

University of Southern California

Viterbi School of Engineering

EE352

Computer Organization and Architecture

Stack Frames

References:

- 1) Textbook
- 2) Mark Redekopp's slide series

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Arguments and Return Values

- MIPS convention is to use certain registers for this task
 - \$a0 - \$a3 used to pass up to 4 arguments. If more arguments, use the stack
 - \$v0 used for return value
 - Only 1 return value but it may be a double-word (64-bits) in which case \$v1 will also be used

Number	Name	Purpose
\$0	\$zero	Constant 0
\$1	\$at	Assembler temporary (psuedo-instrucs.)
\$2-\$3	\$v0-\$v1	Return value (\$v1 only used for dword)
\$4-\$7	\$a0-\$a3	Arguments (first 4 of a subroutine)
\$8-\$15, \$24,\$25	\$t0-\$t9	Temporary registers
\$16-\$23	\$s0-\$s7	Saved registers
\$26-\$27	\$k0-\$k1	Kernel reserved
\$28	\$gp	Global pointer (static global data var's.)
\$29	\$sp	Stack pointer
\$30	\$fp	Frame pointer
\$31	\$ra	Return address

Arguments and Return Values

```
void main() {  
    int ans,arg1,arg2;  
    ans = avg(arg1, arg2);  
}  
  
int avg(int a, int b) {  
    int temp=1; // local var's  
    return a+b >> temp;  
}
```

C Code

```
...  
MAIN:  la    $s1, arg1  
       la    $s2, arg2  
       lw    $a0, 0($s0)  
       lw    $a1, 0($s1)  
       jal   AVG  
       sw    $v0, ($s2)  
...  
AVG:   li    $t0, 1  
       add   $v0,$a0,$a1  
       srav  $v0,$v0,$t0  
       jr    $ra
```

Equivalent Assembly

Assembly & HLL's

- When coding in assembly, a programmer can optimize usage of registers and store only what is needed to memory/stack
 - Can pass additional arguments in registers (beyond \$a0-\$a3)
 - Can allocate variables to registers (not use memory)
 - Can handle spilling registers to memory only when necessary
- When coding in an HLL & using a compiler, certain conventions are followed that may lead to heavier usage of the stack and memory

Compiler Handling of Subroutines

- High level languages (HLL) use the stack:
 - to save register values including the return address
 - to pass additional arguments to a subroutine
 - for storage of local variables declared in the subroutine
- Compilers usually create a data structure called a “frame” on the stack to store this information each time a subroutine is called
- To access this data structure on the stack a pointer called the “frame pointer” (\$fp) is often used in addition to the normal stack pointer (\$sp)

Stack Frame Motivation

- The caller needs to ensure the callee routine does not overwrite a needed register
 1. Caller may have his own arguments in \$a0-\$a3 and then need to call a subroutine and use \$a0-\$a3
 2. Return address (\$ra)
 3. Register values calculated before the call but used after the call (e.g. \$s0)

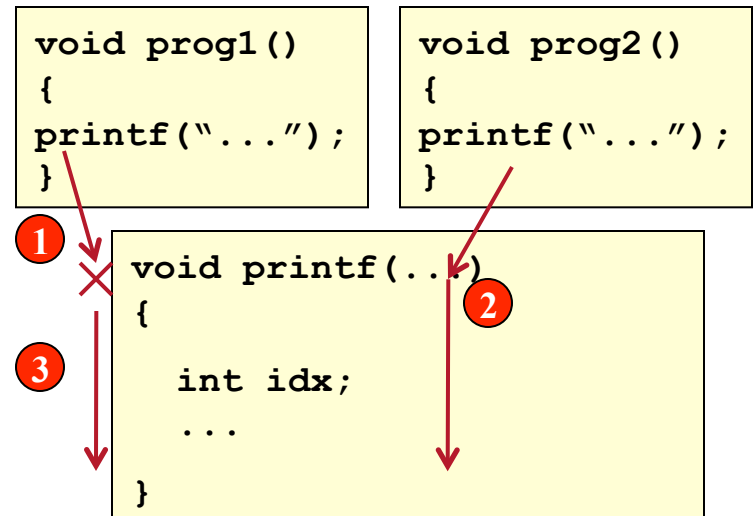
	.text	
MAIN:	lw \$a0, 0(\$t0)	
	lw \$a1, 0(\$t1)	
	jal CALLER	
	...	
CALLER:	lw \$s0, 0(\$a0)	1
	addi \$s0, \$s0, 2	3
	li \$a0, 5	1
	jal CALLEE	2
	add \$s0, \$a0, \$s0	1
	jr \$ra	2
CALLEE:	addi \$s0, \$a0, 5	3
	sra \$v0, \$s0, 1	
	jr \$ra	2

More Stack Frame Motivation

- **Recursive** and **re-entrant** routines need multiple copies of their local variables
 - Recursive routines have multiple copies of arguments and local variables alive at the same time (i.e. fact(3), fact(2), fact(1) will all be live at the same time)
 - In multitasking system, multiple processes may be calling the same routine (i.e. prog1 calls printf and then blocks while prog2 executes and calls printf as well)
- The stack can be used to allow each instance of a routine having its own storage

```
int fact(int n){  
    if(n == 1) return 1;  
    else  
        return n*fact(n-1);  
}
```

Recursive Routine
(multiple copies of n)



Re-entrant Routine
(multiple copies of idx)

MIPS Register Conventions

- Highlighted registers should be “preserved” across subroutine calls (i.e. the callee must save/restore that register if it needs to use it)
- Non-highlighted registers may be overwritten freely by a subroutine
 - Thus the caller must **save/restore** any needed registers **before/after** calling the routine

Number	Name	Purpose
\$0	\$zero	Constant 0
\$1	\$at	Assembler temporary (psuedo-instrucs.)
\$2-\$3	\$v0-\$v1	Return value (\$v1 only used for dwords)
\$4-\$7	\$a0-\$a3	Arguments (first 4 of a subroutine)
\$8-\$15, \$24,\$25	\$t0-\$t9	Temporary registers
\$16-\$23	\$s0-\$s7	Saved registers
\$26-\$27	\$k0-\$k1	Kernel reserved
\$28	\$gp	Global pointer (static global data var's.)
\$29	\$sp	Stack pointer
\$30	\$fp	Frame pointer
\$31	\$ra	Return address

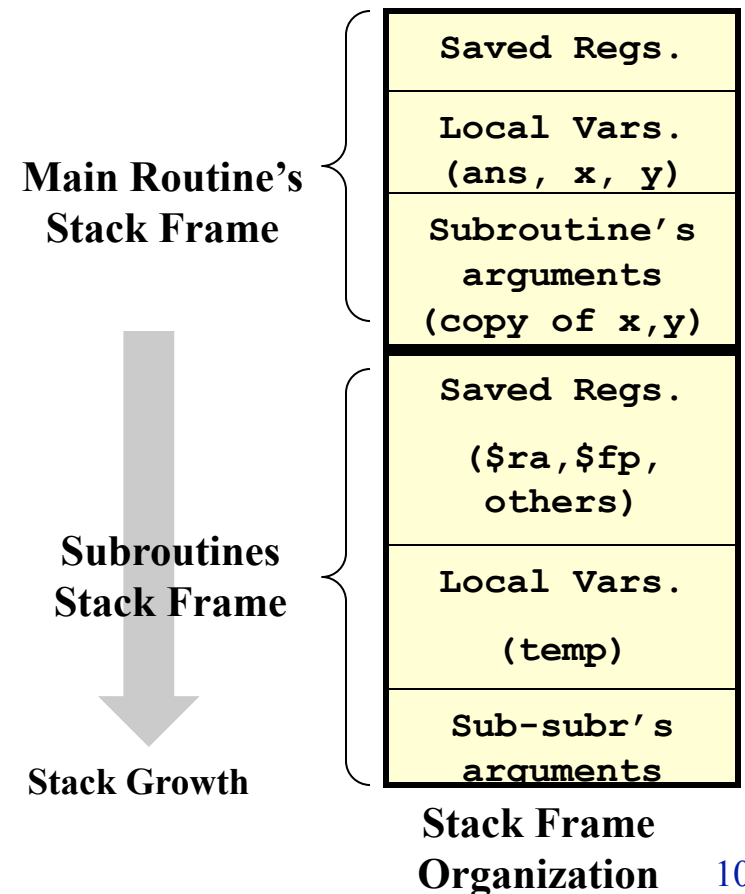
MIPS Register Storage Convention

- MIPS suggests the following convention for who is responsible for saving register values onto the stack
 - Caller is responsible for
 - Saving any `$a0-$a3`, `$t0-$t9`, `$v0-$v1` it will need after the call to the subroutine
 - Stuffing `$a0-$a3` with arguments for the "callee"
 - Pushing additional args. for the "callee" on the stack
 - Callee is responsible for
 - Saving `$ra`, `$fp`, & any `$s0-$s7` it uses
 - Allocating space on the stack for its own local vars.

