

Reinforcement Learning

| Parameter | Description | Parameter | Description |
|-----------|----------------------|-------------|----------------------------|
| i | Type of the Pipe | e_t | Efficiency Percentage |
| j | Transfer Location | T_i | Standard Production Time |
| t | Time (day) | $F_{i,t}$ | Forecast Order Quantity |
| $m_{i,t}$ | Stock Level | $Q_{i,j,t}$ | Total Order Quantity |
| n | Order Quantity Limit | $a_{i,j,t}$ | Transferred Order Quantity |
| c | Stock Capacity | p_t | Penalty |

Table 1: RL Parameters.

State Vector:

$$s_t = (F_{1,t}, \dots, F_{I,t}, Q_{1,1,t}, \dots, Q_{I,J,t}, m_{1,t}, \dots, m_{I,t})$$

Action Vector:

$$a_t = (a_{1,1,t}, \dots, a_{I,J,t})$$

Reward Function:

$$\begin{aligned}
 p_t - T_i &\leftarrow p_t \quad \text{if } c > m_{i,t} + a_{i,1,t} \\
 p_t + T_i &\leftarrow p_t \quad \text{if } Q_{i,t,j} > n \\
 p_t + T_i &\leftarrow p_t \quad \text{if } Q_{i,t,j} > 0 \quad \text{and} \quad m_{i,t} = 0
 \end{aligned}$$

State Transitions:

$$\begin{aligned}
 m_{i,t+1} &= m_{i,t} + a_{i,1,t} + \text{abs}(\min(Q_{i,j,t+1} - a_{i,j,t}, 0)) \\
 Q_{i,j,t+1} &= Q_{i,j,t} - a_{i,j,t}
 \end{aligned}$$