

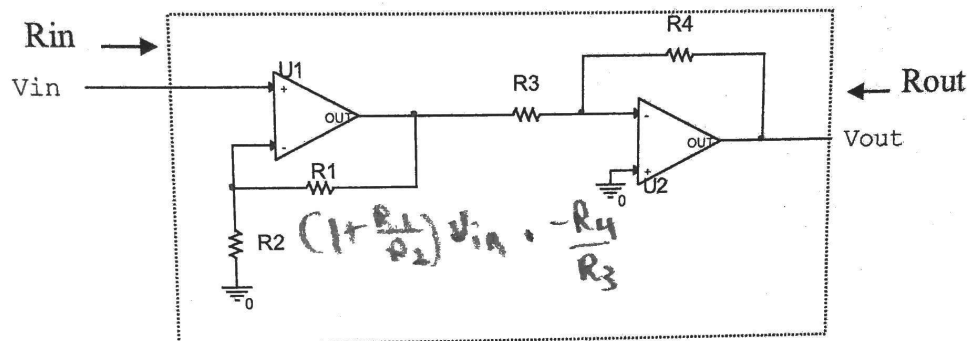
## Homework 3

Reading: Chapter 2.5-2.8

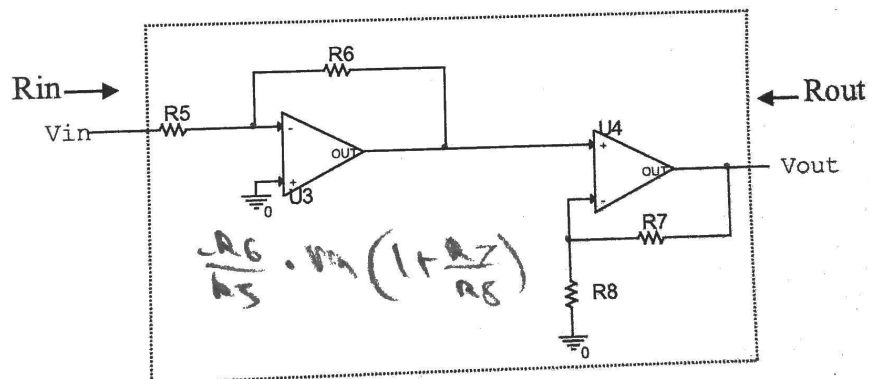
## 1) Amplifier models

For each of the following circuits,

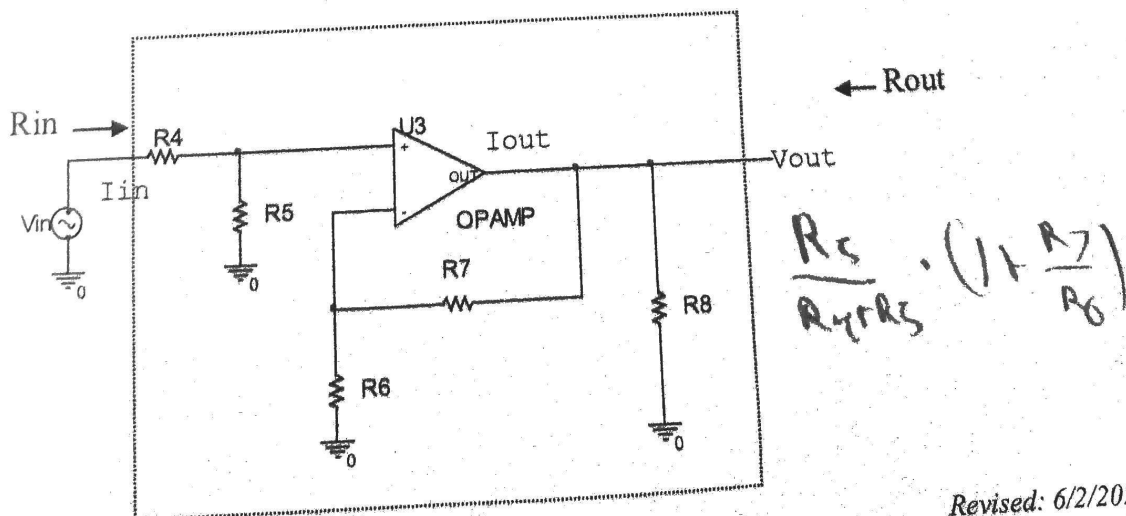
- Determine the input resistance,  $R_{in}$ , seen by the source
- The output resistance,  $R_{out}$ , seen at the load.
- The overall gain of the circuit,  $A_{circuit} = V_{out}/V_{in}$ .
- Redraw the circuit, using the equivalent dependent source model, with



a)

