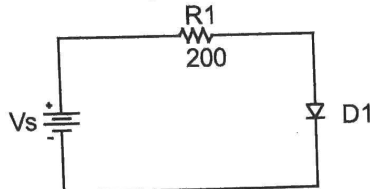


## Homework 8

Reading: 2.7-8, (Chapter 3 concepts), 4.1-3

## Problem 1) Diodes, bias point analysis

For all diodes in this section, the thermal voltage,  $V_{th}$ , is 26mV, the reverse saturation current,  $I_S$ , is 1E-12 A and the non-ideality factor,  $n$ , is 1.



*I use a python script for these problems*

- a) For  $V_s = 2V$ , find the DC bias point of the above diode
- Guess a diode voltage of 0.5V (no work necessary for this step).
  - Use KVL and Ohm's Law to find the current through the resistor (equal to the current through the diode).
  - Use the diode equation to find a diode voltage, based on the part b diode current.
  - Repeat parts b and c, until three significant digits are reached (the first three significant digits are not changing with each iteration).
  - Based on the bias point, determine the diode conductance  $g_D$ .
  - Using the slope of the tangent line ( $g_D$ ), the DC bias point voltage and current, determine the tangent line intercept,  $V_{D0}$ , on the x-axis (voltage axis).
  - Determine the linear equivalent circuit model for the diode,  $r_D = 1/g_D$ , in series with  $V_{D0}$ . Draw the equivalent circuit.
- (At this point, you may want to make script for this. I use a Matlab script, but you can probably set one up on your calculator.)

- b) Repeat the above process for  $V_s = 2.05V$  and  $V_s = 1.95V$ .

a. We can estimate the inverse of the slope of the diode curve using difference approximations,  $\frac{1}{m} = \frac{\Delta V_D}{\Delta I_D}$ . If a linear approximation is valid for the source varying 1.95V to 2.05V, then the slope calculations of the diode curve for source voltages  $V_s = 2V, 2.05V$  and  $V_s = 1.95V, 2V$  will be close in value. For a 100mV variation in source voltage, is a linear approximation of the diode curve valid?

- c) Repeat the above process for  $V_s = 2.5V$  and  $V_s = 1.5V$ .

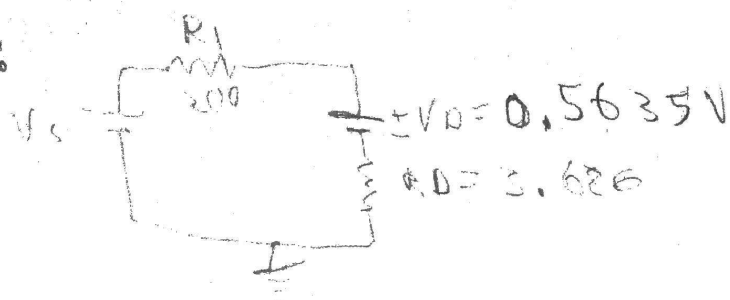
a. We can estimate the inverse of the slope of the diode curve using difference approximations,  $\frac{1}{m} = \frac{\Delta V_D}{\Delta I_D}$ . If a linear approximation is valid for the source varying 1.5V to 2.5V, then the slope calculations of the diode curve for source voltages  $V_s = 2V, 2.5V$  and  $V_s = 1.5V, 2V$  will be close in value. For a 1V variation in source voltage, is a linear approximation of the diode curve valid?

J. Braunstein

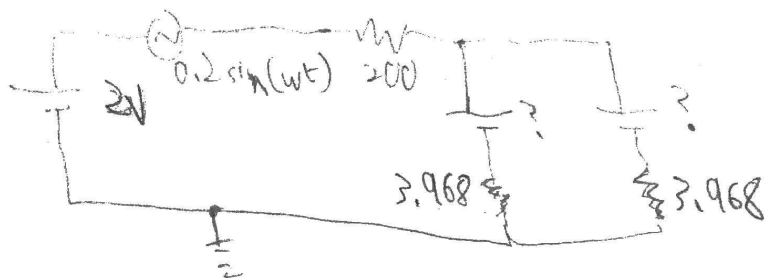
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1A:



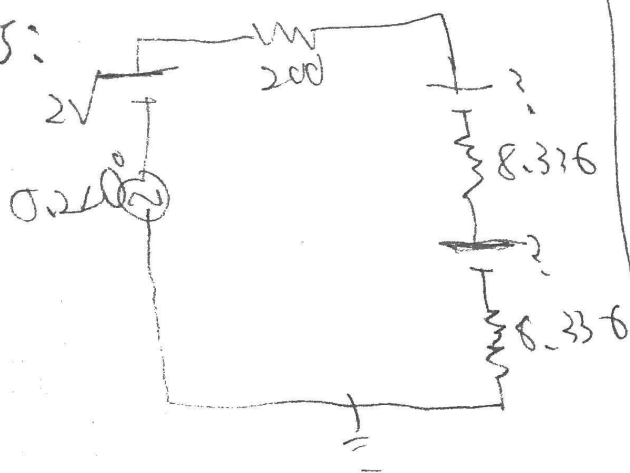
2D:



2E:  $y = mx + b$   $b = -0.167$   $V_{D0} = 0.663$

$A_C = \frac{0.2 \cdot 1.984}{200 + 1.984} = 0.00196 \cdot \sin(wt)$   $V_D = \underline{0.00196 \sin(wt) + 0.663}$

2J:



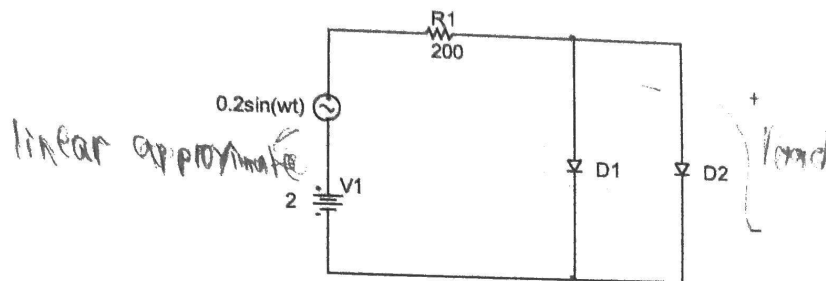
2K:  $y = mx + b$   $b = -0.794$   
 $V_{D0} = 0.6621V$

$A_C = \frac{0.2(8.336 \times 2)}{8.336 \times 2 + 200} = 0.015 \sin(wt)$

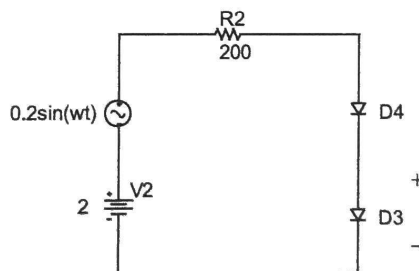
$V_D = 0.6621V + \underline{0.015 \sin(wt)}$

## 2) Diodes, breakpoint analysis

For all diodes in this section, the thermal voltage,  $V_{th}$ , is 26mV, the reverse saturation current,  $I_S$ , is  $1E-14$  and the ideality factor,  $n$ , is 1.  
(Again, you are encouraged to use a script for determining the DC bias points.)



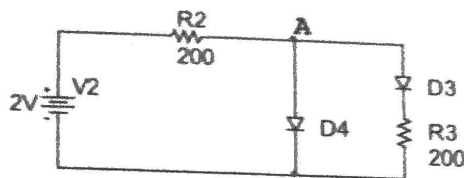
- 1052.21 a) To three significant digits, determine the DC bias characteristics of the above diodes. (In this circuit, what is the relationship between current through a single diode and the resistor current?) Guess 0.5V
- b) Determine the conductance of the diodes,  $g_D = 0.252$
- c) Determine the resistance of the diodes,  $r_D = 3.968$
- d) Redraw the circuit, replacing the diodes with the equivalent linear circuit of a diode resistance and a DC source.
- e) Use superposition analysis to find the small signal AC component of the diode voltage.
- f) For the amplitude of the AC signal, is the linear approximation of the diode reasonable? Yes it is reasonable



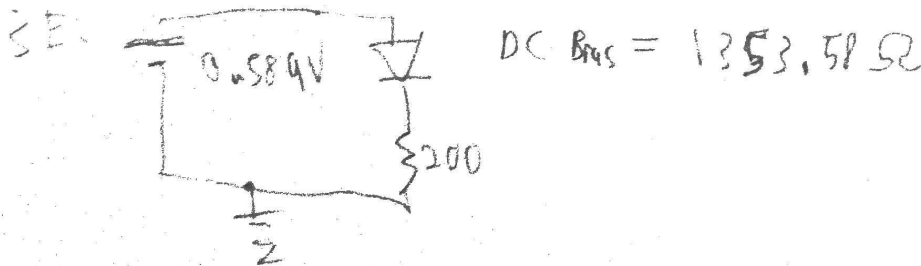
- 220.6.52 g) To three significant digits, determine the DC bias characteristics of the above diodes. (In this circuit, KVL includes two diodes when estimating the resistor voltage.) Guess 0.5V
- h) Determine the conductance of the diodes,  $g_D = 0.1200$
- i) Determine the resistance of the diodes,  $r_D = 8.336$
- j) Redraw the circuit, replacing the diodes with the equivalent linear circuit of a diode resistance and a DC source.
- k) Use superposition analysis to find the small signal AC component of the diode voltage.
- l) For the amplitude of the AC signal, is the linear approximation of the diode reasonable? Yes it is reasonable

## Problem 3) Parallel diodes – bias point analysis

For all diodes in this section, the thermal voltage,  $V_{th}$ , is 26mV, the reverse saturation current,  $I_S$ , is 1E-12 and the ideality factor,  $n$ , is 1.