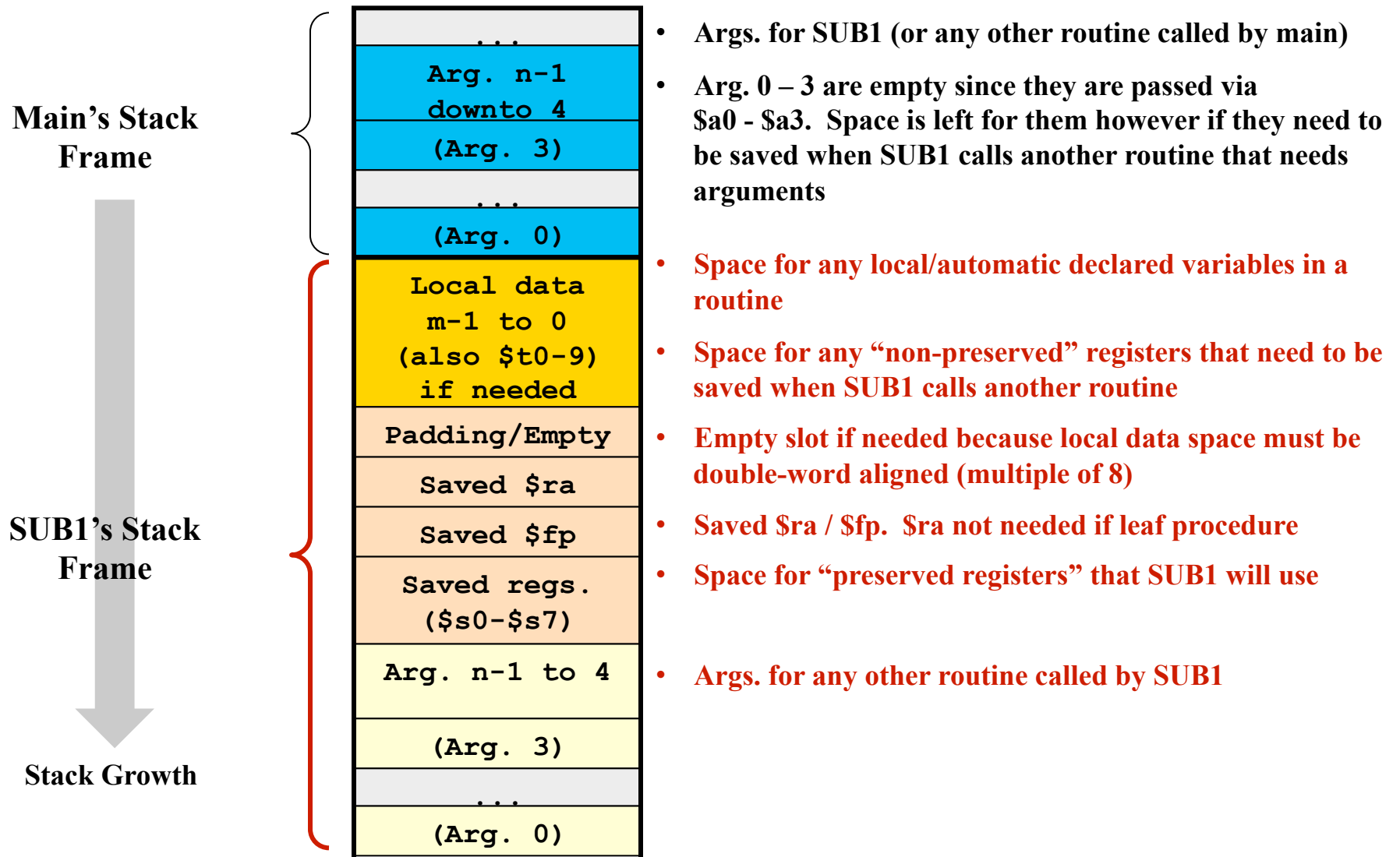
Stack Frames

- Frame = All data on stack belonging to a routine
 - Location for arguments (in addition to \$a0-\$a3)
 - Location for saved registers (\$fp, \$s0-\$s7, \$ra)
 - Location for local variables (those declared in a function)
- See section A.6 in textbook and PDF handout

```
void main() {  
    int ans, x, y;  
    ...  
    ans = avg(x, y);  
}  
  
int avg(int a, int b) {  
    int temp=1; // local var's  
    ...  
}
```



Stack Frame Organization

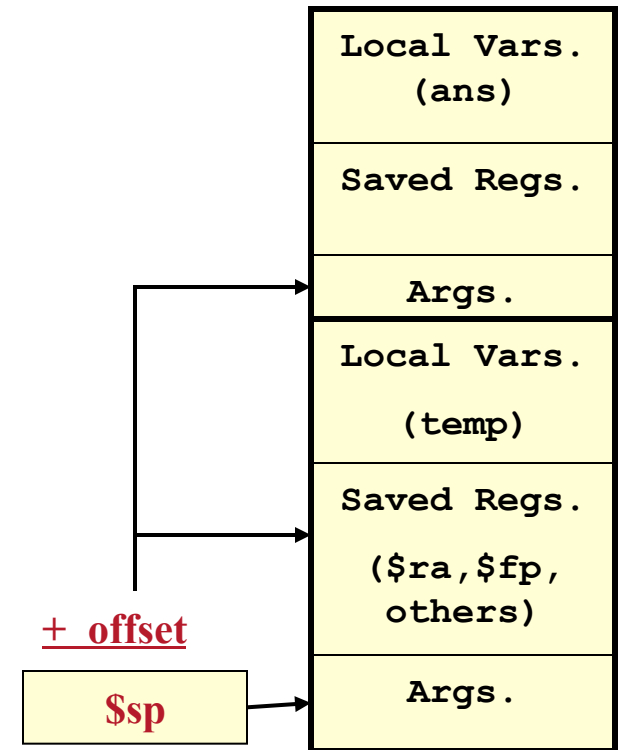


Building a Stack Frame

- Caller routine...
 - Save caller's "unpreserved" registers (\$a0-\$a3 in previous stack frame, \$t0-\$t9 in caller's frame)
 - Fill in arguments (using \$a0-\$a3 & stack)
 - Execute 'jal'
- Callee routine...
 - Allocate space for new frame by moving \$sp down
 - Save "preserved registers" (i.e. \$fp,\$ra,etc.)
 - Setup new \$fp to point to base of new stack frame
 - Execute Code
 - Place return value in \$v0
 - Restore "preserved" registers
 - Deallocate stack frame by moving \$sp up
 - Return using 'jr'
- Caller routine...
 - Restore "unpreserved" registers

Accessing Values on the Stack

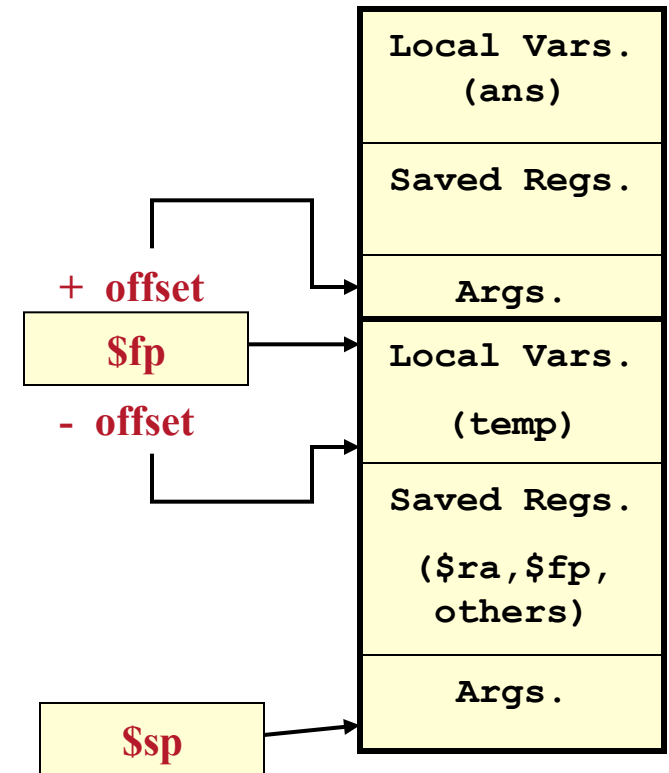
- Stack pointer (\$sp) is usually used to access only the top value on the stack
- To access arguments and local variables, we need to access values buried in the stack
- We could try to use an offset from \$sp, but other push operations by the callee may change the \$sp requiring different displacements at different times for the same variable
- This can work, but can be confusing
- Solution: Use another pointer that doesn't change throughout execution of a subroutine



To access parameters we could try to use some displacement
[i.e. $d(\$sp)$]