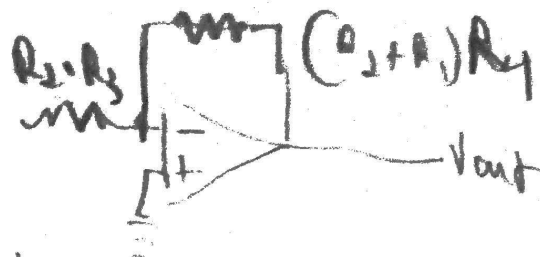


b)



1 A:

i: simplify to

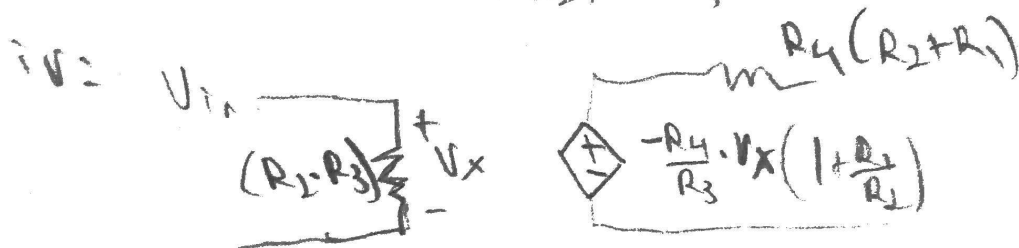


$$R_{in} = R_2 \cdot R_3$$

$$ii: \frac{V_{out}}{I_{out}} = \frac{-R_4}{R_3} \left(1 + \frac{R_1}{R_2}\right) \cdot V_{in} \quad I_{out} = I_{A1} = \frac{V_{in}}{R_2 \cdot R_3}$$

$$R_{out} = R_4(R_2 + R_1)$$

$$iii: \text{gain} = \left(1 + \frac{R_1}{R_2}\right) \cdot \frac{-R_4}{R_3}$$



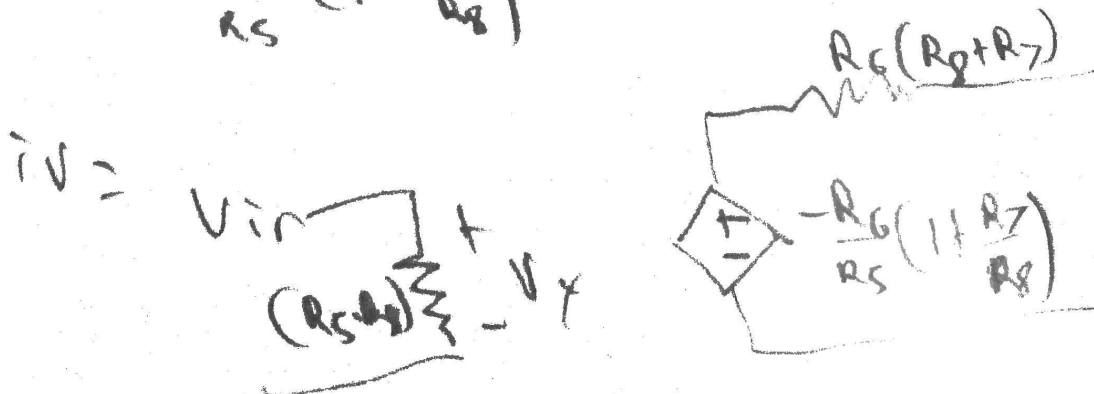
B: i: simplify to:



