Wednesday, October 27, 2021 7:03 PM

## Problem 1:

$$\begin{split} E_{(x,y)}[l(f(x),y)] &= \int_x \left\{ \int_y (z-y)^2 p(y|x) dy \right\} p(x) dx = 0 \\ \frac{\partial}{\partial x} \left[ \int_x \left\{ \int_y (z-y)^2 p(y|x) dy \right\} p(x) dx = 0 \right] \\ \int_x \left\{ \int_y \frac{\partial}{\partial x} (z-y)^2 p(y|x) dy \right\} p(x) dx = 0 \\ \int_x \left\{ \int_y 2 (z-y) p(y|x) dy \right\} p(x) dx = 0 \end{split}$$

$$2z = 2y(p(y|x))$$
  
$$f(x) = E[y|x]$$