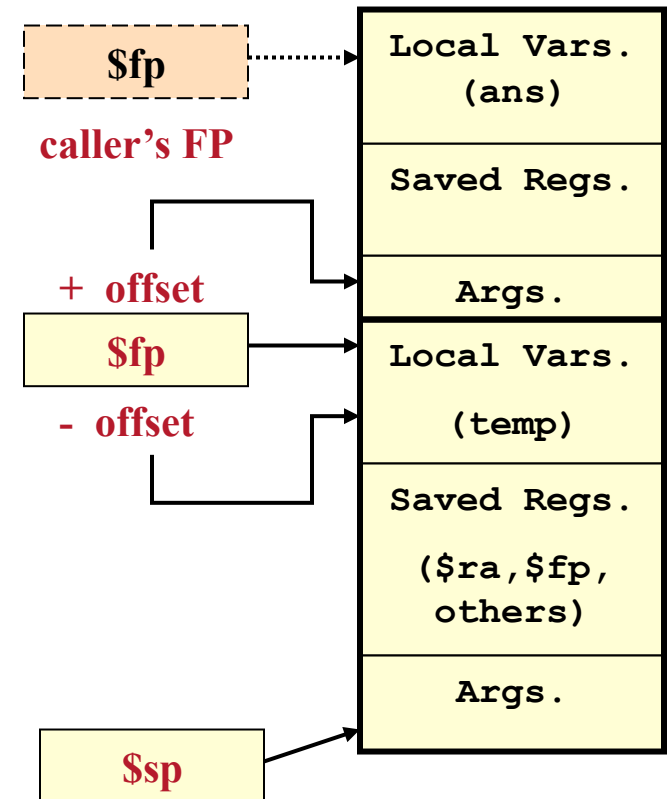
Frame Pointer

- Use a new pointer called Frame Pointer (\$fp) to point to the base of the current routines frame (i.e. the *first* word of the stack frame)
- \$fp will not change during the course of subroutine execution
- Can use constant offsets from \$fp to access parameters or local variables
 - Key 1: \$fp doesn't change during subroutine execution
 - Key 2: Number of arguments, local variables, and saved registers is a known value



Frame Pointer and Subroutines

- Problem is that each executing subroutine needs its own value of \$fp
- The called subroutine must save the caller's \$fp and setup its own \$fp
 - Usually performed immediately after allocating frame space and saving \$ra
- The called subroutine must restore the caller's \$fp before it returns



Example I

C Code

```
void caller(int a){
    callee(1);
}

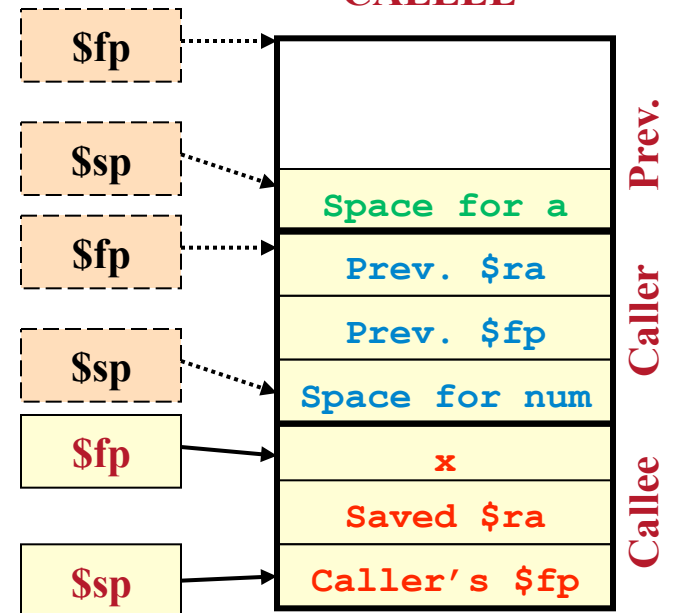
int callee(int num){
    int x = 6;
    return x + num;
}
```

Assembly Code

```
.text
CALLER:  addi  $sp,$sp,-12
         sw   $ra,8($sp)
         sw   $fp,4($sp)
         addi $fp,$sp,8
         sw   $a0,4($fp)
         li   $a0, 1
         jal  CALLEE
         lw   $a0,4($fp)
         lw   $ra,8($sp)
         lw   $fp,4($sp)
         addi $sp,$sp,12
         jr   $ra

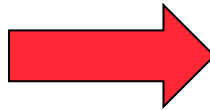
CALLEE:  addi  $sp,$sp,-12
         sw   $ra,4($sp)
         sw   $fp,0($sp)
         addi $fp,$sp,8
         li   $t0,6
         sw   $t0,0($fp)
         add  $v0,$t0,$a0
         lw   $fp,0($sp)
         lw   $ra,4($sp)
         addi $sp,$sp,12
         jr   $ra
```

Stack during execution of CALLEE



Example II

```
int ans;  
void main() {  
    int x = 3;  
    ans = avg(1,5);  
    x = x + 1;  
}  
  
int avg(int a, int b) {  
    int temp = 1;  
    return a + b >> temp;  
}
```



```
.text  
MAIN:  ...  
        li    $s0, 3  
        li    $a0, 1  
        li    $a1, 5  
        jal   AVG  
        sw    $v0, 0($gp)  
        addi   $s0, $s0, 1  
        sw    $s0, -4($fp)  
        ...  
  
AVG:    addi   $sp, $sp, -24  
        sw    $ra, 8($sp)  
        sw    $fp, 4($sp)  
        addi   $fp, $sp, 20  
        sw    $s0, -20($fp)  
        li    $s0, 1  
        sw    $s0, -4($fp)  
        add    $v0, $a0, $a1  
        srav   $v0, $v0, $s0  
        lw    $s0, -20($fp)  
        lw    $fp, 4($sp)  
        lw    $ra, 8($sp)  
        addi   $sp, $sp, 24  
        jr    $ra
```

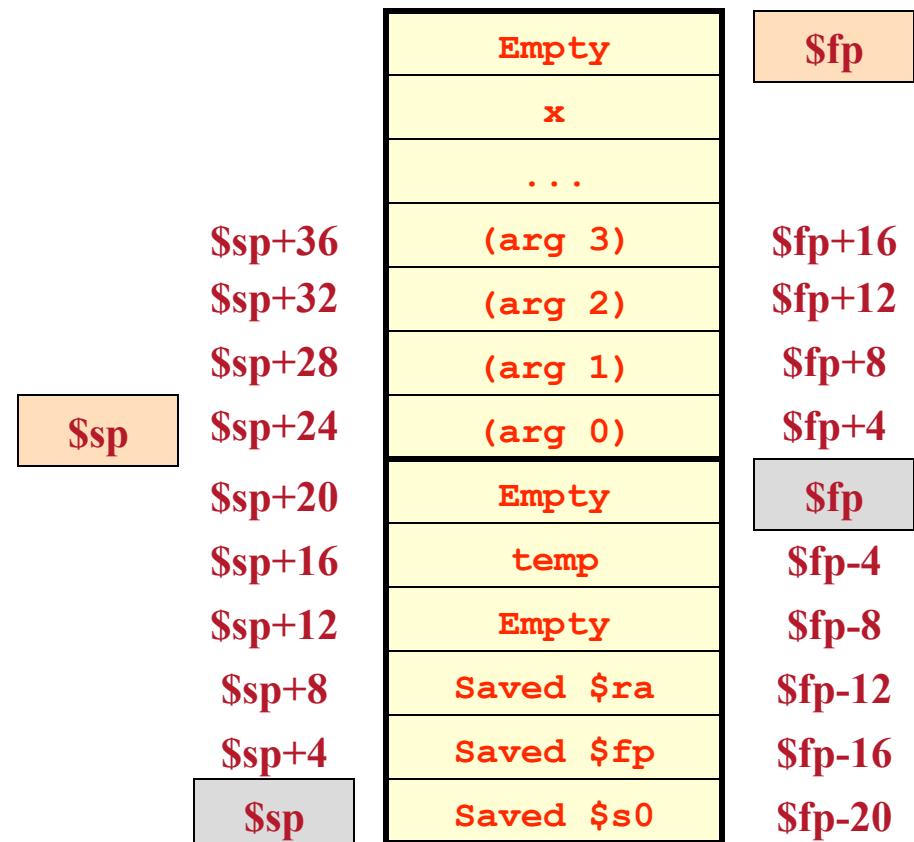
Example II (Cont.)

```

.text
MAIN:
...
li    $s0, 3
li    $a0, 1
li    $a1, 5
jal   AVG
sw    $v0, 0($gp)
addi  $s0, $s0, 1
sw    $s0, -4($fp)
...

AVG:  addi  $sp, $sp, -24
      sw    $ra, 8($sp)
      sw    $fp, 4($sp)
      addi  $fp, $sp, 20
      sw    $s0, -20($fp)
      li    $s0, 1
      sw    $s0, -4($fp)
      add   $v0, $a0, $a1
      srav  $v0, $v0, $s0
      lw    $s0, -20($fp)
      lw    $fp, 4($sp)
      lw    $ra, 8($sp)
      addi  $sp, $sp, 24
      jr    $ra
    
```

Convention: Local variable section must start and end on an 8-byte boundary



Stack during
execution of
AVG

Example III

- Subroutine to sum an array of integers

```
int sumit(int data[], int length)
{
    int sum, int i;
    sum = 0;
    for(i=0; i < length; i++)
        sum = sum + data[i];
    return sum;
}
```

