

Control Systems

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CONTENTS

The Full Circuit referred to this problem is shown below which is a CC-CB amplifier :

1 Feedback Circuits 1

Abstract—The objective of this manual is to introduce control system design at an elementary level.

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1 FEEDBACK CIRCUITS

1.0.1. Complete the table entries given below :

Solution:

0.6

Transistor	$I_E(mA)$	$r_e(ohm)$	$g_m(mA/V)$	$r_\pi(K\Omega)$	β_o	$f_T(MHz)$	$C_\mu(pF)$	$C_\pi(pF)$	$f_\beta(MHz)$
(a)	2				100	500	2		
(b)		25					2	10.7	4
(c)				2.5	100	500		10.7	
(d)	10				100	500	2		
(e)	0.1				100	150	2		
(f)	1				10	500	2		
(g)						800	1	9	80

TABLE 1.0.1: Initial table

We have to fill this table from part a to part g. We can neglect r_π

1.0.2. We have to find the missing values of the table.

Solution: We will solve it part by part.

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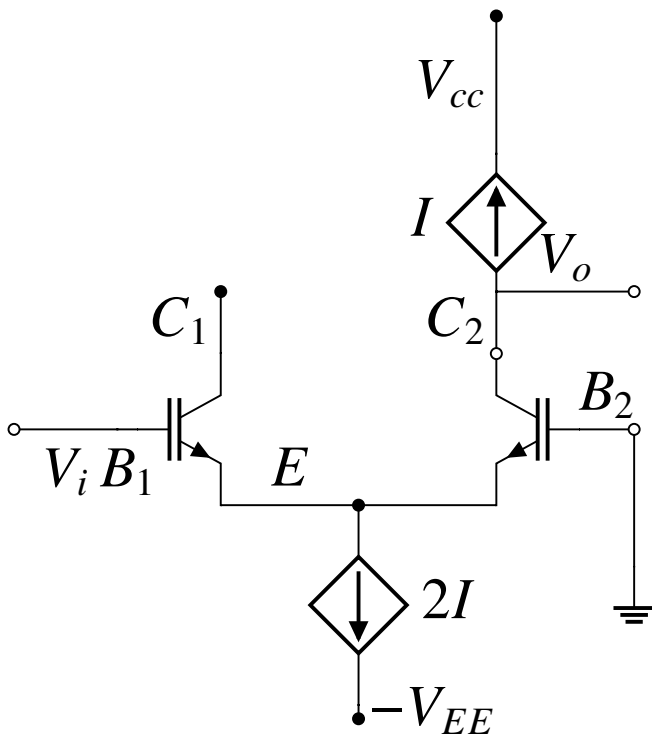


Fig. 1.0.2: Complete Circuit

1.0.3. First we will represent the given circuit using a Small Signal Equivalent Model.

Solution: The simplified small signal circuit for the above complete circuit is shown below :

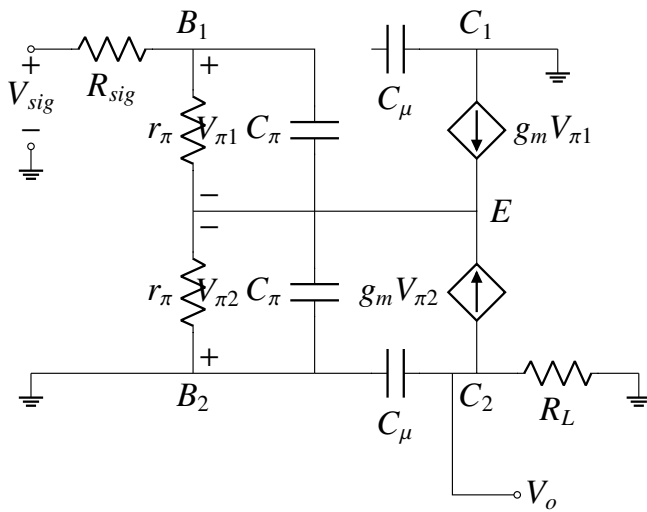


Fig. 1.0.3: Small signal Model

1.0.4. Part A : We have to find values of : r_e , g_m , r_π , C_π , f_β

Solution:

