

Grading: Pick part a or b in Units 1, 2, 3 (Problems 3-6),
You must answer both Problem 1 and Problem 2
This Homework will replace lowest homework score

Problem 1) Filter Design 1

Design a filter that meets the specifications below. You need to pick values for any resistors, capacitors or inductors in your circuit. Simulate the circuit in PSpice to verify that your design meets specifications. Use the ideal amplifier component called OPAMP in your simulations. Note, small deviations from the design specifications are allowed and in a real circuit always exist, but they need to be small. Show calculations to justify your design (guessing in PSpice is not a design solution). (note: this problem has units Hz)

- Highpass filter with a cutoff frequency of 159MHz
- In the specified frequency range, the gain must be $>-3\text{dB}$
- The rolloff in the stopband should be 80dB
- The circuit should contain a single unity gain (voltage follower) amplifier stage (no other amplifiers should be in your circuit).

Second order -

I can't solve this one. I know it's 2nd order and the voltage follower looks like



Problem 2) Filter Design 2

Design a filter that meets the specifications below. You need to pick values for any resistors, capacitors or inductors in your circuit. Simulate the circuit in PSpice to verify that your design meets specifications. Note, small deviations from the design specifications are allowed and in a real circuit always exist, but they need to be small. Show calculations to justify your design (guessing in PSpice is not a design solution).

ω [rad/s]	$ H(s) $ in dB
10	6
100	6
1000	6
1E4	3
1E5	-14
1E6	-34

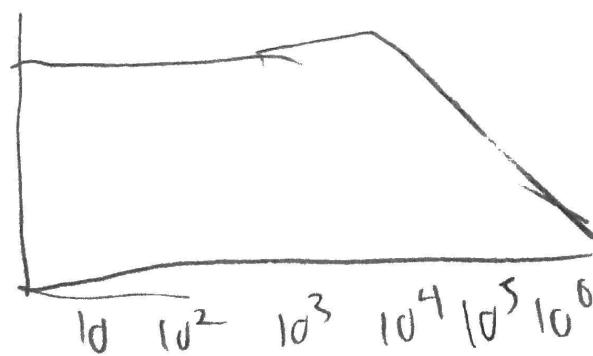
$$\text{cut off} = \frac{10^4}{2\pi} = 159\text{Hz}$$