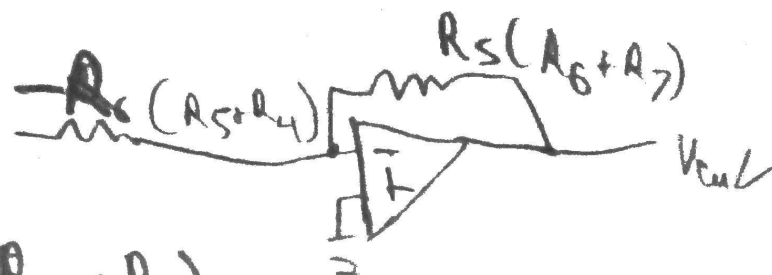
$$R_{in} = R_5 \cdot R_8$$

$$ii: R_{out} = R_6(R_8 + R_7)$$

$$iii: \frac{-R_6}{R_5} \left(1 + \frac{R_7}{R_8}\right)$$



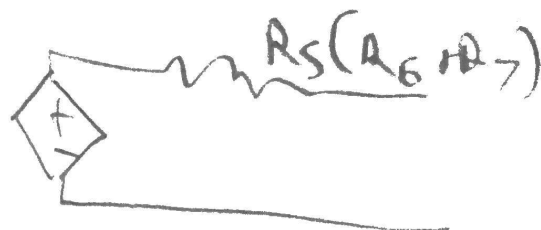
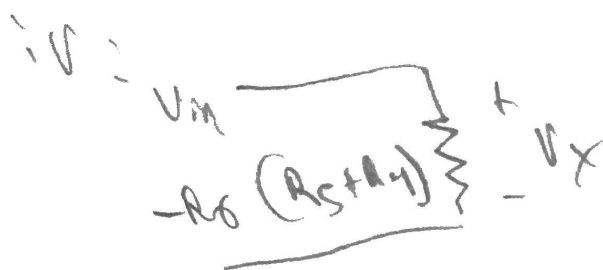
(2) simplify to



$$R_{in} = -R_6(R_5 + R_4)$$

$$ii: R_{out} = R_S(R_6 + R_7)$$

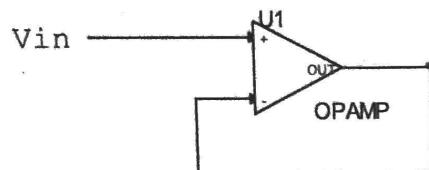
$$iii: \text{gain} = \left( \frac{R_6 + R_7}{R_6} \right) \left( \frac{R_S}{R_5 + R_4} \right)$$



## 2) DC Bias characteristics

The bias characteristics for the following amplifiers are

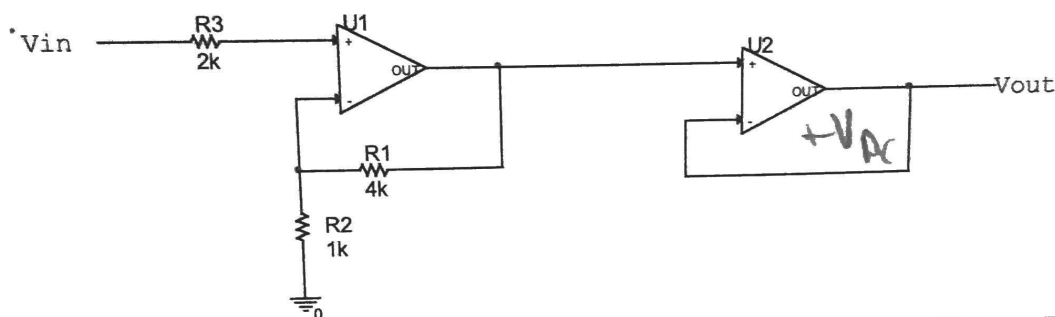
- 1)  $V_{DC\text{offset}} = 5\text{mV}$
- 2)  $I_{\text{bias}}^- = 0.5\mu\text{A}$
- 3)  $I_{\text{bias}}^+ = 0.5\mu\text{A}$



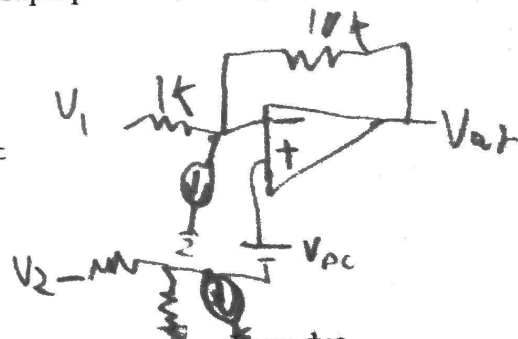
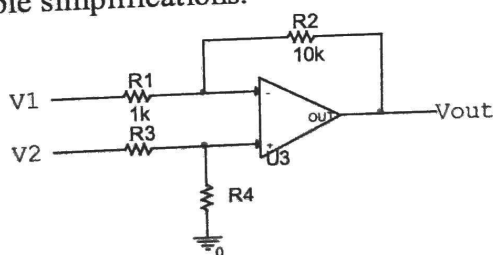
$$V_{\text{out}} = V_{\text{in}} + (1 + \frac{R_2}{R_1})V_{DC} + I_{\text{bias}} R_2$$

$$V_{\text{out}} = V_{\text{in}} + 5\text{mV}$$

- a) Determine the output voltage due to DC biases.