$$r_e = \frac{V_T}{I_E} = 25/2 = 12.5\Omega$$

$$r_e = 12.5\Omega$$

$$g_m = \frac{I_C}{V_T} = \left(\frac{\beta}{\beta + 1}\right) \frac{I_E}{V_T} = \left(\frac{100}{100 + 1}\right) \frac{2}{25}$$

$$g_m = 79.2 \frac{mA}{V}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{100}{79.2 * 0.001} = 1.26k\Omega$$

$$r_\pi = 1.26k\Omega$$

$$f_\beta = \frac{f_T}{\beta} = \frac{500 * 10^6}{100} = 5MHz$$

$$f_\beta = 5MHz$$

$$C_\pi = \frac{g_m}{2\pi f_\beta} - C_\mu$$

$$= \frac{79.2 * 0.001}{2 * \pi * 10^8} - (2 * 10^{-12})$$

$$= 23 \text{ pF}$$

$$C_\pi = 23pF$$

1.0.5. Part B : We have to find values of : I_e , g_m , r_π , β_o , f_T

Solution:

$$I_E = \frac{V_T}{r_e} = \frac{25}{25} = 1mA$$

$$I_E = 1mA$$

$$g_m = \frac{I_E}{V_T} = \frac{1}{25} = 40mA/V$$

$$g_m = 40 \frac{mA}{V}$$

$$r_\pi = \frac{1}{2\pi(C_\pi + C_\mu)f_\beta}$$

$$= \frac{1}{2\pi(10.7 + 2) * 10^{-12} * 4 * 10^6}$$

$$= 3.13 \text{ k}\Omega$$

$$r_\pi = 3.13k\Omega$$

$$\beta_o = g_m r_\pi$$

$$= 3.13 * 10^3 * 40 * 10^{-3}$$

$$= 125$$

$$\beta_o = 125$$

$$f_T = \beta f_\beta$$

$$= 125 * 4 * 10^6$$

$$= 500 \text{ MHz}$$

$$f_T = 500MHz$$

$$f_\beta = \frac{T}{\beta}$$

$$= \frac{500 * 10^6}{100}$$

$$= 5 \text{ MHz}$$

$$f_\beta = 5MHz$$

$$g_m = \frac{\beta}{r_\pi}$$

$$= \frac{100}{2500}$$

$$= 40 \text{ mA/V}$$

$$g_m = 40 \frac{mA}{V}$$

$$I_E = g_m V_T = 40 * 25 = 1mA$$

$$I_E = 1mA$$

$$r_e = \frac{V_T}{I_E}$$

$$= \frac{25}{1} = 25\Omega$$

$$r_e = 25\Omega$$

$$C_\mu = \frac{g_m}{2_T} - C - \pi$$

$$= \frac{40 * 0.001}{2 * \pi * 500 * 10^8} - (10.7 * 10^{-12})$$

$$= 2.03 \text{ pF}$$

$$C_\mu = 2.03pF$$

1.0.6. Part C : We have to find values of : f_β , g_m , r_e , I_E , C_μ

Solution:

1.0.7. Part D : We have to find values of : f_β , g_m ,
 r_e , r_π , C_π

Solution:

$$r_e = \frac{V_T}{I_E} = \frac{25}{10} = 2.5\Omega$$

$$r_e = 2.5\Omega$$

$$g_m = \frac{I_E}{V_T} = \frac{10}{25} = 0.4A/V$$

$$g_m = 0.4 \frac{A}{V}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{100}{0.4} = 250\Omega$$

