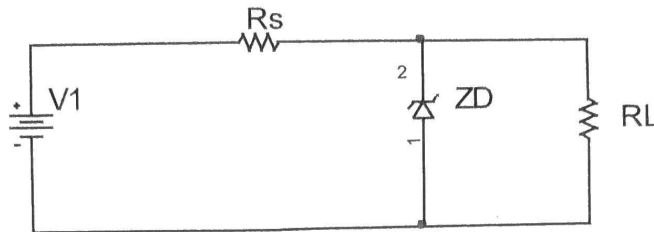


## Homework 9

## Problem 1) Zener Diodes



The above Zener diode has the following Knee voltages and currents,

$$V_{Knee} = 5.05V$$

$$I_{Knee} = 20mA$$

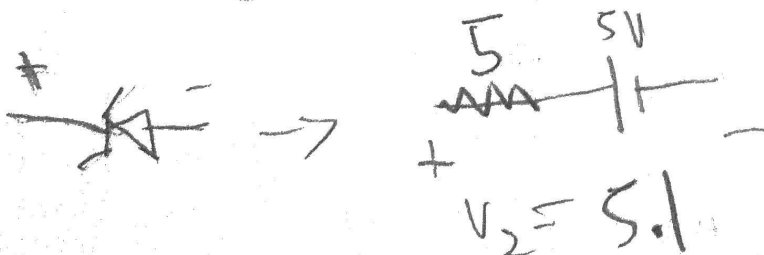
Additionally, the following measurements were taken when the diode was in breakdown

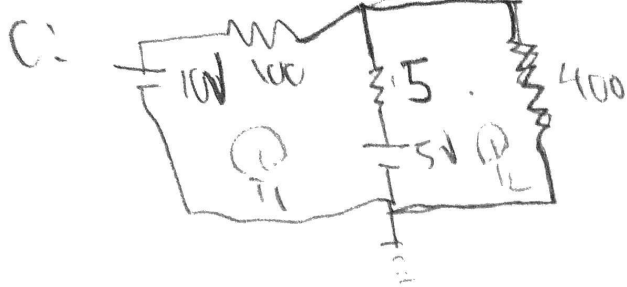
Measurement 1: at  $V_Z = 5.5V$ ,  $I_Z = 100mA$

Measurement 2: at  $V_Z = 5.6V$ ,  $I_Z = 120mA$

- Based on the above parameters, what is the minimum load voltage such that the Zener diode is in the breakdown region of operation.  $V_Z \geq 5.1V$
- Determine the equivalent linear model,  $r_Z$  and  $V_{Z0}$ , when the Zener diode is in breakdown. Sketch the equivalent circuit.
- For  $V_1 = 10V$ ,  $R_s = 100\Omega$ ,  $R_L = 400\Omega$ ,
  - Verify that the diode is in breakdown
  - Determine the power consumed by the diode and the power consumed by the load  $R_L$ .
- For  $V_1 = 15V$ ,  $R_s = 100\Omega$ ,  $R_L = 400\Omega$ ,
  - Verify that the diode is in breakdown
  - Determine the power consumed by the diode and the power consumed by the load  $R_L$
- Qualitatively, what can you say about load power when the circuit is in regulation (when the Zener diode is in breakdown)?
- If the Zener diode has a maximum current of  $100mA$ , what is the maximum source voltage?

B:  $r_Z = \frac{5.6 - 5.5}{(120 - 100) \times 10^{-3}} = 5 \Omega$  Linear analysis  $\rightarrow V_{Z0} = 5.0V$





$$i_1 10S - i_2 S = 5V$$

$$-5i_1 + 40S i_2 = 5V$$

$$i_1 = 0.048$$

$$i_2 = 0.013$$

Verify:  $(i_1 - i_2)S + 5V \geq 5.1$   
 $5.175 \geq 5.1$

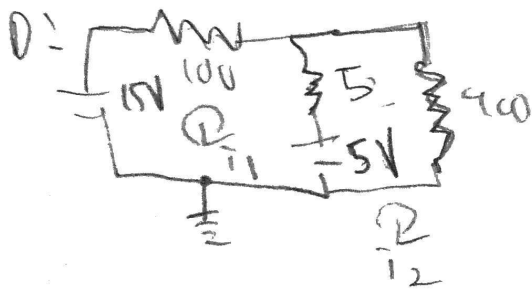
$$P_{RL} = (i_2)^2 R = 0.067 W$$

$$P_{Diode} = (i_1 - i_2)S + (i_1 - i_2)^2 S = 0.181 W$$

$$(i_1 - i_2) \geq 20 mA$$

$$35 mA \geq 20 mA$$

diode in breakdown



$$10S i_1 - i_2 S = 10$$

$$-5i_1 + 40S i_2 = 5V$$

$$i_1 = 0.1$$

$$i_2 = 0.014$$

Verify:  $(i_1 - i_2)S + 5V \geq 5.1$   
 $5.411 \geq 5.1$

$$P_{RL} = (i_2)^2 R = 0.074 W$$

$$P_{Diode} = (i_1 - i_2)S + (i_1 - i_2)^2 S = 0.445 W$$

$$(i_1 - i_2) \geq 20 mA$$

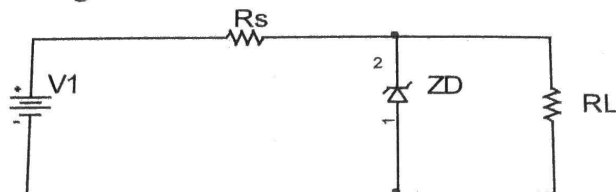
$$82 mA \geq 20 mA$$

diode in breakdown

E: Source power is mostly absorbed by the diode and  $R_S$  when the zener is in breakdown.