pick $R = 100$

$$RC = 150$$

$$C = 1.528 \times 10^{-6}\text{F}$$

low pass

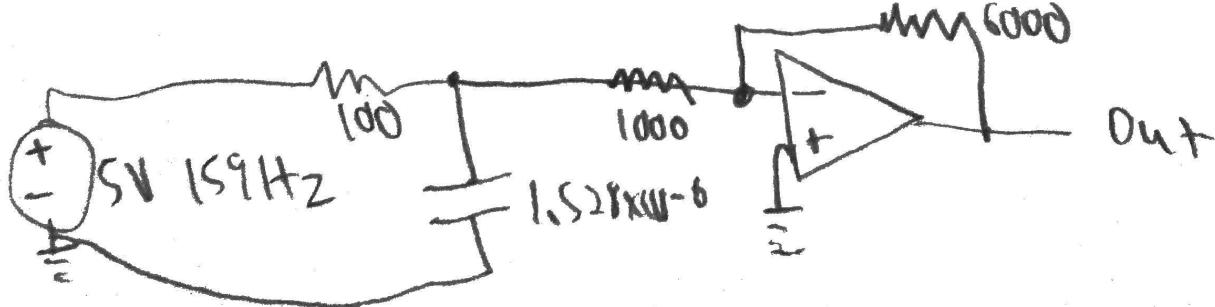


6 graph of $|H(j\omega)|$ in dB

-11 dB per decade

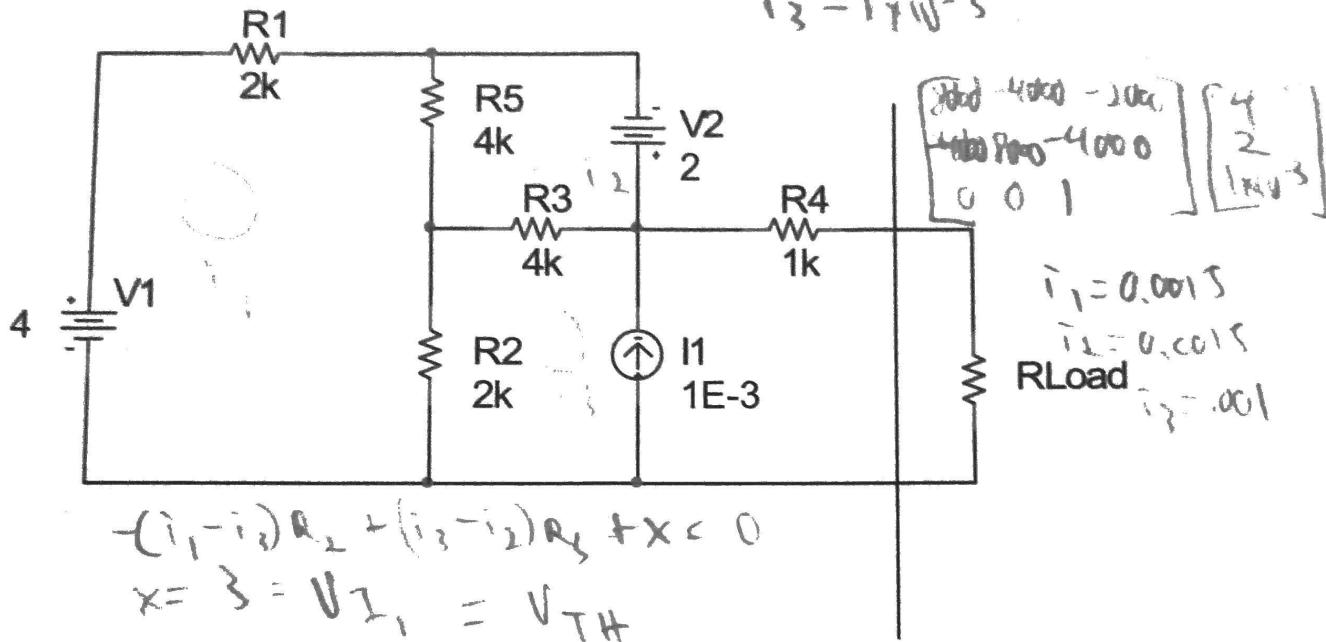
-20 dB/octave

