## EE5600 Assignment 1

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Abstract—This document contains the solution to a Lines and planes problem.

Download all python codes from

https://github.com/sahilsin/AI ML/Assignment 1/ codes

## $F)\left(\frac{3}{2} - \frac{-5}{3}\right)\mathbf{x} = -2$ (1.0.16)

$$\left(\frac{1}{3} \quad \frac{1}{2}\right)\mathbf{x} = \frac{13}{6} \tag{1.0.17}$$

(1.0.18)

## 1 Problem

Find the intersection of the following lines.

$$A) \begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = 14 \tag{1.0.1}$$

$$\begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{x} = 4 \tag{1.0.2}$$

(1.0.3)

A) We converted these line vectors in augmented

2 Solution

**Approach**: For finding the intersection of these

matrix form:

$$B) \begin{pmatrix} 1 & -1 \end{pmatrix} \mathbf{x} = 3 \tag{1.0.4}$$

$$\left(\frac{1}{3} \quad \frac{1}{2}\right)\mathbf{x} = 6\tag{1.0.5}$$

 $\begin{pmatrix} 1 & 1 & 14 \\ 1 & -1 & 4 \end{pmatrix}$ 

(1.0.6)Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

$$C) \begin{pmatrix} 3 & -1 \end{pmatrix} \mathbf{x} = 3 \tag{1.0.7}$$

$$(9 -3)\mathbf{x} = 9 \tag{1.0.8}$$

$$\begin{pmatrix} (1.0.8) \\ (1.0.9) \end{pmatrix} \begin{pmatrix} 1 & 1 & 14 \\ 1 & -2 & -10 \end{pmatrix}$$

Applying 
$$R_2 = \frac{R_2}{-2}$$

Applying  $R_2 = R_2 - R_1$ 

$$D) (0.2 \quad 0.3) \mathbf{x} = 1.3 \tag{1.0.10}$$

Applying  $R_1 = R_1 - R_2$ (1.0.12)

$$E)\left(\sqrt{2} \quad \sqrt{3}\right)\mathbf{x} = 0 \tag{1.0.13}$$

$$\left(\sqrt{3} \quad \sqrt{8}\right)\mathbf{x} = 0 \tag{1.0.14}$$

(1.0.15)

As left part is converted into a identity matrix the intersection vector is (9 5)

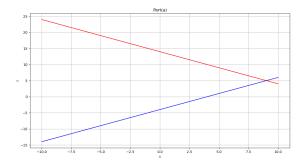


Fig. 0.1: part(a)

B) We converted these line vectors in augmented matrix form:

$$\begin{pmatrix} 1 & -1 & 3 \\ \frac{1}{3} & \frac{1}{2} & 6 \end{pmatrix}$$

Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

Applying  $R_2=6*R_2$ 

$$\begin{pmatrix} 1 & -1 & 3 \\ 2 & 3 & 36 \end{pmatrix}$$

Applying  $R_2 = R_2 - 2 R_1$ 

$$\begin{pmatrix}
1 & -1 & 3 \\
0 & 5 & 30
\end{pmatrix}$$

Applying 
$$R_2 = \frac{R_2}{5}$$

$$\begin{pmatrix} 1 & -1 & 3 \\ 0 & 1 & 6 \end{pmatrix}$$

Applying  $R_1 = R_1 + R_2$ 

$$\begin{pmatrix} 1 & 0 & 9 \\ 0 & 1 & 6 \end{pmatrix}$$

As left part is converted into a identity matrix the intersection vector is (9 6)

C) We converted these line vectors in augmented matrix form:

$$\begin{pmatrix} 3 & -1 & 3 \\ 9 & -3 & 9 \end{pmatrix}$$

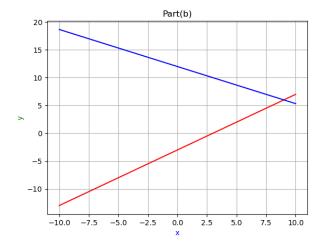


Fig. 0.2: part(b)

Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

Applying 
$$R_2 = \frac{R_2}{3}$$

$$\begin{pmatrix} 1 & -1 & 3 \\ 1 & -1 & 3 \end{pmatrix}$$

As  $R_1 = R_2$ , left part can never be converted into a identity matrix, and we can see now both row are same that means both lines are same they intersect at infinitely many points.