Example III (Cont.)

```
.text
SUMIT: addi  $sp,$sp,-32
       sw    $ra,20($sp)
       sw    $fp,16($sp)
       addi  $fp,$sp,28
       sw    $zero,-4($fp) # sum = 0;
       sw    $zero,0($fp)  # i = 0;
LOOP:  lw    $t0,0($fp)     # $t0 = i
       bge   $t0,$a0,FIN    # is i < length
       lw    $v0,-4($fp)    # $v0 = sum
       sll   $t3,$t0,2      # i = i * 4
       add   $t3,$a0,$t3    # $t3 = &(data[i])
       lw    $t4,0($t3)     # $t4 = data[i]
       add   $v0,$v0,$t4    # sum += data[i]
       sw    $v0,-4($fp)
       addi  $t0,$t0,1      # i++
       sw    $t0,0($fp)
       b     LOOP
FIN:   lw    $fp,16($sp)
       lw    $ra,20($sp)
       addi  $sp,$sp,32
       jr    $ra
```

Naïve, unoptimized implementation

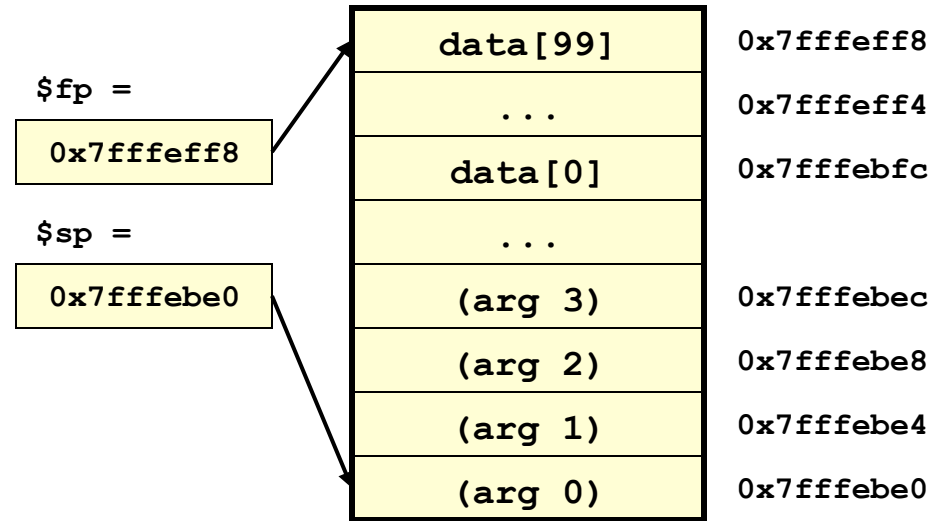
```
.text
SUMIT: move  $v0,$zero      # $v0 = sum = 0
LOOP:  blez  $a1,FIN        # check length > 0
       lw    $t1,0($a0)    # $t1 = data[i]
       add   $v0,$v0,$t1   # sum += data[i]
       addi  $a0,$a0,4      # increment ptr.
       addi  $a1,$a1,-1     # length--
       b     LOOP
FIN:   jr    $ra
```

**Hand-coded assembly implementation
or optimized compiler output**

Example III (Cont.)

```

.text
SUMIT: addi $sp,$sp,-32
      sw   $ra,20($sp)
      sw   $fp,16($sp)
      addi $fp,$sp,28
      sw   $zero,-4($fp) # sum = 0;
      sw   $zero,0($fp)  # i = 0;
LOOP: lw   $t0,0($fp)     # $t0 = i
      bge  $t0,$a0,FIN    # is i < length
      lw   $v0,-4($fp)    # $v0 = sum
      sll  $t3,$t0,2      # i = i * 4
      add  $t3,$a0,$t3    # $t3 = &(data[i])
      lw   $t4,0($t3)     # $t4 = data[i]
      add  $v0,$v0,$t4    # sum += data[i]
      sw   $v0,-4($fp)
      addi $t0,$t0,1      # i++
      sw   $t0,0($fp)
      b    LOOP
FIN:   lw   $fp,16($sp)
      lw   $ra,20($sp)
      addi $sp,$sp,32
      jr   $ra
    
```



At start of SUMIT, FP and SP are pointing to stack frame of routine that is calling SUMIT. Argument \$a0 is a pointer to a locally declared data array and \$a1 is the length (e.g. 100)

Example III (Cont.)

```

.text
SUMIT: addi $sp,$sp,-32
      sw   $ra,20($sp)
      sw   $fp,16($sp)
      addi $fp,$sp,28
      sw   $zero,-4($fp) # sum = 0;
      sw   $zero,0($fp)  # i = 0;
LOOP:  lw   $t0,0($fp)    # $t0 = i
      bge  $t0,$a0,FIN    # is i < length
      lw   $v0,-4($fp)    # $v0 = sum
      sll  $t3,$t0,2      # i = i * 4
      add  $t3,$a0,$t3    # $t3 = &(data[i])
      lw   $t4,0($t3)     # $t4 = data[i]
      add  $v0,$v0,$t4    # sum += data[i]
      sw   $v0,-4($fp)
      addi $t0,$t0,1      # i++
      sw   $t0,0($fp)
      b    LOOP
FIN:   lw   $fp,16($sp)
      lw   $ra,20($sp)
      addi $sp,$sp,32
      jr   $ra
    
```

\$fp =

0x7fffebd0

\$sp =

0x7fffebc0

data[99]	0x7fffeff8
...	0x7fffeff4
data[0]	0x7fffebfc
...	
(arg 3)	0x7fffebec
(arg 2)	0x7fffebe8
(\$a1 = length)	0x7fffebe4
(\$a0 = data)	0x7fffebe0
i	0x7fffebd0
sum	0x7fffebd8
Caller \$ra	0x7fffebd4
0x7fffeff8	0x7fffebd0
(arg 3)	0x7fffebcc
(arg 2)	0x7fffebc8
(arg 1)	0x7fffebc4
(arg 0)	0x7fffebc0

We allocate the stack frame and save the \$fp and \$ra before adjusting the new \$fp

Example III (Cont.)

```

.text
SUMIT: addi $sp,$sp,-32
      sw   $ra,20($sp)
      sw   $fp,16($sp)
      addi $fp,$sp,28
      sw   $zero,-4($fp) # sum = 0;
      sw   $zero,0($fp)  # i = 0;
LOOP:  lw   $t0,0($fp)    # $t0 = i
      bge  $t0,$a0,FIN    # is i < length
      lw   $v0,-4($fp)    # $v0 = sum
      sll  $t3,$t0,2      # i = i * 4
      add  $t3,$a0,$t3    # $t3 = &(data[i])
      lw   $t4,0($t3)     # $t4 = data[i]
      add  $v0,$v0,$t4    # sum += data[i]
      sw   $v0,-4($fp)
      addi $t0,$t0,1      # i++
      sw   $t0,0($fp)
      b    LOOP
FIN:   lw   $fp,16($sp)
      lw   $ra,20($sp)
      addi $sp,$sp,32
      jr   $ra
    
```

\$fp =

0x7fffebd0

\$sp =

0x7fffebc0

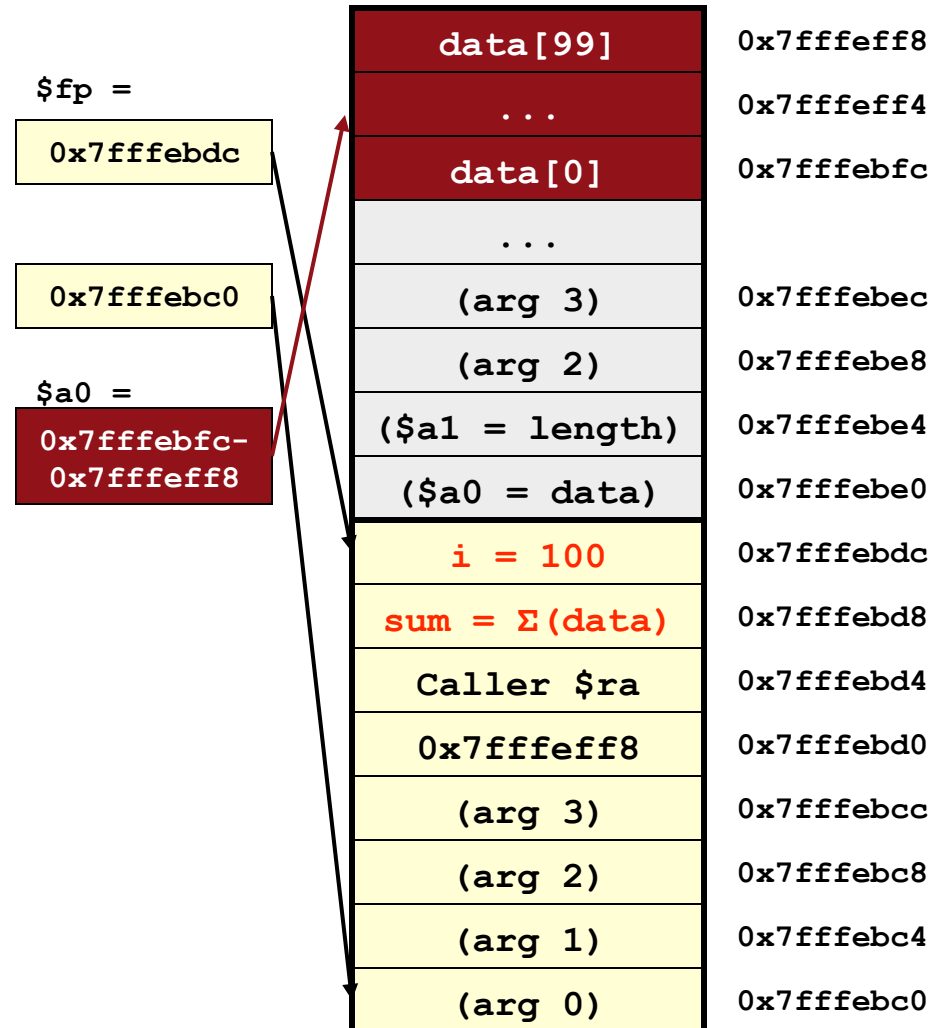
data[99]	0x7fffeff8
...	0x7fffeff4
data[0]	0x7fffebfc
...	
(arg 3)	0x7fffebec
(arg 2)	0x7fffebe8
(\$a1 = length)	0x7fffebe4
(\$a0 = data)	0x7fffebe0
i = 0	0x7fffebd0
sum = 0	0x7fffebd8
Caller \$ra	0x7fffebd4
0x7fffeff8	0x7fffebd0
(arg 3)	0x7fffebcc
(arg 2)	0x7fffebc8
(arg 1)	0x7fffebc4
(arg 0)	0x7fffebc0

