

HW #1  
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1. q: P1:  $3.5 \times 10^9$  clocks.  $\frac{1 \text{ instruction}}{1 \text{ s}} = 2.33 \times 10^9$  instructions / second

P2:  $2.8 \times 10^9$  clocks.  $\frac{1 \text{ instruction}}{1 \text{ s}} = 2.8 \times 10^9$  instructions / second

P3:  $4.0 \times 10^9$  clocks.  $\frac{1}{1 \text{ s}} = 1.82 \times 10^9$  instructions / second

P2 has the highest performance

b: P1:  $2.33 \times 10^9 \cdot 20 = [4.67 \times 10^{10}$  instructions]  $\times 1.5 \text{ cycles} = [6.99 \times 10^{10}$  cycles]

P2:  $2.8 \times 10^9 \cdot 20 = [5.6 \times 10^{10}$  instructions]  $\times 1 = [5.6 \times 10^{10}$  cycles]

P3:  $1.82 \times 10^9$  instructions  $\times 20 = [3.64 \times 10^{10}$  instructions]  $\times 2.2 = [7.99 \times 10^{10}$  cycles]

c:  $C_{\text{putime}} = \frac{\text{Instac} \times \text{CPI}}{\text{CR}}$   ~~$H_{\text{putime}} = IC \cdot 1.15 \text{ CPI} \times CR$~~

~~$P2: 20s = IC \cdot CPI \cdot CR$~~

$14s = IC \cdot 1.15 \text{ CPI} \times CR$

~~$P1: 14s = (4.67 \times 10^{10}) \cdot 1.15 (1.5) \times 3.5 \times 10^9$~~

$x = 1.644$

New  $CR = 5.75 \times 10^9 \text{ Hz}$

$$P2: 14s = 5.6 \times 10^{10} \cdot 1.15(1) / x \cdot 2.8 \times 10^9$$

$$x = 1.642 \quad \boxed{\text{New CR} = 4.6 \times 10^9 \text{ Hz}}$$

$$P3: 14s = 3.64 \times 10^{10} \cdot 1.15(2.2) / x \cdot 4 \times 10^9$$

$$x = 1.6449 \quad \boxed{\text{New CR} = 6.58 \times 10^9 \text{ Hz}}$$

2 a: P1 Avg CPI =  $1(.1) + 2(.2) + 3(.4) + 4(.3) = 2.9$   
 $2.8 \times 10^9 / 2.9 = 9.68 \times 10^8 \text{ instructions/second}$

P2 Avg CPI =  $2(.1) + 3(.2) + 2(.4) + 3(.3) = 2.5$   
 $3.5 \times 10^9 / 2.5 = 1.4 \times 10^9 \text{ instructions/second}$

P2 is faster because it can handle the dataset quicker

b: P1 global =  $1(.1) + 2(.2) + 3(.4) + 4(.3) = 2.9 \text{ CPI}$   
 P2 global =  $2(.1) + 3(.2) + 2(.4) + 3(.3) = 2.5 \text{ CPI}$

c: ~~P1~~ P1:  $2.9 \text{ CPI} \cdot 1 \times 10^6 \text{ instructions} = 2.9 \times 10^6 \text{ cycles}$   
 P2:  $2.5 \text{ CPI} \cdot 1 \times 10^6 \text{ instructions} = 2.5 \times 10^6 \text{ cycles}$

3 A: Comp A: CPI time =  $I/p \cdot (\text{CPI} \cdot 1 \times 10^{-9} \text{ s})$   
 $1.1 = 1 \times 10^9 \cdot \text{CPI} \cdot 1 \times 10^{-9} \text{ s} \quad \boxed{\text{CPI} = 1.1}$

Comp B: CPI time =  $1.4 = 1.3 \times 10^9 \cdot (\text{CPI} \cdot 1 \times 10^{-9} \text{ s})$   
 $\boxed{\text{CPI} = 1.08}$

$$b: \text{comp A} = 1.0_s = 1 \times 10^9 * 1.1 / CR \quad (CR = 1.1 \times 10^9 \text{ Hz})$$

$$\text{Comp B} = 1.0_s = 1.3 \times 10^9 * 1.09 / CR \quad (CR = 1.404 \times 10^9 \text{ Hz})$$

[Compiler B is 1.28 times faster than compiler A]

$$C: \text{Execution time} = 6 \times 10^8 * 1.1 / 1 \times 10^9 = .66 \text{ s}$$

.66 / 1.1 = .6 new is 40% faster than A

~~1.66 / 1.4 = .47~~ new is 53% faster than B

~~4. 10s = 1 cycle + 15 clock cycles~~

~~10s = 1  $\times 10^9 \text{ Hz}$~~   $15 \times 1 \times 10^9 = \text{Clock cycles}$

$$15 \times 10^9 \text{ clock cycles} \times 1.2 = 1.8 \times 10^{10} \text{ clock cycles}$$

$$10s = 1.8 \times 10^{10} \text{ clock cycles} / CR$$

$$CR = 1.8 \times 10^9 \text{ Hz}$$

~~5. A: Average CPI: Total instructions =  $5.256 \times 10^9$~~

~~Arithmetr = 57.08% Load = 38.05% branch = 4.87%~~

$$\begin{aligned} \text{Avg CPI} &= 1(0.5708) + 10(0.3805) + 5(0.0487) \\ &= 4.62 \text{ CPI} \end{aligned}$$