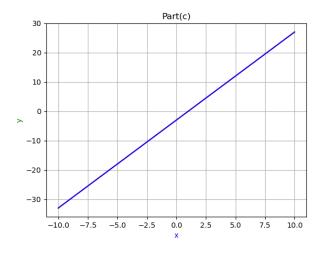


Fig. 0.3: part(c)

D) We converted these line vectors in augmented matrix form:

$$\begin{pmatrix} 0.2 & 0.3 & 1.3 \\ 0.4 & 0.5 & 2.3 \end{pmatrix}$$

Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

Applying  $R_2 = R_2 - 2 R_1$ 

$$\begin{pmatrix} 0.2 & 0.3 & 1.3 \\ 0 & -0.1 & -0.3 \end{pmatrix}$$

Applying 
$$R_2 = \frac{R_2}{-0.1}$$

$$\begin{pmatrix} 0.2 & 0.3 & 1.3 \\ 0 & 1 & 3 \end{pmatrix}$$

Applying  $R_1 = R_1 - 0.3 * R_2$ 

$$\begin{pmatrix}
0.2 & 0 & 0.4 \\
0 & 1 & 3
\end{pmatrix}$$

Applying 
$$R_1 = \frac{R_1}{0.2}$$

$$\begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 3 \end{pmatrix}$$

As left part is converted into a identity matrix the intersection vector is  $\begin{pmatrix} 2 & 3 \end{pmatrix}$ 

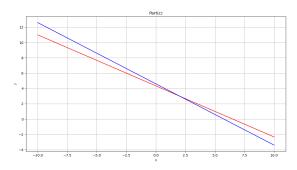


Fig. 0.4: part(d)

E) We converted these line vectors in augmented matrix form:

$$\begin{pmatrix} \sqrt{2} & \sqrt{3} & 0 \\ \sqrt{3} & \sqrt{8} & 0 \end{pmatrix}$$

Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

Applying 
$$R_2 = R_2 - \frac{\sqrt{3}}{\sqrt{2}} * R_1$$

$$\begin{pmatrix}
\sqrt{2} & \sqrt{3} & 0 \\
0 & \frac{1}{\sqrt{2}} & 0
\end{pmatrix}$$

As we see whatever operation we are applying last column of our augmented matrix remains zero. So the lines are homogeneous lines and they always pass through origin, the intersection vector is  $\begin{pmatrix} 0 & 0 \end{pmatrix}$ 

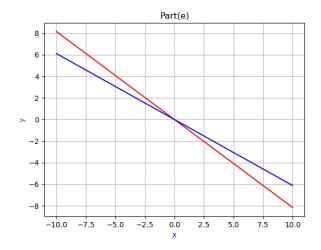


Fig. 0.5: part(e)

F) We converted these line vectors in augmented matrix form:

$$\begin{pmatrix} \frac{3}{2} & \frac{-5}{3} & -2\\ \frac{1}{3} & \frac{1}{2} & \frac{13}{6} \end{pmatrix}$$

Now We will apply Row elementary operation to convert left part of matrix to identity matrix.

Applying  $R_1=6*R_1$  and  $R_2=6*R_2$ 

$$\begin{pmatrix} 9 & -10 & -12 \\ 2 & 3 & 13 \end{pmatrix}$$

Applying  $R_1 = R_1 - 4 R_2$ 

$$\begin{pmatrix} 1 & -22 & -64 \\ 2 & 3 & 13 \end{pmatrix}$$

Applying  $R_2=R_2-2*R_1$ 

$$\begin{pmatrix} 1 & -22 & -64 \\ 0 & 47 & 141 \end{pmatrix}$$

Applying 
$$R_2 = \frac{R_2}{47}$$

$$\begin{pmatrix} 1 & -22 & -64 \\ 0 & 1 & 3 \end{pmatrix}$$

Applying  $R_1 = R_1 + 22 R_2$ 

$$\begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 3 \end{pmatrix}$$

As left part is converted into a identity matrix the intersection vector is  $\begin{pmatrix} 2 & 3 \end{pmatrix}$ 

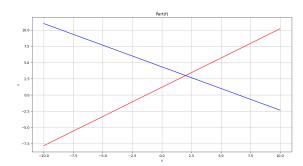


Fig. 0.6: part(f)