straight line approximation
of -20 dB/octave

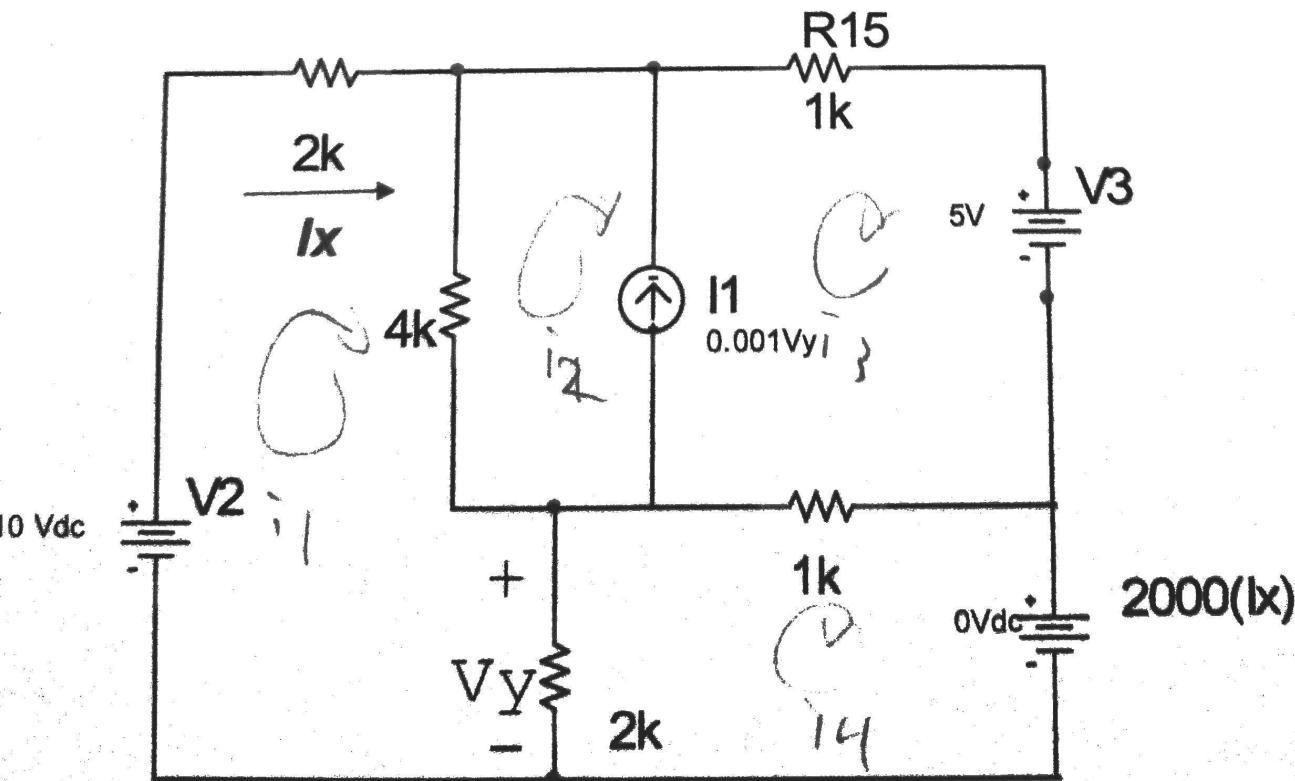


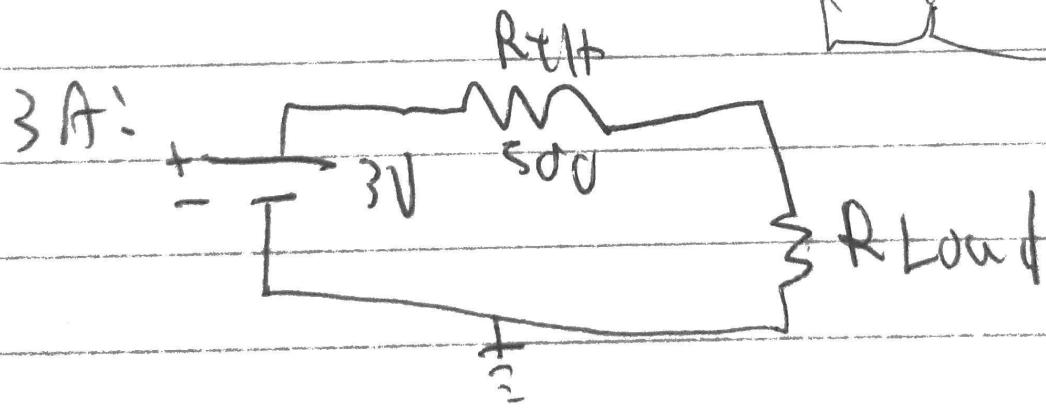
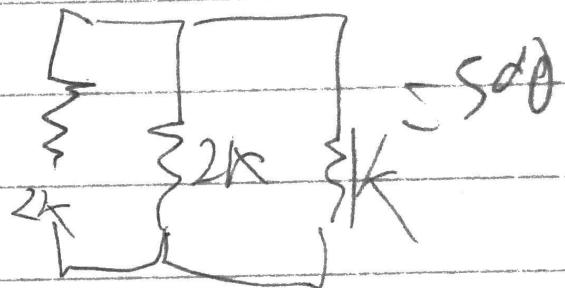
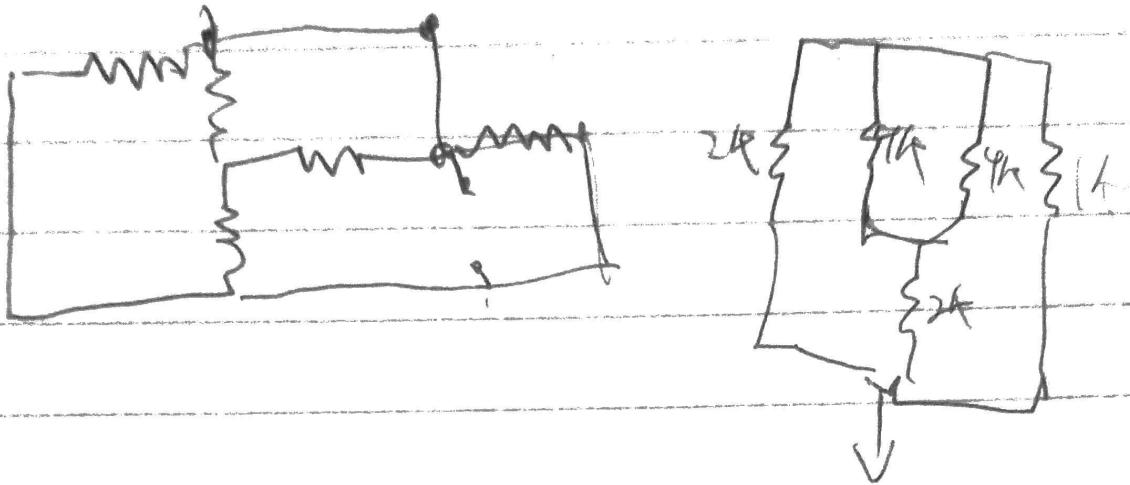
Problem 3) Thevenin/Norton