~~1 Processor: ET =  $5.256 \times 10^9 \cdot 4.62 / 2 \times 10^9 = 12.11 \text{ s}$~~

~~2 Processor: Total instructions =  $2 \times 10^9 + 3 \times 10^9 + 256 \times 10^6$~~ 

$$0.8 \times 2 \quad 0.8 \times 1$$

~~1 Processor: Total =  $2 \times 10^9 + 3 \times 10^9 + 256 \times 10^6 = 2.6225 \times 10^{11}$~~ 

$$0.8 \quad 0.8$$

~~ET =  $2.6225 \times 10^{11} \cdot 4.62 /$~~

$$1 \text{ processor: } Et = 5,256 \times 10^9 \cdot 4,62 / 2 \times 10^9 = 12.14 \text{ s}$$

$$2 \text{ processor: } \frac{3 \times 10^9}{0.8 \times 2} + \frac{2 \times 10^9}{2 \times 0.8} + 256 \times 10^6 = 3,381 \times 10^9$$

$$Et = 3,381 \times 10^9 \cdot 4,62 / 2 \times 10^9 = 7.81 \text{ s}$$

$$1 - \frac{7.81}{12.14} = .36$$

2 processor is 36% faster

$$4 \text{ processor: } \frac{3 \times 10^9}{0.8 \times 4} + \frac{2 \times 10^9}{0.8 \times 4} + 256 \times 10^6 = 1.82 \times 10^9$$

$$Et = 1.82 \times 10^9 \cdot 4,62 / 2 \times 10^9 = 4.2 \text{ s}$$

$$1 - \frac{4.2}{12.14} = .65$$

4 processor is 65% faster

$$8 \text{ processor: } \frac{3 \times 10^9}{0.8 \times 8} + \frac{2 \times 10^9}{0.8 \times 8} + 256 \times 10^6 = 1.037 \times 10^9$$

$$Et = 1.037 \cdot 4,62 / 2 \times 10^9 = 2.405$$

$$1 - \frac{2.405}{12.14} = .80$$

8 processor is 80% faster

b: 1 processor:  $Et = 8,256 \times 10^9 \cdot 4,62 / 2 \times 10^9 = 19.07$

$$19.07 / 12.14 = 1.57 \text{ times slower}$$

$$2 \text{ processor: } \frac{6 \times 10^9}{0.8 \times 2} + \frac{2 \times 10^9}{2 \times 0.8} + 256 \times 10^6 = 5,256 \times 10^9$$

$$Et = 5,256 \times 10^9 \cdot 4,62 / 2 \times 10^9 = 12.14 \text{ s}$$

$$12.14 / 7.81 = 1.55 \text{ times slower}$$

$$4 \text{ processor} = \frac{6 \times 10^9}{0.8 \times 4} + \frac{2 \times 10^9}{0.8 \times 4} + 256 \times 10^6 = 2.756 \times 10^9$$

$$E_t = 2.756 \times 10^9 \cdot 4.62 / 2 \times 10^9 = 6.37 \text{ s}$$

$6.37 / 4.2 = [1.52 \text{ times slower}]$

$$8 \text{ processor} = \frac{6 \times 10^9}{0.8 \times 8} + \frac{2 \times 10^9}{0.8 \times 8} + 256 \times 10^6 = 1.506 \times 10^9$$

$$E_t = 1.506 \times 10^9 \cdot 4.62 / 2 \times 10^9 = 3.47886 \text{ s}$$

$3.47886 / 2.40 = [1.46 \text{ times slower}]$

$$C: (3 \times 10^9 + X + 256 \times 10^6) \cdot 4.62 = 4.2 \text{ s}$$

$$X = \cancel{-1.44} \times 10^9 \text{ instructions}$$

$$6 A: P1: \frac{0.9 \times 5 \times 10^9}{4 \times 10^9} = 1.125 \text{ s}$$

$$P2: \frac{0.75 \times 1 \times 10^9}{3 \times 10^9} = .25 \text{ s}$$

This not true because P2 has lower CR but it has faster CPU time

$$B: P1: \frac{0.9 \times 1 \times 10^9}{4 \times 10^9} = .225 \text{ s}$$

$$P2: \frac{0.75 \times X}{3 \times 10^9} = .225 \text{ s}$$

$$X = 9 \times 10^9 \text{ instructions}$$

$$C: P1: CR \cdot \frac{1}{CPI} = \frac{4.44 \times 10^9}{10^6} \text{ instructions / s} \\ = 4444.44 \text{ MFIPS}$$

$$P2: CR \cdot \frac{1}{CPI} = \frac{4 \times 10^9}{10^6} \\ = 4000 \text{ MFIPS}$$

This is false because we showed that P2 can do the program faster.

$$D: P1: \frac{2 \times 10^9}{1.125 \times 10^6} = 1777.78 \text{ MFLOPS}$$

$$P2: \frac{4 \times 10^8}{25 \times 10^6} = 1600 \text{ MFLOPS}$$

This is misleading because we know P2 is faster