

Time: 30 minutes

Max. Marks: 10

Name and Roll No.: \_\_\_\_\_

**Instructions:**

- Do not plagiarize. Do not assist your classmates in plagiarism.
- Show your full solution for the questions to get full credit.
- Attempt all questions that you can.
- True / False questions will get full credit only if the justification and answer are both correct.
- A multiple choice question may have one or more correct answers. Credit will only be awarded if all correct answers are marked and none of the incorrect answers are marked.
- Match the following questions will have partial grading.
- In the unlikely case that you find a question ambiguous, discuss it with an invigilating TA/invigilator. Please ensure that you clearly write any assumptions you make, even after clarification from the invigilator.

**V. Imp.:** If you do not write your **Name and Roll No.**, you will get a zero.

1. (2 points) Rank the following on how well the entities on the right satisfy the property listed on the left. Write your answer in the form of  $X > Y > Z$ .

- a) Fully Observable: driving; document classification; tutoring a student  
 b) Static: chat room; tennis; chess; tax planning

**Solution:**

- a) Fully Observable: document classification > driving > tutoring a student  
 b) Static: tax planning > chess > chat room > tennis

2. (2 points) Match the left & right columns in the table below. Assume that the sports activities are done in the physical world by human agents.

|   |                             |
|---|-----------------------------|
| A. Playing Soccer                         | I. {PO, St, Sq, D, C, MA}   |
| B. Playing a tennis match                 | II. {FO, St, Ep, D, C, MA.} |
| C. Practicing tennis against a wall       | III. {FO, St, Ep, D, C, SA} |
| D. Shopping for AI books on the Internet. | IV. {PO, Dt, Sq, S, Ds, SA} |

**Legend:** {[PO: partially observable, FO: fully observable] [Dt: deterministic, St: stochastic], [Sq: sequential, Ep: episodic], [S: static, D: dynamic], [Ds: discrete, C: continuous], [SA: single-agent, MA: multi-agent]}.

**Solution:**

**A-I;B-II;C-III;D-IV**

3. (1 point) Prove each of the following statements by specifying the evaluation function  $f(n)$ , or give a counterexample.

- (a) (0.25 point) Breadth-first search is a special case of A\* search.  
 (b) ( $3 \times 0.25 = 0.75$  points) Breadth-first search, Depth-first search and Uniform-cost search are all special cases of Best-first search.

**Solution:**

- (a) When all step costs are equal,  $g(n) \propto \text{depth}(n)$ , and  $h(n) = 0$ , A\* search reproduces breadth-first search.
- (b) BFS:  $f(n) = \text{depth}(n)$ ; DFS:  $f(n) = -\text{depth}(n)$ ; UCS:  $f(n) = g(n)$ .
4. (5 points) Consider the unbounded version of the 2D grid. The initial state is at origin  $(0,0)$  and the goal state is at some  $(x,y)$ . The links are connected to the immediate next nodes in the left, right, up and down directions. For each of the following, answer True or False and provide justification.
- (a)  $h = |u - x| + |v - y|$  is an admissible heuristic for a state at  $(u, v)$ .  
**True.** Since only 4-neighbors (left, right, up & down) are being considered, the smallest distance between two adjacent nodes will be given by  $h$ , which will underestimate the total distance. Therefore, it is an admissible heuristic.
- (b) If certain links are removed, the heuristic  $h$  is no longer admissible.  
**False .** Removing the links will not affect the smallest distance, therefore the heuristic will remain admissible. Adding links, however, will render this heuristic inadmissible (e.g., if 8-neighbors are considered, the heuristic function will no longer underestimate the Euclidean distance between two states). *Note:* In the 2D grid, we implicitly assume that the Euclidean distance between two states is the default evaluation function that is used.
- (c) If new links are added to connect non-adjacent nodes, the heuristic  $h$  remains admissible.  
**False.** Diagonal links could result in a shorter path than the heuristic, making it inadmissible.
- (d) Depth-first search always expands at least as many nodes as A\* search with an admissible heuristic.  
**False:** A lucky DFS might expand exactly  $d$  nodes to reach the goal. A\* largely dominates any graph-search algorithm that is guaranteed to find optimal solutions.
- (e) A reflex-agent does not make use of percepts from the environment.  
**False.** It does not use a *history of percepts*, but picks an action based on its current percept only.