- b) Determine the output voltage due to DC biases. Both op-amps will have DC bias sources. Include sketches of the circuits you use for superposition, though, you can make reasonable simplifications.



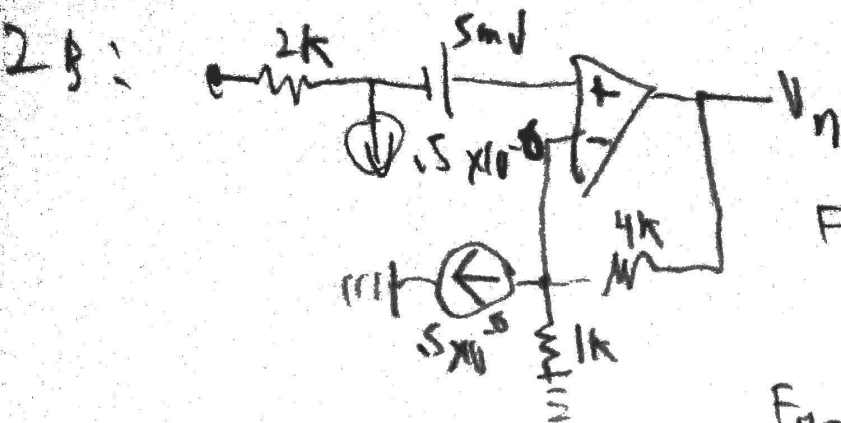
- c) Choose  $R_3$  and  $R_4$  such that the difference amplifier has zero output voltage due to DC bias sources and is balanced,  $V_{\text{out}} = -R_2/R_1 \cdot (V_2 - V_1)$

$$\text{For } V_1 = -10\text{V},$$

$$\text{For } V_2 = \frac{V_2(R_3)}{R_3 + R_4} \cdot (1 + 10)$$

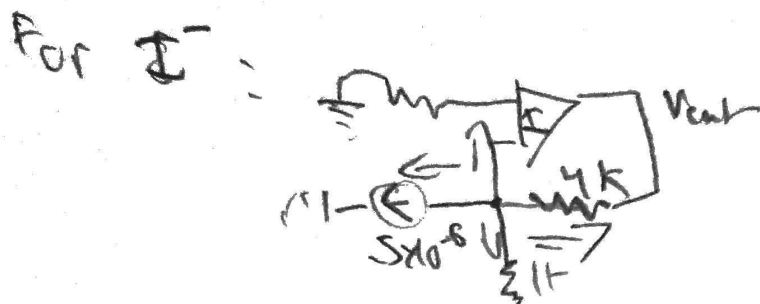
$$V_{DC\text{ offset}} = V_{DC}$$

$$I_{\text{bias}}^+ = -\left(\frac{1}{R_3} + \frac{1}{R_4}\right)^{-1} (11)(0.5\mu\text{A}) = -5.5\mu\text{V} \cdot \left(\frac{1}{R_3} + \frac{1}{R_4}\right)^{-1}$$



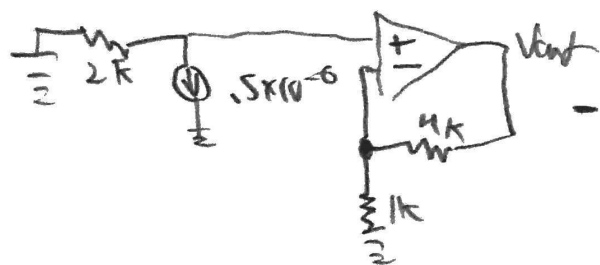
For  $V_{OC}$ :  $V_n = V_{OC}(1+4)$   
 $= 25\text{mV}$

For  $V_1$ :  $V_n = V_1(5)$



$5 \times 10^{-6}(4\text{k}) = .002\text{mV}$

For  $I^+$



$-.5 \times 10^{-6}(2\text{k})(5) = -.005\text{mV}$

$V_{out} = 25\text{mV} + 5V_1 - 5\text{mV} + 2\text{mV} = 5V_1 + 22\text{mV} + 5\text{mV}$

