

1. A path in a digital circuit-switched network has a data rate of 1 Mbps. The exchange of 1000 bits is required for the setup and teardown phases. The distance between two parties is 5000 km. Answer the following questions if the propagation speed is  $2 \times 10^8$  m/s:
- What is the total delay if 1000 bits of data are exchanged during the data-transfer phase?
  - What is the total delay if 100,000 bits of data are exchanged during the data-transfer phase?
  - What is the total delay if 1,000,000 bits of data are exchanged during the data-transfer phase?
  - Find the delay per 1000 bits of data for each of the above cases and compare them. What can you infer?

**Solution**

**Given:**

Total bandwidth or data rate = 1 Mbps

Distance between two parties = 5000 km

1000 bits is required for the setup and teardown phases

Propagation speed =  $2 \times 10^8$  m/s

**Formulas:**

**Total time taken to transmit a message = Connection set up time + Transmission delay + Propagation delay + Tear down time**

where-

**Transmission delay = Message size / Bandwidth**

**Propagation delay = Distance between 2 hops / Propagation speed**

$$1 \text{ km} = 1000 \text{ m} = 10^3 \text{ m}$$

$$1 \text{ ms} = 10^{-3} \text{ s}$$

$$1 \text{ s} = 1000 \text{ ms}$$

- We assume that the setup phase is a two-way communication and the teardown phase is a one-way communication.
- These two phases are common for all three cases.

- The delay for these two phases can be calculated as three propagation delays and three transmission delays.

**Calculating Propagation Delay:**

**Propagation Delay** = (Distance) / (Propagation speed)

$$= 5000 \text{ km} / 2 \times 10^8 \text{ m/s}$$

$$= 5000 * 10^3 \text{ m} / 2 \times 10^8 \text{ m/s}$$

$$= 2500 / 10^5 \text{ s}$$

$$= 25 * 10^{-3} \text{ s}$$

$$= 25 \text{ ms}$$

$$\text{Three propagation delays} = 3 * 25 \text{ ms}$$

$$= 75 \text{ ms}$$

**Calculating Transmission Delay:**

**Transmission delay (T)** = File size / Bandwidth

$$= 1000 \text{ bits} / 1 \text{ Mbps}$$

$$= 1000 \text{ bits} / 10^6 \text{ bits per sec}$$

$$= 1 / 10^3 \text{ sec}$$

$$= 1 \text{ ms}$$

$$\text{Three transmission delays} = 3 * 1 \text{ ms}$$

$$= 3 \text{ ms}$$

**The delay for the setup phase and the teardown phase:**

$$= \text{Three propagation delays} + \text{Three transmission delays}$$

$$= 75 \text{ ms} + 3 \text{ ms}$$

$$= 78 \text{ ms}$$

- We assume that the data transfer is in one direction.
- The total delay is then delay for setup and teardown + propagation delay + transmission delay.

- (i). What is the total delay if 1000 bits of data are exchanged during the data-transfer phase?

**Calculating Propagation Delay:**

$$\begin{aligned}\text{Propagation Delay} &= (\text{Distance}) / (\text{Propagation speed}) \\ &= 5000 \text{ km} / 2 \times 10^8 \text{ m/s} \\ &= 5000 * 10^3 \text{ m} / 2 \times 10^8 \text{ m/s} \\ &= 2500 / 10^5 \text{ s} \\ &= 25 * 10^{-3} \text{ s} \\ &= 25 \text{ ms}\end{aligned}$$

**Calculating Transmission Delay:**

$$\begin{aligned}\text{Transmission delay (T)} &= \text{File size} / \text{Bandwidth} \\ &= 1000 \text{ bits} / 1 \text{ Mbps} \\ &= 1000 \text{ bits} / 10^6 \text{ bits per sec} \\ &= 1 / 10^3 \text{ sec} \\ &= 1 \text{ ms}\end{aligned}$$

**Calculating Total Delay:**

$$\begin{aligned}\text{Total delay} &= \text{Delay for setup \& teardown} + \text{Propagation delay} + \text{Transmission delay} \\ &= 78 \text{ ms} + 25 \text{ ms} + 1 \text{ ms} \\ &= 104 \text{ ms}\end{aligned}$$

- (ii). What is the total delay if 100,000 bits of data are exchanged during the data-transfer phase?