a. Find the Thevenin equivalent circuit.



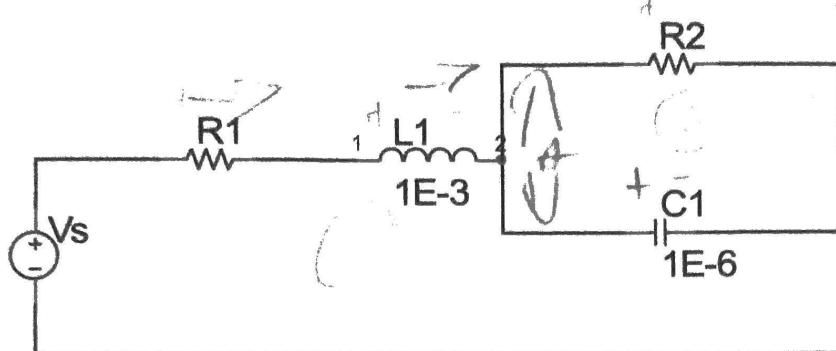
b. Find the current through the 4k resistor





Problem 4) Differential Equations and Laplace

a. Differential equations



$$\begin{aligned} I_{L_1} &= I_{R_1} = I_C \\ I_{L_1} &= \frac{V_C}{R_2} + C \frac{dV_C}{dt} \\ I_{R_1} &= I_{R_2} \\ \frac{V_C}{R_2} + C \frac{dV_C}{dt} &= I_{R_2} \end{aligned}$$

1. Determine the differential relationship for the voltage across C1.

$$\frac{V_C}{R_2} + C \frac{dV_C}{dt} = V_S - L \left(\frac{d^2V_C}{dt^2} + \frac{dV_C^2}{dt^2} \right) - V_C$$

$$\frac{R_1}{R_2} V_C + R_2 C \frac{dV_C}{dt} = V_S - \frac{L}{R_2} \frac{d^2V_C}{dt^2} + L \left(\frac{dV_C}{dt} \right)^2 - V_C$$

2. Determine values for R1 and R2 so that the circuit is underdamped.

2: We choose an extremely high resistance for R2 so it is effectively open circuit.