$$r_\pi = 250\Omega$$

$$f_\beta = \frac{T}{\beta} = \frac{500 * 10^6}{100} = 5MHz$$

$$f_\beta = 5MHz$$

$$C_\pi = \frac{g_m}{2\pi f_T} - C_\mu$$

$$= \frac{0.4}{2 * \pi * 500 * 10^6} - (2 * 10^{-12})$$

$$= 125 \text{ pF}$$

$$C_\pi = 125pF$$

$$r_e = \frac{V_T}{I_E} = \frac{25}{0.1} = 250\Omega$$

$$r_e = 250\Omega$$

$$g_m = \frac{I_E}{V_T} = \frac{0.1}{25} = 4mA/V$$

$$g_m = 4 \frac{mA}{V}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{100}{0.004} = 25K\Omega$$

$$r_\pi = 25K\Omega$$

$$f_\beta = \frac{T}{\beta} = \frac{150 * 10^6}{100} = 1.5MHz$$

$$f_\beta = 1.5MHz$$

$$C_\pi = \frac{g_m}{2\pi f_T} - C_\mu$$

$$= \frac{0.004}{2 * \pi * 150 * 10^6} - (2 * 10^{-12})$$

$$= 2.24 \text{ pF}$$

$$C_\pi = 2.24pF$$

1.0.9. Part F : We have to find values of : f_β , g_m ,
 r_e , r_π , C_π

Solution:

1.0.8. Part E : We have to find values of : f_β , g_m ,
 r_e , r_π , C_π

Solution:

$$r_e = \frac{V_T}{I_E} = \frac{25}{1} = 25\Omega$$

$$r_e = 25\Omega$$

$$g_m = \frac{I_E}{V_T} = \frac{1}{25} = 40mA/V$$

$$g_m = 40 \frac{mA}{V}$$

$$r_\pi = \frac{\beta}{g_m} = \frac{100}{0.004} = 2500\Omega$$

$$r_\pi = 2500\Omega$$

$$f_\beta = \frac{T}{\beta} = \frac{500 * 10^6}{10} = 50MHz$$

$$f_\beta = 50MHz$$

$$C_\pi = \frac{g_m}{2\pi f_T} - C_\mu$$

$$= \frac{0.04}{2 * \pi * 500 * 10^6} - (2 * 10^{-12})$$

$$= 10.7 \text{ pF}$$

$$C_\pi = 10.7pF$$

$$r_\pi = \frac{1}{2\pi(C_\pi + C_\mu)f_\beta}$$

$$= \frac{1}{2\pi(9 + 1) * 10^{-12} * 80 * 10^6}$$

$$= 199 \Omega$$

$$r_\pi = 199\Omega$$

$$g_m = \frac{\beta}{r_\pi} = \frac{10}{199} = 50mA/V$$

$$g_m = 50 \frac{mA}{V}$$

$$I_E = g_m V_T = 0.05 * 0.025 = 1.25mA$$

$$I_E = 1.25mA$$

$$r_e = \frac{V_T}{I_E} = \frac{25}{1.25} = 20\Omega$$

$$r_e = 20\Omega$$

Part G : We have to find values of : β, f_β, g_m
 $, r_e, I_E$

Solution:

$$\beta = \frac{T}{f_\beta} = \frac{800}{80} = 10$$

$$\beta = 10$$

1.0.10. Given the following values the final table is :

Transistor	$I_E(mA)$	$r_e(ohm)$	$g_m(mA/V)$	$r_\pi(K)$	β_o	$f_T(MHz)$	$C_\mu(pF)$	$C_\pi(pF)$	$f_\beta(MHz)$
(a)	2	12.5	79.2	1.26	100	500	2	23	5
(b)	1	25	40	3.13	125	500	2	10.7	4
(c)	1	25	40	2.5	100	500	2.30	10.7	5
(d)	10	2.5	400	0.25	100	500	2	125	5
(e)	0.1	250	4	25	100	150	2	2.24	1.5
(f)	1	25	40	2.5	10	500	2	10.7	50
(g)	1.25	20	50	0.199	10	800	1	9	80

TABLE 1.0.10

1.0.11. Verify the above calculations using a Python code.

Solution:

```
codes/es17btech11019/es17btech11019_calc.
py
```