We initialize the local variables i and sum using appropriate displacements from the \$fp

Example III (Cont.)

```

.text
SUMIT: addi $sp,$sp,-32
      sw   $ra,20($sp)
      sw   $fp,16($sp)
      addi $fp,$sp,28
      sw   $zero,-4($fp) # sum = 0;
      sw   $zero,0($fp)  # i = 0;
LOOP:  lw   $t0,0($fp)    # $t0 = i
      bge  $t0,$a0,FIN    # is i < length
      lw   $v0,-4($fp)    # $v0 = sum
      sll  $t3,$t0,2      # i = i * 4
      add  $t3,$a0,$t3    # $t3 = &(data[i])
      lw   $t4,0($t3)     # $t4 = data[i]
      add  $v0,$v0,$t4    # sum += data[i]
      sw   $v0,-4($fp)
      addi $t0,$t0,1      # i++
      sw   $t0,0($fp)
      b    LOOP
FIN:   lw   $fp,16($sp)
      lw   $ra,20($sp)
      addi $sp,$sp,32
      jr   $ra
    
```



We run through the loop, length number of times (e.g. 100) updating i and sum each iteration. \$t3 acts as a ptr. to the data array allocated in the previous stack frame

Example III (Cont.)

```

.text
SUMIT: addi $sp,$sp,-32
      sw   $ra,20($sp)
      sw   $fp,16($sp)
      addi $fp,$sp,28
      sw   $zero,-4($fp) # sum = 0;
      sw   $zero,0($fp)  # i = 0;
LOOP:  lw   $t0,0($fp)    # $t0 = i
      bge  $t0,$a0,FIN    # is i < length
      lw   $v0,-4($fp)    # $v0 = sum
      sll  $t3,$t0,2      # i = i * 4
      add  $t3,$a0,$t3    # $t3 = &(data[i])
      lw   $t4,0($t3)     # $t4 = data[i]
      add  $v0,$v0,$t4    # sum += data[i]
      sw   $v0,-4($fp)
      addi $t0,$t0,1      # i++
      sw   $t0,0($fp)
      b    LOOP
FIN:   lw   $fp,16($sp)
      lw   $ra,20($sp)
      addi $sp,$sp,32
      jr   $ra
    
```

\$fp =

0x7fffeff8

\$sp =

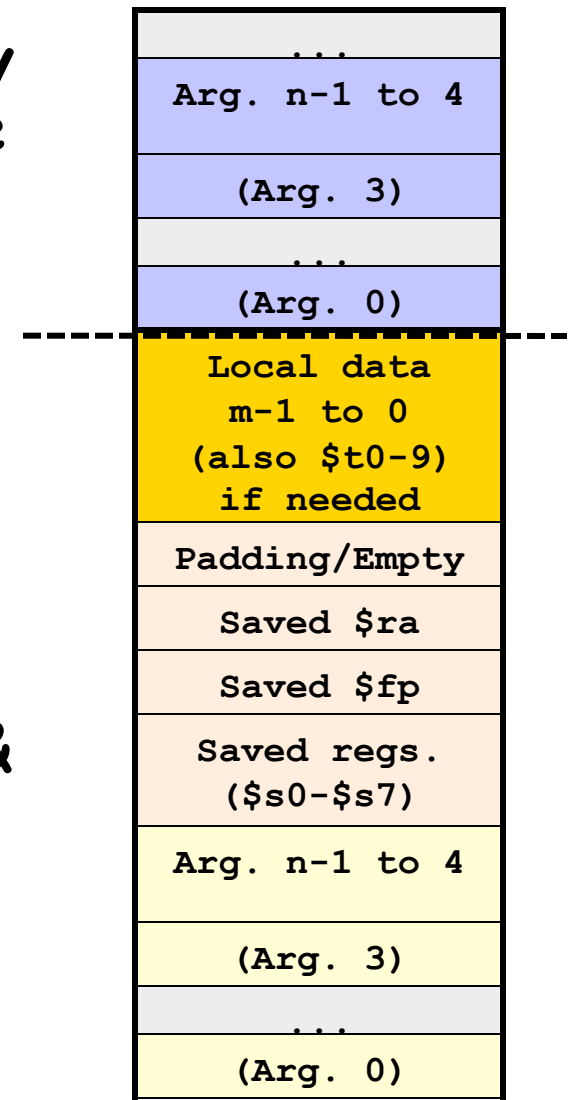
0x7fffebe0

data[99]	0x7fffeff8
...	0x7fffeff4
data[0]	0x7fffebfc
...	
(arg 3)	0x7fffebdc
(arg 2)	0x7fffebe8
(\$a1 = length)	0x7fffebe4
(\$a0 = data)	0x7fffebe0
i = 100	0x7fffebd8
sum = Σ (data)	0x7fffebd4
Caller \$ra	0x7fffebd0
0x7fffeff8	0x7fffebcc
(arg 3)	0x7fffebcb
(arg 2)	0x7fffebca
(arg 1)	0x7fffeb98
(arg 0)	0x7fffeb94

We restore the \$fp and \$ra, then deallocate the stack frame by resetting the \$sp back to its original value

Stack Summary

- Data associated with a subroutine is a many-to-one relationship (i.e. many instances may be running at the same time). A stack allows for any number of concurrent instances to all have their own storage.
- Stack always grows towards lower addresses
- Stack frames defines organization of data related to a subroutine
- A subroutine should leave the stack & \$sp in the same condition it found it
- \$sp and \$fp are dedicated registers to maintaining the system stack



Recursive Routines

- Routines that call themselves
- Good example of why stack frames are needed since each instance of the routine needs its own data
- In the following factorial example a compiler would use the standard stack frame organization, however, we'll hand-code our own

Recursive Factorial Routine

C Code:

```
void main() {
    int x;
    x = fact(3);
}

int fact(int n)
{
    if(n == 1)
        // 1! = 1
        return 1;
    else {
        // calculate (n-1)!
        return n*fact(n-1);
    }
}
```