Prof. Sawyer said I could do this.

like:

$$R_2 = 100 \times 10^6 \text{ ohms}$$

$$\frac{V_C}{R_2} + C \frac{dV_C}{dt} = \frac{V_S - V_C}{R_2}$$

$$-L \frac{d^2V_C}{dt^2} + \frac{dV_C}{dt} \left(R_1 C + \frac{L}{R_2} \right) + V_C \left(\frac{R_1}{R_2} + \frac{1}{L} \right) =$$

$$\frac{dV_C^2}{dt^2} - \frac{R_1 (C_L + L)}{LC R_2} \frac{dV_C}{dt} - \frac{R_1 + R_2}{LC R_2} V_C = -\frac{V_S}{LC}$$

1:

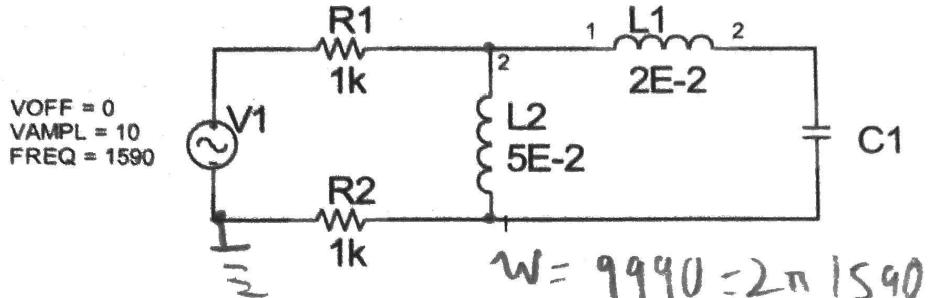
Now it is series RLC circuit

$$\frac{1}{2} \frac{R_1}{L} \angle \frac{1}{\sqrt{LC}} \quad R_1 = 63.24 \Omega$$

$$R_2 = 150 \times 10^6 \text{ ohms}, R_1 = 50 \text{ ohms}$$

Problem 5) AC Steady State Circuit Analysis

a. Phasors

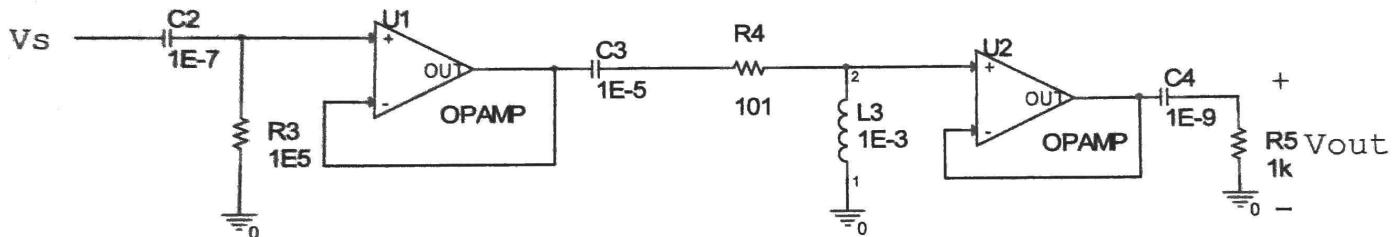


1. Determine a value for C_1 so that the current through the source is 5mA and has zero phase.

$$Z_{eq} = \frac{1}{j\omega C_1} + \left(\frac{1}{R_1} + j\omega L_1 + j\omega L_2 + \frac{1}{R_2} \right)^{-1} + j\omega C_1 = \frac{10}{5\mu\text{V}} + j\omega C_1$$