F:

## Problem 2) Ripple Voltage



The Zener diode in the above circuit has a Knee voltage of 5.1V, a Knee current of 20mA, and a Zener resistance of  $10\Omega$ . You can assume the Knee voltage and current lie on the linear approximation curve of the diode in reverse breakdown.

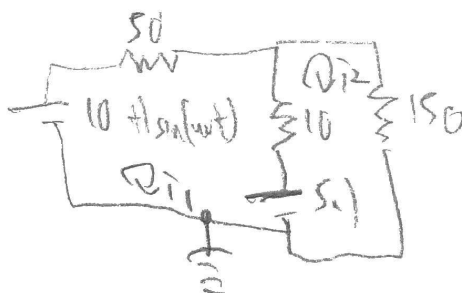
- Removing the diode from the circuit, for  $V1 = 10 + 1\sin(\omega t)$  V,  $R_s = 50\Omega$ ,  $R_L = 150\Omega$ , determine the DC voltage and peak-to-peak voltage of the load. Determine the ratio of the ripple voltage to the DC voltage.
- For the same circuit with the Zener diode included, determine the DC voltage and peak-to-peak voltage of the load. Determine the ratio of the ripple voltage to the DC voltage.
- Qualitatively, what can you say about the effect of the Zener diode when considering the above ratios.
- Add a second Zener diode in parallel with the first and verify that both diodes are in regulation. Again determine the ratio of the peak-to-peak voltage to the DC voltage. Did this ratio improve as expected? Why can't we keep adding Zener diode in parallel?

$$A: V_L = \frac{(10 + 1\sin(\omega t))(150)}{200} = 7.5 + 0.75\sin(\omega t) \quad V_{DC L} = 7.5V$$

$$\frac{V_{rip}}{V_{DC}} = 0.2$$

$$V_{rip} = 1.5V$$

$$B: \quad \begin{array}{c} \text{---} 10 \text{---} | \text{---} 5.1 \text{---} \\ + \quad \quad \quad - \\ v_2 = (20mA)10 + 5.1 = 5.3 \end{array}$$



Continued on  
next page →

$$-10 - 1\sin(\omega t) + i_1 50 + i_1 10 + 5.1 - i_2 10 = 0$$

$$60i_1 - 10i_2 = 4.9 + 1\sin(\omega t)$$

$$-5.1 + i_2 10 - i_1 10 + i_2 150 = 0$$

$$i_1 = 0.082 + 0.017\sin(\omega t) + 0.1$$

$$160i_2 - i_1 10 = 5.1$$

$$160i_2 = 2.62 + 0.17\sin(\omega t)$$

$$i_2 = 0.016 + 0.0010625\sin(\omega t)$$

B: continued  $V_2 = (i_1 - i_2) 10 + 5.1$

$$V_2 = 5.93 + 0.16 \sin(\omega t)$$

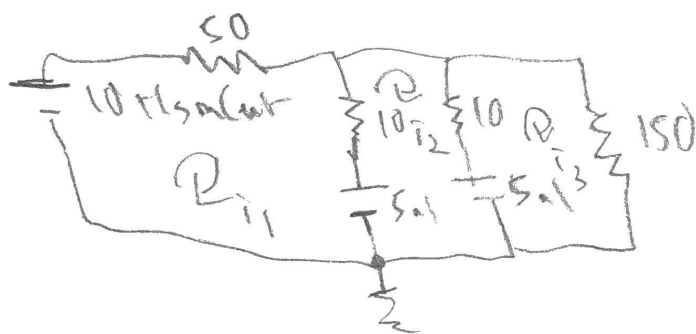
$$V_{OCL} = 5.93$$

$$V_{rip} = 0.32$$

$$\frac{V_{rip}}{V_{OCL}} = 0.05$$

C: The effect of the zener diode is to reduce ratio of the ripple to the load.

D:



$$-10 + i_1 50 - i_2 10 + 5.1 = 0$$

$$0 + i_2 20 - i_1 10 - i_3 10 = 0$$

$$-5.1 + i_3 160 - i_2 10 = 0$$

$$50 i_1 - 10 i_2 = 4.9 + 1 \sin(\omega t) \quad i_1 = 0.082 + 0.017 \sin(\omega t) + 0.17 i_2$$

$$20 i_2 - 10(0.082 + 0.017 \sin(\omega t) + 0.17 i_2) - i_3 10 = 0$$

$$20 i_2 - 0.82 - 0.17 \sin(\omega t) - 1.7 i_2 - i_3 10 = 0 \quad 18.3 i_2 = 0.82 + 0.17 \sin(\omega t) + 10 i_3$$

$$i_2 = 0.045 + 0.1 \sin(\omega t) + 0.55 i_3$$

$$160 i_3 - 10(0.045 + 0.1 \sin(\omega t) + 0.55 i_3) = 5.1$$

$$154.5 i_3 - 0.45 - 1 \sin(\omega t) = 5.1 \quad i_3 = 0.036 + 0.0065 \sin(\omega t)$$

$$R_L \cdot i_3 = V_{out} = 5.4 + 0.97 \sin(\omega t) \rightarrow \text{Voltage across all diodes is enough to cause breakdown.}$$

$$V_{rip} = \frac{1.94}{5.4} = 0.36$$

The ratio did not improve as expected. This is because each diode has small current draw taking it away from the load.

Hw 9 Prob 1 Part F:

KCL at node Above the Diode.

$$\frac{V_Z - V_1}{100} + 100 * 10^{-3} + \frac{V_Z}{400} = 0$$

$$\frac{5.5}{100} - \frac{V_1}{100} + 100 * 10^{-3} + \frac{5.5}{400} = 0$$

$$V_1 = 16.875V$$