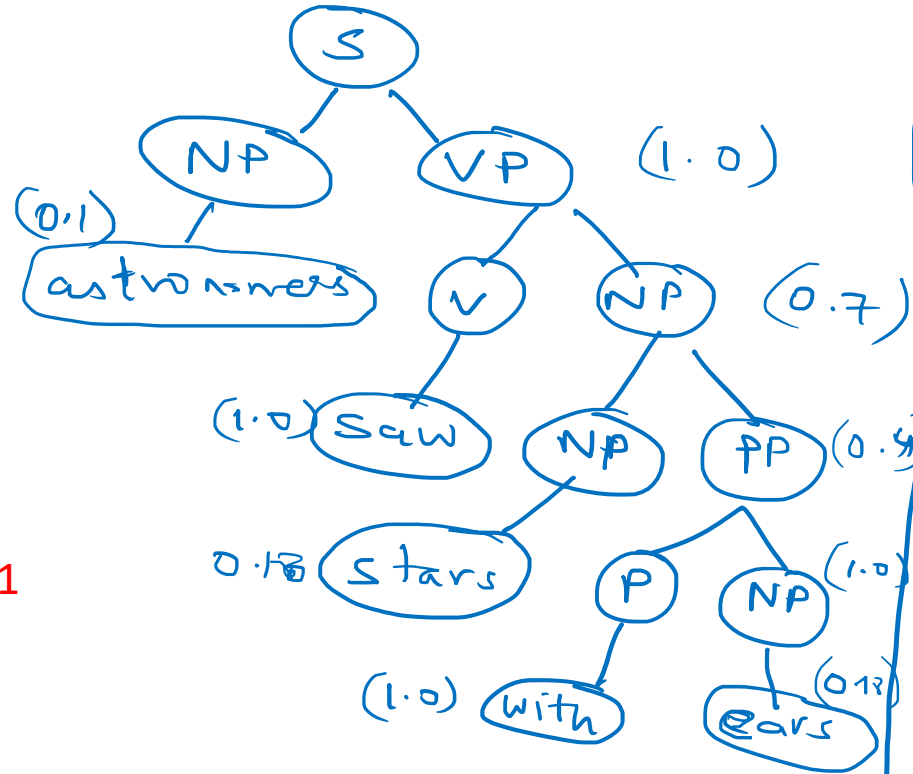
NP → astronomers 0.1

NP → ears 0.18

NP → saw 0.04

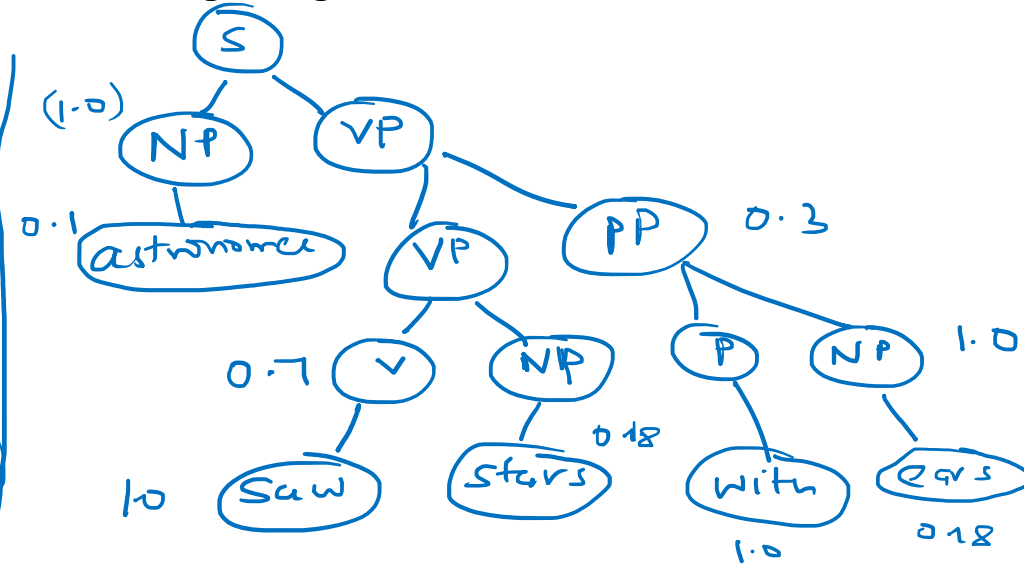
NP → stars 0.18

NP → telescope 0.1



$$P_1 = 1 \times 0.1 \times 0.7 \times 1 \times 0.4 \times 0.18 \times 1 \times 1 \times 0.18$$

$$P_1 = 0.0009072$$



$$P_2 = 1 \times 0.1 \times 0.3 \times 0.7 \times 1.0 \times 1.0 \times 0.18 \times 1.0 \times 0.18 = 0.00068$$

$$P(s) = P_1 + P_2 = 0.00158 //$$