$$C_1 = 5.005 \times 10^{-7} \text{ F}$$

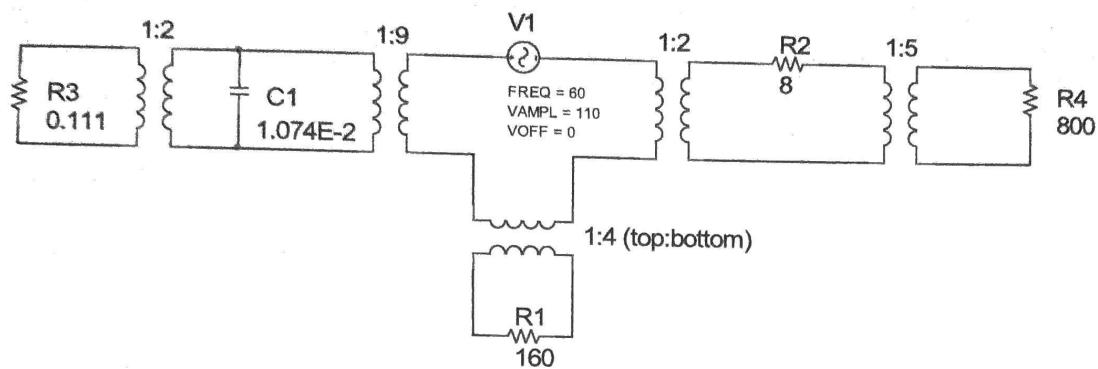
b. Frequency response



1. Sketch the Bode plots for the magnitude and phase, $H(s) = V_{out}/V_{in}$

Problem 6) Transformers and Power Circuits

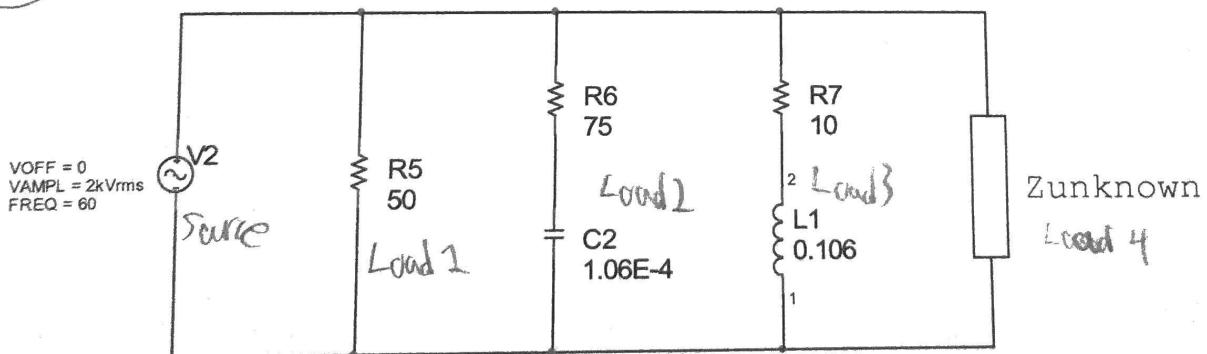
a. Transformers



1. Determine the phasor form of the current through the source.

2. Determine the total power in the left branch, (R_3 and C_1)

b. Power



1. Determine $Z_{unknown}$ such that the power produced is purely real.

2. Determine the power produced in each load and the source

$$\therefore \text{Load 4: } \frac{1}{2} \frac{(2k\sqrt{2})^2}{50} = 80000 \text{ W} = S$$

$$\text{Load 3: } \frac{1}{2} \frac{(2k\sqrt{2})^2}{10 + j10} = 23571.3 + j9418.6 \text{ J} = S$$

$$\text{Load 2: } \frac{1}{2} \frac{(2k\sqrt{2})^2}{75 + j25.02} = 47941 - j16012 \text{ J} = S$$

$$\text{Source: } \frac{(2k\sqrt{2})^2}{2 \cdot 26.4} = 151515.15 = S$$

$$\text{Current Law: } \left(\frac{1}{50} + \frac{1}{75 + j\frac{377}{1.06 \times 10^{-4}}} \right) I = \frac{1}{10 + j377 - 3j15}$$

$\omega = 377$

$$= 0.0377 - 0.01954j \quad \frac{1}{j\omega C} = 0.01954j$$

$$Z_{\text{unknown}} = \frac{1}{0.01954j} = -51.177 \quad Z_{\text{unknown}}$$

$$\frac{1}{j\omega C} = 51.177 \quad (\text{some capacitor}) \quad \frac{1}{j\omega C} = -51.177$$

Ventfraktion:

$$\left(\frac{1}{50} + \frac{1}{75 + j\frac{377}{1.06 \times 10^{-4}}} + \frac{1}{10 + j377 - 3j15} + \frac{1}{j\frac{377 \cdot 5.183 \times 10^{-5}}{F}} \right)^{-1}$$

$$\boxed{1: Z_{\text{unknown}} = \frac{1}{j\frac{377 \cdot 5.183 \times 10^{-5}}{F}} = 26.4 + 0.00j}$$

The circuit wouldn't accept the output of the filter in LTspice for an AC sweep so I disconnected it and as a result the gain was off. The cut off frequency is correct though.