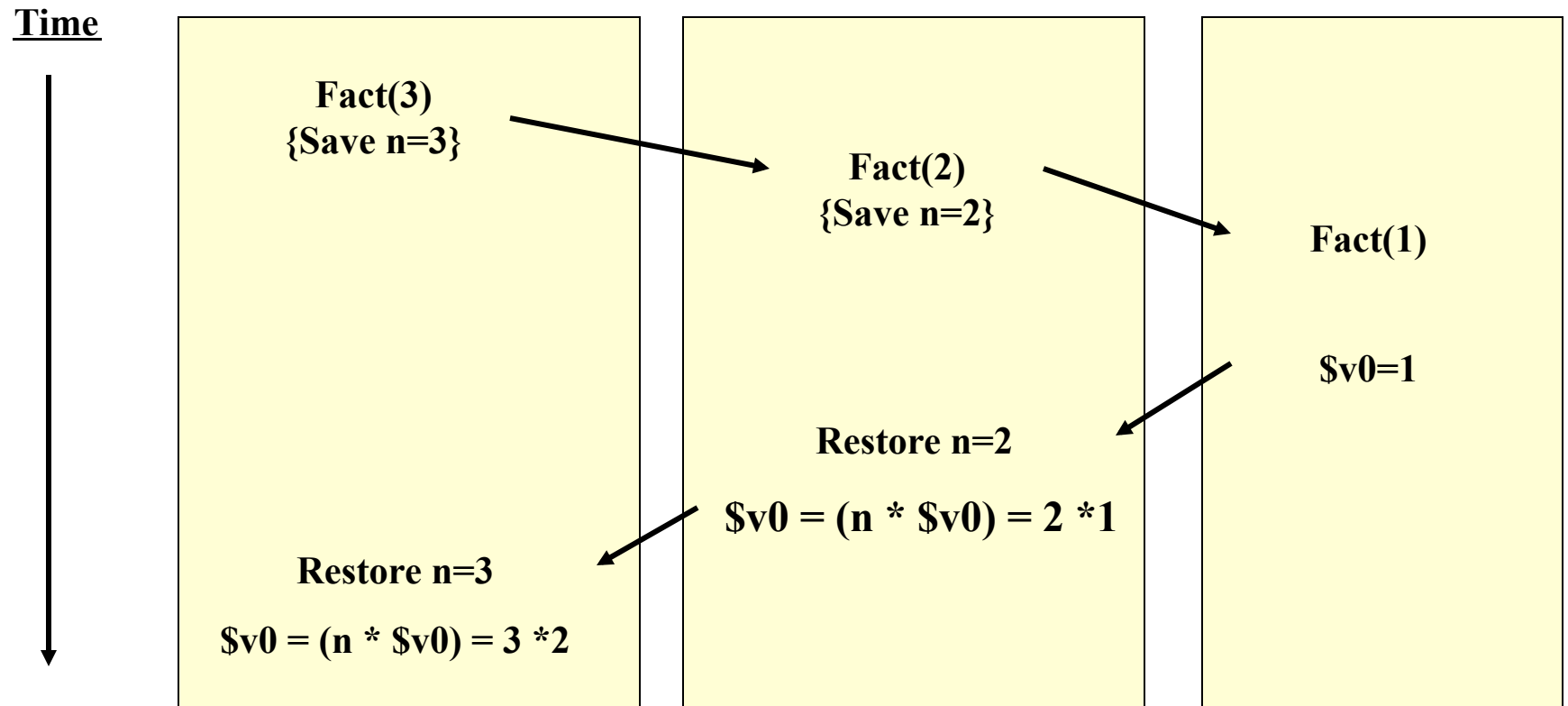
Assembly:

```
.text
MAIN:    addi    $sp,$sp,-8
         li      $a0, 3
         jal     FACT
         sw      $v0,4($sp)

FACT:    addi    $sp,$sp,-8
         sw      $ra,4($sp)
         addi    $v0,$zero,1
         beq     $a0,$v0,L1
         sw      $a0,8($sp)
         addi    $a0,$a0,-1
         jal     FACT
         lw      $a0,8($sp)
         mul     $v0,$a0,$v0
L1:      lw      $ra,4($sp)
         addi    $sp,$sp,8
         jr      $ra
```

- **Key Detail:** Make sure each call of Fact is working with its own value of n

Recursive Call Timeline



- Before calling yourself, you need to save copies of all your locally declared variables/parameters (e.g. `n`)

Recursive Routine Example

```

.text
MAIN:  addi    $sp,$sp,-8
        li     $a0, 3
        jal    FACT
        sw     $v0,4($sp)
    
```

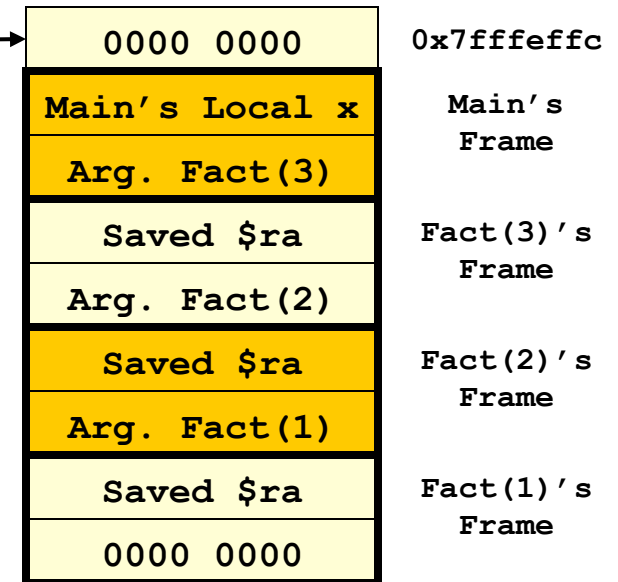
```

FACT:  addi    $sp,$sp,-8
        sw     $ra,4($sp)
        addi   $v0,$zero,1
        beq    $a0,$v0,L1
        sw     $a0,8($sp)
        addi   $a0,$a0,-1
        jal    FACT
        lw     $a0,8($sp)
        mul    $v0,$a0,$v0
L1:     lw     $ra,4($sp)
        addi   $sp,$sp,8
        jr     $ra
    
```

\$sp = 7ffffeffc

\$a0 = 00000000

\$v0 = 00000000



- Initial conditions

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```

\$sp = 7ffffeff4

\$ra = 0040002c

\$a0 = 00000003

\$v0 = 00000000

0000 0000	0x7ffffeffc
0000 0000	0x7ffffeff8
0000 0000	0x7ffffeff4
0000 0000	0x7ffffeff0
0000 0000	0x7ffffefec
0000 0000	0x7ffffefe8
0000 0000	0x7ffffefe4
0000 0000	0x7ffffefe0
0000 0000	0x7ffffefd0

- Allocate space for local var. and arg. \$a0 (n)
- Load the argument for fact(3) call
- Call the fact routine using 'jal'

