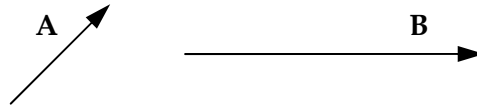
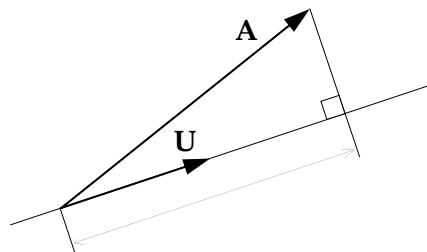


## 1. The Basics

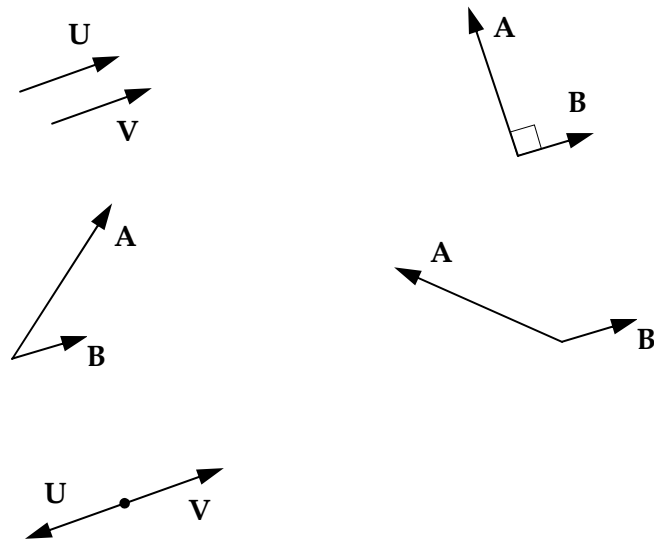
a) Given vectors **A** and **B** as shown, draw the following:



- $\mathbf{A} + \mathbf{B}$
  - $\mathbf{A} - \mathbf{B}$
  - $-\frac{1}{2} \mathbf{A}$
- b) Write two equations for calculating the dot product  $\mathbf{A} \cdot \mathbf{B}$ , where  $\mathbf{A} = [A_x \ A_y \ A_z]$  and  $\mathbf{B} = [B_x \ B_y \ B_z]$ .
- $\mathbf{A} \cdot \mathbf{B} =$
  - $\mathbf{A} \cdot \mathbf{B} =$
- c) Draw  $\mathbf{A} \cdot \mathbf{U}$  on the diagram, given that  $|\mathbf{U}| = 1$ .

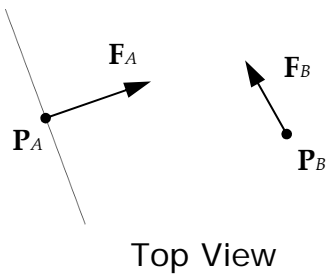


- d) For each pair of vectors **A** and **B**, or **U** and **V**, write an inequality indicating the sign of the dot product... or if possible, write the exact value of the dot product. Note that  $|\mathbf{U}| = |\mathbf{V}| = 1$ , while  $|\mathbf{A}| \neq 1$  and  $|\mathbf{B}| \neq 1$ .



## 2. Can you see me?

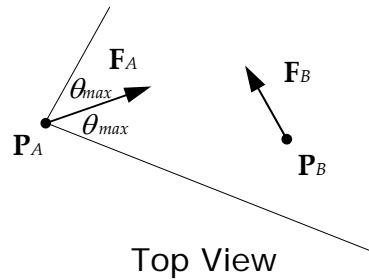
Two characters are standing on a roughly horizontal planar surface. The position of character A is  $\mathbf{P}_A$  and its forward-facing unit vector is  $\mathbf{F}_A$ . Likewise the position and forward vector of character B are  $\mathbf{P}_B$  and  $\mathbf{F}_B$  respectively.



- a) Use the sign of a dot product to determine whether character B is in front of or behind character A.

- b) Assume both characters have a vision cone extending  $\theta_{max}$  radians to either side of their  $\mathbf{F}$  vectors. Write an expression (using a dot product) indicating whether or not character A can “see” character B.

BONUS: How can we avoid finding the inverse cosine,  $\cos^{-1}(\theta_{max})$ ?



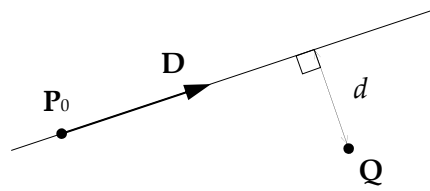
### 3. Wind Tunnel

The designers want to implement a shaft of wind that will affect any character or object that enters its cylindrical boundary.

- a) You are given an arbitrary point  $\mathbf{Q}$  in 3D space, and an infinite line represented by the locus of points  $\mathbf{P}(t)$  defined as follows:

$$\mathbf{P}(t) = \mathbf{P}_0 + t\mathbf{D},$$

where  $\mathbf{P}_0$  is a fixed point on the line, and  $\mathbf{D}$  is a unit vector defining the line's direction. Find the perpendicular distance  $d$  from  $\mathbf{Q}$  to the line.



- b) The cylindrical wind tunnel can be defined by adding a radius  $r$  and length  $L$  to the infinite line from part (a). Assuming the position of our object or character is  $\mathbf{Q}$ , write an expression that can be used to determine whether it will be affected by the wind or not.