**Calculating Propagation Delay:**

$$\begin{aligned}\text{Propagation Delay} &= (\text{Distance}) / (\text{Propagation speed}) \\ &= 5000 \text{ km} / 2 \times 10^8 \text{ m/s} \\ &= 5000 * 10^3 \text{ m} / 2 \times 10^8 \text{ m/s} \\ &= 2500 / 10^5 \text{ s} \\ &= 25 * 10^{-3} \text{ s} \\ &= 25 \text{ ms}\end{aligned}$$

**Calculating Transmission Delay:**

$$\begin{aligned}\text{Transmission delay (T)} &= \text{File size} / \text{Bandwidth} \\ &= 100,000 \text{ bits} / 1 \text{ Mbps} \\ &= 100,000 \text{ bits} / 10^6 \text{ bits per sec} \\ &= 1 / 10 \text{ sec} \\ &= 0.1 * 1000 \text{ ms} \\ &= 100 \text{ ms}\end{aligned}$$

**Calculating Total Delay:**

$$\begin{aligned}\text{Total delay} &= \text{Delay for setup and teardown} + \text{Propagation delay} + \text{Transmission delay} \\ &= 78 \text{ ms} + 25 \text{ ms} + 100 \text{ ms} \\ &= 203 \text{ ms}\end{aligned}$$

- (iii). **What is the total delay if 1,000,000 bits of data are exchanged during the data-transfer phase?**

**Calculating Propagation Delay:**

$$\begin{aligned}\text{Propagation Delay} &= (\text{Distance}) / (\text{Propagation speed}) \\ &= 5000 \text{ km} / 2 \times 10^8 \text{ m/s} \\ &= 5000 * 10^3 \text{ m} / 2 \times 10^8 \text{ m/s} \\ &= 2500 / 10^5 \text{ s} \\ &= 25 * 10^{-3} \text{ s} \\ &= 25 \text{ ms}\end{aligned}$$

**Calculating Transmission Delay:**

$$\begin{aligned}\text{Transmission delay (T)} &= \text{File size} / \text{Bandwidth} \\ &= 1,000,000 \text{ bits} / 1 \text{ Mbps} \\ &= 1,000,000 \text{ bits} / 10^6 \text{ bits per sec} \\ &= 1 \text{ sec} \\ &= 1 * 1000 \text{ ms} \\ &= 1000 \text{ ms}\end{aligned}$$

**Calculating Total Delay:**

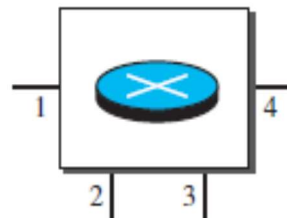
$$\begin{aligned}\text{Total delay} &= \text{Delay for setup and teardown} + \text{Propagation delay} + \text{Transmission delay} \\ &= 78 \text{ ms} + 25 \text{ ms} + 1000 \text{ ms} \\ &= 1103 \text{ ms}\end{aligned}$$

(iv). Find the delay per 1000 bits of data for each of the above cases and compare them. What can you infer?

- In case a, we have 104 ms.
- In case b we have  $203/100 = 2.03$  ms.
- In case c, we have  $1103/1000 = 1.101$  ms.
- The ratio for case c is the smallest because we use one setup and teardown phase to send more data.

2. Figure shows a switch (router) in a datagram network.

Destination address	Output port
1233	3
1456	2
3255	1
4470	4
7176	2
8766	3
9144	2



Find the output port for packets with the following destination addresses:.