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

```

```

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra

```

\$sp = 7ffffefc

\$ra = 0040002c

\$a0 = 00000003

\$v0 = 00000000

0000 0000	0x7ffffefc
0000 0000	0x7ffffef8
0000 0000	0x7ffffef4
0040 002c	0x7ffffef0
0000 0000	0x7ffffefc
0000 0000	0x7ffffefe8
0000 0000	0x7ffffefe4
0000 0000	0x7ffffefe0
0000 0000	0x7ffffefd0

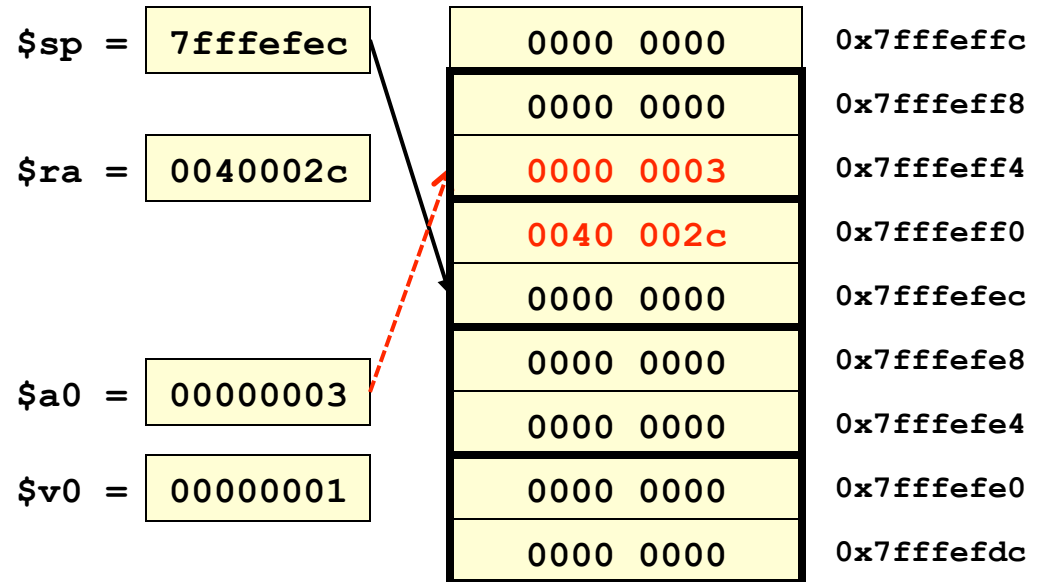
- Allocate room for \$ra and for saving \$a0 when we have to call fact(2)
- Store the \$ra to the stack

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



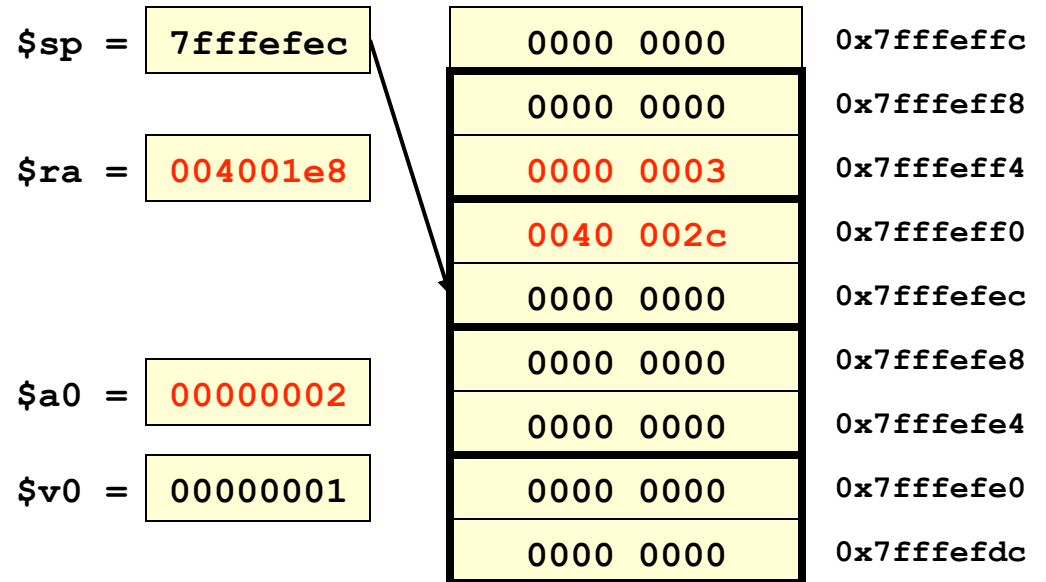
- Perform the comparison of $n == 1$ ($\$a0 == \$v0$)
- Since $n=3$, this branch fails and execution continues by storing the current value of n on the stack before calling `fact(2)`

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



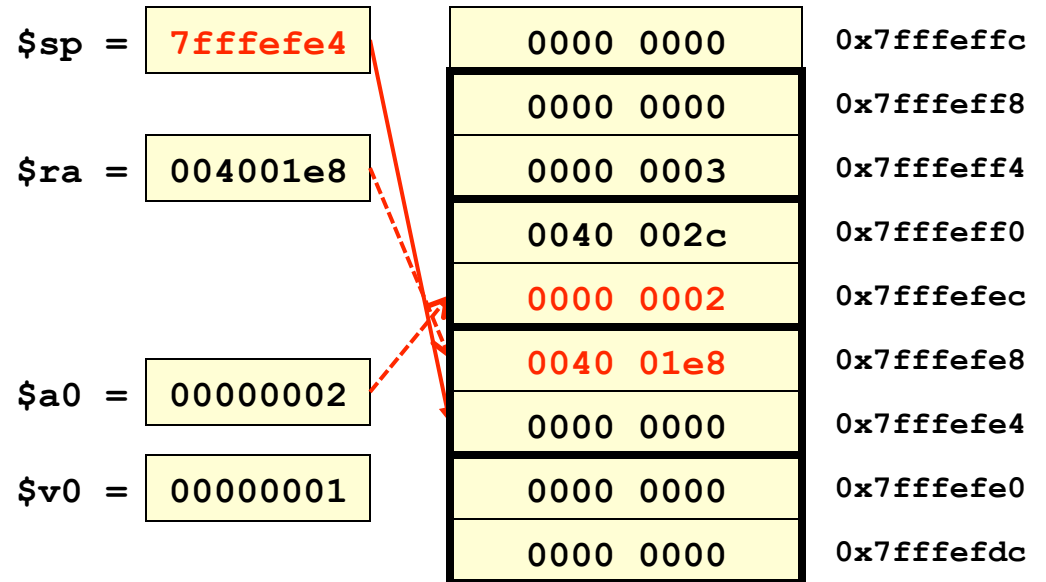
- Set n=2 and call fact(2)
- \$ra is updated with the appropriate return address

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



- Allocate space on stack for fact(2) call
- Save \$ra, perform n==1 comparison which fails
- Store n=2 on the stack before calling fact(1)

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```

\$sp = 7ffffefe4

\$ra = 004001e8

\$a0 = 00000001

\$v0 = 00000001

0000 0000	0x7ffffefc
0000 0000	0x7ffffef8
0000 0003	0x7ffffef4
0040 002c	0x7ffffef0
0000 0002	0x7ffffefc
0040 01e8	0x7ffffefe8
0000 0000	0x7ffffefe4
0000 0000	0x7ffffefe0
0000 0000	0x7ffffefd0

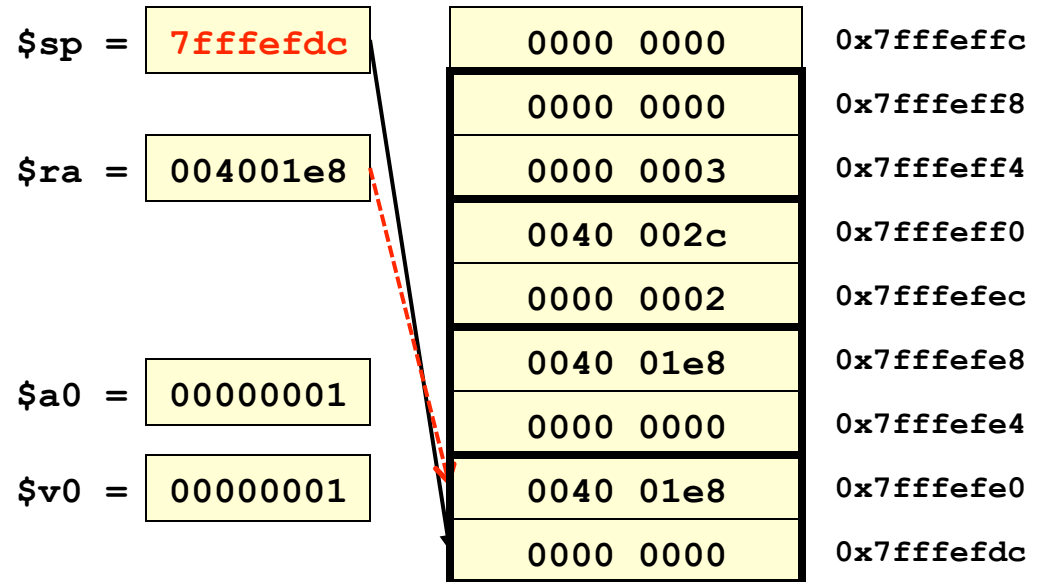
- Set n=1 and call fact(1)
- \$ra is updated with the appropriate return address

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



- Allocate space on stack for fact(1) call
- Save \$ra, perform n==1 comparison which succeeds
- Branch to L1

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```

\$sp = 7ffffefe4

\$ra = 004001e8

\$a0 = 00000001

\$v0 = 00000001

0000 0000	0x7ffffeffc
0000 0000	0x7ffffeff8
0000 0003	0x7ffffeff4
0040 002c	0x7ffffeff0
0000 0002	0x7ffffefec
0040 01e8	0x7ffffefe8
0000 0000	0x7ffffefe4
0040 01e8	0x7ffffefe0
0000 0000	0x7ffffefd0

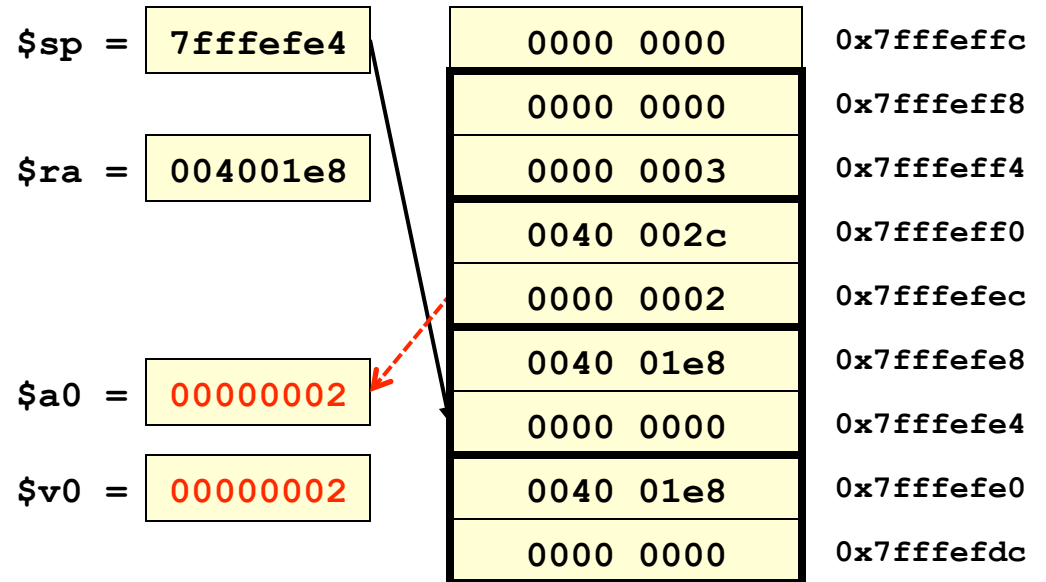
- Pop the \$ra off the stack and return to that address

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



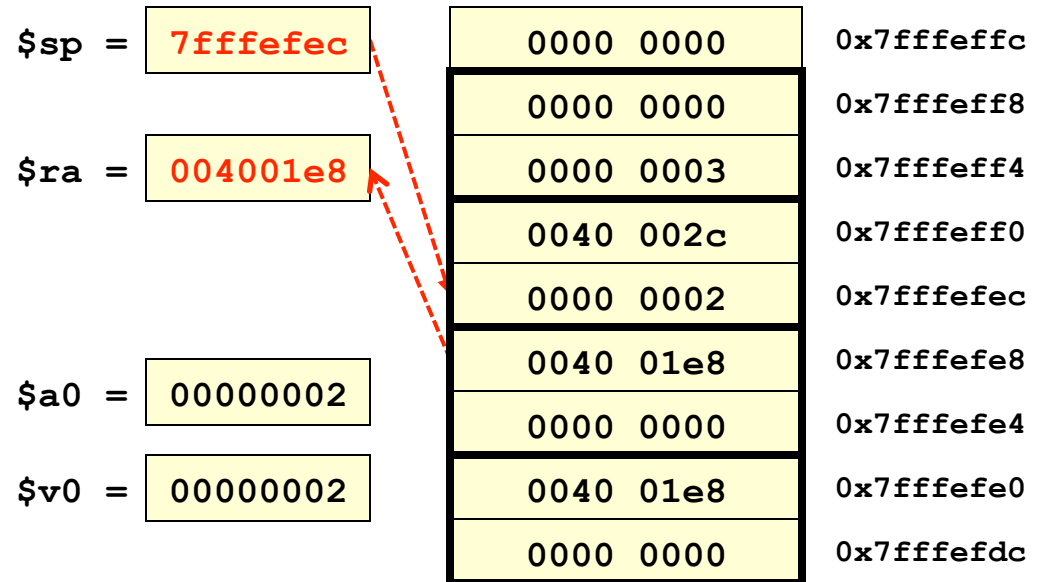
- Restore \$a0 = 2
- Multiply \$v0 = 1 * \$a0 = 2 and store in \$v0

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



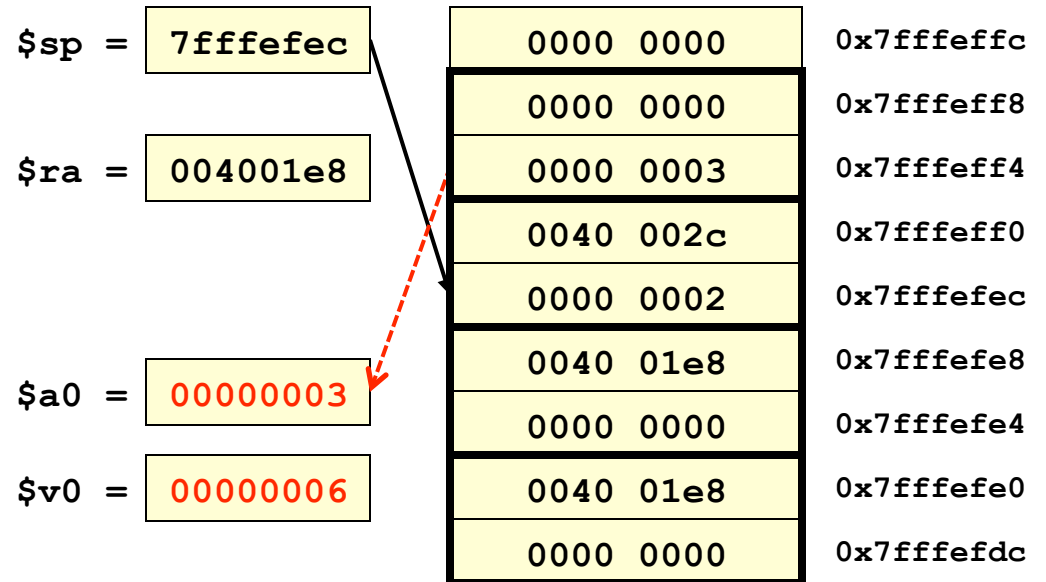
- Pop the \$ra off the stack and return to that address

Recursive Routine Example