$V_{out} = 5V_1 + 22\text{mV} + 5\text{mV}$

$I^-: V_{out} = 0.5\text{mA} \cdot 10\text{k} = 5\text{mV}$

2c

$V_{out} = 10(V_2 - V_1) = 10V_2 - 10V_1$

$= 11V_2 \frac{R_4}{R_3 + R_4} - 10V_1 + 55\text{mV} - 5.5\text{mV} \left( \frac{1}{R_3} + \frac{1}{R_4} \right)^{-1} + 5\text{mV}$

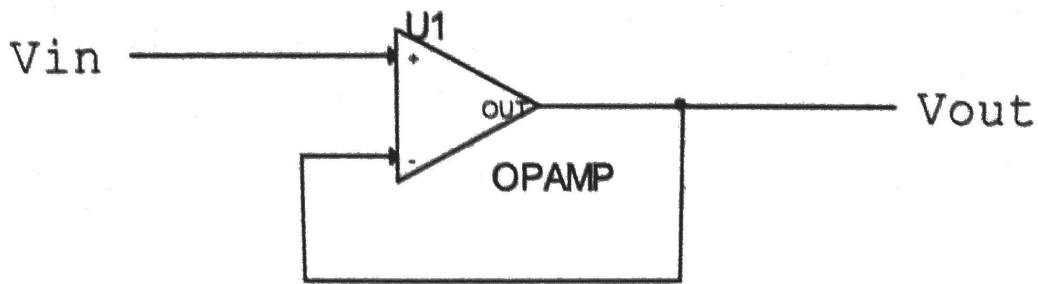
$\frac{R_4}{R_3 + R_4} = \frac{10}{11}$

$\frac{R_3 \cdot R_4}{R_3 + R_4} = \frac{120}{11}$

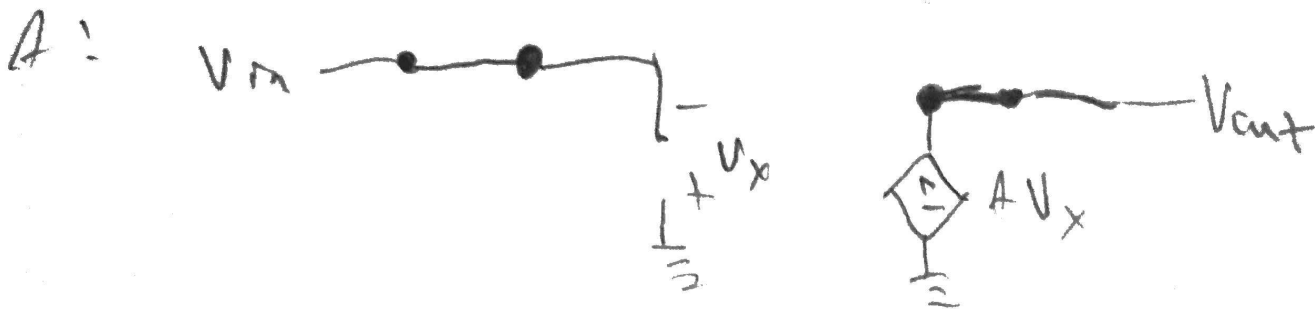
$R_4 = 120$

$R_3 = 12$

## 3) Finite op-amp gain



- Sketch the equivalent circuit when considering the finite gain op-amp model (the dependent source model of the op-amp itself with finite gain  $A_{\text{op-amp}}$ ).
- Verify that your answer approaches the ideal result as  $A_{\text{op-amp}} \rightarrow \infty$ .
- For  $V_{\text{in}} = 5\text{V}$  and an internal finite op-amp gain of  $10^5$ , determine the output voltage. Would you consider the effect due to finite gain to be negligible?



B:

$$V_{\text{out}} = A(V_{\text{in}} - V_{\text{out}}) \quad \text{Gain} = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{A}{A+1}$$

$$A \rightarrow \infty : \frac{\infty}{\infty+1} = 1 \rightarrow \text{needed for voltage follower}$$

C:

$$V_{\text{out}} = \frac{10^5}{10^5 + 1} \cdot 5 \approx 4.999... \text{V}$$

negligible