- Packet 1: 7176
- Packet 2: 1233
- Packet 3: 8766
- Packet 4: 9144

**Solution**

Packet 1: 2

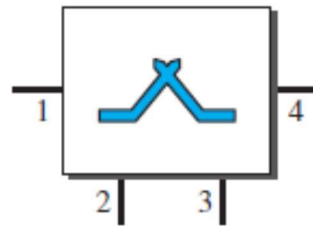
Packet 2: 3

Packet 3: 3

Packet 4: 2

3. Figure shows a switch in a virtual-circuit network.

Incoming		Outgoing	
Port	VCI	Port	VCI
1	14	3	22
2	71	4	41
2	92	1	45
3	58	2	43
3	78	2	70
4	56	3	11



Find the output port and the output VCI for packets with the following input port and input VCI addresses:

- Packet 1: 3, 78
- Packet 2: 2, 92
- Packet 3: 4, 56
- Packet 4: 2, 71

**Solution**

- Packet 1: 3, 78

Output port and the output VCI : 2, 70

- Packet 2: 2, 92

Output port and the output VCI : 1, 45

- Packet 3: 4, 56

Output port and the output VCI : 3, 11

- Packet 4: 2, 71

Output port and the output VCI : 4, 41

4.	<p><b>Design a three-stage, <math>200 \times 200</math> switch (<math>N = 200</math>) with <math>k = 4</math> and <math>n = 20</math>.</b></p> <p><b><u>Solution</u></b></p> <p><b>First stage has <math>N/n</math> crossbars of <math>n \times k</math> crosspoints.</b></p> <p><b>Middle stage <math>k</math> crossbars, each of size <math>(N/n) \times (N/n)</math>.</b></p> <p><b>Third stage has <math>N/n</math> crossbars, each of size <math>k \times n</math>.</b></p> <p>No. of crossbars in the first stage = <math>N/n</math>  <math>= 200 / 20</math>  <math>= 10</math> crossbars, each of size <math>20 \times 4</math></p> <p>No. of crossbars in the second stage = 4 crossbars, each of size <math>10 \times 10</math>.</p> <p>No. of crossbars in the third stage = 10 crossbars, each of size <math>4 \times 20</math>.</p> <p>The total number of crosspoints = <math>2kN + k (N/n)^2</math>  <math>= 2 * 4 * 200 + 4 (200 / 20)^2</math>  <math>= 2000</math> crosspoints</p> $\frac{N}{n} (n \times k) + k \left( \frac{N}{n} \times \frac{N}{n} \right) + \frac{N}{n} (k \times n) = 2kN + k \left( \frac{N}{n} \right)^2$ <p>The total number of crosspoints = <math>10 (20 * 4) + 4 (10 * 10) + 10 (4 * 20)</math>  <math>= 800 + 400 + 800</math>  <math>= 2000</math> crosspoints</p> <p>This is 5 percent of the number of crosspoints in a single-stage switch (<math>200 \times 200 = 40,000</math>).</p>
5.	<p><b>Redesign the previous three-stage, <math>200 \times 200</math> switch, using the Clos criteria with a minimum number of crosspoints.</b></p> <p><b><u>Solution</u></b></p> <p><b>First stage has <math>N/n</math> crossbars of <math>n \times k</math> crosspoints.</b></p> <p><b>Middle stage <math>k</math> crossbars, each of size <math>(N/n) \times (N/n)</math>.</b></p> <p><b>Third stage has <math>N/n</math> crossbars, each of size <math>k \times n</math>.</b></p> <p><b>The number of middle-stage switches must be at least <math>2n - 1</math>.</b></p> <p><b><math>k \geq 2n - 1</math></b></p> <p><b>According to Clos criterion: <math>n = (N/2)^{1/2}</math></b></p> <p><b>Total number of crosspoints <math>\geq 4N [(2N)^{1/2} - 1]</math></b></p>

We let  $n = (200/2)^{1/2}$

$$n = 10$$

We calculate  $k = 2n - 1$

$$= (2 * 10) - 1$$

$$= 19$$

Number of crossbars in the first stage =  $N / n$

$$= 200/10$$

= 20 crossbars, each with  $10 \times 19$  crosspoints.

No. of crossbars in the second stage = 19 crossbars, each with  $20 \times 20$  crosspoints.

No. of crossbars in the third stage = 20 crossbars each with  $19 \times 10$  crosspoints.