```

.text
MAIN:    addi    $sp,$sp,-8
         li      $a0, 3
0x40002c jal     FACT
         sw      $v0,4($sp)

FACT:    addi    $sp,$sp,-8
         sw      $ra,4($sp)
         addi    $v0,$zero,1
         beq     $a0,$v0,L1
         sw      $a0,8($sp)
         addi    $a0,$a0,-1
         jal     FACT
0x4001e8 lw      $a0,8($sp)
         mul     $v0,$a0,$v0
L1:      lw      $ra,4($sp)
         addi    $sp,$sp,8
         jr      $ra
    
```



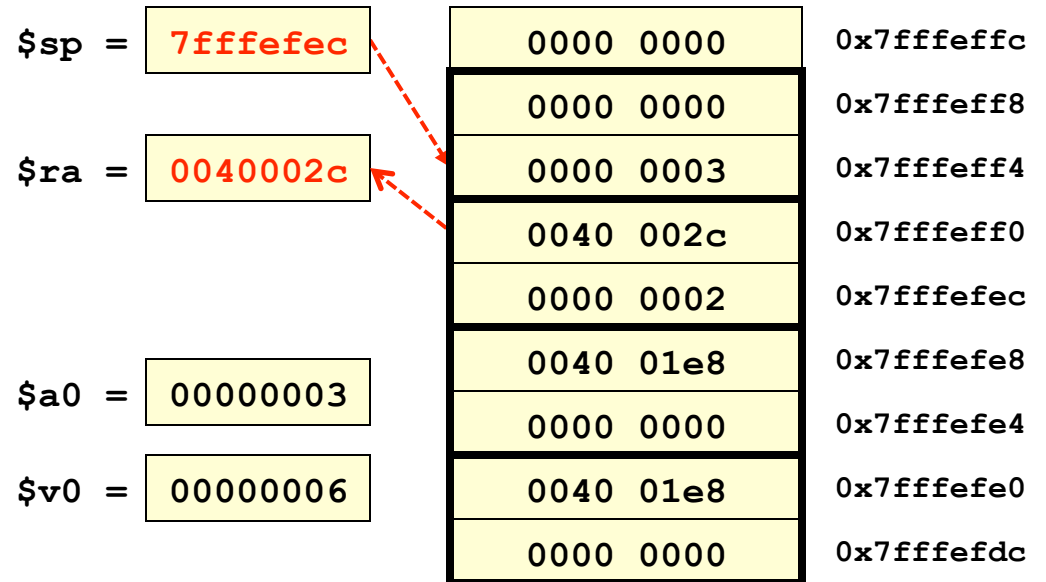
- Restore \$a0 = 3
- Multiply \$v0 = 2 * \$a0 = 3 and store in \$v0

Recursive Routine Example

```

.text
MAIN:      addi    $sp,$sp,-8
           li      $a0, 3
0x40002c   jal     FACT
           sw      $v0,4($sp)

FACT:      addi    $sp,$sp,-8
           sw      $ra,4($sp)
           addi    $v0,$zero,1
           beq     $a0,$v0,L1
           sw      $a0,8($sp)
           addi    $a0,$a0,-1
           jal     FACT
0x4001e8   lw      $a0,8($sp)
           mul     $v0,$a0,$v0
L1:        lw      $ra,4($sp)
           addi    $sp,$sp,8
           jr      $ra
    
```



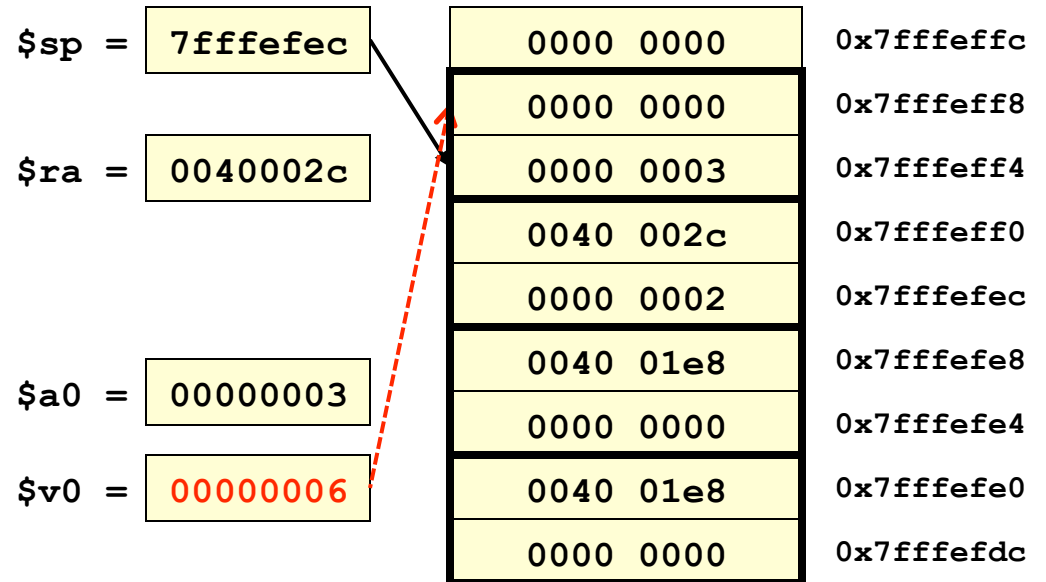
- Pop the \$ra off the stack and return to that address

Recursive Routine Example

```

.text
MAIN:   addi    $sp,$sp,-8
        li      $a0, 3
0x40002c jal     FACT
        sw      $v0,4($sp)

FACT:   addi    $sp,$sp,-8
        sw      $ra,4($sp)
        addi    $v0,$zero,1
        beq     $a0,$v0,L1
        sw      $a0,8($sp)
        addi    $a0,$a0,-1
        jal     FACT
0x4001e8 lw      $a0,8($sp)
        mul     $v0,$a0,$v0
L1:     lw      $ra,4($sp)
        addi    $sp,$sp,8
        jr      $ra
    
```



- \$v0 contains $3! = 6$ and is stored in the local variable