- When considering the above circuit, what can we say about the voltage of D4 relative to the voltage of D3.  $V_{D4} = V_{D3} + V_{R3}$
- Noting that a small change of diode voltage corresponds to a large change in diode current, is the current in D4 much larger or much smaller than the current in D3? *much larger*
- Given your part b answer, what approximation is reasonable when applying KCL at node A? *No current through D3*
- When considering all of the above, is it reasonable to assume the voltage across D4 is approximately equal to the voltage calculated in problem 1? *Yes*
- Using your problem 1 result as the voltage across D3 and R3, find the DC bias point for diode D3. *Guess 0.5V*
- Using your DC bias current through diode D3 and the assumed DC bias voltage across D4, apply KCL at node A to get a 'better' approximation of the DC bias current through D4. Apply the iterative step to get a new approximation of the voltage across D4. Did the voltage change significantly? Were the part a-d approximations reasonable?
- Would the method used to approximate the diode bias points still be valid if R3 were significantly larger (eg., ~20kΩ)? *Yes, Larger difference in V and I*
- Would the method used to approximate the diode bias points still be valid if R3 were significantly smaller (eg., ~22Ω)? *No, diodes are virtually equal in parallel.*
- Redraw the circuit, replacing the diodes with the equivalent linear circuit of a diode resistance and a DC source.
- If an AC source was placed in series with the DC source, approximately determine the variation in the source current.



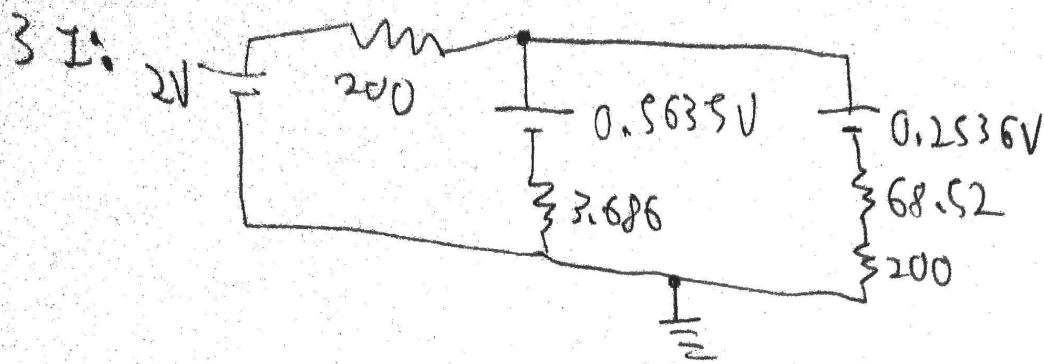
3F:

$$\frac{V_A - 2}{200} = \frac{V_A - V_{D4}}{3.686} + \frac{V_A - V_{D03}}{200 + 68.52} \quad V_A = 0.5326V$$

Voltage did not change significantly.  
Reasonable approximations

Revised: 6/19/2020

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3 J: ignore  $D3/R3$ .  $AC = V_o \sin(\omega t)$

$$\text{KVL: } \frac{(2V + V_o) - 0.5635V}{200 + 3.686} \iff \frac{(2V - V_o) - 0.5635V}{200 + 3.686}$$

$$\frac{(2V \pm V_o) - 0.5635V}{200 + 3.686}$$

#Code written by Saaif Ahmed

#IE HW 8 Problem 1/3 code

import math

vs = 0.5895

vd = 0.5

r = 200

Is = 10\*\*(-12)

n = 1

vtherm = 26/1000

ir1 = 0

count = 0

while count < 10:

print(vd)

vr = vs - vd

ir1 = vr/r

vd = n \* vtherm \* math.log(ir1/Is)

count+=1

print("current:", ir1)

print("voltage: ", vd)

print("DC bias: ", vd/ir1)

print("gD: ", ir1/(n\*vtherm))

print("rD: ", (n\*vtherm)/ir1)

```
#Code written by Saaif Ahmed
```

```
#IE HW 8 Problem 2 code
```

```
import math
```

```
vs = 2.0
```

```
vd = 0.5
```

```
r = 200
```

```
Is = 10**(-14)
```

```
n = 1
```

```
vtherm = 26/1000
```

```
count = 0
```

```
while count < 10:
```

```
    print(vd)
```

```
    #vr = vs - vd
```

```
    vr = vs - (vd + vd)
```

```
    ir1 = vr/r
```

```
    #vd = n * vtherm * math.log((ir1/2)/Is)
```

```
    vd = n * vtherm * math.log(ir1/Is)
```

```
    count+=1
```

```
print("current:", ir1)
```

```
print("voltage: ", vd)
```

```
print("DC bias: ", vd/ir1)
```

```
print("gD: ", ir1/(n*vtherm))
```

```
print("rD: ", (n*vtherm)/ir1)
```