The total number of crosspoints =  $20(10 \times 19) + 19(20 \times 20) + 20(19 \times 10)$

$$= 15200$$

**Total number of crosspoints  $\geq 4N [(2N)^{1/2} - 1]$**

$$= 4 * 200 ((2*200)^{1/2} - 1)$$

$$= 4 * 200 (20-1)$$

$$= 4 * 200 (19)$$

$$= 15200$$

If we use a single-stage switch, we need  $200 \times 200 = 40,000$  crosspoints.

The number of crosspoints in this three-stage switch is 24 percent that of a single-stage switch.

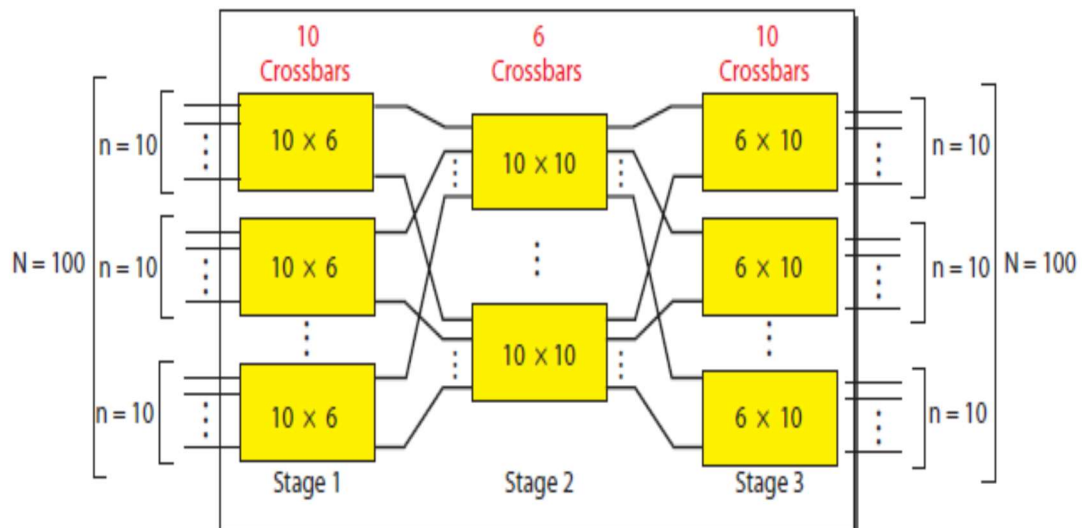
The extra crosspoints are needed to prevent blocking.



6. We need a three-stage space-division switch with  $N = 100$ . We use 10 crossbars at the first and third stages and 4 crossbars at the middle stage.
- Draw the configuration diagram.
  - Calculate the total number of crosspoints.
  - Find the possible number of simultaneous connections.
  - Find the possible number of simultaneous connections if we use a single crossbar ( $100 \times 100$ ).
  - Find the blocking factor, the ratio of the number of connections in part c and in part d.

**Solution**

- Draw the configuration diagram.



- Calculate the total number of crosspoints.

Number of crossbars in the first stage =  $N / n$

$$= 100/10$$

= 10 crossbars, each with  $10 \times 6$  crosspoints.

No. of crossbars in the second stage = 6 crossbars, each with  $10 \times 10$  crosspoints.

No. of crossbars in the third stage = 10 crossbars each with  $6 \times 10$  crosspoints.

The total number of crosspoints =  $10 (10 \times 6) + 6 (10 \times 10) + 10 (6 \times 10)$

$$= 600 + 600 + 600$$

$$= 1800$$

	<p><b>c. Find the possible number of simultaneous connections.</b></p> <p>Only six simultaneous connections are possible for each crossbar at the first stage. This means that the total number of simultaneous connections is 60.</p> <p><b>d. Find the possible number of simultaneous connections if we use a single crossbar (<math>100 \times 100</math>).</b></p> <p>If we use one crossbar (<math>100 \times 100</math>), all input lines can have a connection at the same time, which means 100 simultaneous connections.</p> <p><b>e. Find the blocking factor, the ratio of the number of connections in part c and in part d.</b></p> <p>The blocking factor is 60/100 or 60 percent.</p>
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